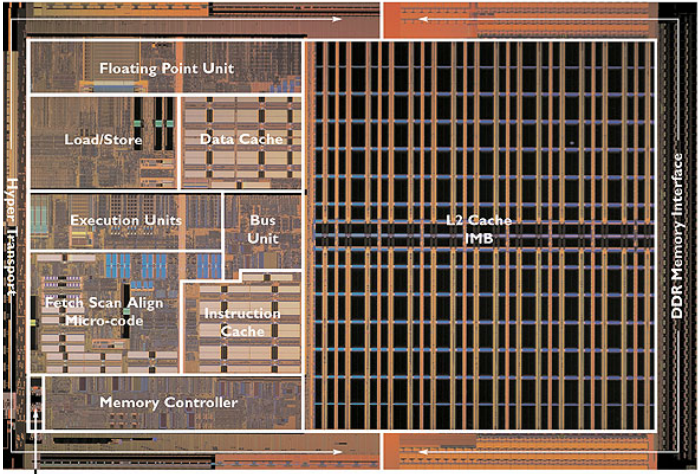
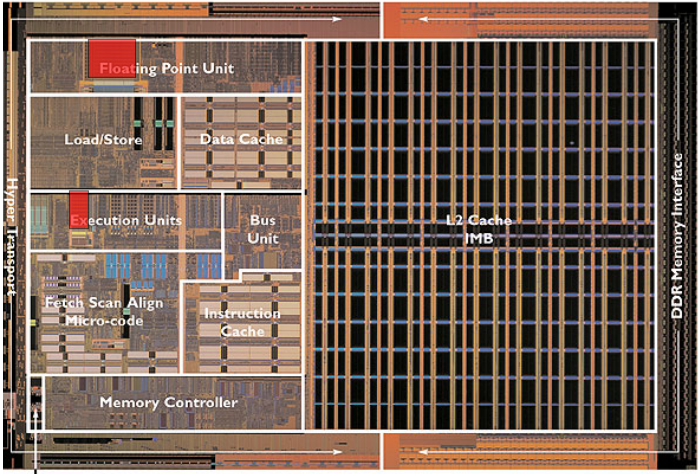
2004 CPU



AMD

ce: approx 2004 AMD press image of Opteron die;
prox register location via chip-architect.org (Hans de Vries)

2004 CPU

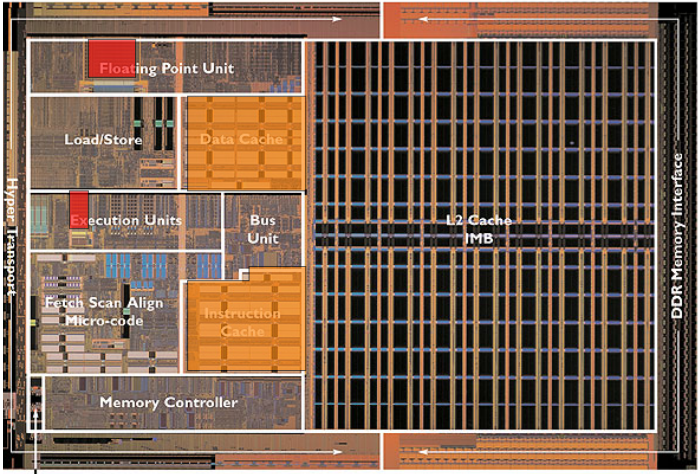


Registers

AMD

Source: approx 2004 AMD press image of Opteron die;
approx register location via chip-architect.org (Hans de Vries)

2004 CPU



AMD

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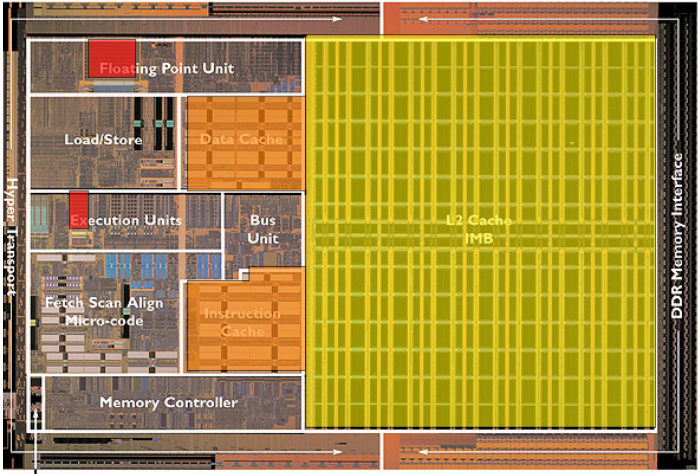
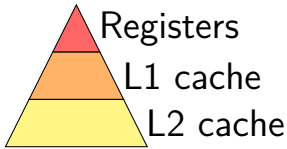
2004 CPU





