## Math 335, Fall 2014 Exam 3

NAME:	
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PLEASE PRINT

You have 75 minutes to complete this exam. No calculators or electronic devices are allowed. Show all work. Unsupported or illegible answers will receive no credit. There are a total of 50 points on this exam.



This exam is open notes.

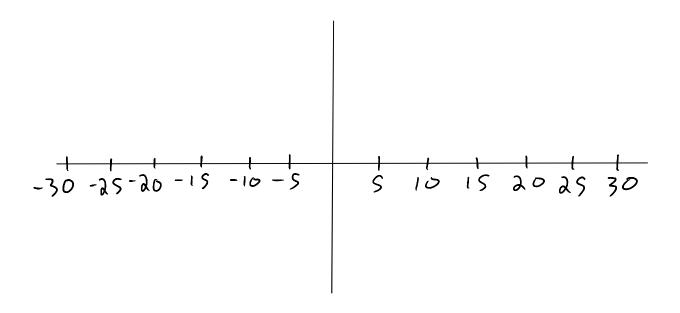
PAGE	SCORE	POINTS
1		10
2		5
3		10
4		10
5		15
TOTAL		50

1.) Let f(x) be the top-hat function

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$$f(x) = \begin{cases} 4 & \text{if } -5 < x < 5 \\ 0 & \text{if } x \le -5 \text{ or } x \ge 5 \end{cases}$$
**a.**) [10 points] Compute the Fourier series of f(x) on the interval (-10,10).

#1 continued...

**b.)** [3 points] Sketch the Fourier series that you computed in part (a) on the axes below for  $-30 \le x \le 30$ . Label the y-axis and clearly indicate function values at discontinuities with open or dark circles.



**c.)** [1 point] What value does the Fourier series converge to at x = 5?

**d.)** [1 point] What value does the Fourier series converge to at x = 10?

**2.)** [10 points] Find the Fourier Cosine Series on  $(0, \pi)$  for  $f(x) = e^x$ . You may make use of the following integration formula:

$$\int e^x \cos(nx) dx = \frac{e^x}{1+n^2} [\cos(nx) + n \sin(nx)]$$

**3.)** [10 points] Consider the following 3rd-order PDE in variables t and z:

$$u_{ttt} = 9u_{zz}$$

 $u_{ttt}=9u_{zz}$  Assume the solution to this PDE is separable. Find the product solution u(t,z) for the case when the separation constant  $\lambda = 0$ . Show all work.

**4.)** [15 points] Solve the boundary value problem below on the interval  $0 \le x \le 3$ .

$$u_{tt} = 25u_{xx}$$

$$u(0,t) = 0, \quad u(3,t) = 0 \quad \text{for all } t \ge 0$$

$$u(x,0) = 0 \quad \text{for } 0 \le x \le 3$$

$$\frac{\partial u}{\partial t}(x,0) = \begin{cases} -2 & \text{if } 0 < x < 1\\ 0 & \text{if } 1 \le x < 3 \end{cases}$$