THE CITADEL THE MILITARY COLLEGE OF SOUTH CAROLINA

Department of Electrical and Computer Engineering

ELEC 318 Electromagnetic Fields

Final exam equation sheets

$$\mathbf{A} = \left| \mathbf{A} \right| = \sqrt{A_x^2 + A_y^2 + A_z^2}$$

$$\mathbf{a} = \mathbf{A} / \left| \mathbf{A} \right| = \mathbf{A} / A$$

$$\mathbf{r}_{PQ} = (x_2 - x_1) \hat{\mathbf{x}} + (y_2 - y_1) \hat{\mathbf{y}} + (y_2 - y_1) \hat{\mathbf{z}}$$

$$\mathbf{A} \cdot \mathbf{B} = \begin{cases} \left| \mathbf{A} \right| \left| \mathbf{B} \right| \cos \theta \\ A B \cos \theta \end{cases} = \begin{pmatrix} (A_x B_x) + (A_y B_y) \\ + (A_z B_z) \end{pmatrix}$$

$$\mathbf{A} \times \mathbf{B} = \begin{cases} \left| \mathbf{A} \right| \left| \mathbf{B} \right| \sin \theta \hat{\mathbf{n}} \\ A B \sin \theta \hat{\mathbf{n}} \end{cases} = \begin{vmatrix} \hat{\mathbf{x}} & \hat{\mathbf{y}} & \hat{\mathbf{z}} \\ A_x & A_y & A_z \\ B & B & B \end{vmatrix}$$

$$x = r\cos\phi, \quad y = r\sin\phi, \quad z = z$$

$$\hat{\mathbf{x}} = \cos\phi \,\hat{\mathbf{r}} - \sin\phi \,\hat{\boldsymbol{\phi}} \qquad \hat{\mathbf{z}} = \hat{\mathbf{z}}$$

$$\hat{\mathbf{y}} = \sin\phi \,\hat{\mathbf{r}} + \cos\phi \,\hat{\boldsymbol{\phi}} \qquad \hat{\mathbf{z}} = \hat{\mathbf{z}}$$

$$\hat{\mathbf{y}} = \sin\phi \,\hat{\mathbf{r}} + \cos\phi \,\hat{\boldsymbol{\phi}} \qquad \hat{\mathbf{y}}$$

$$\hat{\mathbf{z}} = \hat{\mathbf{z}}$$

$$x = R \sin \theta \cos \phi, \quad z = R \cos \theta$$

$$y = R \sin \theta \sin \phi$$

$$\hat{\mathbf{x}} = \sin \theta \cos \phi \, \hat{\mathbf{R}} + \cos \theta \cos \phi \, \hat{\mathbf{\theta}} - \sin \phi \, \hat{\mathbf{\phi}}$$

$$\hat{\mathbf{x}} = \sin \theta \sin \phi \, \hat{\mathbf{x}} + \cos \theta \cos \phi \, \hat{\mathbf{\theta}} - \sin \phi \, \hat{\mathbf{\phi}}$$

$$\hat{\mathbf{x}} = \sin \theta \cos \phi \, \hat{\mathbf{x}} + \sin \theta \sin \phi \, \hat{\mathbf{y}} + \cos \theta \, \hat{\mathbf{z}}$$

$$\hat{\mathbf{y}} = \sin \theta \sin \phi \, \hat{\mathbf{R}} + \cos \theta \sin \phi \, \hat{\mathbf{\theta}} + \cos \phi \, \hat{\mathbf{\phi}}$$

$$\hat{\mathbf{\theta}} = \cos \theta \cos \phi \, \hat{\mathbf{x}} + \cos \theta \sin \phi \, \hat{\mathbf{y}} - \sin \theta \, \hat{\mathbf{z}}$$

$$\hat{\mathbf{z}} = \cos \theta \, \hat{\mathbf{R}} - \sin \theta \, \hat{\mathbf{\theta}}$$

$$\hat{\mathbf{\phi}} = -\sin \phi \, \hat{\mathbf{x}} + \cos \phi \, \hat{\mathbf{y}}$$

$$d\mathbf{l} = dx \,\hat{\mathbf{x}} + dy \,\hat{\mathbf{y}} + dz \,\hat{\mathbf{z}}$$

