

$$f_i = BE_i^{spd} Pr_{spd} + \sum_{j=1}^N BE_{ij} Pr_{pd} - \sum_{j=1}^N SE_{ij} (Pr_{pd} + Pr_{ij}). \quad (1)$$

$$\begin{aligned} F &= \sum_{i=1}^N f_i = \sum_{i=1}^N BE_i^{spd} Pr_{spd} + \sum_{i=1}^N \sum_{j=1}^N BE_{ij} Pr_{pd} - \sum_{i=1}^N \sum_{j=1}^N SE_{ij} (Pr_{pd} + Pr_{ij}) \\ &= \sum_{i=1}^N BE_i^{spd} Pr_{spd} - \sum_{i=1}^N \sum_{j=1}^N SE_{ij} Pr_{ij} \\ &= \sum_{i=1}^N BE_i^{spd} Pr_{spd} - \sum_{i=1}^N \sum_{j=1}^N BE_{ij} Pr_{ij} \end{aligned} \quad (2)$$

$$\begin{aligned} \text{subject to : } &\sum_{i=1}^N BE_i^{spd} + \sum_{i=1}^N \sum_{j=1}^N BE_{ij} = E_0 \\ &\sum_{j=1}^N SE_{ij} \leq (RE_i + PE_i) - CE_i^s \end{aligned} \quad (3)$$

$$\sum_{i=1}^N \sum_{j=1}^N SE_{ij} \leq \sum_{i=1}^N (RE_i + PE_i) - CE_i^s \quad (4)$$

Equation (2) would have:

$$\begin{aligned} F &= (E_0 - \sum_{i=1}^N \sum_{j=1}^N BE_{ij}) Pr_{spd} - \sum_{i=1}^N \sum_{j=1}^N BE_{ij} Pr_{ij} \\ &= E_0 Pr_{spd} - \sum_{i=1}^N \sum_{j=1}^N BE_{ij} (Pr_{spd} + Pr_{ij}) \end{aligned} \quad (5)$$

Therefore:

$$\text{Min } F = \text{Min } (E_0 Pr_{spd} - \sum_{i=1}^N \sum_{j=1}^N BE_{ij} (Pr_{spd} + Pr_{ij})) \quad (6)$$

$$\begin{aligned} &= E_0 Pr_{spd} - \text{Max } \sum_{i=1}^N \sum_{j=1}^N BE_{ij} (Pr_{spd} + Pr_{ij}) \\ &= E_0 Pr_{spd} - \text{Max } \sum_{j=1}^N \sum_{i=1}^N SE_{ji} (Pr_{spd} + Pr_{ji}) \end{aligned} \quad (7)$$

According to (4), equation (7) would have a minimum if and only if:

$$\sum_{i=1}^N \sum_{j=1}^N SE_{ij} = \sum_{i=1}^N (RE_i + PE_i) - CE_i^s \quad (8)$$