

RIS

March 13, 2020

RIS in Ternary Alloys

1. Fractional concentration

$$X_{Fe} = \Omega C_{Fe}$$

$$X_{Cr} = \Omega C_{Cr}$$

$$X_{Ni} = \Omega C_{Ni}$$

Where Average atomic volume

$$\Omega = \frac{1}{N}$$

Atomic density

$$N = 9.1 \times 10^{28} \text{ \#} / m^3$$

2. Continuity equations

$$\frac{dX_{Fe}}{dt} = -\Omega \times \nabla J_{Fe}$$

$$\frac{dX_{Cr}}{dt} = -\Omega \times \nabla J_{Cr}$$

$$\frac{dX_{Ni}}{dt} = -\Omega \times \nabla J_{Ni}$$

$$\frac{dX_v}{dt} = -\Omega \times \nabla J_v + G_v - R \times X_v \times X_i$$

$$\frac{dX_i}{dt} = -\Omega \times \nabla J_i + G_i - R \times X_v \times X_i$$

3. Flux equation for atoms and defects

$$\Omega \times J_{Fe} = -\alpha D_{Fe}(1 - X_{Fe}) \nabla X_{Fe} + [\alpha D_{Cr} \nabla X_{Cr} + \alpha D_{Ni} \nabla X_{Ni} + (d_{Fe}^v - D_v) \nabla X_v + (D_i - d_{Fe}^i) \nabla X_i] X_{Fe}$$

$$\Omega \times J_{Cr} = -\alpha D_{Cr}(1 - X_{Cr}) \nabla X_{Cr} + [\alpha D_{Fe} \nabla X_{Fe} + \alpha D_{Ni} \nabla X_{Ni} + (d_{Cr}^v - D_v) \nabla X_v + (D_i - d_{Cr}^i) \nabla X_i] X_{Cr}$$

$$\Omega \times J_{Ni} = -\alpha D_{Ni}(1 - X_{Ni}) \nabla X_{Ni} + [\alpha D_{Cr} \nabla X_{Cr} + \alpha D_{Fe} \nabla X_{Fe} + (d_{Ni}^v - D_v) \nabla X_v + (D_i - d_{Ni}^i) \nabla X_i] X_{Ni}$$

$$\Omega \times J_v = -D_v \nabla X_v + \alpha X_v (d_{Fe}^v \nabla X_{Fe} + d_{Cr}^v \nabla X_{Cr} + d_{Ni}^v \nabla X_{Ni})$$

$$\Omega \times J_i = -D_i \nabla X_i - \alpha X_i (d_{Fe}^i \nabla X_{Fe} + d_{Cr}^i \nabla X_{Cr} + d_{Ni}^i \nabla X_{Ni})$$

4. Diffusion coefficients

$$D_{Fe} = d_{Fe}^v X_v + d_{Fe}^i X_i$$

$$D_{Cr} = d_{Cr}^v X_v + d_{Cr}^i X_i$$

$$D_{Ni} = d_{Ni}^v X_v + d_{Ni}^i X_i$$

$$D_v = d_{Fe}^v X_{Fe} + d_{Cr}^v X_{Cr} + d_{Ni}^v X_{Ni}$$

$$D_i = d_{Fe}^i X_{Fe} + d_{Cr}^i X_{Cr} + d_{Ni}^i X_{Ni}$$

5. Diffusivities

Vacancies

$$\lambda_a^v = \lambda$$

$$d_{Fe}^v = v_{Fe}^v (\lambda_a^v)^2$$

$$d_{Cr}^v = v_{Cr}^v (\lambda_a^v)^2$$

$$d_{Ni}^v = v_{Ni}^v (\lambda_a^v)^2$$

Interstitial

$$\lambda_a^i = \sqrt{\frac{2}{3}} \lambda$$

$$d_{Fe}^i = v_{Fe}^i (\lambda_a^i)^2$$

$$d_{Cr}^i = v_{Cr}^i (\lambda_a^i)^2$$

$$d_{Ni}^i = v_{Ni}^i (\lambda_a^i)^2$$

6. Jump frequency

$$v_{Fe}^v = v_{Fe}^{v,0} e^{-\frac{E_{Fe}^{v,m}}{k_b T}}$$

$$v_{Cr}^v = v_{Cr}^{v,0} e^{-\frac{E_{Cr}^{v,m}}{k_b T}}$$

$$v_{Ni}^v = v_{Ni}^{v,0} e^{-\frac{E_{Ni}^{v,m}}{k_b T}}$$

$$v_{Fe}^i = f^i v_{Fe}^{i,0} e^{-\frac{E_{Fe}^{i,m}}{k_b T}}$$

$$v_{Cr}^i = f^i v_{Cr}^{i,0} e^{-\frac{E_{Cr}^{i,m}}{k_b T}}$$

$$v_{Ni}^i = f^i v_{Ni}^{i,0} e^{-\frac{E_{Ni}^{i,m}}{k_b T}}$$

7. Migration energy
 Pair interaction energy
 Like atoms

$$E_{CrCr} = \frac{2E_{coh}^{Cr}}{Z}$$

$$E_{FeFe} = \frac{2E_{coh}^{Fe}}{Z}$$

$$E_{NiNi} = \frac{2E_{coh}^{Ni}}{Z}$$

Unlike atoms

$$E_{NiCr} = \frac{E_{NiNi} + E_{CrCr}}{2} - E_{NiCr}^{ord}$$

$$E_{FeCr} = \frac{E_{FeFe} + E_{CrCr}}{2} - E_{FeCr}^{ord}$$

$$E_{FeNi} = \frac{E_{FeFe} + E_{NiNi}}{2} - E_{FeNi}^{ord}$$

Atoms and vacancies

$$E_{Cr-v} = \frac{E_{coh}^{Cr} + E_f^{Cr-v}}{Z}$$

$$E_{Ni-v} = \frac{E_{coh}^{Ni} + E_f^{Ni-v}}{Z}$$

$$E_{Fe-v} = \frac{E_{coh}^{Fe} + E_f^{Fe-v}}{Z}$$

Saddle point energy

$$ES_{pure}^{Cr} = E_m^{Cr-v} + Z(E_{CrCr} + E_{Cr-v})$$

Vacancy migration energy

$$E_{Fe}^{v,m} = C_{Fe}(-\frac{3}{2}E_{Fe}^{coh} + \frac{1}{2}E_{Fe,pure}^{v,m} - \frac{1}{2}E_{Fe}^{v,f}) + C_{Cr}(-E_{Fe}^{coh} - \frac{1}{2}E_{Cr}^{coh} + \frac{1}{2}E_{Cr,pure}^{v,m} - \frac{1}{2}E_{Cr}^{v,f} - ZE_{FeCr}^{ord}) + C_{Ni}(-E_{Fe}^{coh} - \frac{1}{2}$$

