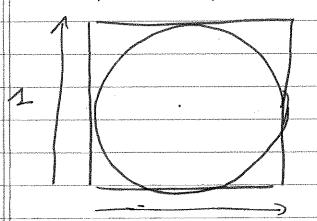
Biometry in Pharmacutics Probability & Buyes

U. Buffalo, March 6th

I/ Buffon's needle +. For this lecture, we'll consider a simplified needle experiment. The goal is to measure n.

Originally proposed in 1733.

Simplified Experiment



What are the odd Re needle falls in the circle?

P= Tr2/A2 = 11/4

Is this experiment practical?

- Uhat conditions, when dropping the needle ment be met

- D Noedle can hit any point with the same probability

x~ U(0,1)

by ~ U(0, 1)

What are the odds the needle hits a specific point? Say (20, 60)?
- o Simpler problem:

	Rose Control of the C	
	A	
A CONTRACTOR OF THE PERSONS NAMED IN		
1	Property Control of the Control	and the state of t

what are the odds the needle falls in box A?

Where N is the total number of outcomes. But a point has dimension O. Thus

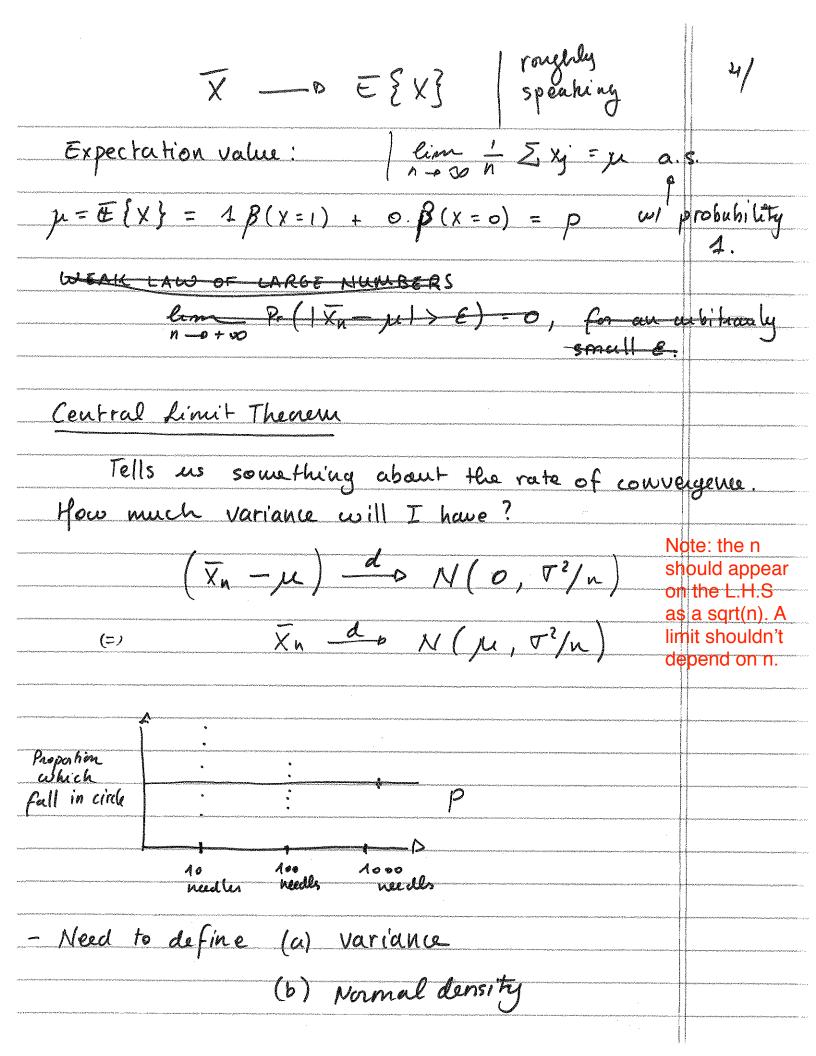
Thus

This does not mean the event is impossible! Hints at some counter-inhuitive results when we deal with continuous spaces.

