

Equations of motion

$$v_{av} = \frac{(u+v)}{2} \quad v = u + at \quad x = t \frac{(u+v)}{2} \quad x = ut + \frac{1}{2}at^2 \quad x = vt - \frac{1}{2}at^2 \quad v^2 = u^2 + 2ax$$

Force as a vector. A force **F** acting at angle **theta** to a direction will have components $F\cos(\theta)$ parallel to the reference direction and $F\sin(\theta)$ perpendicular to the reference direction.

Newtons laws of motion

Inertia: Every object in a state of uniform motion tends to remain in that state of motion unless an external force is applied to it.

When net force is zero, the object will remain in it's state of motion

F = ma (force = mass X acceleration where force is in newtons (N), mass is in kg and acceleration is in ms^{-2})

For every action there is an equal and opposite reaction. The force of object A on object B is the opposite of the force of object B on object A. Contact normal force and gravity is not an action-reaction pair as they both act on the same object. The action-reaction pair is the gravity of the object on the earth and the gravity of the earth on the object.

The normal force is a reaction force supplied by a surface at 90 degrees to its plane.

Momentum

$$p = mv$$

where p is in kg ms^{-1}

where m is mass in kg

where v is velocity in ms^{-1}

Change in momentum is proportional to net force applied.

Impulse

Impulse is measured in Newton seconds (Ns)

$$\text{Impulse} = F_{av} \times t = \Delta p$$

impulse = average force x time = difference in momentum = area under the force time graph.

Conservation of momentum

$$\text{total initial momentum} = \text{total final momentum}$$

or

$$m_1 u_1 + m_2 u_2 = m_1 u_1 + m_2 u_2$$

Work

$$W = Fx$$

Work is in Joules

Force is in Newtons

X is the magnitude in displacement in metres.

$$W = Fx \cos(\theta)$$

where theta is the angle between the applied force and the direction of motion.

Work = area under the force displacement graph = difference in energy

Kinetic energy

$$E_k = \frac{1}{2}mv^2$$

Gravitational potential energy

$\Delta U_g = mg\Delta h$ Difference in gravitational potential energy is equal to mass times acceleration times by difference in height.

Elastic potential energy

$$U_s = \frac{1}{2}k \times \Delta x^2$$

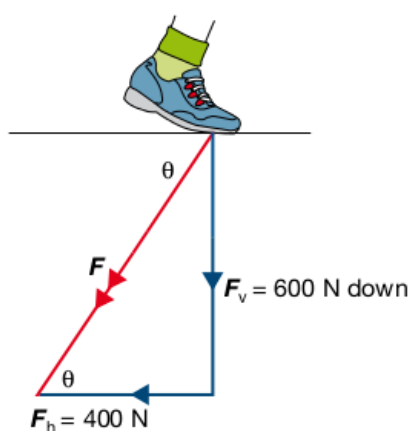
k is the stiffness constant in N m^{-1} and Δx is the extension or compression.

Power

$$\text{power} = \frac{(\text{work done})}{(\text{time taken})}$$

power is in watts

Vectors are added tail to head



Worked example 5.1D

When walking, a person's foot pushes backwards and downwards at the same time. While playing basketball, Kate's foot pushes back along the court with a force of 400 N, and down with a force of 600 N. What is the actual force applied by Kate's foot?

Solution

400 N horizontally and 600 N vertically downwards are the components of the force supplied by Kate's foot. Therefore, the force she supplies will be $F = F_{\text{horizontal}} + F_{\text{vertical}}$ and a vector diagram is needed.

Using Pythagoras' theorem:

$$F = \sqrt{F_h^2 + F_v^2} = \sqrt{400^2 + 600^2} = \sqrt{520\,000} = 721 \text{ N}$$

$$\theta = \tan^{-1} \frac{600}{400} = \tan^{-1} 1.5 = 56^\circ$$

So Kate supplies a force of 721 N backwards at 56° down from the horizontal.