$$E_{Cr}^{v,m} = C_{Cr}(-\frac{3}{2}E_{Cr}^{coh} + \frac{1}{2}E_{Cr,pure}^{v,m} - \frac{1}{2}E_{Cr}^{v,f}) + C_{Fe}(-E_{Cr}^{coh} - \frac{1}{2}E_{Fe}^{coh} + \frac{1}{2}E_{Fe,pure}^{v,m} - \frac{1}{2}E_{Fe}^{v,f} - ZE_{FeCr}^{ord}) + C_{Ni}(-E_{Cr}^{coh} - \frac{1}{2}$$

$$E_{Ni}^{v,m} = C_{Ni}(-\frac{3}{2}E_{Ni}^{coh} + \frac{1}{2}E_{Ni,pure}^{v,m} - \frac{1}{2}E_{Ni}^{v,f}) + C_{Fe}(-E_{Ni}^{coh} - \frac{1}{2}E_{Fe}^{coh} + \frac{1}{2}E_{Fe,pure}^{v,m} - \frac{1}{2}E_{Fe}^{v,f} - ZE_{FeNi}^{ord}) + C_{Cr}(-E_{Ni}^{coh} - \frac{1}{2}$$

Interstitial migration energy

$$E^{i,m} = 0.9eV$$

7. Defect production rate

$$G_v = \eta\phi + \rho D_v (X_v^{th} - X_v)$$

$$X_v^{th} = e^{\frac{s^v f}{k_b}} e^{-\frac{E^v f}{k_b T}}$$

$$G_i = \eta\phi + \rho D_i (X_i^{th} - X_i)$$

$$X_v^{th} = small$$

$$R = [(\nu_{Fe}^v + \nu_{Fe}^i)X_{Fe} + (\nu_{Cr}^v + \nu_{Cr}^i)X_{Cr} + (\nu_{Ni}^v + \nu_{Ni}^i)X_{Ni}]Z$$

Algorithms

- 1) Input data
- 2) Set up all variables
- 3) Claculate energies, jump frequencies, diffusivities, diffusion coefficients
- 4) Discretize fractional concentrations
- 5) Apply PDE solver to continuity equations
- 6) Output fractional concentration tensor (LCETCE5)

Solving Partial Differential Equations

A method of lines for partial differential equations (PDEs) where one reduces a PDE to a system of ODE and then applies standard methods.

$$\frac{\partial u(x, t)}{\partial t} = \beta \frac{\partial^2 u(x, t)}{\partial x^2} + f(x, t), x \in [0, L], t \in [0, T]$$

$$u(0, t) = s(t), t \in [0, T]$$

$$\frac{\partial}{\partial x} u(L, t) = 0, t \in [0, T]$$

$$u(x, 0) = I(x), x \in [0, L]$$

Discretizing the 2nd-order derivative in space with a finite difference on a mesh

$$x_i = i\Delta x, i = 1, \dots, N - 1$$

then ODE:

$$\frac{\partial u_i(t)}{\partial t} = \beta \frac{u_{i+1}(t) - 2u_i(t) + u_{i-1}(t)}{\Delta x^2} + f_i(t), i = 1, \dots, N - 1$$

The boundary condition on $x=0$, $u(0,t)=s(t)$, gives rise to the ODE

$$u'_0 = s'(t), u_0(0) = s(0)$$

At the other end, $x=L$, we use a centered difference approximation The boundary condition on $x=L$, $u(L,t)=s(t)$, gives rise to the ODE

$$\frac{u_{N+1}(t) - u_{N-1}(t)}{2\Delta x} = 0$$

and combine it with the scheme for $i=N$ to obtain the modified boundary ODE

$$\frac{\partial u_N(t)}{\partial t} = \beta \frac{2u_{N-1}(t) - 2u_N(t)}{\partial x^2} + f_N(t)$$

To summarize, the ODE system reads

$$\begin{aligned} \frac{du_0}{dt} &= s'(t) \\ \frac{du_i}{dt} &= \frac{\beta}{\Delta x^2} (u_{i+1}(t) - 2u_i(t) + 2u_{i-1}(t)) + f_i(t), i = 1, \dots, N-1 \\ \frac{du_N}{dt} &= \frac{2\beta}{\Delta x^2} (u_{N-1}(t) - u_N(t)) + f_i(t) \end{aligned}$$

The initial conditions are

$$\begin{aligned} u_0(0) &= s(0) \\ u_i(0) &= I(x_i), i = 1, \dots, N \end{aligned}$$

Points

6/03/2020 Compléter des unités pour chaque paramètre Rlier une variable et son unité Rendre des variables en ordre et lisible Evaluer des algorithmes en fonction de la complexité en temps

13/03/2020 Distinguer des paramètres physiques et ceux-ci numériques Faire une table de tous les parameters avec certaines sets

```
[0]: """
Python version:
This code need Python 2.7 compile environment beacause of a package odespy.

Install odespy:
This operation as followed is uniquely supported in Google Colab. If you use
another platform such as Anaconda, please remove this line and look over a
website https://github.com/hplgit/odespy to install odespy.

No other requirements:
Despite Odespys many dependencies on other software, you can run the basic
solvers implemented in pure Python without any additional software packages.
"""

!pip install git+https://github.com/hplgit/odespy.git
```

```
[0]: # -*- coding: utf-8 -*-
"""
Created on Fri Feb 28 08:50:29 2020

@author: Chao PAN

Simulation for RIS with model MIK (Modified Inverse Kirkendall)
Ternary Alloys Ee-Cr-Ni

This program calculates the amount of radiation induced segregation for a
ternary concentrated alloy. The formulation is based on the perks model
and is solved numerically using the gear subroutines.
```

```

"""

#import odespy
import numpy as np
import matplotlib.pyplot as plt

#####File name#####
ERROR_FILE, OUTPUT_FILE = "error.txt", "output.txt"
#####File name#####

#####Input to MIK#####
# Distance to mesh groups (m)
R1, R2, RF = 4.0, 18.0, 2018.0

# No. of points in mesh groups
N1, N2, N3 = 16, 14, 20

# Input time setp to gear
HO = 1e-9

# Error control parameter
EPS = 1e-9

# Peak displacement rate (dpa/s)
DISPRT = 1.4e-6

# Vacancy/Interstitial production efficiency
ETAV, ETAI = 1.0, 1.0

# Dose
DOSE = 1.0

# Peak temperature (°C)
TEMPC = 360.

# Concentration of B, C (fractional concentration %)
CONCB, CONCC = 0.21, 0.09

# Peak dislocation density (#/m2)
DISL = 1e14

# No. density (#/m3)
NAT = 9.1e28

# Jump distance (m)
LAMBDA = 3.5e-10

