Hello!

Here is some math.

$$\alpha\beta\gamma\delta\Gamma\Delta\Lambda\Theta abcdABCD$$

Now here are some symbols.

$$\int_{-\infty}^{\infty} \sin \theta = \sqrt{\frac{e^{i\pi}}{\sum_{i=0} \epsilon \Gamma \Lambda \cdot i}}$$

Here is a compatibility test. Lowercase letters:

 $\alpha a \beta b \gamma y \delta d \epsilon e \epsilon \eta n \theta o i i \kappa k \lambda l \ell \mu u \nu v \rho p \sigma o \tau t v v \phi o \chi x \omega w$

Uppercase letters:

ΓΕΔΑΘΟΛΑΤΞΕΣΧΥΥ ΟΦΙΨΟΩΟ

Large symbols, text-size:

$$\left[\left(\left\langle\left\{\int S\sum E\right\}\right\rangle\right)\right]$$

Display style:

$$\left[\left(\left\langle\left\{\int S\sum E\right\}\right\rangle\right)\right]$$

Common math symbols:

$$a + \frac{2}{\pi} \neq 15 \Longrightarrow A \in \Pi, \forall A \approx \nabla.$$

Unbound Orbits: Deflection of Light by the Sun

Consider a particle or photon approaching the sun from very great distances. At infinity the metric is Minkowskian, that is, $A(\infty) = B(\infty) = 1$, and we expect motion on a straight line at constant velocity V

$$b \simeq r \sin(\phi - \phi_{\infty}) \simeq r(\phi - \phi_{\infty})$$
$$-V \simeq \frac{d}{dt}(r \cos(\phi - \phi_{\infty})) \simeq \frac{dr}{dt}$$

where b is the "impact parameter" and ϕ_{∞} is the incident direction. We see that they do satisfy the equations of motion at infinity, where A=B=1, and that the constants of motion are:

$$J = bV^2 \tag{1}$$

$$E = 1 - V^2 \tag{2}$$

(Of course a photon has V=1, and as we have already seen, this gives E=0.) It is often more convenient to express J in terms of the distance r_0 of closest approach to the sun, rather than the impact parameter b. At r_0 , $dr/d\phi$ vanishes, so our earlier equations give:

$$J = r_0 \left(\frac{1}{B(r_0)} - 1 + V^2 \right)^{1/2}$$

The orbit is then described by

$$\phi(r) = \phi_{\infty} + \int_{r}^{\infty} \left\{ \frac{A^{\frac{1}{2}}(r)dr}{r^{2} \left(\frac{1}{r_{0}^{2}} \left[\frac{1}{B(r)-1+V^{2}} \right] \left[\frac{1}{B(r)-1+V^{2}} \right]^{-1} - \frac{1}{r^{2}} \right)^{\frac{1}{2}}} \right\}.$$

The total change in ϕ as r decreases from infinity to its minimum value r_0 and then increases again to infinity is just twice its change from ∞ to r_0 , that is, $2|\phi(r_0)-|\phi'_{\infty}|$. If the trajectory were a straight line, this would equal just π ;

$$\Delta \phi = 2|\phi(r_0) - \phi_{\infty}| - \pi.$$

If this is positive, then the angle ϕ changes by more than 180°, that is, the trajectory is bent *toward* the sun; if $\Delta \phi$ is negative then the trajectory is bent away from the sun.

The end.