



# handling writes

what about writing to the cache?

two decision points:

if the value is not in cache, do we add it?

- if yes: need to load rest of block

- if no: missing out on locality?

if value is in cache, when do we update next level?

- if immediately: extra writing

- if later: need to remember to do so

# allocate on write?

processor writes **less than whole** cache block

block not yet in cache

two options:

## write-allocate

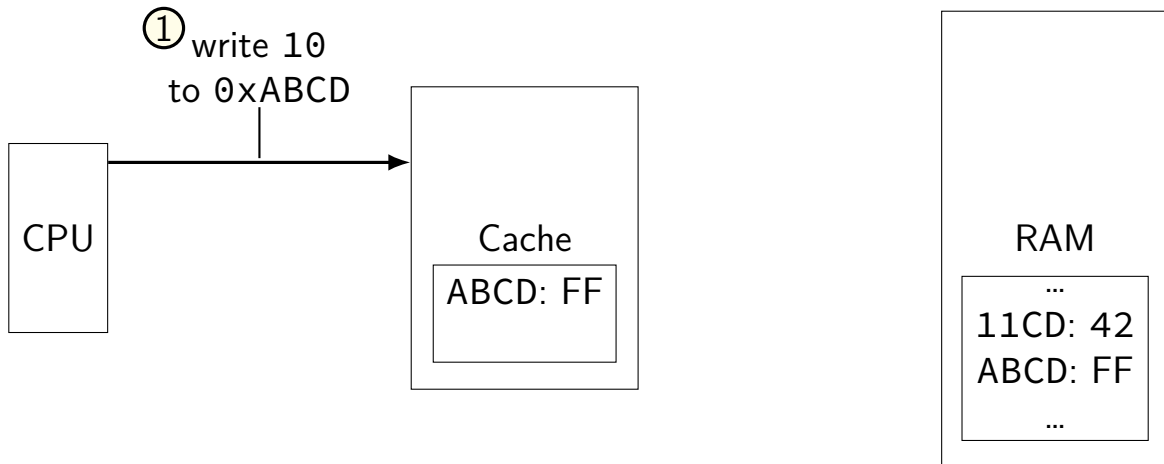
fetch rest of cache block, replace written part  
(then follow write-through or write-back policy)

## write-no-allocate

don't use cache at all (send write to memory *instead*)  
guess: not read soon?

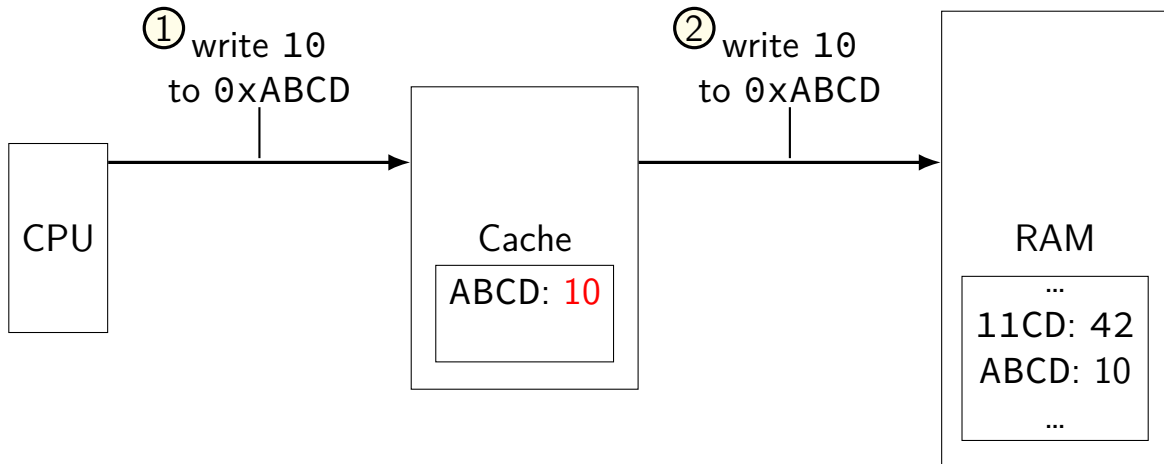
# write-through v. write-back

## option 1: write-through



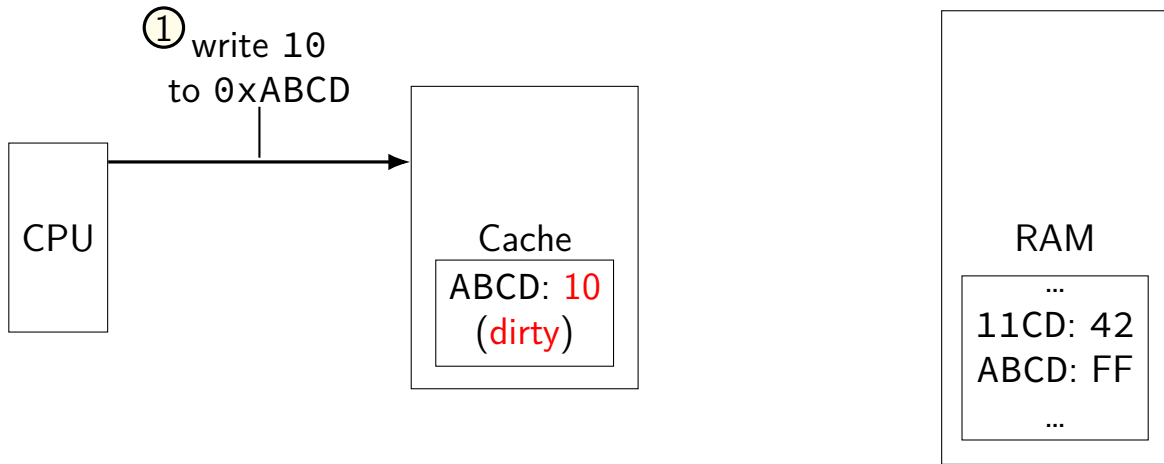
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## option 1: write-through



