

1 A4 2 sides

Fin Econometrics < Final >

3 steps:

1) Model constructions \* Understand property of model

Multicollinearity or near multicollinearity

$$\hookrightarrow \text{Corr}(x_1, x_2) > 0.8$$



2) Estimation

Estimator

$$\text{Endogeneity} = \text{cov}(x, u) \neq 0$$

↑  
z

\*\*\*

3) Inference

$(1-\alpha)CI \rightarrow$  formula bilian:uuu

$\rightarrow \hat{\beta}$

$\rightarrow se$

$\rightarrow$  Critical ✓ degree of Freedom



Panel data  
Times-series

& lag  $\Rightarrow$  lose # obs  
1 1

↪ autoregressive conditional heteroskedasticity

ARCH: mean equation  $y_t = \beta x_t + U_t$

volatility equation

$$\sigma_t^2 = \alpha_0 + \alpha_1 U_{t-1}^2$$

if we don't have endogeneity → can use OLS  
if  $x$  &  $U$  don't correlate  
can use OLS to estimate mean equation, not volatility equation

Dfuller ⇒ test-stat:  $\frac{\hat{\theta}}{\text{se}(\hat{\theta})}$

distribution: Dickey Fuller dist

rule to reject  $H_0$ : test-stat < critical value

, how many times have to do difference to get stationary process

Integration , don't have to do anything

$I(0)$

↳ integration of order zero

$I(2)$

$x$  is not stationary process

but  $\partial(\partial x)$  is stationary process

Final exam:

- Consistency / unbiased
- Hypothesis test, confidence interval
- Interpret  $\beta$ , In  $\square$

E.g. Check whether debt has positive impact for small firm's ROA but

$$H_0: \beta_1 + \beta_2 = 0 \text{ vs. } H_1: \beta_1 + \beta_2 > 0$$

negative impact for large firm's ROA  $\leftarrow H_0: \beta_1 = 0 \text{ vs. } \beta_1 < 0$

How to model it?

1) Cross-section data

dummy  $\begin{cases} 1 & \text{small} \\ 0 & \text{large} \end{cases}$

$$ROA = \beta_0 + \beta_1 \text{debt} + \beta_2 \text{size} \cdot \text{debt} + U$$

2) Panel data

~~pooled cross-section~~

fixed effect  $\rightarrow$  has  $\alpha$ ,  $\alpha$  correlated

random effect

$$ROA_{it} = \beta_0 + \beta_1 \text{debt}_{it} + \beta_2 \text{size}_{it} \cdot \text{debt}_{it} + U_{it}$$

$\downarrow$   
 $\alpha_i$

$i$  individual  
 $t$  time

What is the effect of  $x_1$  on  $y$ ?

$$y = \beta_0 + \beta_1 x_1 + \beta_2 (x_1 - x_2) + \beta_3 (x_1 - x_3)$$

diff by  $x_1$   
then interpret

$$\beta_1 + \beta_2 + \beta_3$$

or back to original

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_1 - \beta_2 x_2 + \beta_3 x_1 - \beta_3 x_3$$

$$= \beta_0 + (\beta_1 + \beta_2 + \beta_3) x_1 - \beta_2 x_2 - \beta_3 x_3$$

## Hausman test

$$y_{it} = \beta_0 + \beta_1 x_{1it} + \beta_2 x_{2it} + \alpha_i + u_{it}$$

not sure is fixed or random

RE estimator  $\Rightarrow \begin{pmatrix} \hat{\beta}_1 \\ \hat{\beta}_2 \end{pmatrix}$

FE estimator  $\Rightarrow \begin{pmatrix} \hat{\beta}_1 \\ \hat{\beta}_2 \end{pmatrix}$

df = 1 instead of 2  
 $\beta$  used to compare

2nd Hausman test ; compare  $\hat{\beta}^{FE}$  &  $\hat{\beta}^{RE}$   $\leftarrow$  close: RE model  
 far: FE model

$$y_{it} = \beta x_{it} + \alpha_i + u_{it}$$

Random Effect Model

$$\text{cov}(\alpha_i, x_{it}) = 0$$

or Fixed Effect Model ?

$$\text{cov}(\alpha_i, x_{it}) \neq 0$$

FE estimator: reg  $y - \bar{y}$  on  $x - \bar{x} \rightarrow \alpha_i$  will be eliminated!  $\rightarrow$  consistent  $\hat{\beta}^{FE} \approx \beta$   
 RE estimator: reg  $y - \bar{y}$  on  $x - \bar{x} \rightarrow$  still has  $\alpha - \bar{\alpha}$   $\rightarrow$  not consistent  $\hat{\beta}^{RE} \approx \beta$   
 1st  $\rightarrow$  keep result

Whether  $\text{cov}(\alpha_i, x_{it}) = 0$  or not  $\rightarrow$  doesn't matter

correlate to  $\hat{\beta}^{FE} \approx \hat{\beta}^{RE}$   
 will be closed to

far  $\hat{\beta}^{FE} \approx \beta$   
 $\hat{\beta}^{RE} \neq \beta$

FINITE Distributed Lags: \*delay effect?

$$y_t = \beta_0 + \sigma_0 x_t + \sigma_1 x_{t-1} + \dots + \sigma_m x_{t-m}$$

depend on relationship btw  $x$  &  $\text{prob}\{y=1|x\}$   
 BINARY Response Model /  $y$  can be either 0 or 1

can use also LPM  $\rightarrow$  Prob  $\{y=1|x\} = x\beta$   
 prob increase linearly

cannot use OLS not linear  $\left\{ \begin{array}{l} \text{PROBIT} \\ \text{LOGIT} \end{array} \right. \left\{ \begin{array}{l} \text{Prob}\{y=1|x\} = \text{CDF}(x\beta) \end{array} \right.$

$y = \begin{cases} 1 & \text{pass} \\ 0 & \text{fail} \end{cases}$   
 prob linear in  $x$   
 LPM:  $y = \beta_0 + \beta_1 \#hrs + \dots + U$   
 Sample: FT 27  $\#hrs \rightarrow (100, 200) \Rightarrow \hat{\beta}$   
 FT 42  $\#hrs \rightarrow (1, 2)$   
 if  $\#hrs = 100$ ;  $-0.3 + 0.005(100) = 0.2$   
 200  $= 0.7$   
 $= \odot \notin (0,1)$   
 not suitable to use this model / need new model / it's not fit!!

36/40  
fin mit B, fin stat B,

$H_1: \beta > 0$