```

```

# Jump correlation factors for A, B, C, interstitial
FAV, FBV, FCV, FI = 0.785, 0.668, 0.872, 0.660

# Relative vacancy jump frequency ratio for A, B, C
# 1.6(1.4), 2.4(2.3) 1.0 or 1.866666666666, 3.3333333333
WAV, WBV, WCV = 1.8, 3.2, 1.0

# Relative interstitial jump frequency ratio for A, B, C
WAI, WBI, WCI = 1.0, 1.0, 1.0

# Cohesive energies: -4.28, -4.10, -4.44 (eV)
ECOHA, ECOHB, ECOHC = -4.28, -4.10, -4.44

# Interstitial migration energies for A, B, C (eV)
EMIA, EMIB, EMIC = 0.9, 0.9, 0.9

# Vacancy formation enthalpy (=kb)
SV = 1.0

# Pure element [vacancy] migratio energies for A, B, C (eV)
EMA, EMB, EMC = 1.28, 0.97, 1.04

# Pure element [vacancy] formation energies for A, B, C (eV)
EFA, EFB, EFC = 1.4, 1.6, 1.79

# Grain boundary formation energy (eV)
EFGB = 1.4

# Ordering energies (eV)
EORDAB, EORDAC, EORDBC = 0.003, -0.001, 0.005

# Debye frequencies (/s)
NUOV, NUOI = 1.5e13, 1.5e12

# Thermo factor
AL = 1.0

# Neighbor atoms
Z = 12.0

# Dislocation bias for vacancy/interstitial
BIASV, BIASI = 1.0, 1.0

# User-required output times
TOUTPT = [1e-0, 1e1, 5e2, 1e3, 5e3, 1.4e4, 5e4, 7.1e4, 1e5, 1.4e5, 3.6e5,
          4.3e5, 7.1e5, 2.1e6, 2.2e6, 2.3e6, 5e6, 7e7, 1e8, 0e0]

```

```

# Indicator whether profiles will be used
FRAC = "N"

# Fraction of max temperature
TFRAC = [1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0,
          1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0]

# Fraction of peak atom A
CAFRAC = [1.0000, 1.0000, 1.0000, 1.0000, 1.0000, 1.0000, 1.0000, 1.0000,
           1.0000, 1.0000, 1.0000, 1.0000, 1.0000, 1.0000, 1.0000]

# Fraction of peak atom B
CBFRAC = [0.1231, 0.2991, 0.3912, 0.4573, 0.5100, 0.6988, 0.8144, 0.8969,
           0.9613, 1.0150, 1.0000, 1.0000, 1.0000, 1.0000, 1.0000]

# Fraction of peak atom C
CCFRAC = [1.1670, 1.1334, 1.1160, 1.1033, 1.0933, 1.0574, 1.0354, 1.0196,
           1.0074, 0.9971, 1.0000, 1.0000, 1.0000, 1.0000, 1.0000]

# Fraction of peak damage
DFRAC = [1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0,
          1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0]

# Fraction of max dislocation density
SFRAC = [1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0,
          1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0]
#####Input to MIK#####

#####Constant#####
# Boltzmann constant = 1.38064852e-23 m2.kg/s/K
BOLTZ = 8.617e-5

#
SCFAC = 1e-9
#####Constant#####

#####Global variables#####
# Time steps
NSTEP = N1+N2+N3
N = 5*NSTEP

# Concentration of A
CONCA = 1.0-(CONCB+CONCC)

# Fraction of max temperature, peak atoms, damage, max dislocation density

```



```

# Profiles will not be used
if FRAC == "N":
    TFRAC = np.ones(NSTEP)
    CAFRAC = np.ones(NSTEP)
    CBFRAC = np.ones(NSTEP)
    CCFRAC = np.ones(NSTEP)
    SFRAC = np.ones(NSTEP)
    DFRAC = np.ones(NSTEP)
else:
    _temp = np.zeros(NSTEP)

    _temp[:NSTEP-1] = TFRAC[:NSTEP-1]
    # TFRAC = np.zeros(NSTEP)
    TFRAC[:NSTEP-1] = _temp[:NSTEP-1]

    _temp[:NSTEP] = CAFRAC[:NSTEP]
    CAFRAC = np.zeros(NSTEP)
    CAFRAC[:NSTEP] = _temp[:NSTEP]

    _temp[:NSTEP] = CBFRAC[:NSTEP]
    CBFRAC = np.zeros(NSTEP)
    CBFRAC[:NSTEP] = _temp[:NSTEP]

    _temp[:NSTEP] = CCFRAC[:NSTEP]
    CCFRAC = np.zeros(NSTEP)
    CCFRAC[:NSTEP] = _temp[:NSTEP]

    _temp[:NSTEP] = SFRAC[:NSTEP]
    SFRAC = np.zeros(NSTEP)
    SFRAC[:NSTEP] = _temp[:NSTEP]

    _temp[:NSTEP] = DFRAC[:NSTEP]
    DFRAC = np.zeros(NSTEP)
    DFRAC[:NSTEP] = _temp[:NSTEP]
    del _temp
#####Global variables#####

class RIS:
    """
    Simulation of RIS is based on MIK
    """
    def __init__(self):
        """
        Initialise model including variables and files.
        Seu up all variables for this model, including concentrations, fluxes,
        diffusivities, geometry, defects, temperature, energy etc.
        Arguments:

