

Microelectronics Circuit Analysis and Design

Donald A. Neamen

Chapter 6

Basic BJT Amplifiers

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-1

In this chapter, we will:

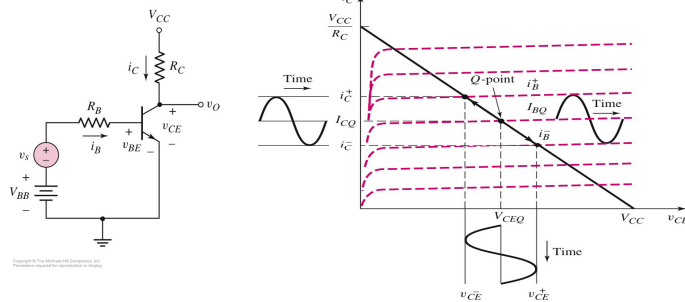
- Understand the principle of a linear amplifier.
- Discuss and compare the three basic transistor amplifier configurations.
 - the common-emitter amplifier.
 - the emitter-follower amplifier.
 - the common-base amplifier.
- Analyze multi-transistor amplifiers.

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-2

Common Emitter with Time-Varying Input

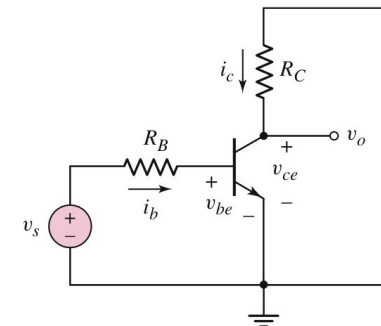


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-3

ac Equivalent Circuit for Common Emitter



Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-4

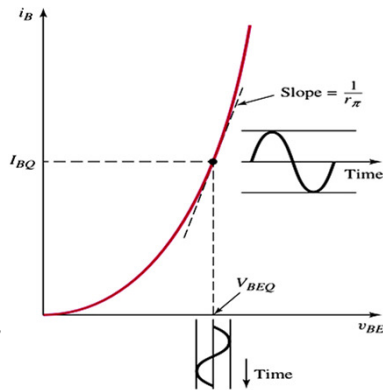
I_B Versus V_{BE} Characteristic

$$v_{BE} = V_{BE} + v_{be}$$

$$i_B = I_{BQ} \exp(v_{be}/V_T)$$

$$e^x \cong 1 + x + \dots$$

$$i_B \cong I_{BQ} \left(1 + \frac{v_{be}}{V_T}\right) = I_{BQ} + i_b$$



Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-5

ac Equivalent Circuit

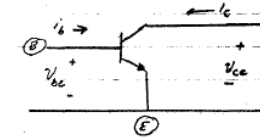
Assumptions

1. 'Q' is biased in Forward Active Mode

2. AC VOLTAGES ARE "Small Signals"

A. HYBRID π Equivalent Ckt

TWO PORT NETWORK FOR CC CKT



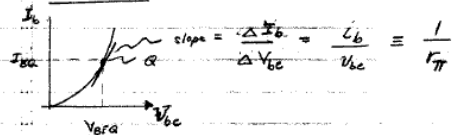
Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-6

ac Equivalent Circuit

1. INPUT PORT



$v_{be} = i_b r_{\pi}$ is the small signal linear constant of proportionality between v_{be} & i_b

$r_{\pi} \equiv$ DIFFUSION RESISTANCE or b-e input resistance.

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-7

ac Equivalent Circuit

Mathematically we have:

$$\frac{1}{r_{\pi}} = \left. \frac{\partial i_b}{\partial v_{be}} \right|_{Qpt} = \frac{2}{2V_{BE}} \left[\frac{I_S}{\beta_F} e^{v_{BE}/V_T} \right] \bigg|_{Qpt} = \frac{1}{V_T} \left[\right] = \frac{I_{BQ}}{V_T}$$

So: $r_{\pi} = \frac{v_{be}}{i_b} = \frac{V_T}{I_{BQ}} = \frac{\beta_F V_T}{I_{CQ}}$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-8

ac Equivalent Circuit

2. Output Port

- Let i_c be independent of v_{ce} [neglect Early Effect]

