CS155 Set 6

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 $March\ 2,\ 2018$

1 Problem 1

1.1 Problem A

1.1.1 Part i

$$p(x|y=c) = p\left((x_1|y=c), (x_2|y=c), (x_3|y=c), \dots, (x_j|y=c)\right)$$
$$p(x|y=c) = \prod_{j=1}^{D} \theta_{xjc}$$

This requires O(DC) parameters to be stored.

1.1.2 Part ii

We would need to store $O(D2^DC)$ parameters because we have to store one parameter for every combination of other parameters and then multiply this by the number of values of C. This is drastically more parameters to store.

1.2 Problem B

The Naive Bayes model has fewer parameters, and for a small training set it will be less prone to overfitting. The Naive Bayes will have lower test set error.

1.3 Problem C

If the sample size N is very large, then the full model will have lower test set error. The larger number of parameters will be able to better capture the large sample size, and it will not have the same overfitting problem if the training set is large enough.

1.4 Problem D

Making a prediction with Naive Bayes requires multiplying D parameters together and there are C classes, making this a O(DC) operation. In the complete case, we must multiply D parameters together, making it a O(D) operation.

2 Problem 2

2.1 Problem A

```
Emission Sequence Max Probability State Sequence
                22222100310
103100310322222
1310331000033100310
5452674261527433
7226213164512267255
File #1:
815833657775062
21310222515963505015
                021011111111111
0202011111111111111021
3131310213
1333333133133100
                20000021313131002133
1310021333133133313133133
Emission Sequence Max Probability State Sequence
                0111201112
011244012441112
90214005402015146362
2111266524665143562534450
                1111111111
110111010000011
```

Figure 1: Output for viterbi algorithm.

2.2 Problem B

2.2.1 Part i

```
.
Running Code For Question 2Bi
ile #0:
4.348e-15
4.739e-18
Emission Sequence Probability of Emitting Sequence
           1.181e-04
2.033e-09
Emission Sequence
5.181e-11
3.315e-15
5.126e-20
4637581156
815833657775062
21310222515963505015
503199452571274006320025
1.141e-04
111266524665143562534450
File #5:
```

Figure 2: Probabilities calculated from forwards algorithm.

2.2.2 Part ii

```
Running Code For Question 2Bii
File #0:
5452674261527433
7226213164512267255
Emission Sequence Probability of Emitting Sequence
             Probability of Emitting Sequence
3.315e-15
5.126e-20
1.297e-25
21310222515963505015
6503199452571274006320025
File #3:
1.063e-16
00214005402015146362
2111266524665143562534450
             Probability of Emitting Sequence
4546566636
```

Figure 3: Probabilities calculated from backwards algorithm.

2.3 Problem C

Transition matrix:

```
Running Code For Question 2C
Transition Matrix:
1.310e-01
                  1.143e-01
2.833e-01
      4.714e-01
2.321e-01
      3.810e-01
            2.940e-01
                  9.284e-02
1.040e-01
      9.760e-02
            3.696e-01
                  4.288e-01
1.883e-01
      9.903e-02
            3.052e-01
                  4.075e-01
```

Figure 4: Transition matrix.

Observation matrix:

Figure 5: Observation matrix.

2.4 Problem D

Transition matrix:

```
ransition Matrix:
.511e-01
         2.475e-01
                  3.013e-01
                           1.103e-04
.584e-01
         2.123e-01
                  3.123e-01
                           1.170e-01
4.402e-09
         9.756e-01
                  2.435e-02
                           1.640e-12
.673e-07
         2.993e-04
                  6.030e-01
                           3.967e-01
```

Figure 6: Learned transition matrix from unsupervised learning.

Observation matrix:

Figure 7: Learned observation matrix from unsupervised learning.