```

```

        None
    Return:
        None
    """
    # Variables
    self.X_Fe_fraction = np.ones(NSTEP)
    self.X_Cr_fraction = np.ones(NSTEP)
    self.X_Ni_fraction = np.ones(NSTEP)
    self.T_fraction = np.ones(NSTEP)
    self.Damage_fraction = np.ones(NSTEP)
    self.Max_dislocation_density = np.ones(NSTEP)
    if FRAC == "N":
        SFRAC = np.ones(NSTEP)
        DFRAC = np.ones(NSTEP)
    # Dose
    self.DOSE = DOSE
    # Time
    self.TOUT = 0.0
    self.TSTOP = DOSE/DISPRT
    #
    self.NOUT = 0

    # Temperature
    self.TEMP = (TEMPC+273)*TFRAC
    self.TKT = BOLTZ*self.TEMP

    # Concentrations
    self.CA = CONCA*CAFRAC
    self.CB = CONCB*CBFRAC
    self.CC = CONCC*CCFRAC
    self.CI = np.zeros(NSTEP)
    self.CVOTHER = self.set_CVOTHER()
    self.CV = self.CVOTHER.copy()
    self.CERR = np.zeros(NSTEP)
    self.NA = np.zeros(NSTEP)
    self.NB = np.zeros(NSTEP)
    self.NC = np.zeros(NSTEP)
    self.NV = np.zeros(NSTEP)
    self.NI = np.zeros(NSTEP)
    # Gradient
    self.GRADCA = np.zeros(NSTEP)
    self.GRADCB = np.zeros(NSTEP)
    self.GRADCC = np.zeros(NSTEP)
    self.GRADCV = np.zeros(NSTEP)
    self.GRADCI = np.zeros(NSTEP)

    #

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```

self.CADOT = np.zeros(NSTEP)
self.CBDOT = np.zeros(NSTEP)
self.CCDOT = np.zeros(NSTEP)
self.CVDOT = np.zeros(NSTEP)
self.CIDOT = np.zeros(NSTEP)
self.RECOMB = np.zeros(NSTEP)
self.INTSINK = np.zeros(NSTEP)
self.VACSINK = np.zeros(NSTEP)
self.VACSOOR = np.zeros(NSTEP)

# Energy
self.EAA = self.calculate_energy("A", "A")
self.EBB = self.calculate_energy("B", "B")
self.ECC = self.calculate_energy("C", "C")
self.EAB = self.calculate_energy("A", "B")
self.EAC = self.calculate_energy("A", "C")
self.EBC = self.calculate_energy("B", "C")
self.EAV = self.calculate_energy("A", "V")
self.EBV = self.calculate_energy("B", "V")
self.ECV = self.calculate_energy("C", "V")
self.ESA = self.calculate_energy("S", "A")
self.ESB = self.calculate_energy("S", "B")
self.ESC = self.calculate_energy("S", "C")
self.EA = self.calculate_energy("A", "VM")
self.EB = self.calculate_energy("B", "VM")
self.EC = self.calculate_energy("C", "VM")

# Jump frequency between defects (vacancy or interstitial)
# and atoms (Fe, Cr, Ni)
self.NUIA = self.calculate_NU_dk("I", "A")
self.NUIB = self.calculate_NU_dk("I", "B")
self.NUIC = self.calculate_NU_dk("I", "C")
self.NUVA = self.calculate_NU_dk("V", "A")
self.NUVB = self.calculate_NU_dk("V", "B")
self.NUVC = self.calculate_NU_dk("V", "C")

# Diffusivities
self.DAI = self.calculate_D_dk("I", "A")
self.DBI = self.calculate_D_dk("I", "B")
self.DCI = self.calculate_D_dk("I", "C")
self.DAV = self.calculate_D_dk("V", "A")
self.DBV = self.calculate_D_dk("V", "B")
self.DCV = self.calculate_D_dk("V", "C")
self.RECA = self.set_REC_k("A")
self.RECB = self.set_REC_k("B")
self.RECC = self.set_REC_k("C")
self.DA = self.calculate_D_dk(None, "A")

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```

self.DB = self.calculate_D_dk(None, "B")
self.DC = self.calculate_D_dk(None, "C")
self.DV = self.calculate_D_dk("V", None)
self.DI = self.calculate_D_dk("I", None)
self.DIFV = self.calculate_D_dk("V", None)
self.DIFI = self.calculate_D_dk("I", None)

# Geometry
self.MESHSP = np.zeros(NSTEP)
self.XVALUE = np.zeros(NSTEP)
self.MESHSI = np.zeros(NSTEP)

# Fluxes
self.JA = np.zeros(NSTEP)
self.JB = np.zeros(NSTEP)
self.JC = np.zeros(NSTEP)
self.JV = np.zeros(NSTEP)
self.JI = np.zeros(NSTEP)
self.JO = np.zeros(NSTEP)
self.JAO = 0.0
self.JBO = 0.0
self.JCO = 0.0
self.DIVJA = np.zeros(NSTEP)
self.DIVJB = np.zeros(NSTEP)
self.DIVJC = np.zeros(NSTEP)
self.DIVJV = np.zeros(NSTEP)
self.DIVJI = np.zeros(NSTEP)

# Defects
self.DISLOC = DISL*SFRAC
self.DISPV = np.zeros(NSTEP)
self.DISPI = np.zeros(NSTEP)

# Displacement of vacancy/interstitial
self.DISPV = self.calculate_displacement_d("V")
self.DISPI = self.calculate_displacement_d("I")

#
# YO[N], Y[N], YDOT[N], RWORK[N**2+20], IWORK[2*N+20]
self.YO = np.zeros(N)
self.YO[:NSTEP] = self.CA
self.YO[NSTEP:2*NSTEP] = self.CB
self.YO[2*NSTEP:3*NSTEP] = self.CC
self.YO[3*NSTEP:4*NSTEP] = self.CV
self.YO[4*NSTEP:] = self.CI
self.Y = np.zeros(N)
self.YDOT = np.zeros(N)

```

```

self.RWORK = np.zeros(N**2+20)
self.IWORK = np.zeros(2*N+20)
self.XOUT = np.zeros(NSTEP)

#
self.MF = 0
self.IERR = 0
self.ITOL = 0
self.IOPT = 0
self.ITASK = 0
self.ISTEP = 0
self.TO = 0

#
self.EPSA = 0.0

#
self.PSTOP = "N"

self.fn = ""
self.flag = True

#
self.PD = np.zeros(NSTEP)

def main(self):
    """

    """
    self.empty_files()

    self.write_input_data()

    # Mesh grid
    self.mesh()

    while self.V["PSTOP"] == "N":
        self.preprocess()
        if self.V["PSTOP"] == "Y":
            break
        self.fex()
        self.solve()
        if self.IERR < -1:
            with open(ERROR_FILE, 'a+') as f:
                f.write("ERROR RETURN WITH IERR= {} \n".format(self.IERR))
            print("Terminated with error")
            return

```

```

        elif self.IERR == -1:
            self.IERR = 2
        else:
            pass
        self.output()
        print("Completed")

def set_CVTHER(self):
    """
    """
    CVTHER = np.exp(SV)*np.exp(-EFGB/self.TKT)
    CVTHER[-1] = CVTHER[-2]
    for i in range(1, NSTEP-1):
        CVTHER[i] = 0.5*(CVTHER[i]+CVTHER[i-1])
    return CVTHER

def set_REC_k(self, k):
    """
    """
    return Z*(eval("self.NUI"+k)+eval("self.NUV"+k))

def set_GRAD_C(self, token):
    """
    """
    _res = np.zeros(NSTEP)
    _res[:-1] = eval("self.C"+token)[1:]-eval("self.C"+token)[: -1]
    _res = _res/self.MESHSP
    return _res

def empty_files(self):
    """
    Clean up all contents of ancient files. This operation is usually
    done at the beginning of one simulation.
    """
    # Clean up ancient files
    for FILE in [ERROR_FILE, OUTPUT_FILE]:
        with open(FILE, "w") as f:
            f.write("")

def set_DIVJ(self):
    """
    """
    self.DIVJA[0] = 2.0*(self.JA[0]-self.JAO)/self.MESHSP[0]
    self.DIVJB[0] = 2.0*(self.JB[0]-self.JBO)/self.MESHSP[0]
    self.DIVJC[0] = 2.0*(self.JC[0]-self.JCO)/self.MESHSP[0]