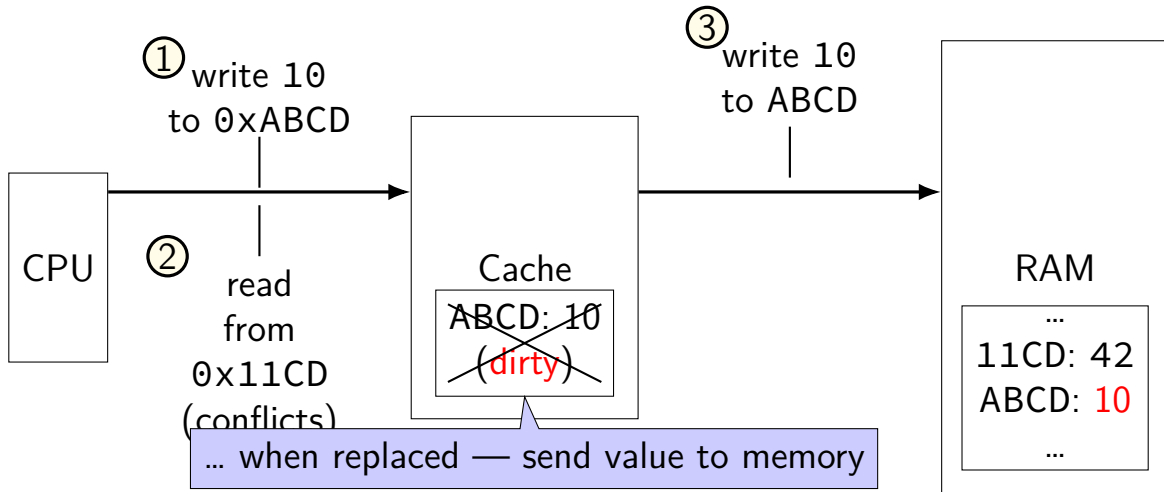
# write-through v. write-back

## option 2: write-back

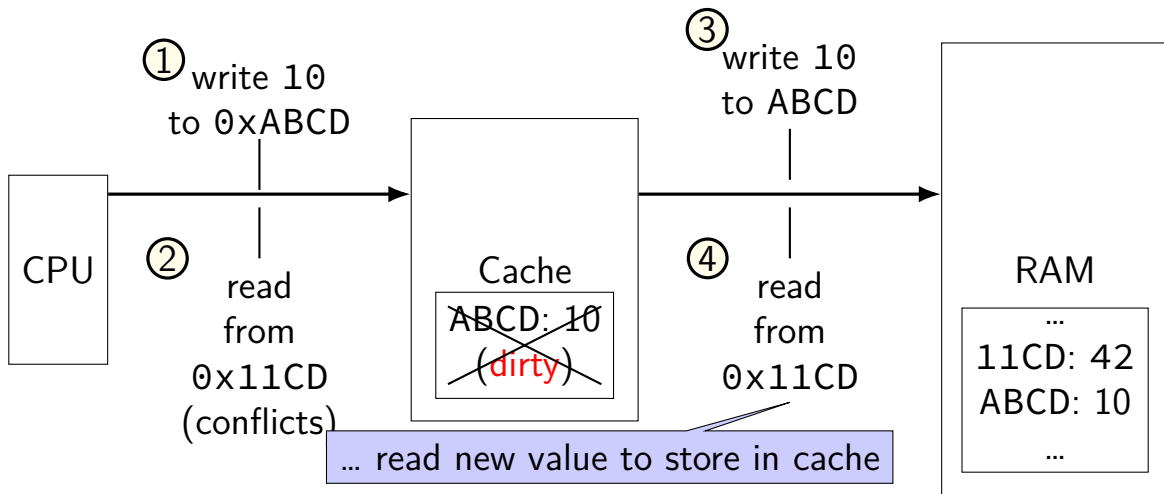


# write-through v. write-back

## option 2: write-back



# write-through v. write-back





# writeback policy

changed value!

