

1. Design, implement, and test a Queue data structure that:

1. uses a linked-list to store values in the queue

```
2
3  template <typename T>
4  class Node {
5  public:
6      T data;
7      Node<T>* next;
8
9      Node(T val) : data(val), next(nullptr) {}
10 };
11
```

2. has an enqueue method that will appropriately add a value to the back of the queue as an appropriate element

```
void enqueue(T val) {
    Node<T>* newNode = new Node<T>(val);
    if (rear == nullptr) {
        front = rear = newNode;
    } else {
        rear->next = newNode;
        rear = newNode;
    }
    size++;
}
```

3.has a dequeue method that will appropriately remove an element from the front of the queue and return its value

```
T dequeue() {  
    if (isEmpty()) {  
        throw std::out_of_range("Queue is empty");  
    }  
    T val = front->data;  
    Node<T>* temp = front;  
    front = front->next;  
    if (front == nullptr) {  
        rear = nullptr;  
    }  
    delete temp;  
    size--;  
    return val;  
}
```

4.Optionally has a peek method that returns the value at the front of the queue without removing it

```
T peek() {  
    if (isEmpty()) {  
        throw std::out_of_range("Queue is empty");  
    }  
    return front->data;  
}
```

Testing:

Enqueue:

```
75 // Test enqueue method
76 Queue<int> q;
77 q.enqueue(10);
78 q.enqueue(20);
79 q.enqueue(30);
80 std::cout << "Queue after enqueueing: ";
81 while (!q.isEmpty()) {
82     std::cout << q.dequeue() << " ";
83 }
84 std::cout << std::endl;
```

Dequeue:

```
86 // Test dequeue method
87 Queue<int> q2;
88 q2.enqueue(100);
89 q2.enqueue(200);
90 q2.enqueue(300);
91 std::cout << "Dequeuing from queue: ";
92 std::cout << q2.dequeue() << std::endl;
93
```

Peek:

```
94 // Test peek method
95 Queue<int> q3;
96 q3.enqueue(1000);
97 q3.enqueue(2000);
98 q3.enqueue(3000);
99 std::cout << "Peeking at front element: ";
100 std::cout << q3.peek() << std::endl;
101
```