Department of Computer Science & Engineering, Motilal Nehru National Institute of Technology Allahabad, Mid Semester Examination September-2018 MCA-III Semester

Subject: Analysis of Algorithms Duration: 90 Minutes

Paper code: CA-3304 Max. Marks: 20

Note: Attempt all questions. Make assumptions wherever necessary and quote it.

Q1. Consider the array A={26, 17, 41, 14, 21, 30, 47, 10, 16, 19, 21, 28, 38, 7, 12, 14, 20, 35, 39, 3}. Create binary search tree with one more attributes its size of node. Retrieve 17th smallest element in the tree and rank the 12th element. [4 Marks]

Q2. Write down the Radix sort and Merge sort pseudocode and give the complete complexity analysis with help of some example. [4 Marks]

Q3. Solve the following using Master Theorems: $[1 \times 2 = 2 Marks]$

(a)
$$T(n) = 3T\left(\frac{n}{4}\right) + n\log n$$

(b)
$$T(n) = 3T\left(\frac{n}{2}\right) + \bigcap$$

n

Q4. Find upper bound for $n^4 + 100n^2 + 50$ [1 Marks]

Q5. Find the complexity of the below function: [2 Marks]

```
function(int n) {
  for (int i=0; i<n; i++)
    for(int j=i; j<i*i; j++)
        if(j%i==0) {
        for(int k=0; k<j; k++)
            print("*")
        }
  }
```

Q6. Prove that the complexity of heap sort is O(nlogn). [4 Marks]

Q7. Construct the Huffman coding tree for the text of characters with given frequencies:

	Characters T	7			4	quono	103.	
П	Frequencies 43	V K	$L \qquad E$	0	7	n		
	Trequencies 45	38 16 8	56 , 12	41	12	P	R	
			100/12	41	13	22	6	

Also find the variable length Huffman codes and frequency path length for corresponding above characters.