Sig figs

All non-zero digits are significant

Zeros between two non-zero digits are significant

Trailing zeros (after a decimal point) are significant

Trailing zeros in a number without a decimal point are ambiguous

In scientific notation, only the digits expressed are significant

Sig figs are bold, ambiguous digits are italicised.

You cannot have more sig figs in the answer than the lowest amount in the question. (but be careful about rounding too early)

0.00010

0.002406

42000

3.204 $\times 10^3$

Prefixes

Giga (G)	10^9
Mega (M)	10^6
Kilo (k)	10^3
Milli (m)	10^{-3}
Mirco (u)	10^{-6}
Nano (n)	10^{-9}

Snells Law $\sin(i) \times n_i = \sin(r) \times n_r$

$\frac{\sin(i)}{\sin(r)} = \frac{v_1}{v_2} = \frac{n_2}{n_1} = n^*$ where i is the incident angle, and r is the refracted angle, v is the speed the light is going, n is the index of refraction and n^* is the relative index of refraction.

Lens/Mirror Formula $\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$

where f is the focal length, u is the object distance and v is the image distance

Magnification $M = \frac{-v}{u} = \frac{H_i}{H_o}$

Where H_i is the image height, H_o is the object height, u is the object distance and v is the image distance.

if M is positive image is upright and virtual, and if it is negative image is upside down and real.

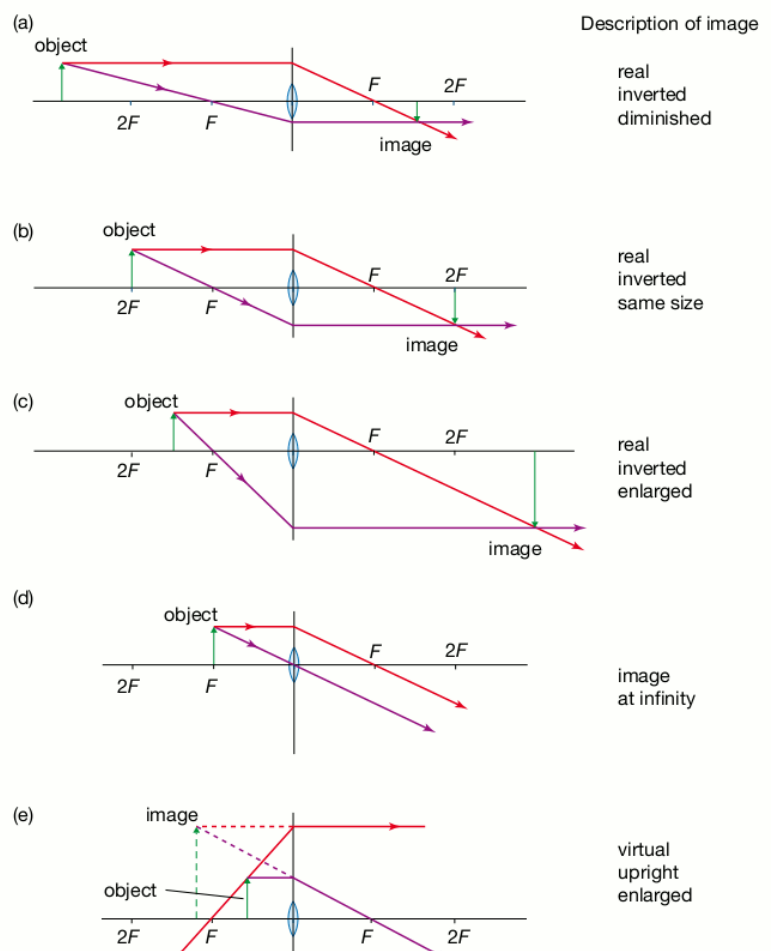
Critical angle $\sin(\theta_c) \times n_i = n_r$ or $\theta_c = \sin^{-1}\left(\frac{n_r}{n_i}\right)$ where θ_c is the critical angle, and n_i is the index of refraction of the substance that the incident ray is in and n_r is the index of refraction that the refracted angle travels to.