$$d\mathbf{l} = dr \,\hat{\mathbf{r}} + r \,d\phi \,\hat{\boldsymbol{\phi}} + dz \,\hat{\mathbf{z}}$$

$$d\mathbf{l} = dr \,\hat{\mathbf{R}} + R \,d\theta \,\hat{\boldsymbol{\theta}}$$

$$+ R \sin\theta \,d\phi \,\hat{\boldsymbol{\phi}}$$

$$d\mathbf{S} = dy \,dz \,\hat{\mathbf{x}}$$

$$d\mathbf{S} = r \,d\phi \,dz \,\hat{\mathbf{r}}$$

$$d\mathbf{S} = R^2 \sin\theta \,d\theta \,d\phi \,\hat{\mathbf{R}}$$

$$d\mathbf{S} = R \sin\theta \,dR \,d\phi \,\hat{\boldsymbol{\theta}}$$

$$d\mathbf{S} = R \sin\theta \,dR \,d\phi \,\hat{\boldsymbol{\theta}}$$

$$d\mathbf{S} = R \,dR \,d\theta \,\hat{\boldsymbol{\phi}}$$

$$d\mathbf{S} = R \,dR \,d\theta \,d\phi$$

$$\nabla V = \frac{\partial V}{\partial x} \hat{\mathbf{x}} + \frac{\partial V}{\partial y} \hat{\mathbf{y}} + \frac{\partial V}{\partial z} \hat{\mathbf{z}} = \frac{\partial V}{\partial r} \hat{\mathbf{r}} + \frac{1}{r} \frac{\partial V}{\partial \phi} \hat{\boldsymbol{\phi}} + \frac{\partial V}{\partial z} \hat{\mathbf{z}}$$
$$= \frac{\partial V}{\partial R} \hat{\mathbf{R}} + \frac{1}{R} \frac{\partial V}{\partial \theta} \hat{\boldsymbol{\theta}} + \frac{1}{R \sin \theta} \frac{\partial V}{\partial \phi} \hat{\boldsymbol{\phi}}$$

$$\nabla \cdot \mathbf{A} = \frac{\partial A_x}{\partial x} + \frac{\partial A_y}{\partial y} + \frac{\partial A_z}{\partial z} = \frac{1}{r} \frac{\partial}{\partial r} (rA_r) + \frac{1}{r} \frac{\partial}{\partial \phi} A_{\phi} + \frac{\partial}{\partial z} A_z$$

$$= \frac{1}{R^2} \frac{\partial}{\partial R} (R^2 A_R) + \frac{1}{R \sin \theta} \frac{\partial}{\partial \theta} (A_{\theta} \sin \theta) + \frac{1}{R \sin \theta} \frac{\partial}{\partial \phi} A_{\phi}$$

$$\nabla \times \mathbf{A} = \begin{bmatrix} \hat{\mathbf{x}} & \hat{\mathbf{y}} & \hat{\mathbf{z}} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ A_x & A_y & A_z \end{bmatrix} = \begin{bmatrix} \hat{\mathbf{r}} & r \hat{\boldsymbol{\phi}} & \hat{\mathbf{z}} \\ \frac{\partial}{\partial r} & \frac{\partial}{\partial \phi} & \frac{\partial}{\partial z} \\ A_r & rA_{\phi} & A_z \end{bmatrix} = \begin{bmatrix} \hat{\mathbf{R}} & R \hat{\boldsymbol{\theta}} & R \sin \theta \hat{\boldsymbol{\phi}} \\ \frac{\partial}{\partial R} & \frac{\partial}{\partial \theta} & \frac{\partial}{\partial \phi} \\ A_R & RA_{\theta} & R \sin \theta A_{\phi} \end{bmatrix}$$

$$\nabla^{2}V = \frac{\partial^{2}V}{\partial x^{2}} + \frac{\partial^{2}V}{\partial y^{2}} + \frac{\partial^{2}V}{\partial z^{2}}$$

$$= \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial V}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2}V}{\partial \phi^{2}} + \frac{\partial^{2}V}{\partial z^{2}}$$

$$= \frac{1}{R^{2}} \frac{\partial}{\partial R} \left(R^{2} \frac{\partial V}{\partial R} \right) + \frac{1}{R^{2} \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial V}{\partial \theta} \right) + \frac{1}{R^{2} \sin^{2}\theta} \frac{\partial^{2}V}{\partial \phi^{2}}$$