2.5 Problem E

The supervised model is likely more accurate because it's trained on both the values and the labels. The supervised model is guaranteed to have the correct states while the unsupervised model is guessing at how many states there are. The unsupervised transition matrix sometimes pushes the transition probability between two states to near zero, which the supervised matrix does not. The two transition matrices have little resemblance. Similarly, the observation matrix for unsupervised has some values very close to zero, which the transition matrix does not. The supervised matrix is likely a better representation because it's trained on labeled data. One way to improve the unsupervised model is to either feed it even more data or to somehow include regularization.

2.6 Problem F

```
Running Code For Question 2F
32750646202047231007
20765604155267256676
74074524464205042425
57754715447534627667
File #2:
25933914327162187651
67915872296229567231
03955770776070501019
02203350002021520021
32061223300050015061
56232623665446214130
20666664426231142114
61416541163266160460
File #4:
65336442643615252350
40022506465531631352
64541016460603326303
File #5:
14061644864604461156
54864485446544642434
34348848628331833635
```

Figure 8: Emitted sequences.

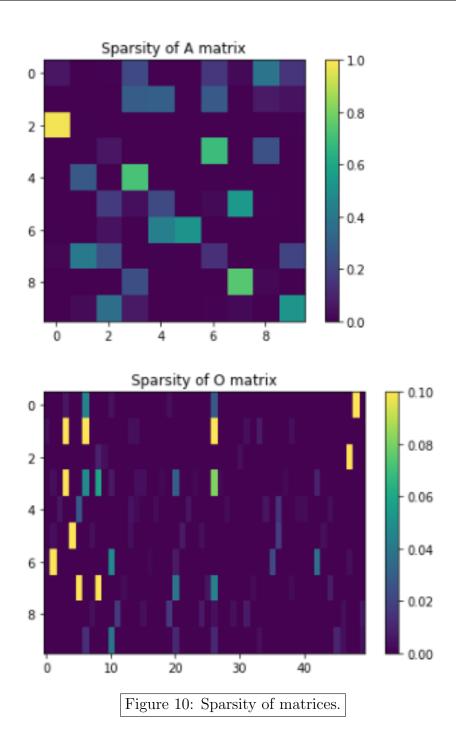
2.7 Problem G

Word cloud visualization of constitution:

Constitution



Figure 9: Word cloud representing US constitution.



Both the trained A and O matrices are fairly sparse. A large portion of both matrices are 0. This means that there are many possible state transitions that never happen, or there are some states that cannot emit certain observations. This makes sense, as there are some states - such as verb to verb - that may be unlikely.

2.8 Problem H

Sample Sentence:

And of their shall disorderly having to trial in except shall being which person any page be impeachment be writ the house shall interlined records...

Figure 11: Emission with 1 state.

Sample Sentence:

Of power may state such shall as as shall which houses respective inferior be manner for from the of such be not propose be according...

Figure 12: Emission with 2 states.

Sample Sentence:

Of power may state such shall as as shall which houses respective inferior be manner for from the of such be not propose be according...

Figure 13: Emission with 4 states.

```
print('Sample Sentence:\n=========')
print(sample_sentence(hmm8, obs_map, n_words=25))
```

Sample Sentence:

Years and direct shall day expedient facto be for by publish a to be as ministers to approved majority which from the united of the...

Figure 14: Emission with 10 states.

Sample Sentence:

Be secure the trial but present necessary and insure deem appoint power shall than not this entered of the thing impairing before not of the...

Figure 15: Emission with 16 states.

The sample emissions become somewhat more meaningful as the number of states changes. In the special case of only one state, the sentence makes no grammatical sense. Adding more hidden states will likely improve performance but only to a certain point. If there are too many hidden states, then the HMM may try to extract meaning that does not exist.

2.9 Problem I

State 4 seems to represent descriptors of the legislative branch. The words "congress," "house," and "senate" all appear in the word cloud. This states differs from some others like state 8, which has no dominant words. The words in state 4 all appear to be describing something similar, rather than being a part of speech.