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## **QUESTION 1**

## <u>1.1</u>

```
library(matrixStats)
library(ggplot2)
library(glmnet)

## Loading required package: Matrix

## Loaded glmnet 4.0-2

library(e1071)

house_votes = read.csv("house_votes.csv")

taxbill_vote = data.frame(tapply(house_votes$outcome, house_votes$democrat, FUN=sum))

colnames(taxbill_vote) = "Votes"
rownames(taxbill_vote) = c("Republican", "Democrat")

num_repub = sum(house_votes$republican)
num_democ = sum(house_votes$democrat)
```

I immediately observe that 0 out of 173 democrats voted for this bill while 191 out of 203 republicans voted for this bill.

## <u>1.2</u>

```
repub_house_votes = house_votes[house_votes$republican == 1, ]
set.seed(02139)

training_data_idxs = sort(sample(c(1:203), 160, replace = FALSE)) #finding ra
ndom sample indices for data set

training_data = repub_house_votes[training_data_idxs,]
test_data = repub_house_votes[-training_data_idxs,]

predictors = training_data[,c(499:657)]
```

test\_data\_p = test\_data[,c(499:657)] #same subsetted columns as training data
predictors

## <u>1.3</u>

```
combined_matrix = cbind(training_data$outcome, predictors)

ols_model = lm(combined_matrix$`training_data$outcome` ~. , data = combined_m atrix)

print(paste("The unadjusted R^2 for the data is 0.894."))
## [1] "The unadjusted R^2 for the data is 0.894."
```

R^2 values tell us how well the data fits the model. This R^2 tells us that data fits to the OLS model relatively well but could be much better.

```
yhat ols = predict(ols model, newdata = test data p)
## Warning in predict.lm(ols_model, newdata = test_data_p): prediction from a
rank-
## deficient fit may be misleading
Y vote ols = c()
Y_vote_ols[which(yhat_ols >= 0.5)] = 1
Y_vote_ols[which(yhat_ols < 0.5)] = 0</pre>
size = length(yhat_ols)
matches_ols = data.frame(Match=integer(size), TruePositive=integer(size), Tru
eNegative=integer(size), FalsePositive=integer(size), FalseNegative=integer(s
ize)) #creating a data frame to keep track of all of the information
for (idx in 1:size){
  if (Y_vote_ols[idx] == test_data$outcome[idx]){ #checking for matches
    matches ols[idx, "Match"] = 1
    if ((test_data$outcome[idx] == 1) && (Y_vote_ols[idx] == 1)){ #checking f
or true positive
      matches ols[idx, "TruePositive"] = 1
    if ((test_data$outcome[idx] == 0) && (Y vote_ols[idx] == 0)){ #checking f
or true negative
      matches ols[idx, "TrueNegative"] = 1
    }
  }
  else{
```

```
matches_ols[idx, "Match"] = 0 # non-matches
    if ((test data$outcome[idx] == 0) && (Y vote ols[idx] == 1)){ #checking f
or false positive
      matches_ols[idx, "FalsePositive"] = 1
    if ((test data$outcome[idx] == 1) && (Y vote ols[idx] == 0)){ #checking f
or false negative
      matches ols[idx, "FalseNegative"] = 1
   }
  }
}
num correct pred ols = sum(matches ols$Match)
precision = sum(matches ols$TruePositive)/(sum(matches ols$TruePositive) + su
m(matches ols$FalsePositive))
recall = sum(matches ols$TruePositive)/(sum(matches ols$TruePositive) + sum(m
atches ols$FalseNegative))
F1 = 2/((1/precision)+(1/recall))
print(paste("Precision: ", toString(precision)))
## [1] "Precision: 0.973684210526316"
print(paste("Recall: ", toString(recall)))
## [1] "Recall: 0.902439024390244"
print(paste("F1: ", toString(F1)))
## [1] "F1: 0.936708860759494"
```