```

```

self.MESHSI[1:-1] = 0.5*(self.MESHSP[1:-1]+self.MESHSP[:-2])
self.DIVJA[1:-1] = (self.JA[1:-1]-self.JA[:-2])/self.MESHSI[1:-1]
self.DIVJB[1:-1] = (self.JB[1:-1]-self.JB[:-2])/self.MESHSI[1:-1]
self.DIVJC[1:-1] = (self.JC[1:-1]-self.JC[:-2])/self.MESHSI[1:-1]
self.DIVJV[1:-1] = (self.JV[1:-1]-self.JV[:-2])/self.MESHSI[1:-1]
self.DIVJI[1:-1] = (self.JI[1:-1]-self.JI[:-2])/self.MESHSI[1:-1]

self.DIVJA[-1] = 2.0*(self.JA[-1]-self.JA[-2])/self.MESHSP[-2]
self.DIVJB[-1] = 2.0*(self.JB[-1]-self.JB[-2])/self.MESHSP[-2]
self.DIVJC[-1] = 2.0*(self.JC[-1]-self.JC[-2])/self.MESHSP[-2]
self.DIVJV[-1] = 2.0*(self.JV[-1]-self.JV[-2])/self.MESHSP[-2]
self.DIVJI[-1] = 2.0*(self.JI[-1]-self.JI[-2])/self.MESHSP[-2]

```

```

def calculate_energy(self, i, j):

```

```

    """

```

For like atoms, the pair interaction energy is the cohesive energy, E_{coh} divided by the number of nearest neighbor bond pairs.

```

e.g. EAA = ECOHA/(Z/2)
     EBB = ECOHB/(Z/2)
     ECC = ECOHC/(Z/2)

```

For unlike atoms, pair interaction energies are determined from the average value of the like-atom pair energies less any ordering energy.

```

e.g. EAB = 0.5*(EAA+EBB)-EORDAB
     EAC = 0.5*(EAA+ECC)-EORDAC
     EBC = 0.5*(EBB+ECC)-EORDBC

```

For atoms and vacancies, pair interaction energies is fitted to the formation energy of the pure metal.

```

e.g. EAV = (ECOHA+EFA)/Z
     EBV = (ECOHB+EFB)/Z
     ECV = (ECOHC+EFC)/Z

```

The saddle point energy in the pure metal

```

e.g. ESA = EMA+Z*(EAA+EAV)
     ESB = EMB+Z*(EBB+EBV)
     ESC = EMC+Z*(ECC+ECV)

```

The migration energy for Cr, Ni and Fe via vacancies can be expressed as:

```

EA(I)=(ESA+ESA*NA(I)+ESB*NB(I)+ESC*NC(I))/2-
      ((Z*(NA(I)*EAA+NB(I)*EAB+NC(I)*EAC+NV(I)*EAV))
      +(Z*(NA(I)*EAV+NB(I)*EBV+NC(I)*ECV)))
EB(I)=(ESB+ESA*NA(I)+ESB*NB(I)+ESC*NC(I))/2-
      ((Z*(NA(I)*EAB+NB(I)*EBB+NC(I)*EBC+NV(I)*EBV))
      +(Z*(NA(I)*EAV+NB(I)*EBV+NC(I)*ECV)))
EC(I)=(ESC+ESA*NA(I)+ESB*NB(I)+ESC*NC(I))/2-

```

```

        ((Z*(NA(I)*EAC+NB(I)*EBC+NC(I)*ECC+NV(I)*ECV))
        +(Z*(NA(I)*EAV+NB(I)*EBV+NC(I)*ECV)))
Arguments:
    i: atom (Fe, Cr, Ni) or defect (vacancy, interstitial) or
        saddle point
    j: atom (Fe, Cr, Ni) or defect (Vacancy, interstitial) or
        saddle point
Return:
    Energy (Migration energy, saddle point energy) value in float
    """
    _atoms = ["A", "B", "C"]
    _res = 0
    if i in _atoms and j in _atoms:
        # Like atoms
        if i == j:
            _res = eval("ECOH{}".format(i))/(Z/2)
        # Unlike atoms
        else:
            _res = 0.5*(eval("self.E"+i+i)+
                        eval("self.E"+j+j))-eval("EORD"+i+j)
    # Interaction energy between atoms and vacancies
    elif i in _atoms and j == "V":
        _res = (eval("ECOH"+i)+eval("EF"+i))/Z
    # Migration energy for Fe Cr Ni via vacancies
    elif i in _atoms and j == "VM":
        _term1 = (eval("self.ES"+i)+self.ESA*self.NA+self.ESB*self.NB+
                  self.ESC*self.NC)/2
        if i == "A":
            _term2 = Z*(self.NA*self.EAA+self.NB*self.EAB+
                        self.NC*self.EAC+self.NV*eval("self.E"+i+"V"))
        elif i == "B":
            _term2 = Z*(self.NA*self.EAB+self.NB*self.EBB+
                        self.NC*self.EBC+self.NV*eval("self.E"+i+"V"))
        elif i == "C":
            _term2 = Z*(self.NA*self.EAC+self.NB*self.EBC+
                        self.NC*self.ECC+self.NV*eval("self.E"+i+"V"))
        else:
            assert False, "Wrong arguments: {}".format(i)
        _term3 = (Z*(self.NA*self.EAV+self.NB*self.EBV+self.NC*self.ECV))
        _res = _term1-( _term2+_term3)
    # Saddle point energy
    elif i == "S" and j in _atoms:
        _res = eval("EM"+j)+Z*(eval("self.E"+j+j)+eval("self.E"+j+"V"))
    else:
        assert False, "Wrong arguments: {} {}".format(i, j)
    return _res

