

Traitement d'images

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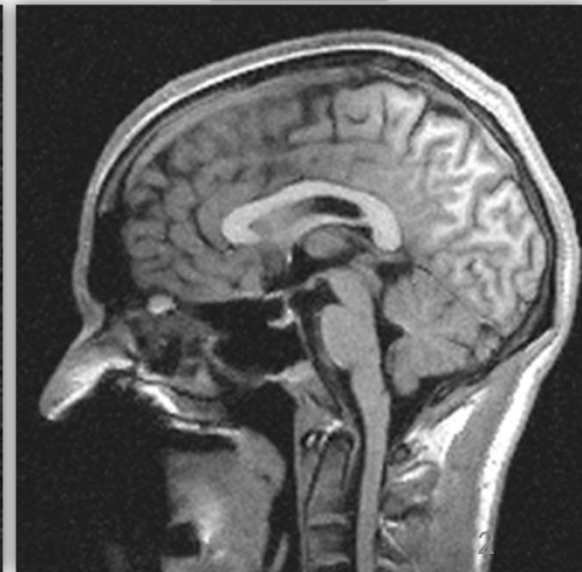
Restauration et débruitage



noisy



denoised



http://www.cs.utah.edu/~suyash/pubs/denoising_mri/

Restauration et débruitage

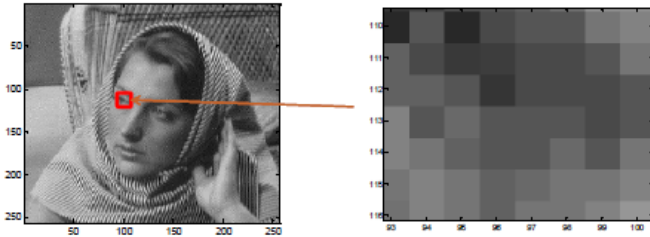
- Par filtrage spatial linéaire
 - Le filtre est représenté par un masque 3x3 (aussi appelé noyau, fenêtre, window)

$$g(x, y) = \sum_{i=-1}^1 \sum_{j=-1}^1 h(x-i, y-j) f(i, j)$$

Un pixel $f(i,j)$ est remplacé par une somme pondérée de lui-même et des pixels de son voisinage

Filters

- A filter is a process that removes or enhances some feature of an image.
- Commonly, the word “filter” describes an operation on the *neighborhood* of an image.



Linear Filters

- A linear filter is a neighborhood operation that can be written as a convolution.

$$g(x, y) = (f * w)(x, y) \\ = \sum_m \sum_n f(m, n) w(x - m, y - n)$$

- f = original image
- w = filter
- g = filtered image

Linear Filters

- Digitally, we slide the filter w around the image f and compute the weighted average of that neighborhood.
- We usually choose the filter to have size $N \times N$ where N is odd.

$$W = \begin{bmatrix} w_1 & w_2 & w_3 \\ w_4 & w_5 & w_6 \\ w_7 & w_8 & w_9 \end{bmatrix}$$

$$f = \begin{bmatrix} f_1 & f_2 & f_3 & f_4 & f_5 \\ f_6 & f_7 & f_8 & f_9 & f_{10} \\ f_{11} & f_{12} & f_{13} & f_{14} & f_{15} \\ f_{16} & f_{17} & f_{18} & f_{19} & f_{20} \\ f_{21} & f_{22} & f_{23} & f_{24} & f_{25} \end{bmatrix}$$

$$g_{13} = w_1 f_7 + w_2 f_8 + w_3 f_9 + w_4 f_{12} + w_5 f_{13} + w_6 f_{14} + w_7 f_{17} + w_8 f_{18} + w_9 f_{19}$$

- The boundaries have to be handled carefully.