2-way set associative, 4 byte blocks, 2 sets

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

1 = dirty (different than memory)  
needs to be written if evicted

# write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address 0x04?

index 0, tag 000001

# write-allocate + write-back

2-way set associative, LRU, writeback

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1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address 0x04?

index 0, tag 000001

step 1: find **least recently used** block

# write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address 0x04?

index 0, tag 000001

step 1: find **least recently used** block

step 2: possibly writeback old block

# write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	000001	0xFF mem[0x05]	1	0
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address 0x04?

index 0, tag 000001

step 1: find **least recently used** block

step 2: possibly writeback old block

step 3a: read in new block – to get mem[0x05]

step 3b: update LRU information

# write-no-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address 0x04?

step 1: is it in cache yet?

step 2: no, just send it to memory

# exercise (1)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	001100	mem[0x30] mem[0x31]	0	1	010000	mem[0x40]* mem[0x41]*	1	0
1	1	011000	mem[0x62] mem[0x63]	0	1	001100	mem[0x32]* mem[0x33]*	1	1

for each of the following accesses, performed alone, would it require (a) reading a value from memory (or next level of cache) and (b) writing a value to the memory (or next level of cache)?

writing 1 byte to 0x33

reading 1 byte from 0x52

reading 1 byte from 0x50

## exercise (2)

2-way set associative, LRU, write-no-allocate, write-through

index	valid	tag	value	valid	tag	value	LRU
0	1	001100	mem[0x30] mem[0x31]	1	010000	mem[0x40] mem[0x41]	0
1	1	011000	mem[0x62] mem[0x63]	1	001100	mem[0x32] mem[0x33]	1

for each of the following accesses, performed alone, would it require (a) reading a value from memory and (b) writing a value to the memory?

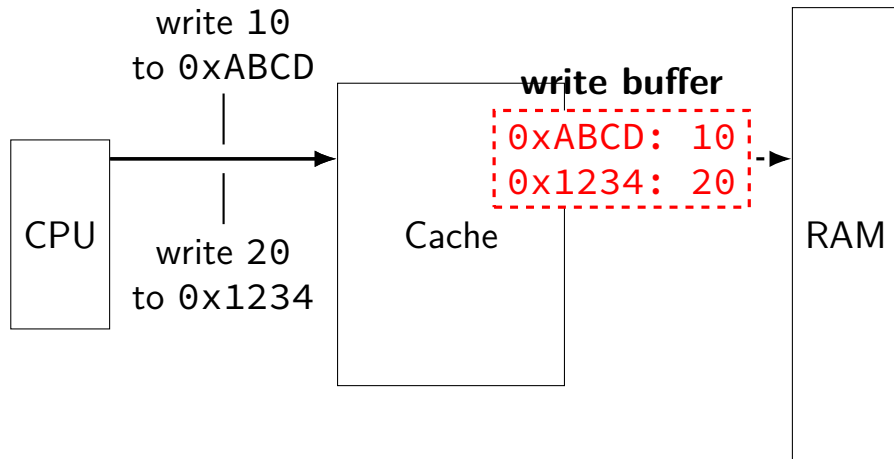
writing 1 byte to 0x33

reading 1 byte from 0x52

reading 1 byte from 0x50



# fast writes



write appears to complete immediately when placed in buffer  
memory can be much slower

# cache miss types

common to categorize misses:

roughly “cause” of miss assuming cache block size fixed

*compulsory* (or *cold*) — **first time** accessing something  
adding more sets or blocks/set wouldn't change

*conflict* — sets aren't big/flexible enough  
a fully-associative (1-set) cache of the same size would have done better

*capacity* — cache was not big enough

*coherence* — from sync'ing cache with other caches  
only issue with multiple cores

# making any cache look bad

1. access enough blocks, to fill the cache
2. access an additional block, replacing something
3. access last block replaced
4. access last block replaced
5. access last block replaced
- ...

but — typical real programs have **locality**

# cache optimizations

(assuming typical locality + keeping cache size constant if possible...)

	miss rate	hit time	miss penalty
increase cache size	better	worse	—
increase associativity	better	worse	worse?
increase block size	depends	worse	worse
add secondary cache	—	—	better
write-allocate	better	—	?
writeback	—	—	?
LRU replacement	better	?	worse?
prefetching	better	—	—

prefetching = guess what program will use, access in advance

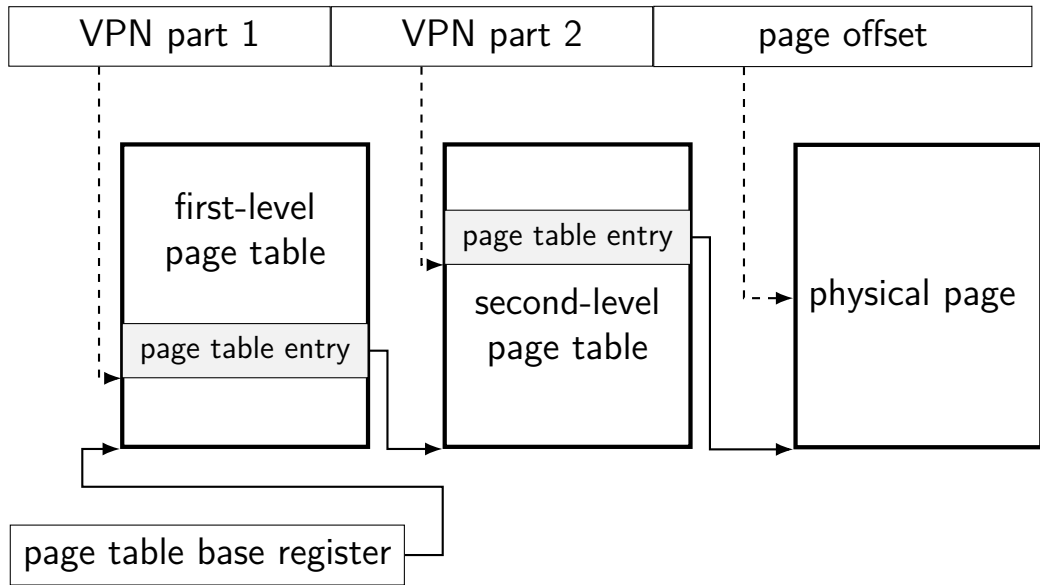
$$\text{average time} = \text{hit time} + \text{miss rate} \times \text{miss penalty}$$

