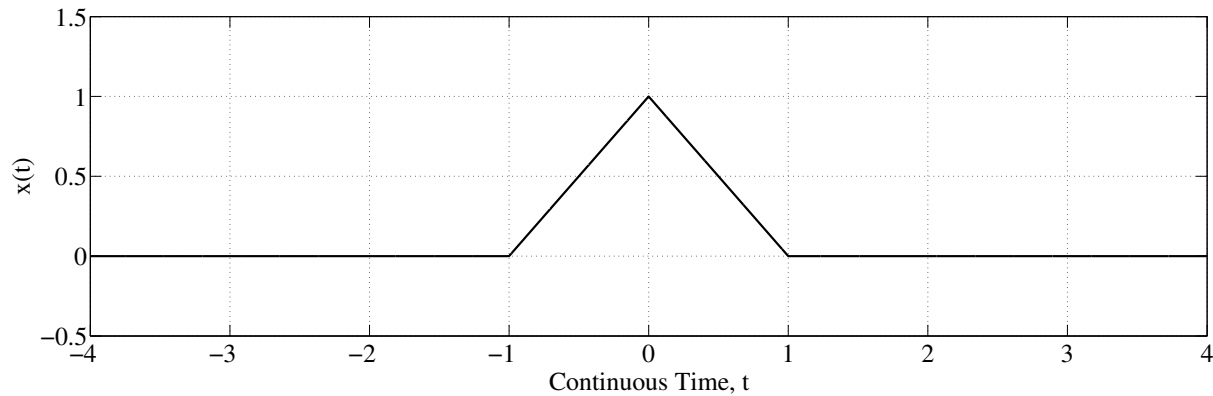


Name: SOLUTIONS

Quiz 1: 10/10

ELEC 309 – Signals & Systems

Consider the following signals  $x(t)$  and  $y(t)$  (on back):



(a) (5 points) Express  $x(t)$  as a single (not piecewise) expression using unit step functions.

The signal  $x(t)$  is given by

$$\begin{aligned}
 x(t) &= \begin{cases} t+1 & -1 \leq t < 0 \\ 1-t & 0 \leq t < 1 \\ 0 & \text{otherwise.} \end{cases} \\
 &= \boxed{(t+1)[u(t+1) - u(t)] + (1-t)[u(t) - u(t-1)]} \\
 &= \boxed{(t+1)u(t+1) - 2tu(t) + (t-1)u(t-1)}
 \end{aligned}$$

(b) (5 points) Evaluate

$$\int_{-4}^4 x(t) [\delta(t+1) + \delta(t+0.5) + \delta(t) + \delta(t-0.5) + \delta(t-1)] dt.$$

$$\begin{aligned}
 &\int_{-4}^4 x(t) [\delta(t+1) + \delta(t+0.5) + \delta(t) + \delta(t-0.5) + \delta(t-1)] dt \\
 &= x(-1) + x(-0.5) + x(0) + x(0.5) + x(1) = 0 + 0.5 + 1 + 0.5 + 0 = \boxed{2}.
 \end{aligned}$$