$$= \frac{1}{R^{2}} \frac{\partial}{\partial R} \left(R^{2} \frac{\partial V}{\partial R} \right) + \frac{1}{R^{2} \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial V}{\partial \theta} \right) + \frac{1}{R^{2} \sin^{2}\theta} \frac{\partial^{2}V}{\partial \phi^{2}}$$

$$= \frac{\partial^{2}V}{\partial x^{2}} = 0 \quad \Rightarrow \quad V = V_{1}x + V_{2}$$

$$= \frac{\partial^{2}V}{\partial x^{2}} = 0 \quad \Rightarrow \quad V = V_{1} \ln (r) + V_{2}$$

$$= \frac{\partial^{2}V}{\partial R} \left(R^{2} \frac{\partial V}{\partial R} \right) + \frac{1}{R^{2} \sin \theta} \frac{\partial^{2}V}{\partial \theta} \left(\sin \theta \frac{\partial V}{\partial \theta} \right) + \frac{1}{R^{2} \sin^{2}\theta} \frac{\partial^{2}V}{\partial \phi^{2}}$$

$$= \frac{\partial^{2}V}{\partial R} \left(R^{2} \frac{\partial V}{\partial R} \right) = 0 \quad \Rightarrow \quad V = \frac{V_{1}}{R} + V_{2}$$

$$\oint_{S} \mathbf{A} \cdot d\mathbf{S} = \int_{V} \nabla \cdot \mathbf{A} \ dV \qquad \qquad \oint_{L} \mathbf{A} \cdot d\mathbf{l} = \int_{S} (\nabla \times \mathbf{A}) \cdot d\mathbf{S} \qquad \qquad d\mathbf{S} = dS \ \hat{\mathbf{n}} \qquad \qquad \hat{\mathbf{n}} = \frac{\nabla f}{|\nabla f|}$$

$$\mathbf{F} = \frac{q_1 q_2}{4\pi\varepsilon_0} \cdot \frac{\mathbf{R} - \mathbf{R}'}{\left|\mathbf{R} - \mathbf{R}'\right|^3} \qquad d\mathbf{E} = \frac{dq}{4\pi\varepsilon_0} \cdot \frac{\mathbf{R} - \mathbf{R}'}{\left|\mathbf{R} - \mathbf{R}'\right|^3} \qquad \mathbf{E} = \frac{\mathbf{F}}{q} \qquad \mathbf{E} = \sum_{k=1}^{N} \frac{q_k}{4\pi\varepsilon_0} \cdot \frac{\mathbf{R} - \mathbf{R}'_k}{\left|\mathbf{R} - \mathbf{R}'_k\right|^3}$$

$$\mathbf{E} = \frac{q}{4\pi\varepsilon_0} \cdot \frac{\mathbf{R} - \mathbf{R}'}{\left|\mathbf{R} - \mathbf{R}'\right|^3} \qquad dq = \rho_i dl \qquad \mathbf{E} = \frac{1}{4\pi\varepsilon_0} \int dq \frac{\mathbf{R} - \mathbf{R}'}{\left|\mathbf{R} - \mathbf{R}'\right|^3}$$

$$\nabla^{2}V = -\frac{\rho_{v}}{\varepsilon}$$

$$\mathbf{E} = -\nabla V$$

$$V_{AB} = \frac{W}{q} = -\int_{A}^{B} \mathbf{E} \cdot d\mathbf{l}$$

$$dV = \frac{dq}{4\pi\varepsilon_{0} |\mathbf{R} - \mathbf{R}'|}$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\int_{L}^{\Phi} \mathbf{E} \cdot d\mathbf{l} = -\frac{\partial}{\partial t} \iint_{S} \mathbf{B} \cdot d\mathbf{S}$$

$$V_{\text{charge}}^{\text{point}} = \frac{q}{4\pi\varepsilon_{0} |\mathbf{R} - \mathbf{R}'|}$$

$$\mathbf{E}_{\text{charge}}^{\text{point}} = \frac{q}{4\pi\varepsilon_{0}R^{2}}\hat{\mathbf{R}}$$

$$\mathbf{E}_{\text{line charge}}^{\text{infinite}} = \frac{\rho_l}{2\pi\varepsilon_0 r} \,\hat{\mathbf{r}}$$