```



```

def mesh(self):
    """
    In order to discretize PDE, it is necessary to have a well-mesh grid.
    Arguments:
        MESHSP:
        XVALUE:
    Return:
        None
    """
    # ??? Why ignore last element
    self.MESHSP[:N1-1] = R1*SCFAC/N1
    # ??? Why ignore last element
    self.MESHSP[N1-1:N1+N2-1] = (R2-R1)*SCFAC/N2
    self.MESHSP[N1+N2-1:N1+N2+N3-1] = (R3-R2)*SCFAC/N3

    for i in range(1, NSTEP):
        self.XVALUE[i] = self.XVALUE[i-1]+self.MESHSP[i-1]

def calculate_displacement_d(self, d):
    """
    Defect displacement (vacancy or interstitial) =
    displacement ratio * defect production efficiency * defect fraction
    e.g. DISPV(I)=DISPRT*ETAV*DFRAC(I)
        DISPI(I)=DISPRT*ETAI*DFRAC(I)
    Arguments:
        d: token for defect type (vacancy or interstitial)
    Return:
        array of defect displacement
    """
    return DISPRT*eval("ETA"+d)*DFRAC

def calculate_NU_dk(self, d, k):
    """
    Jump frequency includes vacancy jump frequency and interstitial jump
    frequency.

    Formula:
        
$$NU = NUO * W * F * \exp(-EM/kb/T)$$

    where:
        NU: jump frequency
        NUO: debye frequency
        W: relative defect jump frequency
        EM: defect migration energies
        kb: boltzmann constant
        T: Temperature
        NUO*W*F: standard jump frequency
    """

```

For vacancy jump frequency:

e.g. $NUVA(I) = NUOV * WAV * FAV * \exp((-1 * EA(I) / TKT(I)))$
 $NUVB(I) = NUOV * WBV * FBV * \exp((-1 * EB(I) / TKT(I)))$
 $NUVC(I) = NUOV * WCV * FCV * \exp((-1 * EC(I) / TKT(I)))$

For interstitial jump frequency:

e.g. $NUIA(I) = NUOI * WAI * FI * \exp((-1 * EMIA) / TKT(I))$
 $NUIB(I) = NUOI * WBI * FI * \exp((-1 * EMIB) / TKT(I))$
 $NUIC(I) = NUOI * WCI * FI * \exp((-1 * EMIC) / TKT(I))$

Notion:

A same standard interstitial jump frequency and a same interstitial correlation factor for Fe/Cr/Ni

Arguments:

k: token for one of three (Fe, Cr, Ni)

d: token for one of two (vacancy, interstitial)

return:

array of jump frequency for k and d

"""

if d == "V":

 _res = NUOV*eval("W"+k+"V")*eval("F"+k+"V")*\
 np.exp(-eval("self.E"+k)/self.TKT)

elif d == "I":

 _res = NUOI*eval("W"+k+"I")*FI*np.exp(-eval("EMI"+k)/self.TKT)

else:

 assert False, "Wrong defect type of d={}".format(d)

return _res

def calculate_D_dk(self, d, k):

"""

This function is to calculate diffusivity between atom and defect.

Formula:

$D(d, k) = NU(d, k) * \lambda(d)^2$

where:

D: diffusivity between defects and atoms

lambda(d): unit cell size for defect

NU(d, k): jump frequency between defects and atoms

e.g. $DAIO(I) = 0.66667 * NUIA(I) * LAMBDA ** 2$

$DBIO(I) = 0.66667 * NUIB(I) * LAMBDA ** 2$

$DCIO(I) = 0.66667 * NUIC(I) * LAMBDA ** 2$

$DAV(I) = NUVA(I) * LAMBDA ** 2$

$DBV(I) = NUVB(I) * LAMBDA ** 2$

$DCV(I) = NUVC(I) * LAMBDA ** 2$

Formula:

```
DA(I)=DAV(I)*NV(I)+DAI(I)*NI(I)
DB(I)=DBV(I)*NV(I)+DBI(I)*NI(I)
DC(I)=DCV(I)*NV(I)+DCI(I)*NI(I)
DIFV(I)=DAV(I)*NA(I)+DBV(I)*NB(I)+DCV(I)*NC(I)
DIFI(I)=DAI(I)*NA(I)+DBI(I)*NB(I)+DCI(I)*NC(I)
```

Parameters:

k: token for one of three Fe, Cr, Ni
d: token for one of two defects vacancy, interstitial

return:

array of diffusivity between atom and defect

"""

```
if k is None:
    _res = eval("self.DA"+d)*self.NA+eval("self.DB"+d)*self.NB+\
            eval("self.DC"+d)*self.NC
elif d is None:
    _res = eval("self.D"+k+"V")*self.NV+eval("self.D"+k+"I")*self.NI
else:
    if d == "I":
        _res = 2/3*eval("self.NUI"+k)*LAMBDA**2
    elif d == "V":
        _res = eval("self.NUV"+k)*LAMBDA**2
    else:
        assert False, "Wrong defect type of d={}".format(d)
return _res
```

```
def calculate_J_dk(self, d, k):
```

"""

```
JV(I)=NAT*(-1*DVI)*GRADCV(I)+NV(I)*AL*(DAV(I)*GRADCA(I)+
        DBV(I)*GRADCB(I)+DCV(I)*GRADCC(I))
JI(I)=NAT*(-1*DI(I)*GRADCI(I)-NI(I)*AL*(DAI(I)*GRADCA(I)+
        DBI(I)*GRADCB(I)+DCI(I)*GRADCC(I))
JA(I)=NAT*(-1*DA(I)*AL*GRADCA(I)+NA(I)*(DAV(I)*GRADCV(I)-
        DAI(I)*GRADCI(I)))-JO(I)*NA(I)
JB(I)=NAT*(-1*DB(I)*AL*GRADCB(I)+NB(I)*(DBV(I)*GRADCV(I)-
        DBI(I)*GRADCI(I)))-JO(I)*NB(I)
JC(I)=NAT*(-1*DC(I)*AL*GRADCC(I)+NC(I)*(DCV(I)*GRADCV(I)-
        DCI(I)*GRADCI(I)))-JO(I)*NC(I)
```