Since $\Delta i_c = \left. \frac{\partial i_c}{\partial i_b} \right|_{a-p} \Delta i_b$

$$= \left. \frac{\partial i_c}{\partial i_b} \right|_{a-p} i_b$$

Define $\beta = \left. \frac{\partial i_c}{\partial i_b} \right|_{a-p} = \text{AC C-E CURRENT GAIN}$

then we write

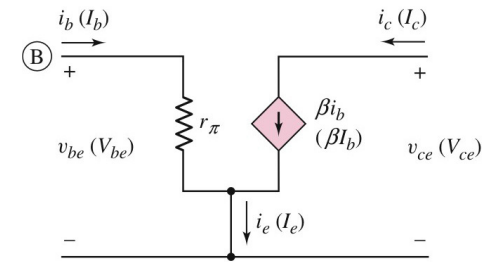
$$i_c = \beta i_b$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-9

Small-Signal Equivalent Circuit Using Common-Emitter Current Gain

Copyright © The McGraw-Hill Companies, Inc.
Permission required for reproduction or display.

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-10

ac Equivalent Circuit

the transconductance g_m Since v_{be} and i_b are related by r_{π} , we canequally represent i_c as a function of v_{be}

$$i_c = \left. \frac{\partial i_c}{\partial v_{be}} \right|_{a-p} v_{be}$$

Define $g_m = \left. \frac{\partial i_c}{\partial v_{be}} \right|_{a-p} = \frac{I_{CQ}}{V_T}$

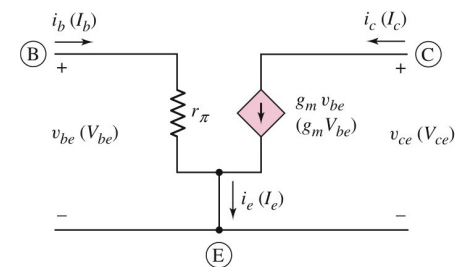
$$i_b = i_{BQ} e^{v_{be}/V_T}$$

$$\frac{\partial i_b}{\partial v_{be}} = \frac{1}{V_T} \cdot I_{BQ}$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-11

Small-Signal Hybrid π Model for npn BJTCopyright © The McGraw-Hill Companies, Inc.
Permission required for reproduction or display.

Phasor signals are shown in parentheses.

$$g_m = \frac{I_{CQ}}{V_T}$$

$$r_{\pi} = \frac{\beta V_T}{I_{CQ}}$$

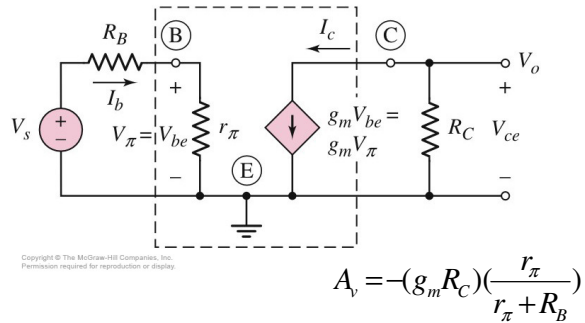
$$g_m r_{\pi} = \beta$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-12

Small-Signal Equivalent Circuit for npn Common Emitter circuit



Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-13

Problem-Solving Technique: BJT AC Analysis

1. Analyze circuit with only dc sources to find Q point.
2. Replace each element in circuit with small-signal model, including the hybrid π model for the transistor.
3. Analyze the small-signal equivalent circuit after setting dc source components to zero.

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-14

Transformation of Elements

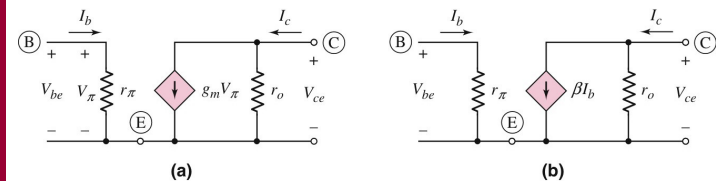
Element	DC Model	AC Model
Resistor	R	R
Capacitor	Open	C
Inductor	Short	L
Diode	$+V_{\gamma} \quad r_f -$ 	$r_d = V_T / I_D$
Independent Constant Voltage Source	$+V_S -$ 	Short
Independent Constant Current Source	I_S	Open