$$V_{\text{charge}}^{\text{line}} = \frac{\rho_l}{2\pi\varepsilon_0} \ln(r)$$

$$\mathbf{E}_{\text{dipole}}^{\text{electric}} \approx \frac{q \cdot d \cdot \cos \theta}{2 \pi \varepsilon_0 R^3} \hat{\mathbf{R}} + \frac{q \cdot d \cdot \sin \theta}{4 \pi \varepsilon_0 R^3} \hat{\boldsymbol{\theta}}$$

$$\mathbf{E}_{\text{surf charge}}^{\text{infinite}} = \frac{\rho_s}{2\varepsilon_0} \hat{\mathbf{n}}$$

$$\nabla \cdot \mathbf{D} = \rho_{\mathbf{v}}$$

$$Q = \int_{S} \mathbf{D} \cdot d\mathbf{S}$$

$$\mathbf{D} = \varepsilon \mathbf{E}$$

$$\mathbf{D} = \varepsilon_0 \mathbf{E} + \mathbf{P}$$
$$= (1 + \chi_e) \varepsilon_0 \mathbf{E}$$

$$\varepsilon = \varepsilon_r \varepsilon_0$$

$$E_{1t} = E_2$$

$$\varepsilon = \varepsilon_r \varepsilon_0 \qquad \qquad E_{1t} = E_{2t} \qquad \qquad D_{1n} - D_{2n} = \rho_s$$

$$J = \sigma E$$

$$\mathbf{J} = \rho_{\mathbf{v}} \cdot \mathbf{u}$$

$$I = \frac{dQ}{dt}$$

$$\mathbf{J} = \frac{dI}{dS}\hat{\mathbf{n}}$$

$$I = \int_{S} \mathbf{J} \cdot d\mathbf{S}$$

$$R = \frac{V}{I} = \frac{\int_{L} \mathbf{E} \cdot d\mathbf{l}}{\int_{S} \sigma \, \mathbf{E} \cdot d\mathbf{S}}$$

$$C = \frac{Q}{V} = \frac{\varepsilon \int_{s} \mathbf{E} \cdot d\mathbf{S}}{\int_{L} \mathbf{E} \cdot d\mathbf{l}} \qquad C_{\text{plates}}^{\text{parallel}} = \varepsilon \frac{A}{d}$$

$$C_{\text{plates}}^{\text{parallel}} = \varepsilon \frac{A}{d}$$

$$R_{\text{cross sec}}^{\text{uniform}} = \frac{l}{\sigma A}$$

$$C_{\text{line}}^{\text{coaxial}} = \frac{2\pi \ \varepsilon \ l}{\ln \left(b/a \right)}$$

$$C_{\text{spheres}}^{\text{two}} = \frac{4\pi \ \varepsilon}{\frac{1}{a} - \frac{1}{b}}$$

$$W_E = \frac{1}{2} \sum_{k=1}^N q_k V_k$$

$$W_E = \frac{1}{2} \sum_{k=0}^{N} q_k V_k$$
 $W_E = \frac{1}{2} \int_{V} \varepsilon \left| \mathbf{E} \right|^2 dV$ $W_E = \frac{1}{2} C V^2$ $\varepsilon_0 = 8.854 \times 10^{-12} \text{ F/m}$

$$W_E = \frac{1}{2} C V^2$$

$$\varepsilon_0 = 8.854 \times 10^{-12} \text{ F/m}$$

$$S_{\text{cylinder}} = 2\pi r^2 + 2\pi rh$$

$$v_{\text{cylinder}} = \pi r^2 h$$

$$c_{\rm circle} = 2 \pi r$$

$$S_{\rm sphere} = 4 \pi r^2$$

$$v_{\rm sphere} = \frac{4}{3} \pi r^3$$

$$S_{\rm circle} = \pi r^2$$

$$l_{\rm arc} = r \phi$$

$$dl_{\rm arc} = r \ d\phi$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{I}}{\partial t}$$

$$\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} \qquad \qquad \int_{L} \mathbf{H} \cdot d\mathbf{l} = I + \frac{\partial}{\partial t} \iint_{S} \mathbf{D} \cdot d\mathbf{S}$$