With an F1 score of 0.94 I can conclude that the OLS model performs well with relatively little errors. This being said, it definitely could be more accurate. Republican defectors would people that were predicted to vote in favor but ended up not. In this case, they would be false positives. The model was able to detect one false positive. I'm not sure if it detected all defectors but it was able to detect at least one.

```
#implementing support vector machine
svm_model = svm(predictors, training_data$outcome, kernel = "radial")
## Warning in svm.default(predictors, training_data$outcome, kernel = "radial"):
## Variable(s) 'vote_515' and 'vote_519' and 'vote_521' and 'vote_526' and
## 'vote_534' and 'vote_535' and 'vote_540' and 'vote_547' and 'vote_552' and
## 'vote_553' and 'vote_555' and 'vote_563' and 'vote_574' and 'vote_575' and
```

```
## 'vote_576' and 'vote_577' and 'vote_584' and 'vote_586' and 'vote_604' and
## 'vote_612' and 'vote_628' constant. Cannot scale data.
yhat_svm = predict(svm_model, test_data_p)
Y \text{ vote svm} = c()
Y vote svm[which(yhat svm >= 0.5)] = 1
Y vote svm[which(yhat svm < 0.5)] = 0
size = length(yhat_svm)
matches svm = data.frame(Match=integer(size), TruePositive=integer(size), Tru
eNegative=integer(size), FalsePositive=integer(size), FalseNegative=integer(s
ize))
for (idx in 1:size){
  if (Y_vote_svm[idx] == test_data$outcome[idx]){
    matches_svm[idx, "Match"] = 1
    if ((test_data$outcome[idx] == 1) && (Y_vote_svm[idx] == 1)){
      matches_svm[idx, "TruePositive"] = 1
    if ((test_data$outcome[idx] == 0) && (Y_vote_svm[idx] == 0)){
      matches svm[idx, "TrueNegative"] = 1
    }
  }
  else{
    matches_svm[idx, "Match"] = 0
    if ((test_data$outcome[idx] == 0) && (Y_vote_svm[idx] == 1)){
      matches svm[idx, "FalsePositive"] = 1
    }
    if ((test data$outcome[idx] == 1) && (Y vote svm[idx] == 0)){
      matches svm[idx, "FalseNegative"] = 1
    }
  }
}
```

```
num_correct_pred_svm = sum(matches_svm$Match)
precision = sum(matches_svm$TruePositive)/(sum(matches_svm$TruePositive) + su
m(matches_svm$FalsePositive))
recall = sum(matches_svm$TruePositive)/(sum(matches_svm$TruePositive) + sum(m
atches_svm$FalseNegative))
F1 = 2/((1/precision)+(1/recall))
```

```
print(paste("Precision: ", toString(precision)))
## [1] "Precision: 0.976190476190476"

print(paste("Recall: ", toString(recall)))
## [1] "Recall: 1"

print(paste("F1: ", toString(F1)))
## [1] "F1: 0.987951807228916"
```