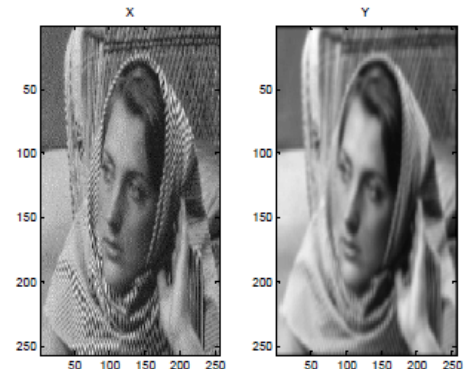
Mean Filter

- For example, we could choose the 3×3 *mean (box) filter*.
- Note we generally normalize the weights to one to preserve the overall gray level of the image.

$$w = \frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

- The Matlab command `imfilter` performs convolutions.

```
load woman;
w=1/9*ones(3,3);
Y=imfilter(X,w);
```



Gaussian Filter

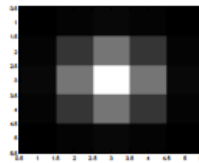
- To put more emphasis on the center pixel, we could make a digital *Gaussian filter*.

$$G = \frac{1}{16} \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

- The Matlab command *fspecial* can build filters.

```
G = fspecial('gaussian',[5,5],0.8)
```

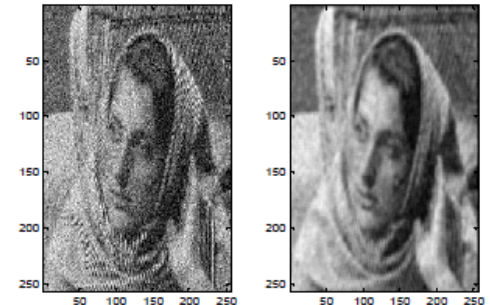
```
G =
0.0005    0.0050    0.0109    0.0050    0.0005
0.0050    0.0522    0.1141    0.0522    0.0050
0.0109    0.1141    0.2491    0.1141    0.0109
0.0050    0.0522    0.1141    0.0522    0.0050
0.0005    0.0050    0.0109    0.0050    0.0005
```



Gaussian Filter

- Although a Gaussian filter is good at removing Gaussian noise, it also blurs the image.

```
load woman;
f = imnoise(uint8(X),'gaussian', 0, 0.02);
G = fspecial('gaussian', [5,5], 0.5);
g = imfilter(f,G);
```



Median Filter

- The median filter computes the median of the neighborhood centered over the pixel.
- Compared to the mean filter, the median filter preserves edges better.

255	255	0
255	100	0
255	255	0

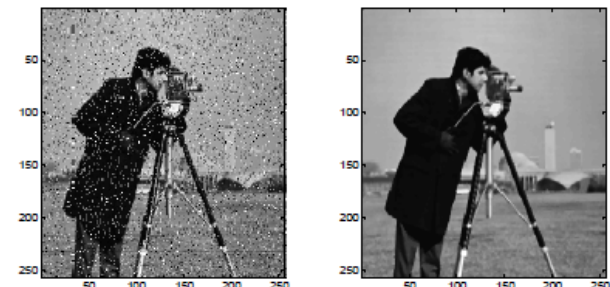
Mean = 152.8

Median = 255

Median Filter

- The median filter and its variants are well-suited for salt & pepper noise.
- The Matlab command *nlfilter* calculates nonlinear functions on neighborhoods. It is much slower than *imfilter*.

```
B = nlfilter(A, [3,3], @(x) median(x(:)) );
```

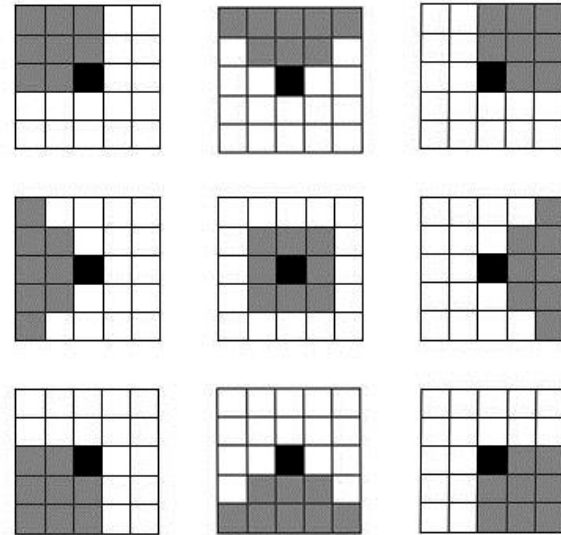


Complexité

- complexité du filtre : nombre d'opérations nécessaires pour calculer sa valeur en chaque pixel de l'image

Autres filtres non-linéaires

- Filtre de Nagao (1979)



Filtre de Nagao



Bruit impulsionnel (densité=2%)