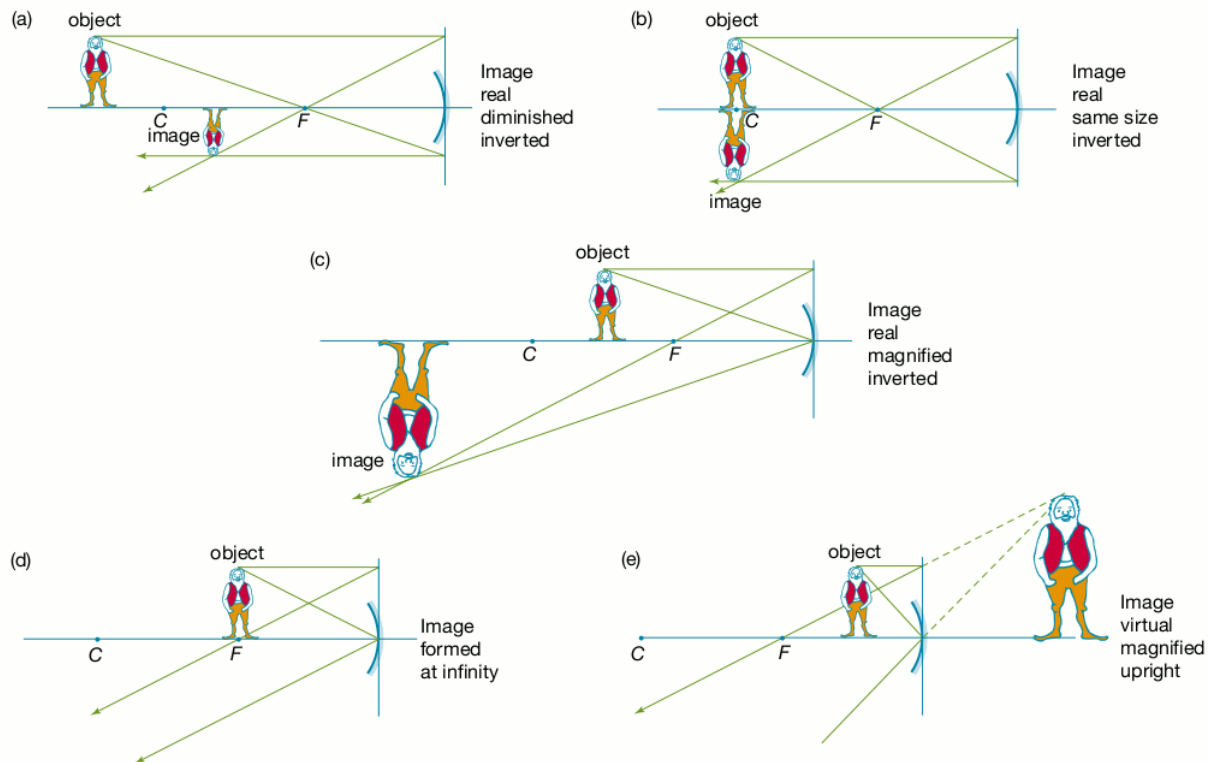
Wave Equation $Speed = frequency \times wavelength = \frac{wavelength}{period}$

Frequency $Frequency = \frac{1}{period}$

Refraction Slow down = light moves towards normal

f focal length
F focal point
P pole or centre of mirror
R radius of circle
C centre of circle





Transparent substances allow light through and do not scatter the light, allowing for image formation.

Translucent substances allow light through and do scatter the light, not allowing image formation.

Polarisation is when the orientation of the transverse wave of a body of light is all in the same direction. In unpolarised light, the orientations are at random. If light goes through a polarisation filter, the amplitude of the resulting wave is related to how big the angle difference between the filter and the traverse wave is.

Waves that come to an unyielding boundary not undergo a phase shift. Waves that come to the free end of a string will undergo a phase shift of half the wavelength. Waves that collide from two different ends of a rope will undergo interference. They will then add together.

Blue light = Higher frequency = Shorter wavelength = Higher energy = More refracted = Slower Speed
 Red light = Lower frequency = Longer wavelength = Lower energy = Less refracted = Faster speed