# cache optimizations by miss type

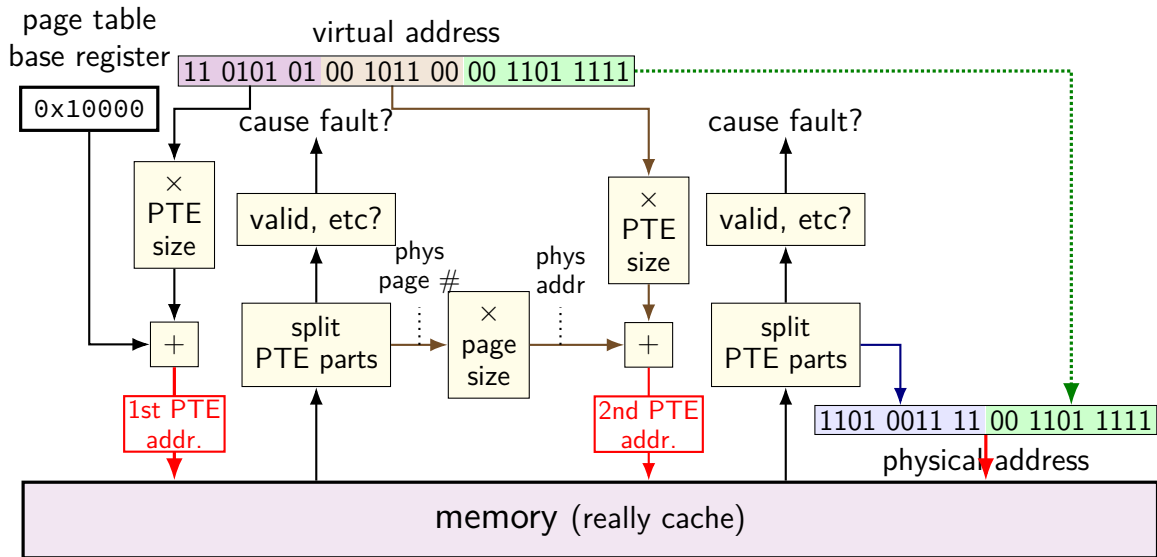
(assuming other listed parameters remain constant)

	capacity	conflict	compulsory
increase cache size	fewer misses	fewer misses	—
increase associativity	—	fewer misses	—
increase block size	more misses?	more misses?	fewer misses
LRU replacement	—	fewer misses	—
prefetching	—	—	fewer misses

## another view



# two-level page table lookup



## cache accesses and multi-level PTs

four-level page tables — five cache accesses per program memory access

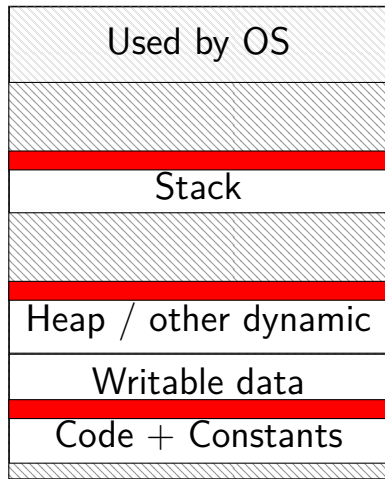
L1 cache hits — typically a couple cycles each?

so add 8 cycles to each program memory access?

not acceptable



# program memory active sets



0xFFFF FFFF FFFF FFFF

0xFFFF 8000 0000 0000

0x7F...

small areas of memory active at a time  
one or two pages in each area?

0x0000 0000 0040 0000

# page table entries and locality

page table entries have **excellent temporal locality**

typically one or two pages of the stack active

typically one or two pages of code active

typically one or two pages of heap/globals active

each page contains **whole functions**, arrays, stack frames, etc.

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typically one or two pages of code active

typically one or two pages of heap/globals active

each page contains **whole functions**, arrays, stack frames, etc.

needed page table entries are **very small**

# page table entry cache

called a **TLB** (translation lookaside buffer)

very small cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

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only caches the page table lookup itself (generally) just entries from the last-level page tables	

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L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
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not much spatial locality between page table entries  
(they're used for kilobytes of data already)  
(and if spatial locality, maybe use larger page size?)