$$\mathbf{H} = \int_{L} \frac{I}{4\pi} \frac{d\mathbf{l} \times (\mathbf{R} - \mathbf{R}')}{|\mathbf{R} - \mathbf{R}'|^{3}}$$

$$\mathbf{H} = \iint_{S} \frac{\mathbf{J}_{s} \times (\mathbf{R} - \mathbf{R}')}{4\pi |\mathbf{R} - \mathbf{R}'|^{3}} dS$$

$$\mathbf{H} = \iiint_{v} \frac{\mathbf{J}_{v} \times (\mathbf{R} - \mathbf{R}')}{4\pi |\mathbf{R} - \mathbf{R}'|^{3}} dv$$

$$\mathbf{H}_{\text{line}}^{\text{infinite}} = \frac{I}{2\pi r} \mathbf{q}$$

$$\mathbf{H}_{\text{line}}^{\text{infinite}} = \frac{I}{2\pi r} \hat{\boldsymbol{\phi}} \qquad \qquad \mathbf{H}_{\text{current}}^{\text{ring of}} = \frac{I a^2}{2(a^2 + z^2)^{3/2}} \hat{\mathbf{z}}$$

$$\mathbf{H}_{\text{dipole}}^{\text{magnetic}} = \frac{a^2 I}{4 R^3} \left\{ 2 \cdot \cos \theta \, \hat{\mathbf{R}} + \sin \theta \, \hat{\boldsymbol{\theta}} \right\}$$

$$\mathbf{H}_{\text{sheet}}^{\text{infinite}} = \begin{cases} -\hat{\mathbf{y}} J_s / 2 & z > 0 \\ +\hat{\mathbf{y}} J_s / 2 & z < 0 \end{cases}$$

$$\mathbf{H}_{\text{filament}}^{\text{straight}} = \frac{I}{4\pi r} \{ \cos \theta_1 - \cos \theta_2 \} \hat{\boldsymbol{\phi}}$$

$$\mathbf{B} = \mu \mathbf{H}$$

$$\mathbf{B} = \mu_0 \mathbf{H} + \mathbf{M}$$
$$= (1 + \chi_m) \mu_0 \mathbf{H}$$

$$\mu = \mu_r \mu_0$$

$$B_{1n} = B_{2n}$$
 $H_{1t} - H_{2t} = J_{s}$

$$\mathbf{F}_{\mathbf{m}} = q \left(\mathbf{u} \times \mathbf{B} \right)$$

$$\mathbf{F} = q \left(\mathbf{E} + \mathbf{u} \times \mathbf{B} \right)$$

$$\mathbf{F} = I \int_{L} d\mathbf{l} \times \mathbf{B}$$

$$T = \mathbf{d} \times \mathbf{F}$$
$$= \mathbf{m} \times \mathbf{B}$$

$$\mathbf{m} = N \cdot I \cdot S \ \hat{\mathbf{n}}$$

$$L = \frac{\lambda}{I}$$

$$L = \frac{\lambda}{I} \qquad M_{12} = \frac{\lambda_{12}}{I_2} \qquad \lambda = N \Psi$$

$$\lambda = N \Upsilon$$

$$\Psi = \int_{S} \mathbf{B} \cdot d\mathbf{S}$$

$$L_{\text{line}}^{\text{coaxial}} = \frac{\mu_0 l}{2\pi} \ln \left(\frac{b}{a}\right)$$

$$L_{\rm line}^{\rm coaxial} = \frac{\mu_0 l}{2\pi} \ln \left(\frac{b}{a}\right) \qquad L_{\rm coil}^{\rm toroidal} = \frac{\mu N^2 h}{2\pi} \ln \left(\frac{b}{a}\right) \qquad L_{\rm solenoid} = \frac{\mu_0 N^2 S}{l} \qquad L_{\rm wires}^{\rm parallel} = \frac{\mu_0 l}{\pi} \ln \left(\frac{d}{a}\right)$$

$$L_{\text{solenoid}} = \frac{\mu_0 N^2 S}{l}$$

$$L_{\text{wires}}^{\text{parallel}} = \frac{\mu_0 l}{\pi} \ln \left(\frac{d}{a} \right)$$

