MECH 539: Computational Aerodynamics Department of Mechanical Engineering, McGill University

Project #2 Due 5th March, 2013

Consider the Laplace equation on a unit square with Dirichlet boundary conditions, u(x, 0) = u(0, y) = u(1, y) = 0, and u(x, 1) = 1. Discretize the second derivatives of u with respect to x and y with a second-order finite-difference spatial discretization. Write the following numerical codes to solve the linear system using the Jacobi, Gauss-Seidel, and Successive Over-Relaxation (SOR) on three grid sizes, 100×100 , 200×200 , and 400×400 . [Note: You may use a single precision floating-point format.] Provide the following in a written report:

- 1. Demonstrate the solution of the Laplace Equation for the 400×400 .
- 2. Convergence of the residual versus the number of iterations for all three methods on the same plot. Provide a plot for each grid size. Discuss the difference between the schemes. Compute the condition number of the matrix using the Forsythe-Moler method and discuss the results.
- 3. Convergence of the residual versus the CPU time for all three methods on the same plot. Discuss the difference between the schemes. Comment on the number of vectors and arrays that were necessary for each scheme and compare the algorithms in terms of memory usage.
- 4. Effect of the relaxation parameter on the SOR. Try several different values and discuss your findings. Show plots of the convergence of the residual for various relaxation parameters. Is there an optimum relaxation parameter? Is the optimum the same for all grid sizes.