The SVM model was able to detect the one False Positive value that the OLS model detected. Based on the statistics, SVM outperformed the OLS model with a higher F1 value.

```
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
## The following object is masked from 'package:ggplot2':
##
##
       margin
rF_model = randomForest(predictors, training_data$outcome, kernel ="radial")
## Warning in randomForest.default(predictors, training data$outcome, kernel
## "radial"): The response has five or fewer unique values. Are you sure you
want
## to do regression?
yhat rF = predict(rF model, test data p)
Y vote rF = c()
Y_vote_rF[which(yhat_rF >= 0.5)] = 1
Y_vote_rF[which(yhat_rF < 0.5)] = 0
size = length(yhat_rF)
matches_rF = data.frame(Match=integer(size), TruePositive=integer(size), True
Negative=integer(size), FalsePositive=integer(size), FalseNegative=integer(si
ze))
for (idx in 1:size){
```

```
if (Y_vote_rF[idx] == test_data$outcome[idx]){
    matches_rF[idx, "Match"] = 1
    if ((test data$outcome[idx] == 1) && (Y vote rF[idx] == 1)){
      matches rF[idx, "TruePositive"] = 1
    if ((test data$outcome[idx] == 0) && (Y vote rF[idx] == 0)){
      matches rF[idx, "TrueNegative"] = 1
    }
  }
  else{
    matches_rF[idx, "Match"] = 0
    if ((test_data$outcome[idx] == 0) && (Y_vote_rF[idx] == 1)){
      matches_rF[idx, "FalsePositive"] = 1
    }
    if ((test_data$outcome[idx] == 1) && (Y_vote_rF[idx] == 0)){
      matches rF[idx, "FalseNegative"] = 1
    }
  }
}
num correct pred rF = sum(matches rF$Match)
precision = sum(matches_rf$TruePositive)/(sum(matches_rf$TruePositive) + sum(
matches_rF$FalsePositive))
recall = sum(matches rf$TruePositive)/(sum(matches rf$TruePositive) + sum(mat
ches rF$FalseNegative))
F1 = 2/((1/precision) + (1/recall))
print(paste("Precision: ", toString(precision)))
## [1] "Precision: 0.953488372093023"
print(paste("Recall: ", toString(recall)))
## [1] "Recall: 1"
print(paste("F1: ", toString(F1)))
## [1] "F1: 0.976190476190476"
```

In comparing F1 values, the random Forest model performs better than the OLS model but not quite as well as the SVM model.

#### **QUESTION 2**

#### 2.1

```
prctrain = read.csv("pres_results_by_county_train.csv")
prctrain_county = prctrain[prctrain$Geographic.Subtype == "County",] #subsett
ing for just counties

prctrain_county$Trump.Share = prctrain_county$Donald.J..Trump/prctrain_county
$Total.Vote #this is is trump share with the NA values still included

prctrain_county = prctrain_county[!is.na(prctrain_county$Trump.Share),] #remo
ving rows where trump share contains NA value

prctrain_subset = prctrain_county[, c(9:59)] #what we are putting into regres
sion

summary(prctrain_county$Trump.Share)

## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.04087 0.55526 0.66889 0.63903 0.74958 0.94585
```

Yes, this does contradict the fact that Clinton won the popular vote. From what this data says, Trump's average vote share was 63%, that being a majority of votes. I find this interesting and I'm not quite sure what the explanation for this could be. I think this could point to how bias can arise in data science and how people can use their own personal analysis to support narratives that aren't true.

#### 2.2

```
mod_lasso = glmnet(y = prctrain_county$Trump.Share, x = data.matrix(prctrain_subset), alpha = 1)
```

```
mse_min = Inf
choice_lamba = NaN

#iterate through Lambda values and find minimum mse value
for (lambda in mod_lasso$lambda){

    yhat.lasso = predict(mod_lasso, newx=as.matrix(prctrain_subset), s=lambda)
) #calculate predicted values

    mse = mean((prctrain_county$Trump.Share-yhat.lasso)^2)

    if (mse < mse_min){ #check to see if current mse is smaller than current min</pre>
```

```
mse_min = mse
    choice_lamba = lambda

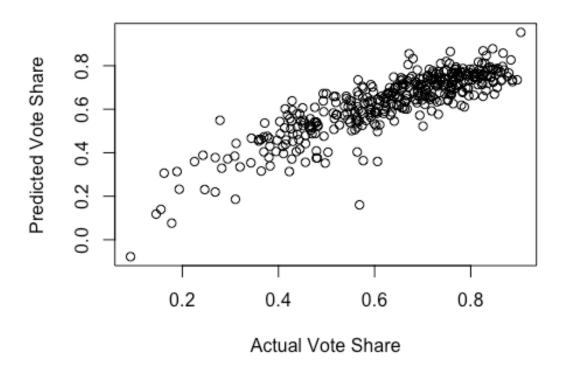
}

print(paste(toString(choice_lamba), " is the best lambda value with an in-sam
ple MSE value of ", toString(mse_min), "."))

## [1] "8.7849245941921e-06 is the best lambda value with an in-sample MSE v
alue of 0.00610317920178813 ."
```