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-15

Hybrid π Model for npn with Early Effect



$$r_o = \frac{V_A}{I_{CQ}}$$

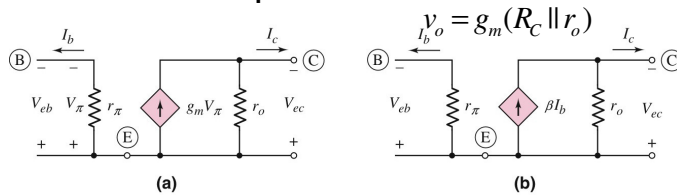
Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-16

Hybrid p Model for pnp with Early Effect

All voltage and current polarities are reversed.
Gain equation are the SAME.



$$v_o = g_m v_\pi (R_C \parallel r_o)$$

$$v_o = \beta i_b (R_C \parallel r_o)$$

$$v_\pi = -v_s \left(\frac{r_\pi}{r_\pi + R_B} \right)$$

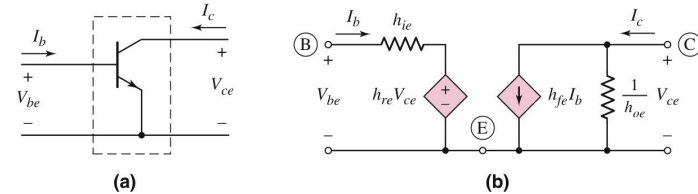
$$i_b = \left(\frac{-v_s}{r_\pi + R_B} \right)$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-17

h-Parameter Model for npn



$$V_{be} = h_{ie} I_b + h_{re} V_{ce}$$

KVL at input loop

$$I_c = h_{fe} I_b + h_{oe} V_{ce}$$

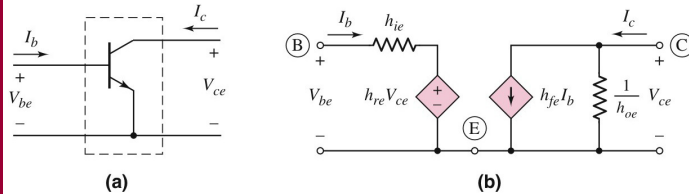
KCL at output loop

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-18

h-Parameter Model for npn



$$h_{ie} = r_b + r_\pi \parallel r_\mu$$

$$h_{fe} = \beta$$

$$h_{re} \cong \frac{r_\pi}{r_\mu}$$

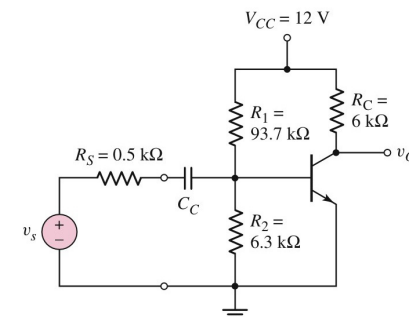
$$h_{oe} = \frac{1 + \beta}{r_\mu} + \frac{1}{r_o}$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-19

