

CMPT 459 Fall 2017

DataMining

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Assignment 3

Assignment 3.1 (40 Marks)

- a) Salary has the smallest gini index of 0.16 and is chosen as the split attribute for the root.

$$\begin{aligned}\text{gini(Age)} &= 5/10 * \text{gini(age=young)} \\ &\quad + 2/10 * \text{gini(age=medium)} \\ &\quad + 3/10 * \text{gini(age=old)} \\ &= 0.5 * 0.48 + 0.2 * 0.5 + 0.3 * 0.44 \\ &= 0.472\end{aligned}$$

$$\begin{aligned}\text{gini(age=young)} &= 1 - (3/5)^2 - (2/5)^2 = 0.48 \\ \text{gini(age=medium)} &= 1 - (1/2)^2 - (1/2)^2 = 0.5 \\ \text{gini(age=old)} &= 1 - (2/3)^2 - (1/3)^2 = 0.44\end{aligned}$$

$$\begin{aligned}\text{gini(salary)} &= 3/10 * \text{gini(salary=low)} \\ &\quad + 5/10 * \text{gini(salary=medium)} \\ &\quad + 2/10 * \text{gini(salary=high)} \\ &= 0.3 * 0 + 0.5 * 0.32 + 0.2 * 0 \\ &= 0.16\end{aligned}$$

$$\begin{aligned}\text{gini(salary=low)} &= 1 - (3/3)^2 = 0 \\ \text{gini(salary=medium)} &= 1 - (4/5)^2 - (1/5)^2 = 0.32 \\ \text{gini(salary=high)} &= 1 - (2/2)^2 = 0\end{aligned}$$

$$\begin{aligned}\text{gini(city)} &= 4/10 * \text{gini(city=Vancouver)} \\ &\quad + 2/10 * \text{gini(city=Burnaby)} \\ &\quad + 2/10 * \text{gini(city=Coquitlam)} \\ &\quad + 2/10 * \text{gini(city=Richmond)} \\ &= 0.4 * 0.5 + 0.2 * 0.5 + 0.2 * 0 + 0.2 * 0.5 \\ &= 0.4\end{aligned}$$

$$\begin{aligned}\text{gini(city=Vancouver)} &= 1 - (2/4)^2 - (2/4)^2 = 0.5 \\ \text{gini(city=Burnaby)} &= 1 - (1/2)^2 - (1/2)^2 = 0.5 \\ \text{gini(city=Coquitlam)} &= 1 - (2/2)^2 = 0 \\ \text{gini(city=Richmond)} &= 1 - (1/2)^2 - (1/2)^2 = 0.5\end{aligned}$$

- b) The gini index favors attributes with few distinct values. An attribute with few distinct values is more likely to have a low gini index. By definition, the gini index is a measure of inequality, or statistical dispersion. So the fewer amount of distinct values will result in a lower gini index. A gini index of 0 would express perfect equality.
- c) b) suggests to choose the attribute with fewer distinct values between two attributes that have the same smallest gini index.

Assignment 3.2 (40 marks)

- a)
- | | | |
|------------------------------------------------------|-----------------------------------------------------|--------------------------------------------------|
| $P(\text{good}) = 0.6$ | $P(\text{bad}) = 0.4$ | |
| $P(\text{Age}=\text{young} \text{good}) = 0.5$ | $P(\text{Age}=\text{medium} \text{good}) = 0.17$ | $P(\text{Age}=\text{old} \text{good}) = 0.33$ |
| $P(\text{Age}=\text{young} \text{bad}) = 0.5$ | $P(\text{Age}=\text{medium} \text{bad}) = 0.25$ | $P(\text{Age}=\text{old} \text{bad}) = 0.25$ |
| $P(\text{Salary}=\text{low} \text{good}) = 0.0$ | $P(\text{Salary}=\text{medium} \text{good}) = 0.66$ | $P(\text{Salary}=\text{high} \text{good}) = 0.3$ |
| $P(\text{Salary}=\text{low} \text{bad}) = 0.75$ | $P(\text{Salary}=\text{medium} \text{bad}) = 0.25$ | $P(\text{Salary}=\text{high} \text{bad}) = 0.0$ |
| $P(\text{City}=\text{Vancouver} \text{good}) = 0.33$ | $P(\text{City}=\text{Vancouver} \text{bad}) = 0.5$ | |
| $P(\text{City}=\text{Burnaby} \text{good}) = 0.17$ | $P(\text{City}=\text{Burnaby} \text{bad}) = 0.25$ | |
| $P(\text{City}=\text{Coquitlam} \text{good}) = 0.33$ | $P(\text{City}=\text{Coquitlam} \text{bad}) = 0.0$ | |
| $P(\text{City}=\text{Richmond} \text{good}) = 0.17$ | $P(\text{City}=\text{Richmond} \text{bad}) = 0.25$ | |

- b)
- Age = "Young"
Salary = "high"
City = "Richmond"

Result of the decision function for class "good":

$$P(\text{good}) * P(\text{Age}=\text{Young}|\text{good}) * P(\text{Salary}=\text{high}|\text{good}) * P(\text{City}=\text{Richmond}|\text{good}) \\ = 0.6 * 0.5 * 0.3 * 0.17 = 0.0153$$

Result of the decision function for class "bad":

$$P(\text{bad}) * P(\text{Age}=\text{young}|\text{bad}) * P(\text{Salary}=\text{high}|\text{bad}) * P(\text{City}=\text{Richmond}|\text{bad}) \\ = 0.4 * 0.5 * 0 * 0.25 = 0.0$$

The classifier predicts good.

Assignment 3.3 (20 marks)