

1.

- (a) Recursion is a programming technique in which a method can call itself to fulfill its purpose.
- (b) All recursive definitions must have a non-recursive part in order to terminate the recursive path. A definition without a non-recursive part causes infinite recursion.
- (c) Base case is needed to prevent the definition from infinite looping (infinite recursion).
- (d) No. Recursion is not necessary.
- (e) Recursion has the overhead of multiple method invocations. But for some problems, recursive solutions are often more simple and elegant to express. However, a recursive solution may be less efficient compared to an iterative solution.

2.

- (a) The expected case for finding an element with a linear search is $n/2$, which is $O(n)$; the worst case is also $O(n)$ and the best case is $O(1)$.
- (b) The best case for finding an element with a binary search is $O(1)$, the expected case is $O(\log(n))$, and the worst case performance is $O(\log(n))$.
- (c) Linear search would be preferred over a binary search when the list is unsorted.
- (d) Binary search requires the list to be sorted.
- (e) When would a sequential sort be preferable to a recursive one?
- (f) Selection sort orders a list of values by repetitively putting a particular value into its final position.
- (g) The Bubble Sort orders a list of values by repetitively comparing neighboring elements and swapping their positions if necessary.
- (h) The best case for sorting with Bubble sort is $O(n)$, expected case is $O(n^2)$ and the worst case is $O(n^2)$.
- (i) Quick sort orders values by partitioning the list around one element, then sorting each partition.
- (j) The best case for sorting with quick sort is $O(n\log(n))$, expected case is $O(n\log(n))$, and the worst case is $O(n^2)$.

3.

(a) A tree is a non-linear structure in which elements are organized into a hierarchy. A tree is comprised of a set of nodes in which elements are stored and edges connect one node to another. Each node is located on a particular level. There is only one root node in the tree.

(b) The root is the only node which has no parent. We can follow a path through a tree from parent to child, starting at the root. A node is an ancestor of a node if it is above it on the path from the root.

(c) A node that has no children is a leaf node.

(d) The height of a tree is the length of the longest path from the root to a leaf.

(e) Given a tree of height N , it would take $O(\log(n))$.