# page table entry cache

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L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

few active page table entries at a time  
enables highly associative cache designs

# TLB and multi-level page tables

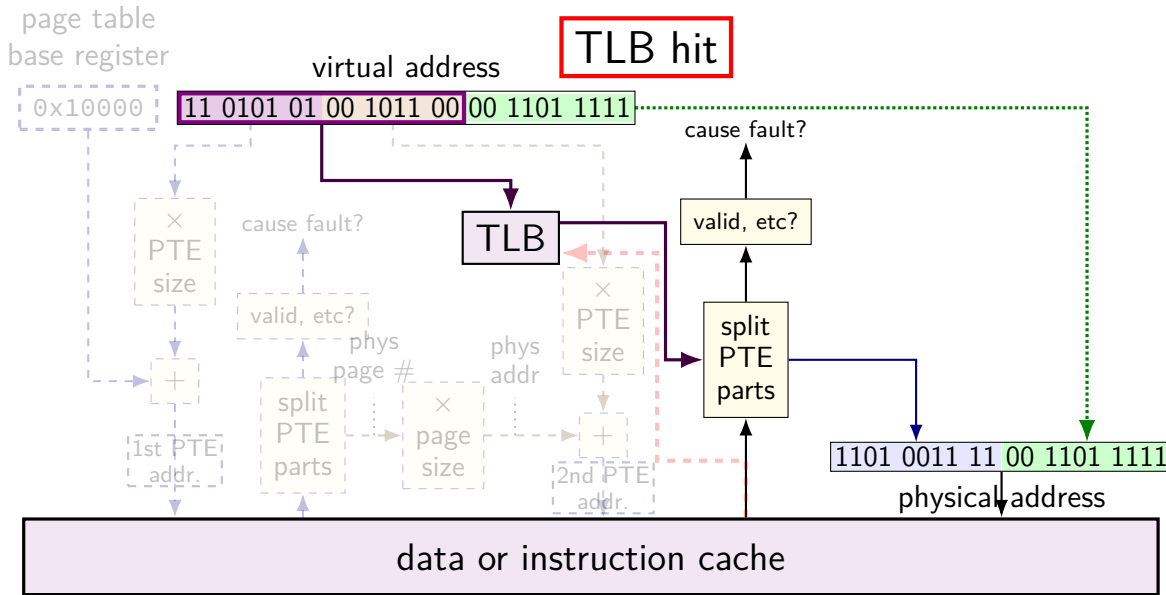
TLB caches **valid last-level page table entries**

doesn't matter which last-level page table

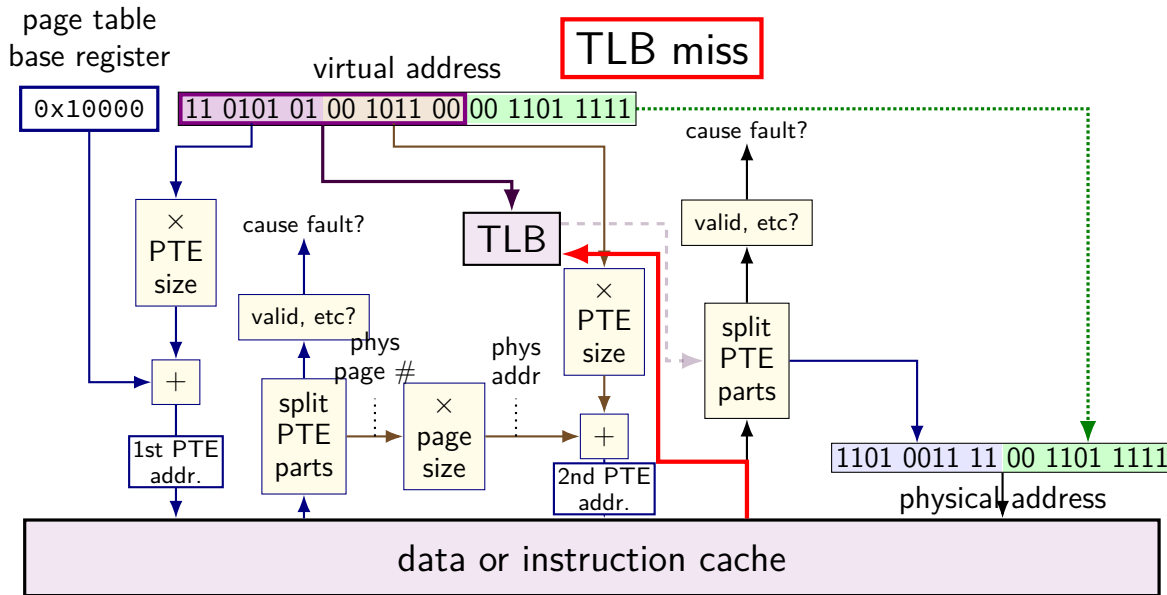
means TLB output can be used directly to form address