Probability measure: maps a set to [0;1] Example of sets/events manue o a point (20, yo) o the box A 1/16 11/4 o the circle o the whole space

Our prob. measure is the area of the set.

al 25 de de la recurso esse que primisio recurso en que que a sistemistra la primisio secundo de conseguencia d	Suppose à is anknown (which it is!)
	Or suppose ue have a complicated shape:
	How can we measure the area? Using probability.
	Jahine variable
	Let A = { noodle falls in circle } RC the complement.
	Then X = MANDE 100 (mues/failure) Suppose we drop n needles.
	Xx, 111, Xn ~ Bernouilli (p) (dewrity)
	$\beta \propto p^{\alpha}(1-p)^{1-2\alpha}$ (Talk about independence)
	Assigns probability mass to n=1 and n=0_
	1-11/4 If we drop a lot of needles, the average of X converges to P!
	STRONG LAW OF LARGE # !



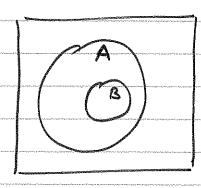
Pa continuous distributions:

$$M = \int_{R} n \rho_{0,0} dn$$

More generally, for any random function f(X):

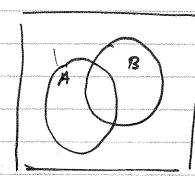
$$E\{f(x)\} = \int_{\mathbb{R}} f(x) p(x) dx$$

Conditional Probability



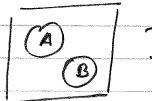
$$\frac{P(BIA) = \frac{P(B)}{P(A)}}{P(A)}$$

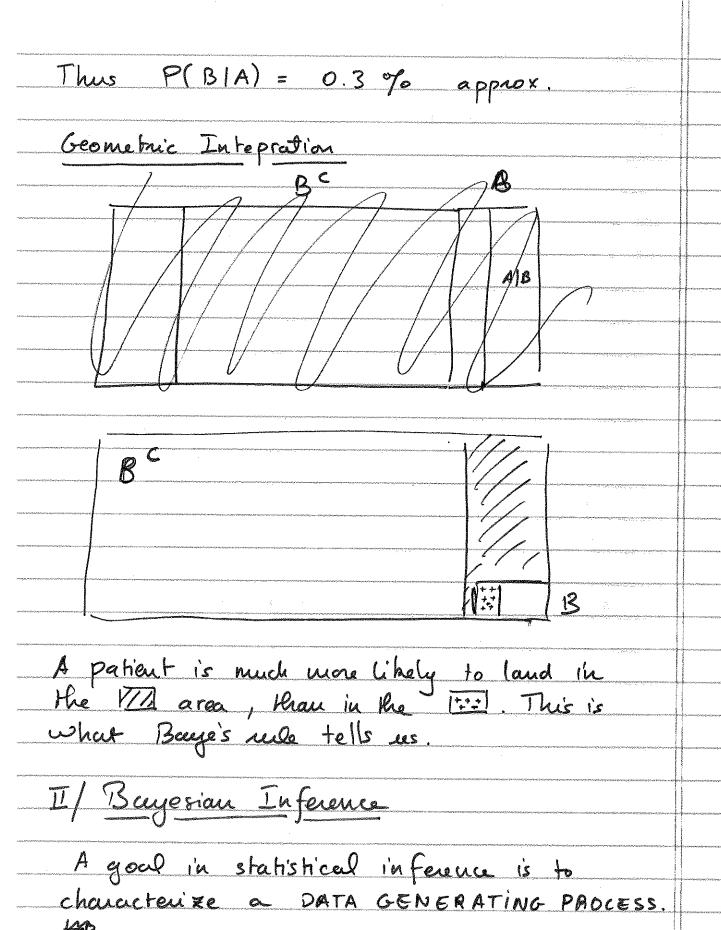
What about P(AIB)?



