

# Teaching *Computation* not just *Code*

Two tools 'most everyone uses,  
two tools Dave uses too,  
and one tool nobody should use for CS1

# *Notional Machines* and teaching about *Computation*

Students (and teachers) sometimes focus on *code* and *output*

Rich and accurate (or, at least, extensible) understanding of computation matters!

- "Notional Machine" [[DuBoulay](#) '81]
  - should be actively taught, not implicit
- Alternative notional machines [[Krishnamurthi](#), others]
  - "Dictionary notional machine"
    - computation = update "state" (program counter + variables and objects) to get result
  - "Substitution notional machine"
    - computation = rewrite (code + input) until you get the result
- Visualizers for notional machines [[Sorva](#), others]
  - Should be "presenters" or "realizers" or "evincers", use vision, sound, touch, as needed

# Visualizing the Dictionary Notional Machine

There are a rich variety of visualization tools for the D.N.M.

## Standard Debugger

- Shows position in code, stack of variables, associated values
- Scales well to professional level
- Obscures subtlety of state

## Python Tutor [[Guo '21](#)]

- Limited amount of code, number of steps
- Highlights structure of state

*Demos, as time permits!*

# Challenges of the Dictionary Notional Machine

```
def copyElement(dest, src, x, y):
```

13

```
    """
```

```
    Copy src[x][y] over dest[x][y]
```

```
>>> a1 = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
```

```
>>> a10 = [[10, 20, 30], [40, 50, 60], [70, 80, 90]]
```

```
>>> copyElement(a1, a10, 2, 0)
```

```
>>> a1 # note the 70 below
```

```
[[1, 2, 3], [4, 5, 6], [70, 8, 9]]
```

```
    """
```

```
checkTotal = (sum(sum(row) for row in src) +  
               sum(sum(row) for row in dest)) # total value
```

```
increase = src[x][y] - dest[x][y] # e.g. changing 3 to 7 is increase 4
```

```
dest[x][y] = src[x][y]
```

```
newTotal = (sum(sum(row) for row in src) +  
            sum(sum(row) for row in dest))
```

```
assert checkTotal + increase == newTotal
```

*Does this code work?*

# Challenges of the Dictionary Notional Machine

```
def copyElement(dest, src, x, y):  dest: [[1, 3, 5], [2, 4, 6], [3, 5, 7]]
    checkTotal = (sum(sum(row) for row in src) +  checkTotal: 99
                  sum(sum(row) for row in dest))  # total value
    increase = src[x][y] - dest[x][y] # e.g. changing 3 to 7 is increase by 4
    dest[x][y] = src[x][y]
    newTotal = (sum(sum(row) for row in src) +
                sum(sum(row) for row in dest))
    assert checkTotal + increase == newTotal

def demo():
    (magic, byTwo) = setup()
    copyElement(byTwo, magic, 2, 2)
```

*Does this tool help us  
understand why the code does  
not work?*

copyElement()

Evaluate expression (Enter) or add a watch (Ctrl+Shift+Enter)

```
checkTotal = {int} 99
> dest = {list: 4} [[1, 3, 5], [2, 4, 6], [3, 5, 7], [4, 6, 8]]
> src = {list: 3} [[8, 1, 6], [3, 5, 7], [4, 9, 2]]
x = {int} 2
y = {int} 2
```

# Challenges of the Dictionary Notional Machine

```

Python 3.11
known limitations
def copyElement(dest, src, x, y):
    """
    Copy src[x][y] over dest[x][y]

    >>> a1 = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
    >>> a10 = [[10, 20, 30], [40, 50, 60], [70, 80, 90]]
    >>> copyElement(a1, a10, 2, 0)
    >>> a1 # note the 70 below
    [[1, 2, 3], [4, 5, 6], [70, 8, 9]]
    """
    checkTotal = (sum( sum(row) for row in src ) +
                   sum( sum(row) for row in dest)) #
    increase = src[x][y]-dest[x][y] # e.g. changing 3
    dest[x][y] = src[x][y]
    newTotal = (sum( sum(row) for row in src ) +
                 sum( sum(row) for row in dest))
    assert checkTotal + increase == newTotal

```

```
def demo():
```

that just executed  
line to execute

[Edit this code](#)

<< First < Prev Next > Last >>

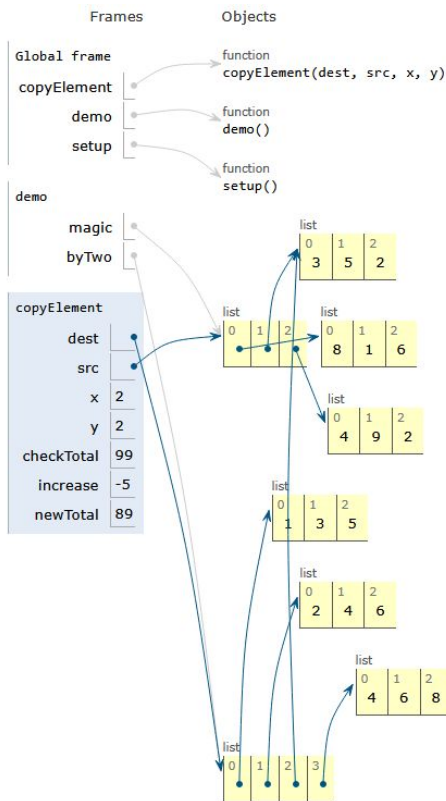
Done running (77 steps)

## zionError

[SUPPORTED FEATURES](#) or scroll down to **chat with AI Tutor** to debug

improve this tool by taking a 3-question survey

- hide objects



What about this tool?