"""

```
if k is None:
    _term1 = -1*eval("self.D"+d)*eval("self.GRADC"+d)
    _term2 = eval("self.DA"+d)*self.GRADCA+\
            eval("self.DB"+d)*self.GRADCB+eval("self.DC"+d)*self.GRADCC
    if d == "V":
        _term2 = self.NV*AL*_term2
    elif d == "I":
```

```

        _term2 = -self.NI*AL*_term2
    _res = _term1 + _term2
elif d is None:
    _res = NAT*(-eval("self.D"+k)*AL*eval("self.GRADC"+k)+
                eval("self.N"+k)*(eval("self.D"+k+"V")*self.GRADCV-
                                   eval("self.D"+k+"I")*self.GRADCI))-
                self.J0*eval("self.N"+k)

return _res

def write_input_data(self):
    """Export input data"""
    with open(OUTPUT_FILE, "a+") as f:
        f.write("EPS={}\n".format(EPS))
        f.write("DISPRT={}, ETAV={}, ETAI={}, DOSE={}\n".format(DISPRT,
            ETAV, ETAI, DOSE))
        f.write("TEMP={} °C\n".format(TEMPC))
        f.write("CB={}, CC={}\n".format(CONCB, CONCC))
        f.write("DISL={}, NAT={}, LAMBDA={}\n".format(DISL, NAT, LAMBDA))
        f.write("FAV={}, FBV={}, FCV={}, FI={}\n".format(FAV, FBV, FCV,
            FI))
        f.write("WAV={}, WBV={}, WCV={}\n".format(WAV, WBV, WCV))
        f.write("WAI={}, WBI={}, WCI={}\n".format(WAI, WBI, WCI))
        f.write("ECOHA={}, ECOHB={}, ECOHC={}\n".format(ECOHA, ECOHB,
            ECOHC))
        f.write("EMIA={}, EMIB={}, EMIC={}, SV={}\n".format(EMIA, EMIB,
            EMIC, SV))
        f.write("EMA={}, EMB={}, EMC={}\n".format(EMA, EMB, EMC))
        f.write("EFA={}, EFB={}, EFC={}, EFGB={}\n".format(EFA, EFB,
            EFC, EFGB))
        f.write("EORDAB={}, EORDAC={}, EORDBC={}\n".format(EORDAB, EORDAC,
            EORDBC))
        f.write("NUOV={}, NUOI={}\n".format(NUOV, NUOI))
        f.write("AL={}, Z={}, BIASV={}, BIASI={}\n".format(AL, Z, BIASV,
            BIASI))
        f.write("TFRAC=\n{}\n".format(" ".join(TFRAC.astype(str))))
        f.write("CAFRAC=\n{}\n".format(" ".join(CAFRAC.astype(str))))
        f.write("CBFRAC=\n{}\n".format(" ".join(CBFRAC.astype(str))))
        f.write("CCFRAC=\n{}\n".format(" ".join(CCFRAC.astype(str))))
        f.write("DFRAC=\n{}\n".format(" ".join(DFRAC.astype(str))))
        f.write("SFRAC=\n{}\n".format(" ".join(SFRAC.astype(str))))

def write_error_info(self, _error_info):
    with open(ERROR_FILE, 'a+') as f:
        f.write("ERROR RETURN WITH IERR= {}\n".format(self.IERR))

def preprocess(self):
    """

```

```

"""
if self.ISTEP == 0:
    self.TO = 0
    self.MF = 222
    self.IERR = 1
    self.TOUT = TOUTPT[0]
    self.ISTEP += 1
    self.ITOL = 1
    self.ITASK = 1
    self.IOPT = 1
    self.Y = self.Y0.copy()
    self.IWORK[5] = 1000000
elif self.ISTEP < self.NOUT:
    self.ISTEP += 1
    self.TOUT = TOUTPT[self.ISTEP]
else:
    self.PSTOP = "Y"
    with open(ERROR_FILE, 'a+') as f:
        f.write("Stopping Time Reached\n")

def fex(self, u, t):
    """
    Right-hand side of the ODE
    """
    self.CA = self.Y[:NSTEP]
    self.CB = self.Y[NSTEP:2*NSTEP]
    self.CC = self.Y[2*NSTEP:3*NSTEP]
    self.CV = self.Y[3*NSTEP:4*NSTEP]
    self.CI = self.Y[4:NSTEP]

    self.NA[:NSTEP] = 0.5*(self.CA[1:]+self.CA[:NSTEP])
    self.NB[:NSTEP] = 0.5*(self.CB[1:]+self.CB[:NSTEP])
    self.NC[:NSTEP] = 0.5*(self.CC[1:]+self.CC[:NSTEP])
    self.NV[:NSTEP] = 0.5*(self.CV[1:]+self.CV[:NSTEP])
    self.NI[:NSTEP] = 0.5*(self.CI[1:]+self.CI[:NSTEP])

    self.NUVA = self.calculate_NU_dk("V", "A")
    self.NUVB = self.calculate_NU_dk("V", "B")
    self.NUVC = self.calculate_NU_dk("V", "C")

    self.DAV = self.calculate_D_dk("V", "A")
    self.DBV = self.calculate_D_dk("V", "B")
    self.DCV = self.calculate_D_dk("V", "C")

    self.RECA = self.set_REC_k("A")
    self.RECB = self.set_REC_k("B")

```

```

self.RECC = self.set_REC_k("C")
self.RECA[-1] = self.RECA[-2]
self.RECB[-1] = self.RECB[-2]
self.RECC[-1] = self.RECC[-2]
self.CVOTHER[-1] = self.CVOTHER[-2]
self.DIFV = self.calculate_D_dk("V", None)
self.DIFI = self.calculate_D_dk("I", None)
self.DIFV[-1] = self.DIFV[-2]
self.DIFI[-1] = self.DIFI[-2]
self.RECA[1:-1] = 0.5*(self.RECA[1:-1]+self.RECA[:-2])
self.RECB[1:-1] = 0.5*(self.RECB[1:-1]+self.RECB[:-2])
self.RECC[1:-1] = 0.5*(self.RECC[1:-1]+self.RECC[:-2])
self.CVOTHER[1:-1] = 0.5*(self.CVOTHER[1:-1]+self.CVOTHER[:-2])
self.DIFV[1:-1] = 0.5*(self.DIFV[1:-1]+self.DIFV[:-2])
self.DIFI[1:-1] = 0.5*(self.DIFI[1:-1]+self.DIFI[:-2])

self.JAO = self.JBO = self.JCO = 0.0
self.JA[-1] = self.JB[-1] = self.JC[-1] = 0.0
self.GRADCA = self.set_GRAD_C("A")
self.GRADCB = self.set_GRAD_C("B")
self.GRADCC = self.set_GRAD_C("C")
self.GRADCV = self.set_GRAD_C("V")
self.GRADCI = self.set_GRAD_C("I")
self.DA = self.calculate_D_dk(None, "A")
self.DB = self.calculate_D_dk(None, "B")
self.DC = self.calculate_D_dk(None, "C")
self.DV = self.calculate_D_dk("V", None)
self.DI = self.calculate_D_dk("I", None)

self.JV = self.calculate_J_dk("V", None)
self.JI = self.calculate_J_dk("I", None)
self.JO = self.JI-self.JV
self.JA = self.calculate_J_dk(None, "A")
self.JB = self.calculate_J_dk(None, "B")
self.JC = self.calculate_J_dk(None, "C")
self.JV = self.JV-self.JO*self.NV
self.JI = self.JI-self.JO*self.NI

self.set_DIVJ()

self.CADOT = -self.DIVJA/NAT
self.CBDOT = -self.DIVJB/NAT
self.CCDOT = -self.DIVJC/NAT
self.RECOMB = self.RECA*self.CA+self.RECB*self.CB+self.RECC*self.CC
self.INTSINK = self.DISLOC*self.DIFI
self.VACSINK = self.DISLOC*self.DIFV
self.VACSOUR = self.DISLOC*self.DIFV*self.CVOTHER

