

Homework 4

Due: Sunday October 27th, 11:59 p.m.

Before start, please read the following.

1. The questions in this homework allow you to practice your R skills for Decomposition and Exponential Smoothing models (Chapter 6 and 7).
2. For all questions, you must submit **1) the source file that contains the R commands, and 2) the snapshot of what R outputs after you run your R program.**
3. I strongly prefer if you **electronically submit** your homework through Canvas by putting all files in a zip folder.
4. Please assign numbers for each solutions, so it would be easy for me to read the answers.

Good Luck! ☺

Question 1 (5 credits):

Show that a MA is equivalent to a 7-term weighted moving average with weights of 0.067, 0.133, 0.200, 0.200, 0.200, 0.133, and 0.067.

Question 2 (5+5+5+5+3+2=25 credits):

The plastics data set consists of the monthly sales (in thousands) of product A for a plastics manufacturer for five years.

- Plot the time series of sales of product A. Can you identify seasonal fluctuations and/or a trend-cycle?
- Use a classical multiplicative decomposition to calculate the trend-cycle and seasonal indices.
- Do the results support the graphical interpretation from part a?
- Compute and plot the seasonally adjusted data.
- Change one observation to be an outlier (e.g., add 500 to one observation), and calculate the seasonally adjusted data. What is the effect of the outlier?
- Does it make any difference if the outlier is near the end rather than in the middle of the time series?

Question 3 (5+5+5+5+5+5+5 = 40 credits):

For this exercise, use the quarterly UK passenger vehicle production data from 1977Q1–2005Q1 (data set `ukcars`).

- Plot the data and describe the main features of the series.
- Decompose the series using STL and obtain the seasonally adjusted data.
- Forecast the next two years of the series using an additive damped trend method applied to the seasonally adjusted data. (This can be done in one step using `stlf()` with arguments `etsmodel="AAN"`, `damped=TRUE`.)
- Forecast the next two years of the series using Holt's linear method applied to the seasonally adjusted data (as before but with `damped=FALSE`).
- Now use `ets()` to choose a seasonal model for the data.
- Compare the RMSE of the ETS model with the RMSE of the models you obtained using STL decompositions. Which gives the better in-sample fits?
- Compare the forecasts from the three approaches? Which seems most reasonable?
- Check the residuals of your preferred model.

Question 4 (5+5+5+5+5+5= 30 credits):

For this exercise, use the monthly Australian short-term overseas visitors data, May 1985–April 2005. (Data set: `visitors`)

- Make a time plot of your data and describe the main features of the series.

- b. Split your data into a training set and a test set comprising the last two years of available data. Forecast the test set using Holt-Winters' multiplicative method.
- c. Why is multiplicative seasonality necessary here?
- d. Forecast the two-year test set using each of the following methods:
 - i. an ETS model;
 - ii. an additive ETS model applied to a Box-Cox transformed series;
 - iii. a seasonal naïve method;
 - iv. an STL decomposition applied to the Box-Cox transformed data followed by an ETS model applied to the seasonally adjusted (transformed) data.
- e. Which method gives the best forecasts? Does it pass the residual tests?
- f. Compare the same four methods using time series cross-validation with the tsCV function instead of using a training and test set. Do you come to the same conclusions?