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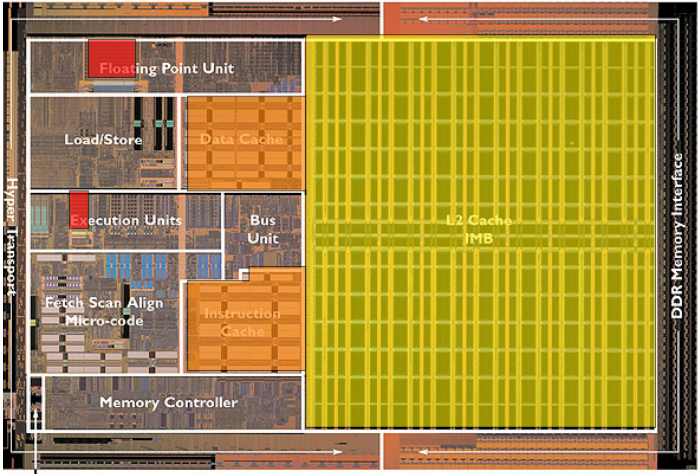
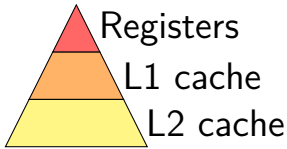
2004 CPU





AMD

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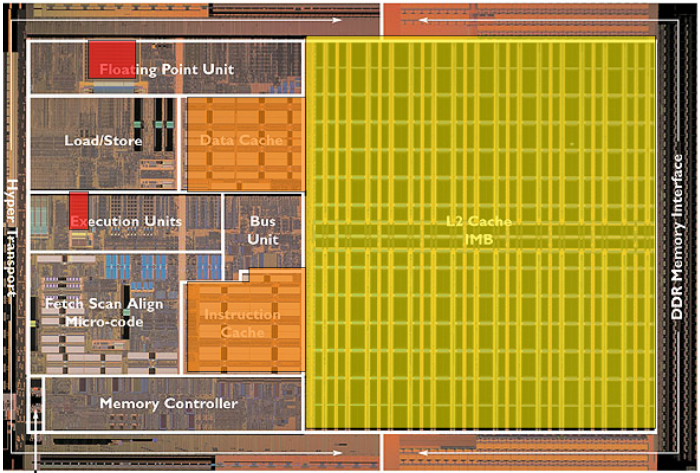
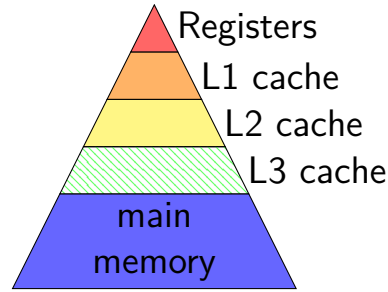
2004 CPU