Image filtrée

Filtres non-locaux

- Les filtres vus précédemment utilisent des pixels proches du pixel à estimer (voisinage)
- Ici on cherche des pixels « proches » au sens de l'intensité
- Filtre bilatéral

Filtres non-locaux

- Noisy source image:



Filtres non-locaux

- Gaussian Filter

Low noise,
Low detail



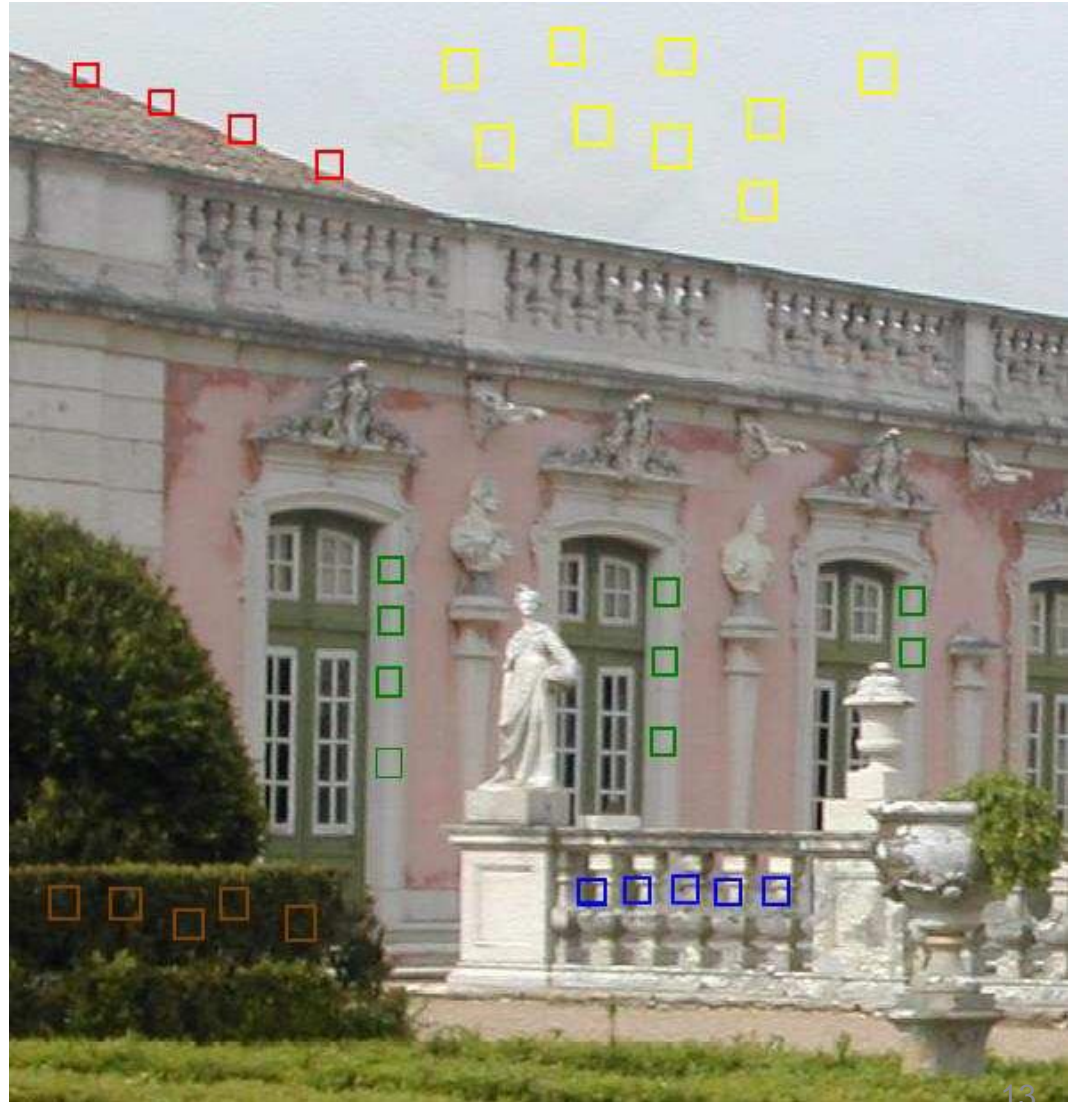
Filtres non-locaux

- Bilateral Filter



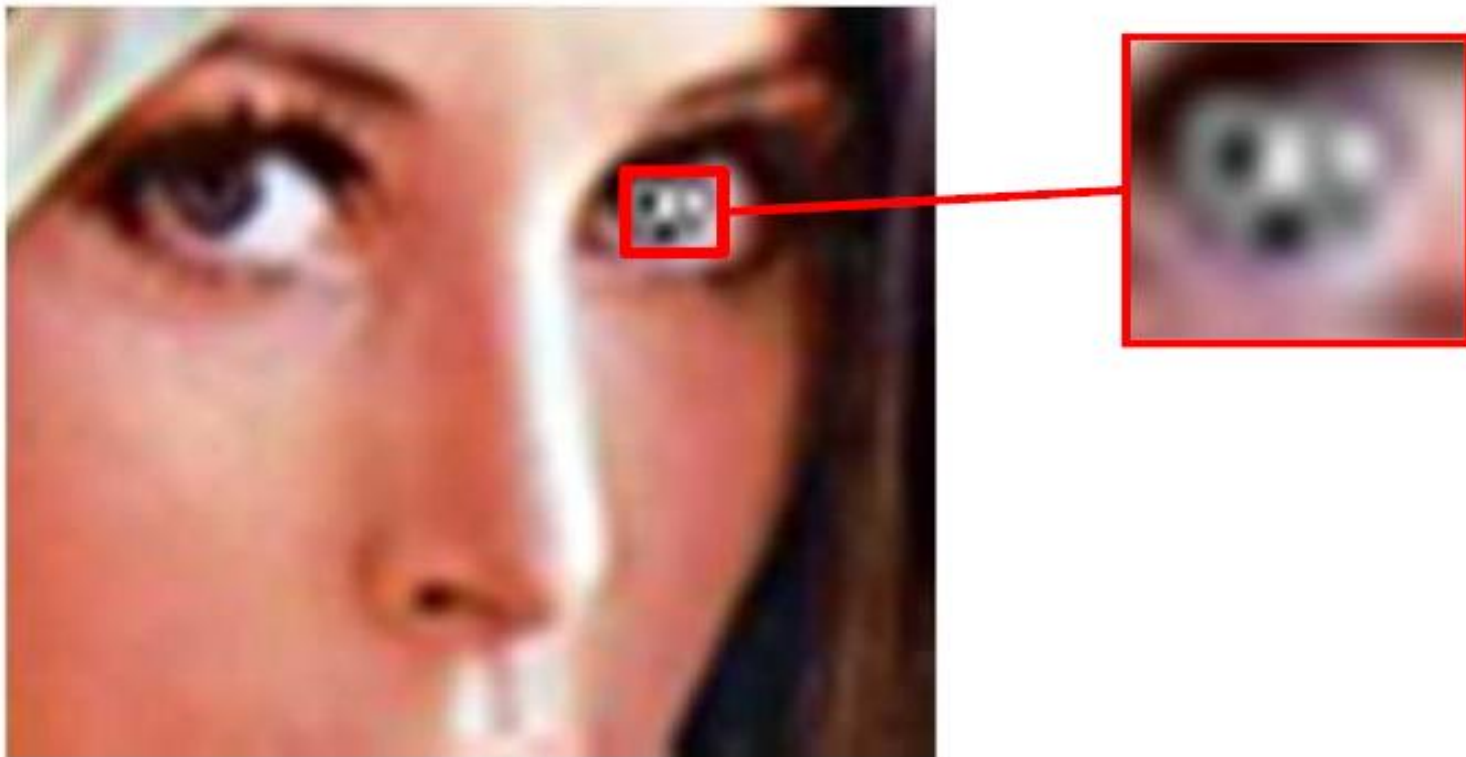
Filtre NL Means (2005)

- NL Means :
Chercher non plus
des pixels mais
des **voisinages** qui
se ressemblent
dans toute
l'image...