Common Emitter with Voltage-Divider Bias and a Coupling Capacitor

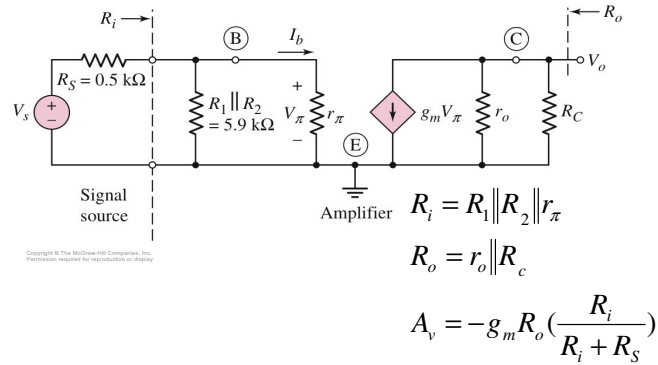


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-20

Small-Signal Equivalent Circuit – Coupling Capacitor assumed a Short

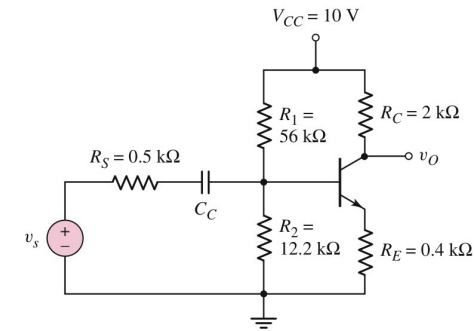


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-21

nnp Common Emitter with Emitter Resistor

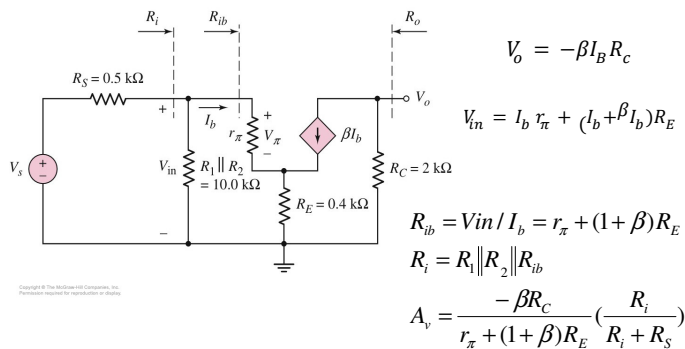


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-22

Small-Signal Equivalent Circuit: Common Emitter with R_E

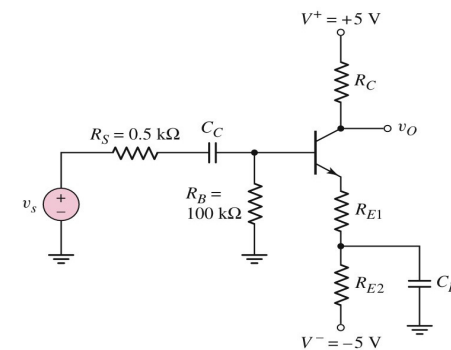


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-23

R_E and Emitter Bypass Capacitor

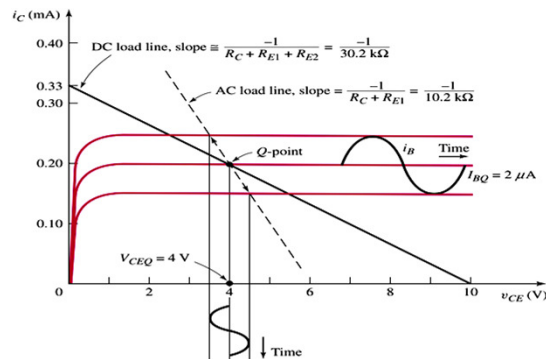


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-24

DC and AC Load Lines: R_E and Emitter Bypass Capacitor



Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-25

Problem-Solving Technique: Maximum Symmetrical Swing

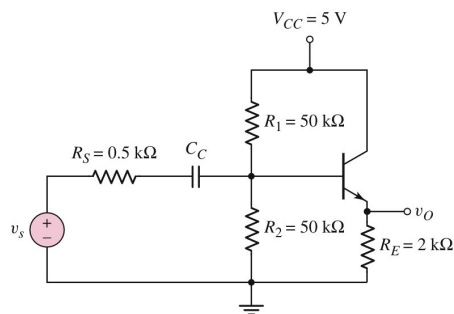
1. Write dc load line equation that relates I_{CQ} and V_{CEQ} .
2. Write ac load line equations that relates i_c and v_{ce}
3. In general, $i_c = I_{CQ} - I_{C(\min)}$, where $I_{C(\min)}$ is zero or other minimum collector current.
4. In general, $v_{ce} = V_{CEQ} - V_{CE(\min)}$, where $V_{CE(\min)}$ is some specified minimum collector-emitter voltage.
5. Combine above 4 equations to find optimum I_{CQ} and V_{CEQ} .

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-26

Common-Collector or Emitter-Follower Amplifier

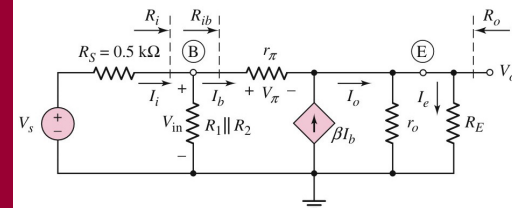


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-27

Small-Signal Equivalent Circuit: Emitter Follower



$$I_o = (1 + \beta) I_b \quad \text{so} \quad v_o = I_o (1 + \beta) (r_o \parallel R_E)$$

$$v_o = I_b [r_{\pi} + (1 + \beta) (r_o \parallel R_E)]$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-28