$$\frac{P(B|A) = \frac{P(A \cap B)}{P(A)}}{P(A)}$$

What about

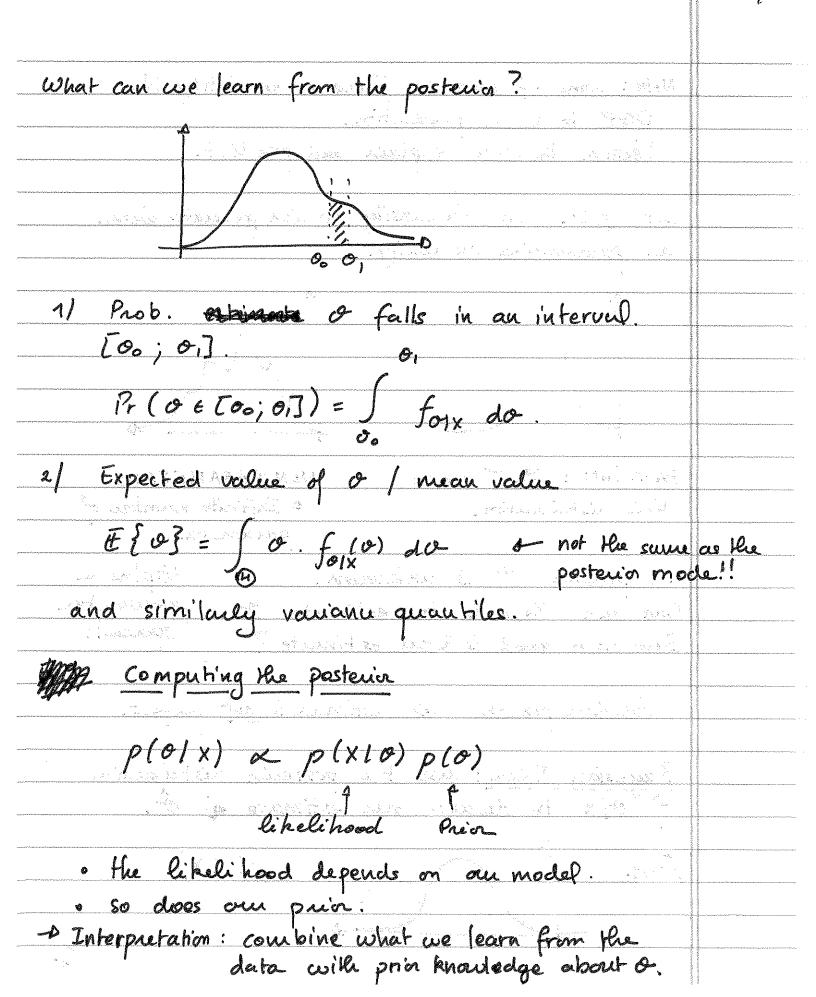




Note: some of statistics focusor on emulating the DGP to make prediction.

Tension between explain and predict. Lef f(.) be the density which generates data. Can parametrize the density. GAUSSIAN: pt, V control NON-PARAMETRIC - Infinite number of Huis distribution. paramaters. In practice & 13 unknown. Explose a parameter Can use X1,111, Xn to estimate O. But how good is Born estimate? Random process => estimate is not perfect. Bayesian Idea: ux the posterior distribution of OIX to describe our estimate of ô. MOSX)

the forest is building to the control of the con-



The pria: - Prior knowledge:
· h is around 3.14
· A parameter hous a mechanishic
interpretation à can use expert knowldge.
a annual
V of gut - o w/ some vaviation.
V~ N(Vo, To?)
· A regularization device
-o can help model fitting process
- o makes au parameter search
more targeted exploration of target
space.
Eig Immitation game / code Breaking.
Example: $\times 2, \dots, \times n \stackrel{iid}{\sim} N(\sigma, \sigma^2), \Gamma is$ $\sigma n N(\mu, \tau^2) \text{known}.$
Their main and their Cibaliland alexandell
togesler: The form of the f
$P_{\alpha} = \frac{1}{\sqrt{2\pi}} e^{-\frac{\pi}{2}} \left(\frac{1}{\sqrt{2\pi}} \left(\frac{1}{\sqrt{2\pi}} - \frac{1}{\sqrt{2\pi}} \right) \right)$
JA T
Produces a posteria $N\left(\frac{M/T + \sum_{i} x_i/\sigma^2}{1/T^2 + n/\sigma^2}, \frac{1}{1/T^2 + n/\sigma^2}\right)$
1/22+11/02 1/22+1/02/

 $N\left(\frac{1/\zeta' + \chi/\sigma^2/n}{1/\zeta' + \chi/\sigma^2/n}\right)$ The mean is a compromise or a weighted average between u and X.
The weighting is 1/VAR => How uncurrainty is penalized. As n - 0 +00, the data/likelihood dominates the priority section of the section Var = 1/2 + N/T? goes to 0, if we have strong prior (low variance) or a bot of data. FOR Questions, time allowing. Feulle topics - In practice rend to estimate pos Feu'n disfribution. - MCMC etc.