Filtre NL means

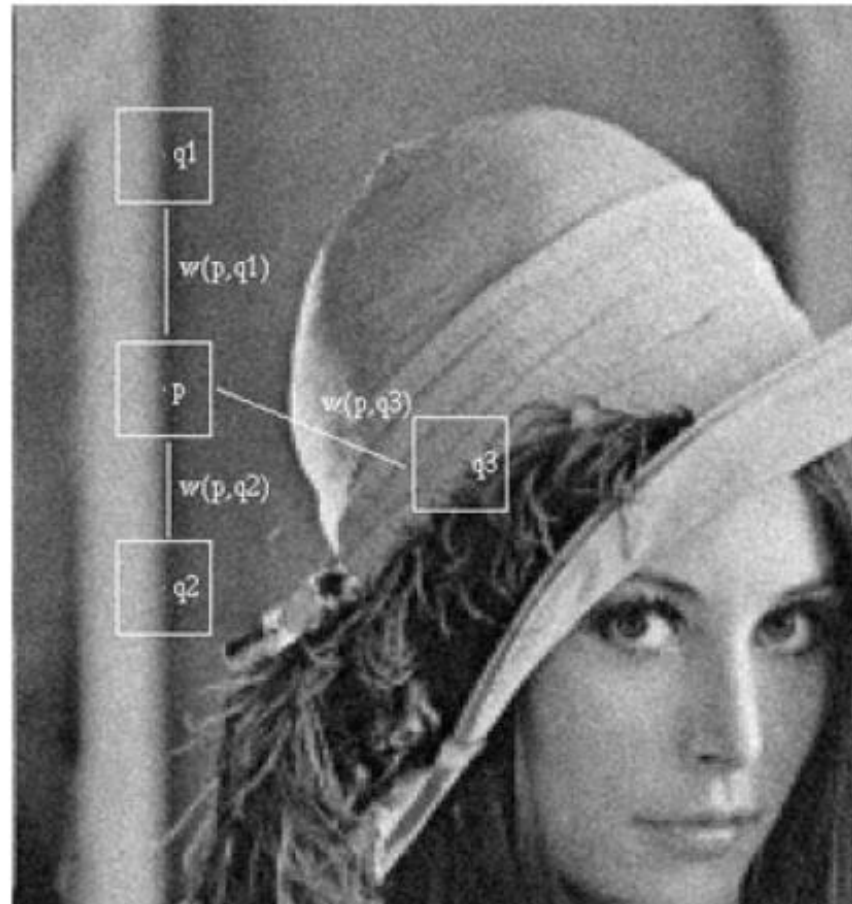
- Suppose Lena's left eye was obscured by noise.
- A neighborhood around the eye will not tell us the eye's true color.



- *Solution:* Look at the other eye!