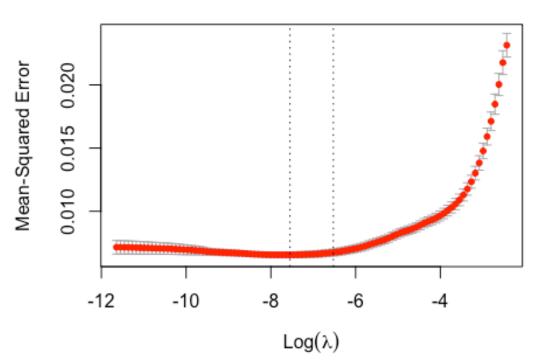
```
prctest = read.csv("pres results by county test.csv")
prctest_county = prctest[prctest$Geographic.Subtype == "County",]
prctest_county$Trump.Share = prctest_county$Donald.J..Trump/prctest_county$To
tal. Vote #this is is trump share with the NA values still included
prctest_county = prctest_county[!is.na(prctest_county$Trump.Share),]
prctest_subset = prctest_county[, c(9:59)] #what we are putting into regressi
on
#performing prediction based on parameters chosen before
yhat.lasso = predict(mod_lasso, newx=as.matrix(prctest_subset), s=choice_lamb
a)
mse = mean((prctest county$Trump.Share-yhat.lasso)^2)
print(paste("The MSE for the data is", toString(mse), "."))
## [1] "The MSE for the data is 0.00678634250799078 ."
plot(prctest_county$Trump.Share, yhat.lasso,
    xlab = "Actual Vote Share",
     ylab = "Predicted Vote Share")
title("Predicted Vote Share against Actual Vote Share") #apparently this shou
Ld have a Length of 413 according to Piazza?
```

# Predicted Vote Share against Actual Vote Share



```
set.seed(02139)
#implementing cross validated lasso regression
mod_lasso_cross = cv.glmnet(y = prctrain_county$Trump.Share, x = data.matrix(
prctrain_subset), alpha = 1)
plot(mod_lasso_cross)
```





```
#extracting chosen Lambda value and its MSE
selected_lambda = mod_lasso_cross$lambda.min
selected_MSE = mod_lasso_cross$cvm[which(mod_lasso_cross$lambda==selected_lambda)]

print(paste("The selected lambda value is", toString(selected_lambda), "with
an MSE of", toString(selected_MSE), "."))

## [1] "The selected lambda value is 0.00052664239143802 with an MSE of 0.006
55438268655898 ."
```

```
#cross validated model used on test data

yhat.lasso.cross = predict(mod_lasso_cross, newx=as.matrix(prctest_subset), s
=selected_lambda)
mse.cross = mean((prctest_county$Trump.Share-yhat.lasso.cross)^2)

print(paste("The MSE for the data is", toString(mse.cross), "."))
## [1] "The MSE for the data is 0.00678106918208572 ."
```

```
print(paste("The MSE from the previous model (", toString(mse),") is greater
than the MSE from the cross-validated model(", toString(mse.cross), "), there
fore the cross-validated model performed better."), sep="")
## [1] "The MSE from the previous model ( 0.00678634250799078 ) is greater th
an the MSE from the cross-validated model( 0.00678106918208572 ), therefore t
he cross-validated model performed better."
```

### <u>2.7</u>

```
coeff = mod_lasso_cross$nzero[which(mod_lasso_cross$lambda==selected_lambda)]
print(coeff)
## s55
## 37
```

The lambda that was chosen has 37 non-zero coefficients.