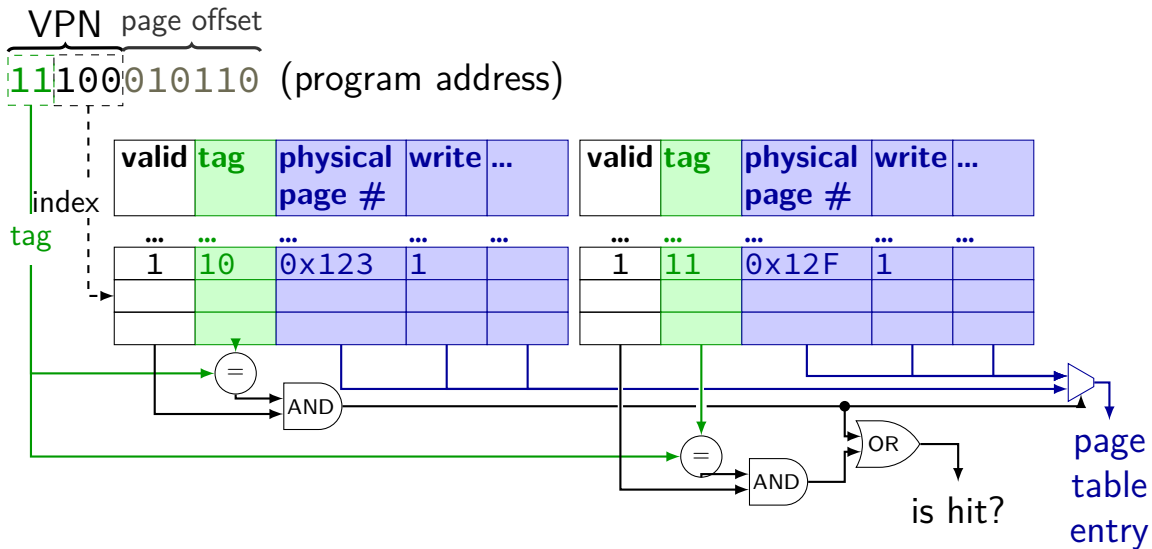
## TLB and two-level lookup



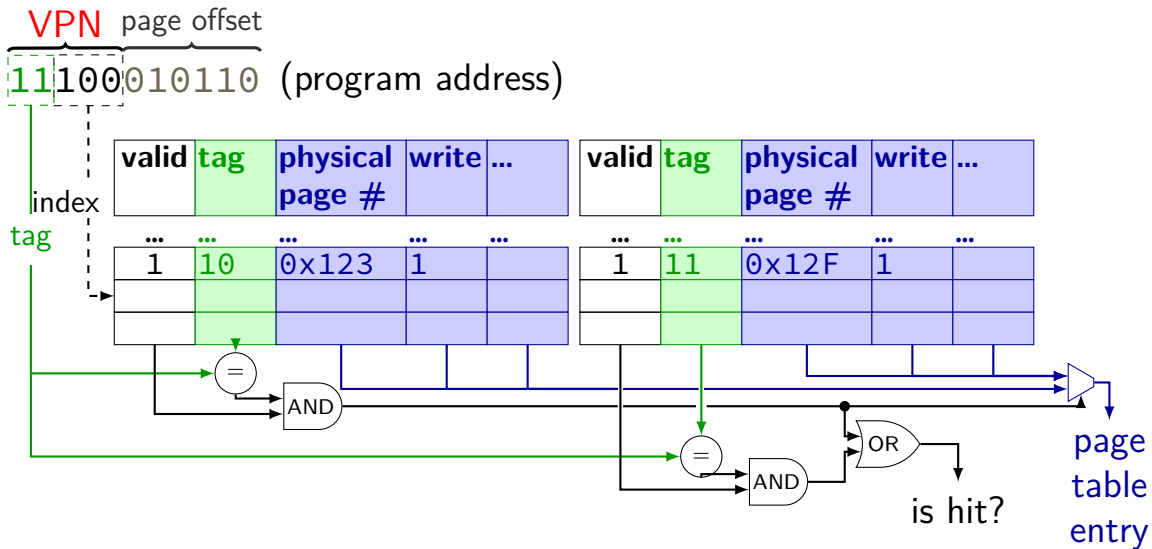
# TLB and two-level lookup



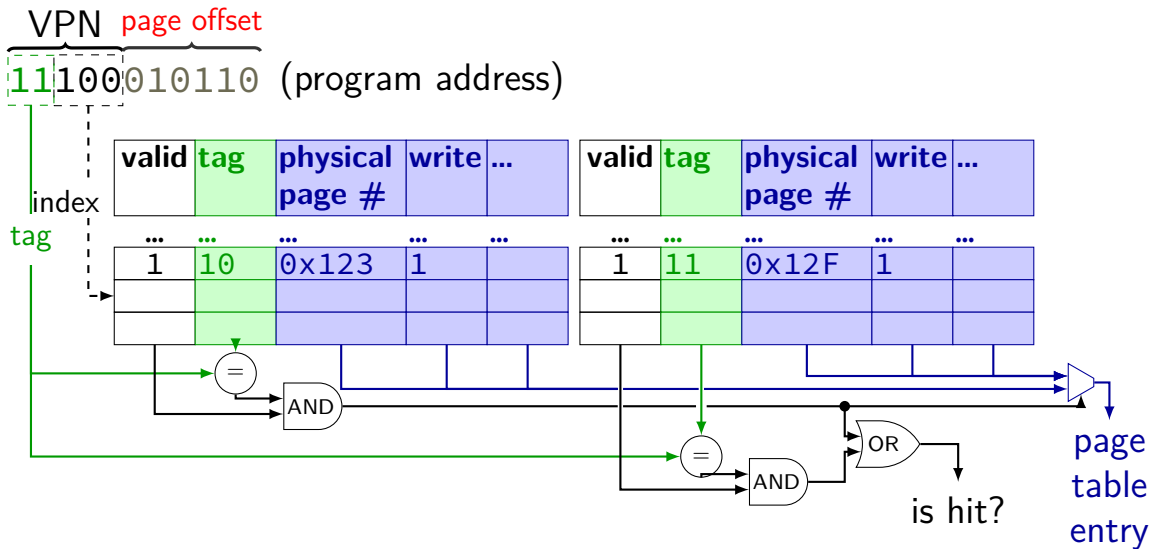
# TLB organization (2-way set associative)