Filtre NL means

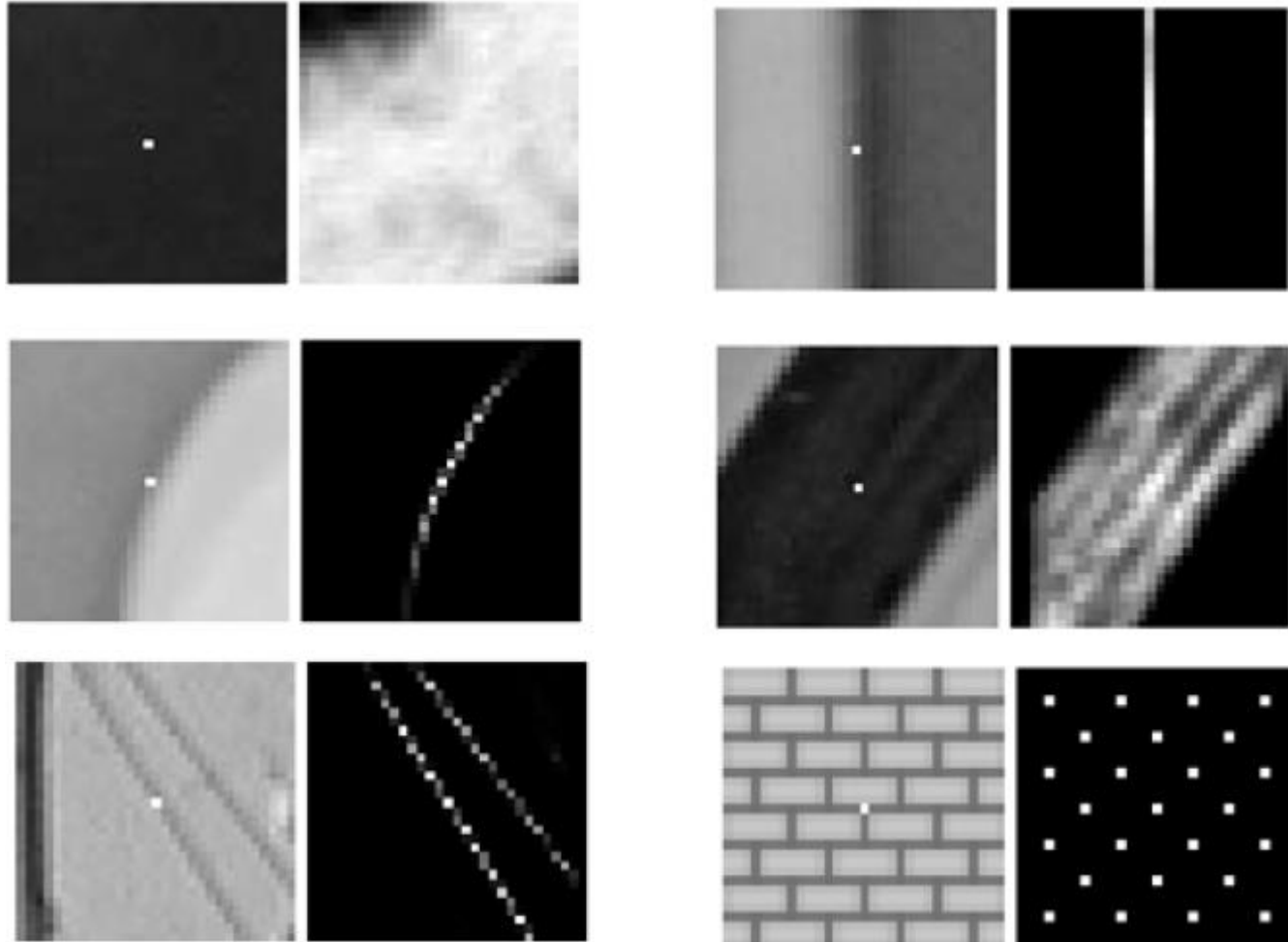
- Natural images tend to have similar neighborhoods.



Un peu de formalisme au tableau...