Small-Signal Equivalent Circuit: Emitter Follower

$$I_o = (1+\beta)I_b \quad \text{or} \quad V_o = I_b(1+\beta)(r_o \parallel R_E)$$

$$V_{in} = I_b [r_\pi + (1+\beta)(r_o \parallel R_E)]$$

$$R_{ib} = \frac{V_{in}}{I_b} = r_\pi + (1+\beta)(r_o \parallel R_E)$$

$$R_i = R_1 \parallel R_2 \parallel R_{ib} \quad \text{Typically a large value due to the reflected impedance}$$

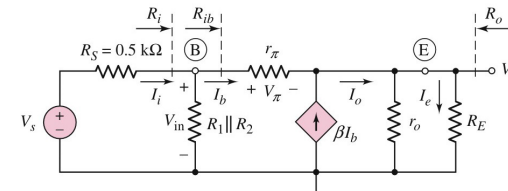
$$V_{in} = \left(\frac{R_i}{R_i + R_s} \right) \cdot V_s$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-29

S-S Equivalent : Emitter Follower



$$A_v = \frac{V_o}{V_s} = \frac{I_b(1+\beta)(r_o \parallel R_E)}{I_b [r_\pi + (1+\beta)(r_o \parallel R_E)] \left(\frac{R_i + R_s}{R_i} \right)}$$

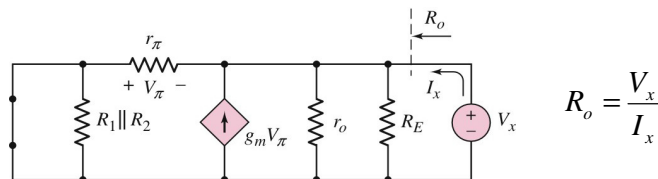
$$A_v = \frac{(1+\beta)(r_o \parallel R_E)}{r_\pi + (1+\beta)(r_o \parallel R_E)} \left(\frac{R_i}{R_i + R_s} \right) \cong 1$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-30

Output Resistance: Emitter Follower



$$R_o = r_o \parallel R_E \parallel \left(\frac{r_\pi}{1+\beta} \right) \quad \text{(base circuit reflected into emitter)}$$

$$R_o = \frac{r_\pi}{1+\beta} \parallel R_E \parallel r_o \quad \text{Typically a low value due to the reflected impedance}$$

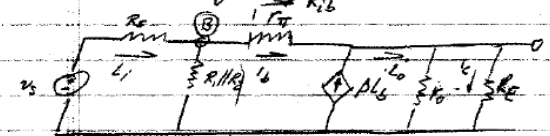
Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-31

Emitter Follower Current Gain

Recall the small signal Emitter follower circuit:



$$I_b = \left(\frac{R_1 \parallel R_2}{R_1 \parallel R_2 + R_{ib}} \right) I_i \quad \leftarrow \text{current divider}$$

$$I_o = (1+\beta)I_b = (1+\beta) \left(\frac{R_1 \parallel R_2}{R_1 \parallel R_2 + R_{ib}} \right) I_i$$

$$\text{Then } I_e = \left(\frac{r_o}{r_o + R_E} \right) I_o$$

Emitter Follower Current Gain

So finally:

$$A_i = \frac{i_e}{i_i} = (1+\beta) \left(\frac{R_E \parallel R_L}{R_E \parallel R_L + R_{ib}} \right) \left(\frac{r_o}{r_o + R_E} \right)$$

assuming $R_E \parallel R_L \gg R_{ib} \Rightarrow \text{Then } ① \approx 1$

and if $r_o \gg R_E \Rightarrow \text{Then } ② \approx 1$

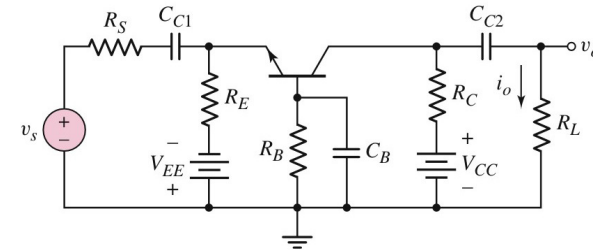
and $A_i \approx (1+\beta)$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-33

Common-Base Amplifier



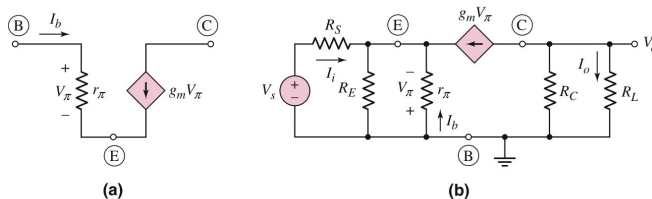
Copyright © The McGraw-Hill Companies, Inc.
Permission required for reproduction or display.