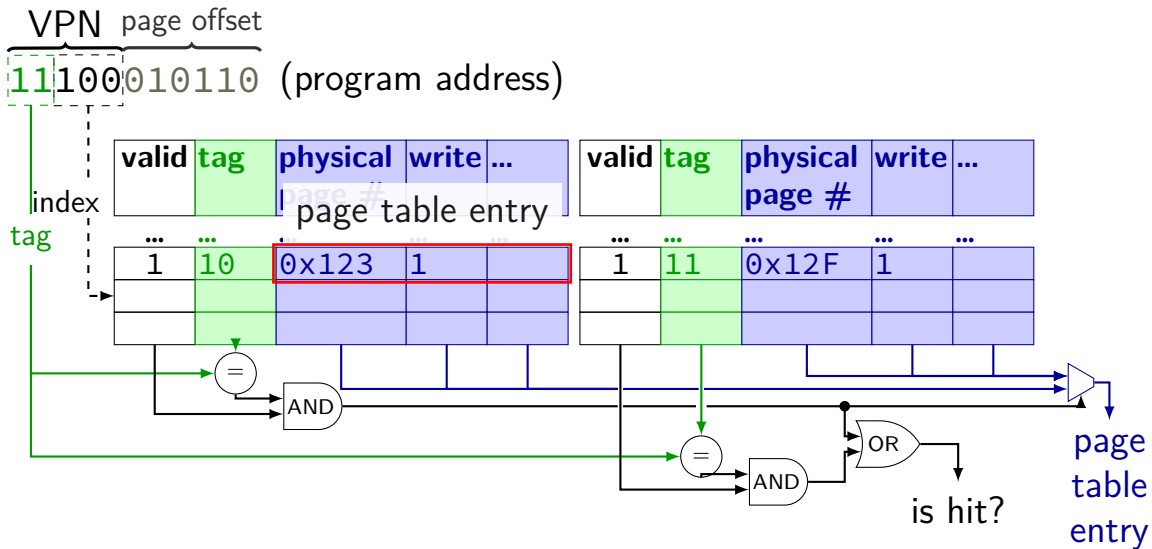
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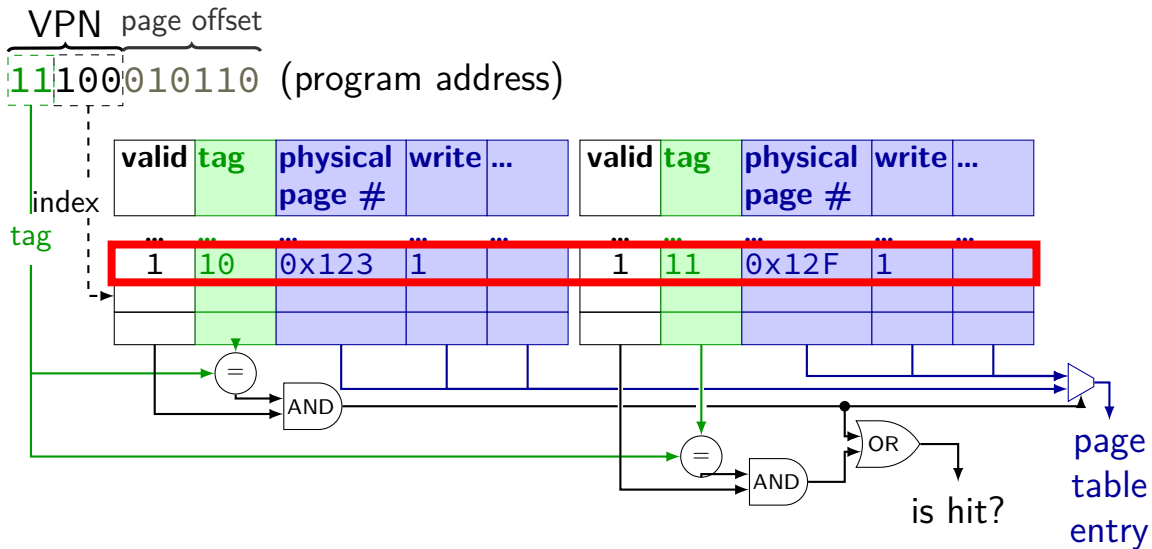
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# address splitting for TLBs (1)

my desktop:

4KB ( $2^{12}$  byte) pages; 48-bit virtual address

64-entry, 4-way L1 data TLB

TLB index bits?

TLB tag bits?



## address splitting for TLBs (2)

my desktop:

4KB ( $2^{12}$  byte) pages; 48-bit virtual address

1536-entry ( $3 \cdot 2^9$ ), 12-way L2 TLB

TLB index bits?

TLB tag bits?

## exercise: TLB access pattern (setup)

4-entry, 2-way TLB, LRU replacement policy, initially empty

4096 byte pages

how many index bits?

TLB index of virtual address 0x12345?

## exercise: TLB access pattern

4-entry, 2-way TLB, LRU replacement policy, initially empty

4096 byte pages

type	virtual	physical
read	0x440030	0x554030
write	0x440034	0x554034
read	0x7FFFE008	0x556008
read	0x7FFFE000	0x556000
read	0x7FFFDFF8	0x5F8FF8
read	0x664080	0x5F9080
read	0x440038	0x554038
write	0x7FFFDFF0	0x5F8FF0

which are TLB hits? which are TLB misses? final contents of TLB?

# changing page tables

what happens to TLB when page table base pointer is changed?

e.g. context switch

most entries in TLB refer to things from **wrong process**

oops — read from the wrong process's stack?