$$W_{m} = \frac{1}{2} \iiint_{v} \mu \left| \mathbf{H} \right|^{2} dv$$

$$W_{m} = \frac{1}{2}LI$$

$$V_{\rm emf} = -N \frac{\partial}{\partial t} Y$$

$$V_{\text{emf}}^{\text{transformer}} = -\iint_{S} \frac{d\mathbf{B}}{dt} \cdot d\mathbf{S}$$

$$V_{\text{emf}} = -N \frac{\partial}{\partial t} \Psi \qquad V_{\text{emf}}^{\text{transformer}} = -\iint_{S} \frac{d\mathbf{B}}{dt} \cdot d\mathbf{S} \qquad V_{\text{emf}}^{\text{motional}} = -\iint_{S} \mathbf{B} \cdot \frac{d\mathbf{S}}{dt} = -\iint_{L} (\mathbf{u} \times \mathbf{B}) \cdot d\mathbf{l}$$

$$\frac{V_2}{V_1} = \frac{N_2}{N_1} = \frac{I_1}{I_2} \qquad \qquad \mathbf{J}_d = \frac{\partial \mathbf{D}}{\partial t} \qquad \qquad I_d = \frac{\partial}{\partial t} \iint_{\mathcal{S}} \mathbf{D} \cdot d\mathbf{S}$$

$$\mathbf{J}_{d} = \frac{\partial \mathbf{I}}{\partial t}$$

$$I_d = \frac{\partial}{\partial t} \iint_S \mathbf{D} \cdot d\mathbf{S}$$

$$I_{\text{RMS}} = \frac{I_m}{\sqrt{2}}$$

$$\nabla \cdot \hat{\mathbf{D}} = \hat{\rho}$$

$$\nabla \times \mathbf{E} = -j\omega \mathbf{E}$$

$$\nabla \cdot \tilde{\mathbf{D}} = \tilde{\rho}_{v} \qquad \qquad \nabla \times \tilde{\mathbf{E}} = -j\omega \tilde{\mathbf{B}} \qquad \qquad \nabla \times \tilde{\mathbf{H}} = \tilde{\mathbf{J}} + j\omega \tilde{\mathbf{D}} \qquad \qquad \nabla \cdot \tilde{\mathbf{B}} = 0$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\mathbf{E}\left(z,t\right) = E_{0}e^{-\alpha z}\cos\left(\omega t - \beta z + \phi_{0}\right)\hat{\mathbf{x}} \qquad \Leftrightarrow \qquad \mathbf{\tilde{E}} = E_{0}e^{-\alpha z}e^{-j\beta z + j\phi_{0}}\hat{\mathbf{x}}$$

$$\Leftrightarrow$$

$$\mathbf{\tilde{E}} = E_0 e^{-\alpha z} e^{-j\beta z + j\phi_0} \hat{\mathbf{x}}$$

$$\tilde{\mathbf{J}}_{d} = j\omega \tilde{\mathbf{D}}$$

$$\frac{dz}{dt} = u = \frac{\omega}{\beta} = \frac{1}{\sqrt{\mu\varepsilon}}$$

$$\lambda = \frac{2\pi}{\beta} \qquad f = \frac{\omega}{2\pi} \qquad T = \frac{1}{f}$$

$$f = \frac{\omega}{2\pi}$$

$$T = \frac{1}{f}$$

$$\alpha, \beta = \omega \sqrt{\frac{\mu \varepsilon}{2} \left[\sqrt{1 + \left(\frac{\sigma}{\omega \varepsilon} \right)^2} \mp 1 \right]} \qquad \eta = \frac{E_0}{H_0} = \frac{\omega \mu}{\beta - j\alpha} \qquad \tan \theta = \frac{\sigma}{\omega \varepsilon} \qquad \delta = \frac{1}{\alpha}$$

$$\eta = \frac{E_0}{H_0} = \frac{\omega \mu}{\beta - j\alpha}$$

$$\tan \theta = \frac{\sigma}{\omega \varepsilon}$$

$$\delta = \frac{1}{2}$$

$$\mathscr{S} = \mathbf{E} \times \mathbf{H}$$

$$\mathscr{S} = \mathbf{E} \times \mathbf{H} \qquad \qquad P = \iint_{S} \mathscr{S} \cdot d\mathbf{S}$$

$$u = \frac{dx}{dt} \qquad \qquad a = \frac{du}{dt}$$

$$a = \frac{du}{dt}$$