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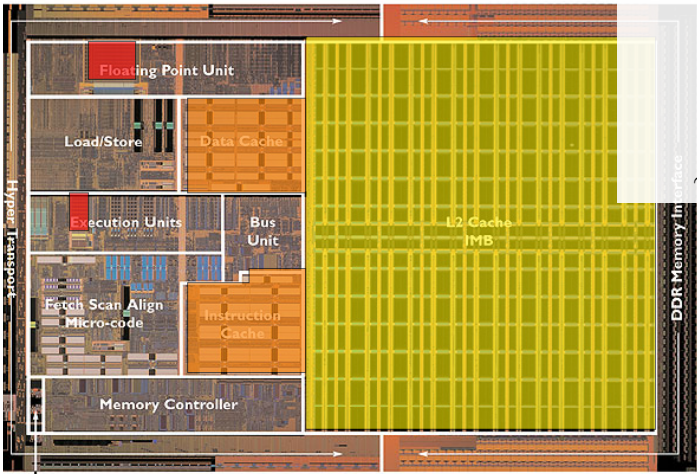
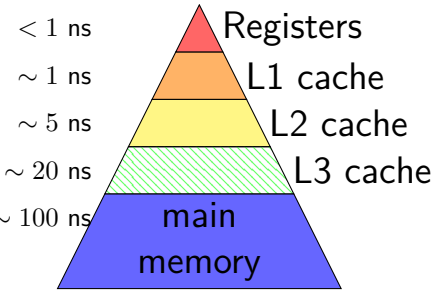
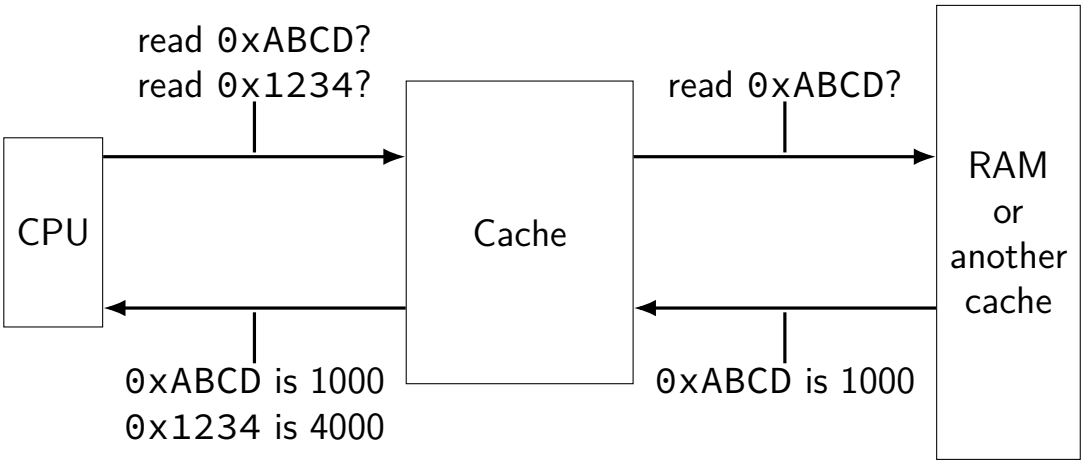
2004 CPU





ce: approx 2004 AMD press image of Opteron die;
prox register location via chip-architect.org (Hans de Vries)

the place of cache (1)



memory hierarchy goals

performance of the fastest (smallest) memory

- hide 100x latency difference? 99+% hit (= value found in cache) rate

capacity of the largest (slowest) memory

memory hierarchy assumptions

temporal locality

"if a value is accessed now, it will be accessed again soon"

caches should keep recently accessed values

spatial locality

"if a value is accessed now, adjacent values will be accessed soon"

caches should store adjacent values at the same time

natural properties of programs — think about loops

locality examples

```
double computeMean(int length, double *values) {
    double total = 0.0;
    for (int i = 0; i < length; ++i) {
        total += values[i];
    }
    return total / length;
}
```

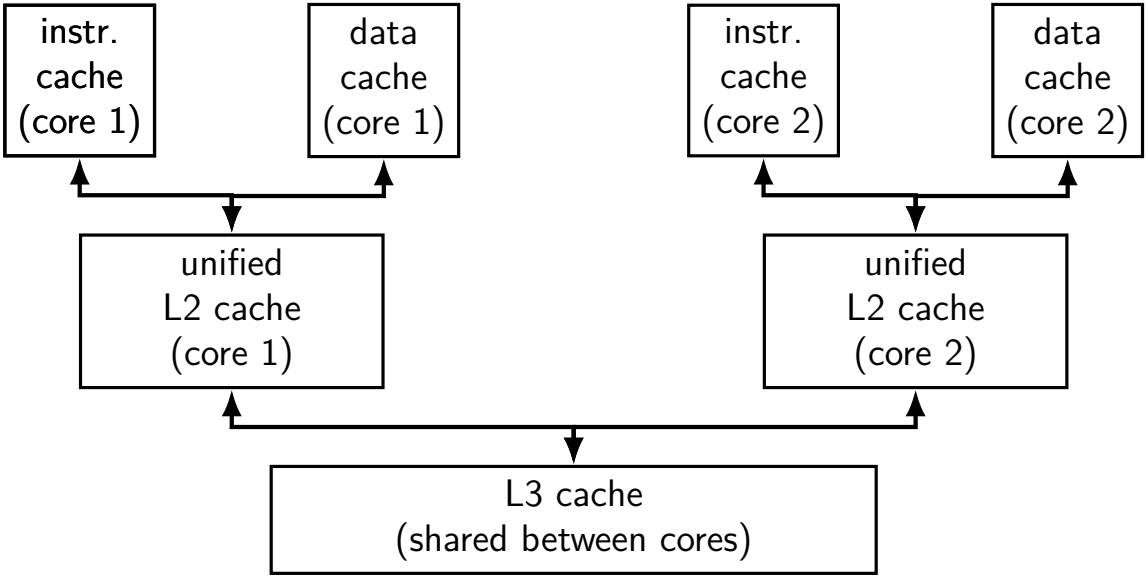
temporal locality: machine code of the loop