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option 1: **invalidate** all TLB entries

side effect on “change page table base register” instruction

# changing page tables

what happens to TLB when page table base pointer is changed?

e.g. context switch

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oops — read from the wrong process's stack?

option 1: **invalidate** all TLB entries

side effect on “change page table base register” instruction

option 2: TLB entries contain process ID

set by OS (special register)

checked by TLB in addition to TLB tag, valid bit

# editing page tables

what happens to TLB when OS changes a page table entry?

most common choice: has to be handled **in software**

# editing page tables

what happens to TLB when OS changes a page table entry?

most common choice: has to be handled **in software**

invalid to valid — nothing needed

- TLB doesn't contain invalid entries

- MMU will check memory again

valid to invalid — **OS needs to tell processor** to invalidate it

- special instruction (x86: `invlpg`)

valid to other valid — **OS needs to tell processor** to invalidate it

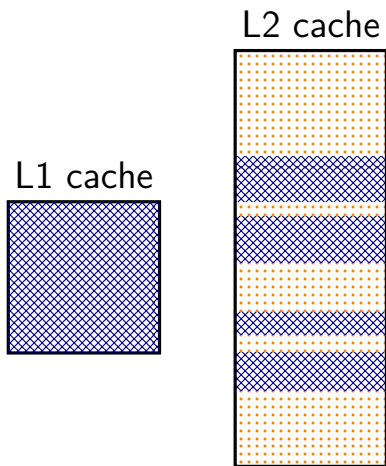


**backup slides**

# inclusive versus exclusive

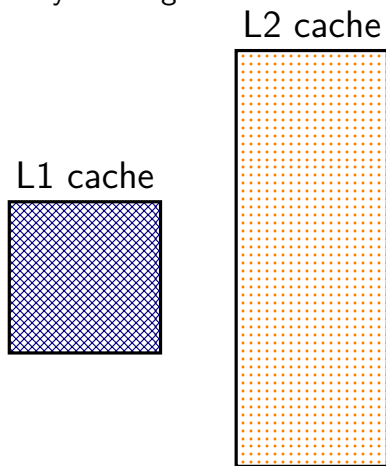
## L2 inclusive of L1

everything in L1 cache duplicated in L2  
adding to L1 also adds to L2



## L2 exclusive of L1

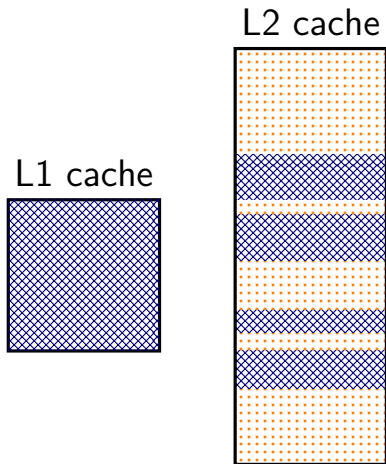
L2 contains different data than L1  
adding to L1 must remove from L2  
probably evicting from L1 adds to L2



# inclusive versus exclusive

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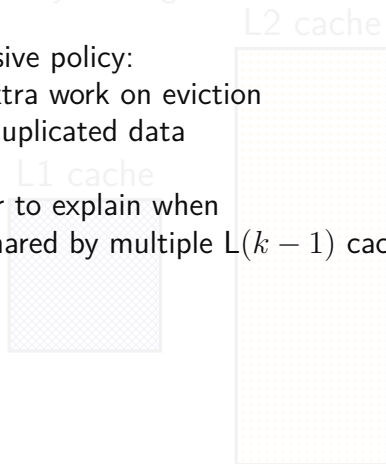


## L2 exclusive of L1

L2 contains different data than L1  
adding to L1 must remove from L2  
probably evicting from L1 adds to L2

inclusive policy:  
no extra work on eviction  
but duplicated data

easier to explain when  
 $L_k$  shared by multiple  $L(k-1)$  caches?



# inclusive versus exclusive

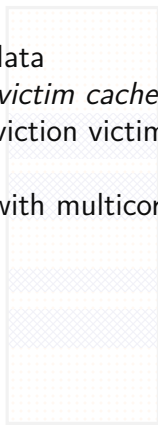
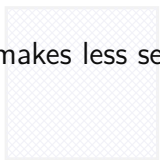
## L2 inclusive of L1

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adding to L1 also adds to L2

### L2 cache

exclusive policy:  
avoid duplicated data  
sometimes called *victim cache*  
(contains cache eviction victims)

makes less sense with multicore

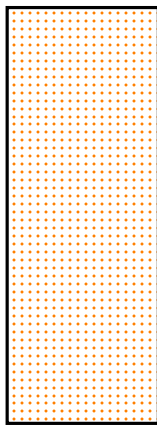
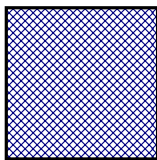


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adding to L1 must remove from L2  
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### L2 cache

### L1 cache



# Tag-Index-Offset formulas (direct-mapped)

(formulas derivable from prior slides)

$S = 2^s$                       number of sets

$s$                               (set) index bits

$B = 2^b$                       block size

$b$                               (block) offset bits

$m$                               memory addresses bits

$t = m - (s + b)$       tag bits

$C = B \times S$               cache size (if direct-mapped)

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