

Department of Computer Science & Engineering,  
Motilal Nehru National Institute of Technology, Allahabad.  
End Semester Examination  
November-2017  
MCA-III Semester

Subject: Analysis of Algorithms  
Duration: 3 Hours

Paper code: CA-3304  
Max. Marks: 60

*Note: Attempt all questions. Write all used formula in questions. Make assumptions wherever necessary and quote it.*

**Q1.** What is an optimal Huffman code for the following set of frequencies? Solve with description of Huffman algorithm. [5 Marks]

Character	Frequency
A	5
B	9
C	12
D	13
E	16
F	45

**Q2.** What are greedy approaches? How it is different from backtracking and dynamic programming? Give the complete solution (step by step) for 8-Queen problem using backtracking with pseudocode and explanation of each step. [8 Marks]

**Q3.** Explain the optimal sub-structure and overlapping sub-problem with help of Fibonacci series and give the complete solution of Fibonacci series using dynamic programming with complexity analysis. [6 Marks]

**Q4.** Find the length of longest increasing subsequence of given sequence {11, 21, 9, 32, 20, 49, 40, 59} such that all element of the subsequence are sorted in increasing order. [6 Marks]

**Q5.** Consider the rod of length and piece of all prices smaller than 7, find the most profitable way of cutting of rod. [6 Marks]

Length	1	2	3	4	5	6	7
Prices in \$	2	6	9	11	18	19	21

**Q6.** Find the optimal way to multiply the following matrices to perform the fewest multiplications. [6 Marks]

Matrix	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>
Dimension	5×11	11×4	4×15	15×23

**Q7.** Consider the array A={26, 17, 41, 14, 21, 30, 47, 10, 16, 19, 21, 28, 38, 7, 12, 14, 20, 35, 39, 3}. Create RED-BLACK tree with one more attributes its size of node. Retrieve 17<sup>th</sup> smallest element in the RED-BLACK tree. [6 Marks]

Q8. Show the comparisons the naive string matcher makes for the pattern  $P = 0001$  in the text  $T = 000010001010001$ . [3 Marks]

Q9. Working modulo  $q = 11$ , how many spurious hits does the Rabin-Karp matcher encounter in the text  $T = 3141592653589793$  when looking for the pattern  $P = 26$ ? [3 Marks]

Q10. Construct the string-matching automaton for the pattern  $P = aabab$  and illustrate its operation on the text string  $T = aaababaabaababaab$ . [3 Marks]

Q11. Write short note on: [2×4=8 Marks]

- Floyd Warshall algorithm.
- Optimal binary search tree.
- Naive string matching algorithm.
- Polynomial and non-polynomial time verification.