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-34

Small-Signal Equivalent Circuit: Common Base



Copyright © The McGraw-Hill Companies, Inc.
Permission required for reproduction or display.

$$A_v \approx g_m (R_C \parallel R_L)$$

$$A_i = g_m \left(\frac{R_C}{R_C + R_L} \right) \left[\frac{r_\pi}{1+\beta} \parallel R_E \right]$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-35

Small-Signal Equivalent Circuit: Common Base

$$\Delta v_o = -g_m v_\pi (R_C \parallel R_L)$$

now need v_π in terms of v_s

KCL at Emitter node: Assume all current enters the emitter.

$$\frac{v_s - (-v_\pi)}{R_S} + \frac{v_\pi}{R_E} + \frac{v_\pi}{r_\pi} + g_m v_\pi = 0$$

$$\frac{v_s}{R_S} + v_\pi \left(g_m + \frac{1}{r_\pi} + \frac{1}{R_E} + \frac{1}{R_S} \right) = 0 \quad \left\{ \begin{array}{l} \text{note } g_m r_\pi = \beta \\ \text{so: } g_m = \beta / r_\pi \end{array} \right.$$

$$v_\pi \left(\frac{\beta+1}{r_\pi} + \frac{1}{R_E} + \frac{1}{R_S} \right) = -\frac{v_s}{R_S}$$

$$v_\pi = -\frac{v_s}{R_S} \left[\left(\frac{r_\pi}{\beta+1} \parallel R_E \parallel R_S \right) \right]$$

McGraw-Hill

Small-Signal Equivalent Circuit: Common Base

Subst into Δ given

$$\frac{v_o}{v_s} = +g_m \left(\frac{1}{R_s} \right) (R_c \parallel R_L) \left[\left(\frac{r_\pi}{1+\beta} \right) \parallel R_E \parallel R_s \right]$$

Note: For R_s small: eg $R_s \ll R_E \approx \frac{r_\pi}{1+\beta}$

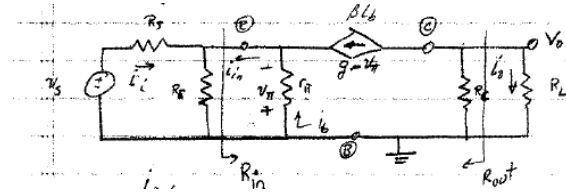
$$\boxed{\frac{v_o}{v_s} \approx +g_m (R_c \parallel R_L) \left[\frac{R_s}{R_s} \right]}$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-37

Common Base



D. Input : Output Impedance

$$R_{in} = \frac{v_\pi}{i_{in}} = \frac{i_b r_\pi}{i_b + \beta i_b} = \boxed{\frac{r_\pi}{1+\beta}} \quad \text{Small}$$

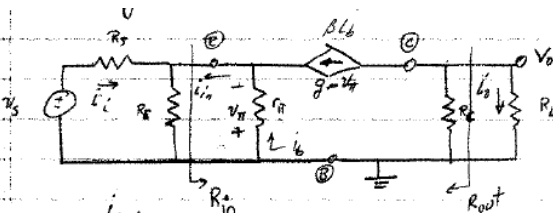
$$\boxed{R_{out} = R_c} \quad \text{assuming } r_o = \infty$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-38

Common Base



$$A_i = \frac{i_o}{i_i}$$

$$i_o = -g_m v_\pi \left(\frac{R_c}{R_c + R_L} \right) \quad \text{by current division}$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-39

Common Base

$$\text{KCL at } \textcircled{E} \text{ node: } i_i + \frac{v_\pi}{R_s} + \frac{v_\pi}{r_\pi} + g_m v_\pi = 0$$

$$v_\pi \left[\frac{1}{R_s} + \frac{1}{r_\pi} + \beta \right] = -i_i$$

$$v_\pi = -i_i \left(R_s \parallel \frac{r_\pi}{1+\beta} \right)$$

$$\text{So } A_i = \frac{i_o}{i_i} = g_m \left(\frac{R_c}{R_c + R_L} \right) \left[\left(\frac{r_\pi}{1+\beta} \right) \parallel R_s \right]$$

$$= \left(\frac{R_c}{R_c + R_L} \right) \left[\left(\frac{g_m r_\pi}{1+\beta} \right) \parallel R_s \right]$$

conversely for small R_L ≈ 1 , but < 1

$$\approx \frac{\beta}{1+\beta} = \alpha$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-40