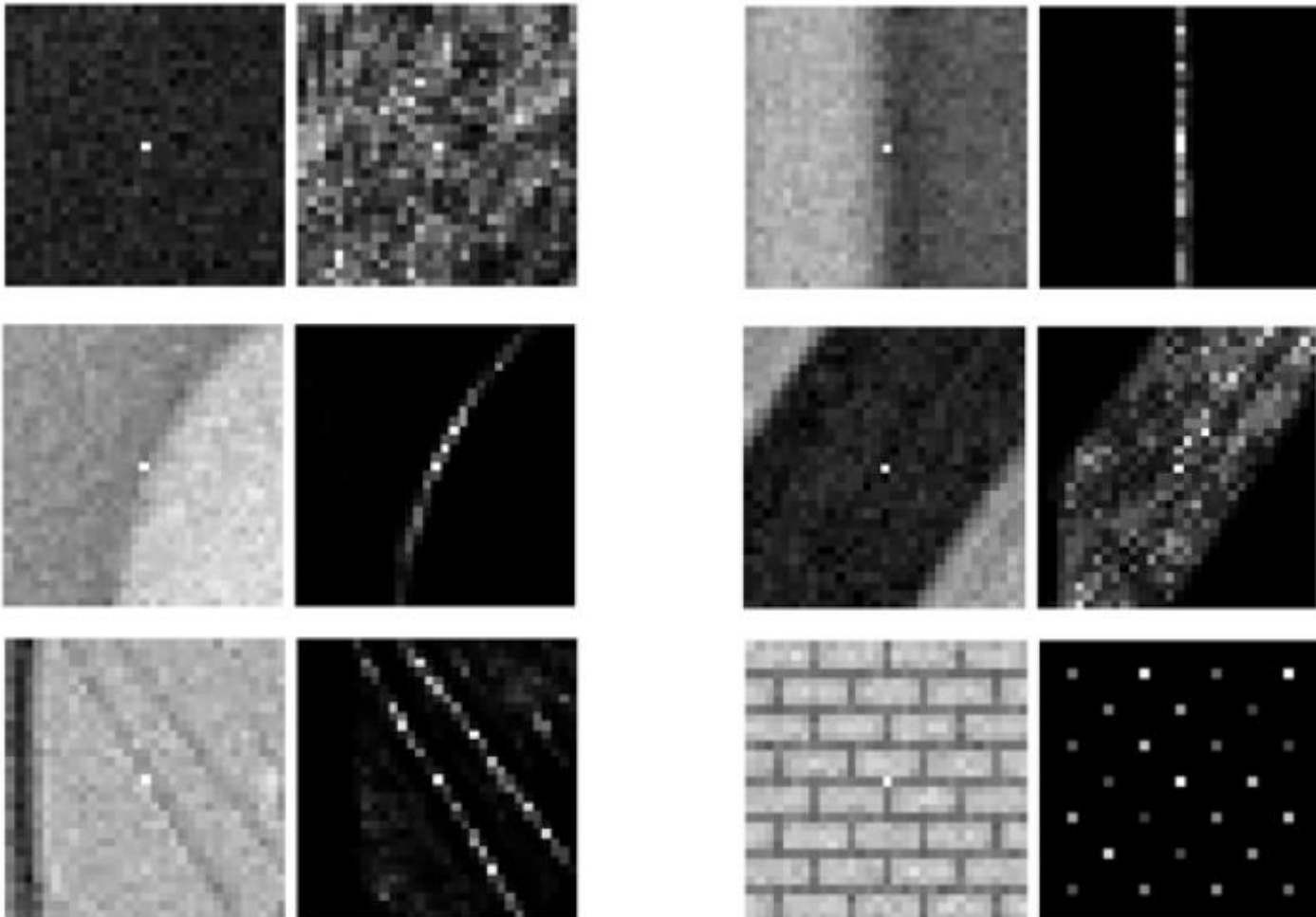
Filtre NL means

- Poids $w(x,p)$:
Ils donnent de l'importance
aux régions
similaires



Filtre NL means

- Poids $w(x,p)$ pour images bruitées



Filtre NL Means

Exemples de résultats

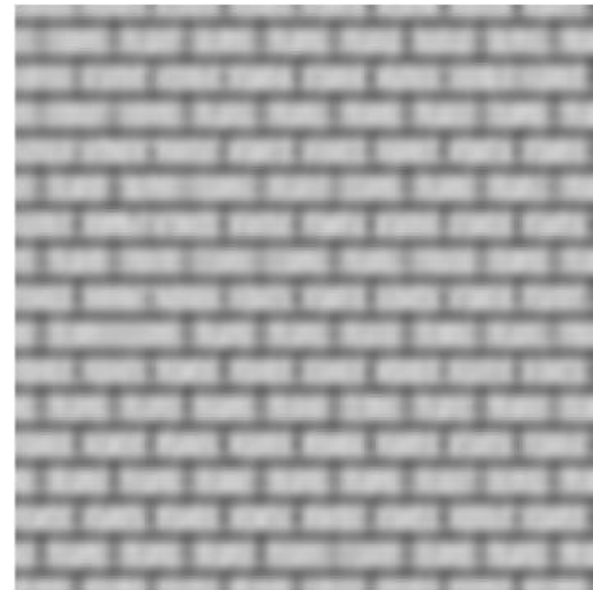
- Comparaison au filtre gaussien



Noisy



Gauss Filtered



NL-Means

Filtres non-locaux

NL-Means Filter (Buades 2005)

- Bilateral Filter



Filtres non-locaux

NL-Means Filter (Buades 2005)

- NL-Means:

Sharp,
Low noise,
Few artifacts.



Filtre NL means

- Débruitage de surfaces



Noisy

Mean Curvature Smoothing

NL-Means

- Considéré comme le meilleur filtre débruiteur aujourd'hui
- Pb du filtre NL means : très lent...

Références

- Cours B Nazarian, Imagerie numérique, Centre IRMf La Timone
- Cours R Zapata, Vision, LIRMM, Univ. Montpellier
- Cours C. Fernandez-Maloigne, Vision artificielle, IRCOM-SIC, Univ. Poitiers
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- Cours A. Dieterlen, Traitement d'images
- Cours X. Clady, Traitement d'images
- Filters: Linear to Nonlinear, Local to Nonlocal, Todd Wittman, College of Charleston, 2012
- Non local image processing, JM Morel & Capo 2011
- Cours Julien Lefevre, Univ Aix Marseille