# Challenges of the Dictionary Notional Machine

Python 3.11  
[known limitations](#)

```
def copyElement(dest, src, x, y):
    """
    Copy src[x][y] over dest[x][y]

    >>> a1 = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
    >>> a10 = [[10, 20, 30], [40, 50, 60], [70, 80, 90]]
    >>> copyElement(a1, a10, 2, 0)
    >>> a1 # note the 70 below
    [[1, 2, 3], [4, 5, 6], [70, 8, 9]]
    """
    checkTotal = (sum( sum(row) for row in src ) +
                   sum( sum(row) for row in dest)) #
    increase = src[x][y]-dest[x][y] # e.g. changing 3
    dest[x][y] = src[x][y]
    newTotal = (sum( sum(row) for row in src ) +
                sum( sum(row) for row in dest))
    assert checkTotal + increase == newTotal
```

---

```
def demo():
```

[Edit this code](#)

not just executed  
 ine to execute

---

<< First   < Prev   Next >   Last >>

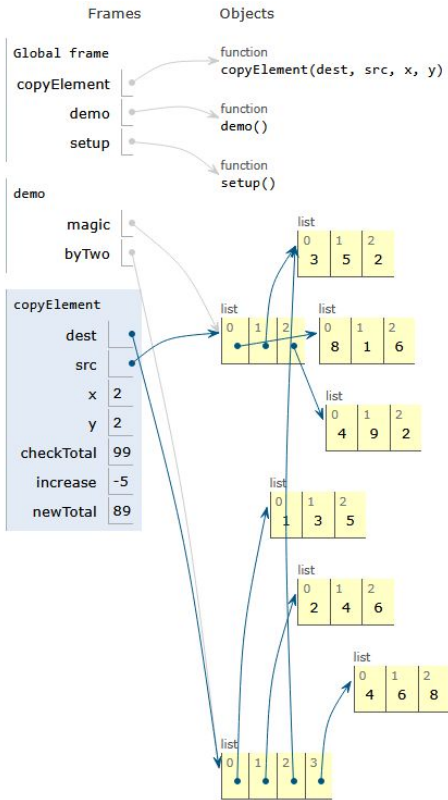
Done running (77 steps)

**tionError**

[UPDATED FEATURES](#) or scroll down to **chat with AI Tutor** to debug

prove this tool by taking a [3-question survey](#)

d hide nbierte



What about this tool?

For imperative code,  
We must know both  
(name x scope)  $\rightarrow$  object  
and  
object  $\rightarrow$  value  
relationships.

Visualizer must present both!

# Visualizing the Substitution Notional Machine

Fewer tools; at undergraduate level, only suitable for pure-functional code

## "Refactor" menu in IDE

- helps convince students that substitution is "real" and industry-relevant
- many steps not available, e.g., refactor `if False:` or `6*7`

## N-Dolphin [[Wonnacott, Reichard '23](#)]

- abstract, symbolic, re-orderable substitution machine
- core pure-functional language, currently renders as Python
- substitution, plus a bridge to proofs/discrete math [Wonnacott & Osera]

## DrRacket Stepper (specific to racket language) [[Clements, Flatt, Felleisen '01](#)]

*Demos, as time permits!*



# Challenges of the Substitution Notional Machine

No (normal) loops, so much think about everything in terms of recursion


 N-Dolphin 0.12.0, April 2025 davew@yao

```
def fib(n: int) -> int:
  if (n<3):
    return 1
  else:
    return (fib((n-1))+fib((n-2)))
```

fib(5)


# Challenges of the Substitution Notional Machine

No (normal) loops, so must think about everything in terms of recursion

 N-Dolphin 0.12.0, April 2025 davew@yao

```
def fib(n: int) -> int:  
  if (n<3):  
    return 1  
  else:  
    return (fib((n-1))+fib((n-2)))
```

```
(1  
  if (5<3) else  
  (fib((5-1))+fib((5-2)))) |
```

 N-Dolphin 0.12.0, April 2025 davew@yao

```
def fib(n: int) -> int:  
  if (n<3):  
    return 1  
  else:  
    return (fib((n-1))+fib((n-2)))
```

```
(1  
  if False else  
  (fib((5-1))+fib((5-2)))) |
```

```
(fib((5-1))+fib((5-2))) |
```

```
(3+2) |
```

```
5
```

# Updating tools

All tools should communicate in ways that reach the user

Audio output is vital for visually-impaired programmers/students

- Still a work in progress
- Particularly weak for state information of the D.N.M. and imperative code

Choice of language should be allowed

- Python Tutor supports many languages, though not Chapel :-(
- N-Dolphin could be adapted to support Chapel (I think) relatively easily
  - Just need to map A.S.T. to printed output

**"This is extremely nasty"**

Why Dave hates teaching with Jupyter (or other) "notebook"s

As time permits, demo/rant about "spring surprise"

# The "Notebook" notional machine ... not quite the DNM

Spring Surprise.ipynb ☆

File Edit View Insert Runtime Tools Help

imands + Code + Text ▶ Run all ▼

✓ RAM ☐ Disk ☐

```
[33] legsPerSpider = 8
```

```
[34] nSpiders = 1
```

```
print("Total spider legs:", nSpiders*legsPerSpider)
```

↻ Total spider legs: 8

Note that we can intermix *explanation* text with *code*, and include mathematics in our explanations if we want to.

```
[36] nLadyBugs = 20
```

```
[37] legsPerInsect = 8
```

```
[38] print("Total lady bug legs:", nLadyBugs * legsPerInsect)
```

↻ Total lady bug legs: 160

↑ ↓ 🔗 💬 ✎ 📄 🗑

If we had more time, I could show code that produces a nice **graph** or something, to make clear why the computational scientists really like this tool.

Consider this notebook

What happens when we change  $n\text{Spiders}$ ?

What about when we correct  $\text{legsPerInsect}$ ?