Summary of 3 Amplifiers

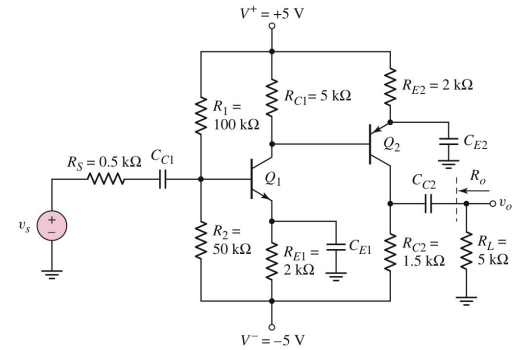
Config	A_v	A_i	R_i	R_o
C-E	$A_v > 1$	$A_i > 1$	(low $k\Omega$) Moderate	(high but function of R_C) Mod to H_i
C-C (emitter follower)	$A_v \approx 1$	$A_i > 1$	(50-100k) High	(10s Ω) Low
CB	$A_v > 1$	$A_v \approx 1$	(10s Ω) Low	(high but function of R_C) Mod to H_i

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-41

Common Emitter Cascade Amplifier

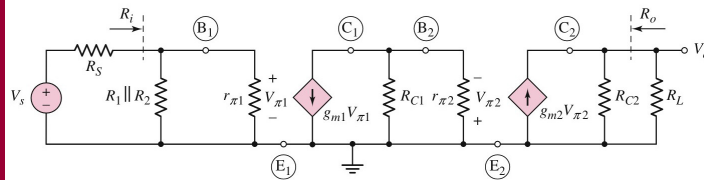


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-42

Small-Signal Equivalent Circuit: Cascade Amplifier

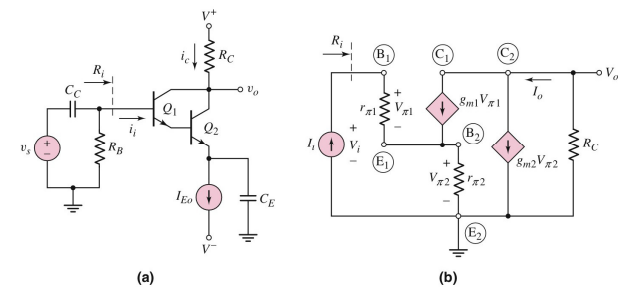


Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-43

Darlington Pair



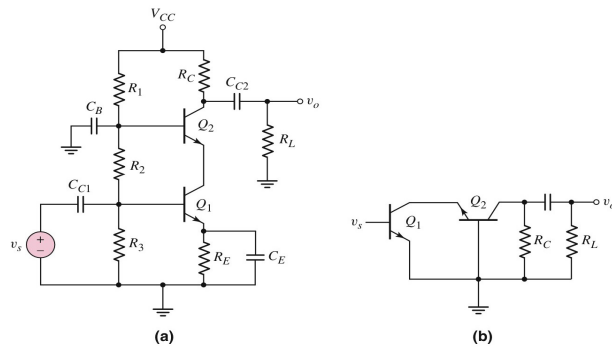
$$A_i \approx \beta_1 \beta_2$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-44

Cascode Amplifier

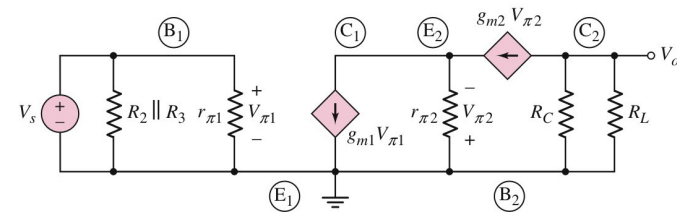

Copyright © The McGraw-Hill Companies, Inc. Permission is required for reproduction or display.

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-45

Small-Signal Equivalent Circuit: Cascode Amplifier


Copyright © The McGraw-Hill Companies, Inc. Permission is required for reproduction or display.

$$A_v \cong -g_{m1}(R_C \parallel R_L)$$

Neamen

Microelectronics, 4e
McGraw-Hill

Chapter 6-46