```

```

self.CVDOT[0] = 0.0
self.CIDOT[0] = 0.0
self.CVDOT[1:] = -self.DIVJV[1:]/NAT-self.RECOMB[1:]*self.CV[1:]*\
    self.CI[1:]-BIASV*self.VACSINK[1:]*self.CV[1:]+\
    self.VACSOOR[1:]+self.DISPV[1:]
self.CIDOT[1:] = -self.DIVJI[1:]/NAT-self.RECOMB[1:]*self.CV[1:]*\
    self.CI[1:]-BIASI*self.INTSINK[1:]*self.CI[1:]+\
    self.DISPI[1:]

self.Y[:NSTEP] = self.CA
self.Y[NSTEP:2*NSTEP] = self.CB
self.Y[2*NSTEP:3*NSTEP] = self.CC
self.Y[3*NSTEP:4*NSTEP] = self.CV
self.Y[4*NSTEP:] = self.CI
self.YDOT[:NSTEP] = self.CADOT
self.YDOT[NSTEP:2*NSTEP] = self.CBDOT
self.YDOT[2*NSTEP:3*NSTEP] = self.CCDOT
self.YDOT[3*NSTEP:4*NSTEP] = self.CVDOT
self.YDOT[4*NSTEP:] = self.CIDOT

def set_pde(self, u, t, L=None, beta=None, x=None):
    N = len(u) - 1
    dx = x[1] - x[0]
    rhs = np.zeros(N+1)
    rhs[0] = self.dsdt(t)
    for i in range(1, N):
        rhs[i] = (beta/dx**2)*(u[i+1] - 2*u[i] + u[i-1]) + self.f(x[i], t)
    rhs[N] = (beta/dx**2)*(2*u[i-1] - 2*u[i]) + self.f(x[N], t)
    return rhs

def set_jacobian(self, u, t, L=None, beta=None, x=None):
    N = len(u) - 1
    dx = x[1] - x[0]
    K = np.zeros((N+1,N+1))
    K[0,0] = 0
    for i in range(1, N):
        K[i,i-1] = beta/dx**2
        K[i,i] = -2*beta/dx**2
        K[i,i+1] = beta/dx**2
    K[N,N-1] = (beta/dx**2)*2
    K[N,N] = (beta/dx**2)*(-2)
    return K

def s(self, t):
    return 423

```

```

def dsdt(self, t):
    return 0

def f(self, x, t):
    return 0

def solve(self, method='RKC'):
    N = 40
    L = 1
    x = np.linspace(0, L, N+1)
    f_kwargs = dict(L=L, beta=1, x=x)
    u = np.zeros(N+1)

    U_0 = np.zeros(N+1)
    U_0[0] = self.s(0)
    U_0[1:] = 283

    solvers = {
        "FE": odespy.ForwardEuler(self.set_pde, f_kwargs=f_kwargs),
        "BE": odespy.BackwardEuler(self.set_pde, f_is_linear=True,
                                   jac=self.set_jacobian,
                                   f_kwargs=f_kwargs,
                                   jac_kwargs=f_kwargs),
        "B2": odespy.Backward2Step(self.set_pde, f_is_linear=True,
                                   jac=self.set_jacobian,
                                   f_kwargs=f_kwargs,
                                   jac_kwargs=f_kwargs),
        "theta": odespy.ThetaRule(self.set_pde, f_is_linear=True,
                                   jac=self.set_jacobian, theta=0.5,
                                   f_kwargs=f_kwargs,
                                   jac_kwargs=f_kwargs),
        "RKF": odespy.RKFehlberg(self.set_pde, rtol=1E-6, atol=1E-8,
                                   f_kwargs=f_kwargs),
        "RKC": odespy.RKC(self.set_pde, rtol=1E-6, atol=1E-8,
                           f_kwargs=f_kwargs, jac_constant=True)
    }

    dx = x[1] - x[0]
    beta = 1
    dt = dx**2/(2*beta) # Forward Euler limit
    print("Forward Euler stability limit:{}".format(dt))
    T = 1.2

    solver = solvers[method]
    solver.set_initial_condition(U_0)
    N_t = int(round(T/float(dt)))
    time_points = np.linspace(0, T, N_t+1)
    u, t = solver.solve(time_points)

```



```

        return u, t

def output(self):
    """
    """
    self.CA = self.Y[:NSTEP]
    self.CB = self.Y[NSTEP:2*NSTEP]
    self.CC = self.Y[2*NSTEP:3*NSTEP]
    self.CV = self.Y[3*NSTEP:4*NSTEP]
    self.CI = self.Y[4:NSTEP]
    self.DOSE = DISPRT*TOUTPT[self.ISTEP]

    print("TOUT={}, DOSE={}".format(TOUTPT[self.ISTEP], self.DOSE))
    self.CERR = 1-(self.CA+self.CB+self.CC)
    self.XOUT = self.XVALUE*1e9

    TEMP1 = (self.CA*np.exp(-self.XOUT/0.8452)).sum()/\
        np.exp(-self.XOUT/0.8452).sum()
    TEMP2 = (self.CB*np.exp(-self.XOUT/0.7474)).sum()/\
        np.exp(-self.XOUT/0.7474).sum()
    TEMP3 = (self.CC*np.exp(-self.XOUT/0.9472)).sum()/\
        np.exp(-self.XOUT/0.9472).sum()
    CASURF = TEMP1/(TEMP1+TEMP2+TEMP3)
    CBSURF = TEMP2/(TEMP1+TEMP2+TEMP3)
    CCSURF = TEMP3/(TEMP1+TEMP2+TEMP3)

    with open(OUTPUT_FILE, "a+") as f:
        f.write("TIME={}, DOSE={}\\n".format(TOUTPT[self.ISTEP],
            self.DOSE))
        for i in range(NSTEP):
            f.write("{} {} {} {} {} {}\\n".format(self.XOUT[i], self.CA[i],
                self.CB[i], self.CC[i], self.CV[i], self.CI[i]))
        f.write("CASURF={}, CBSURF={}, CCSURF={}\\n".format(CASURF,
            CBSURF, CCSURF))

def is_stop(self):
    """
    u[step_no] holds solution at t[step_no]
    """
    return

if __name__ == "__main__":
    ris = RIS()

```

Reference:

A Tutorial for the Odespy Interface to ODE Solvers

http://hplgit.github.io/odespy/doc/pub/tutorial/html/main_odespy.html

Example codes

https://github.com/hplgit/odespy/blob/master/doc/src/tutorial/src-odespy/pde_diffusion.py