spatial locality: machine code of most consecutive instructions

temporal locality: `total`, `i`, `length` accessed repeatedly

spatial locality: `values[i+1]` accessed after `values[i]`

split caches; multiple cores (one design)



hierarchy and instruction/data caches

typically separate data and instruction caches for L1

(almost) never going to read instructions as data or vice-versa

avoids instructions evicting data and vice-versa

can optimize instruction cache for different access pattern

easier to build fast caches: that handles less accesses at a time

one-block cache

Cache

value
00 00

Memory

addresses	bytes
00000–00001	00 11
00010–00011	22 33
00100–00101	55 55
00110–00111	66 77
01000–01001	88 99
01010–01011	AA BB
01100–01101	CC DD
01110–01111	EE FF
10000–10001	F0 F1
…	…

one-block cache

decision: divide memory into two-byte blocks
put exactly one of these blocks in the cache

Cache

value
00 00

Memory

addresses	bytes
00000–00001	00 11
00010–00011	22 33
00100–00101	55 55
00110–00111	66 77
01000–01001	88 99
01010–01011	AA BB
01100–01101	CC DD
01110–01111	EE FF
10000–10001	F0 F1
…	…

one-block cache

read byte at 01011?

Cache

value
00 00

Memory

addresses	bytes
00000–00001	00 11
00010–00011	22 33
00100–00101	55 55
00110–00111	66 77
01000–01001	88 99
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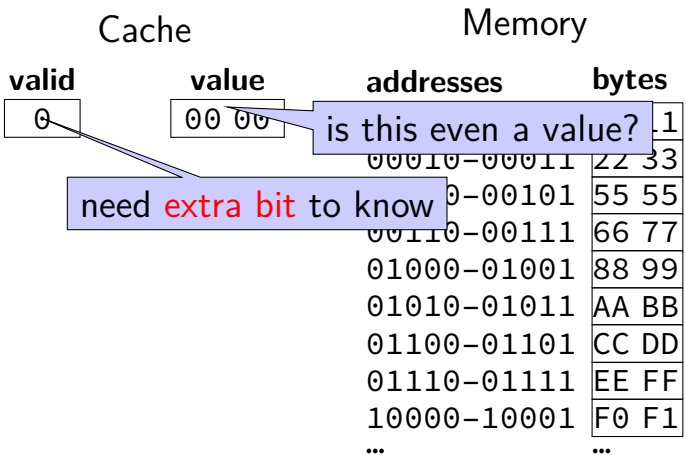
…	…

one-block cache

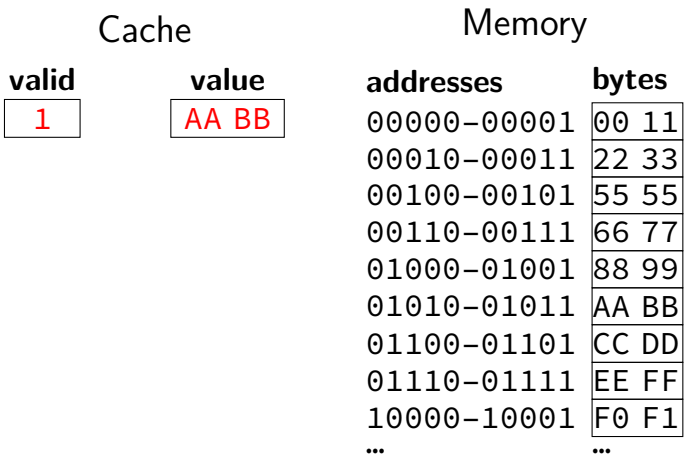
read byte at 01011?



one-block cache

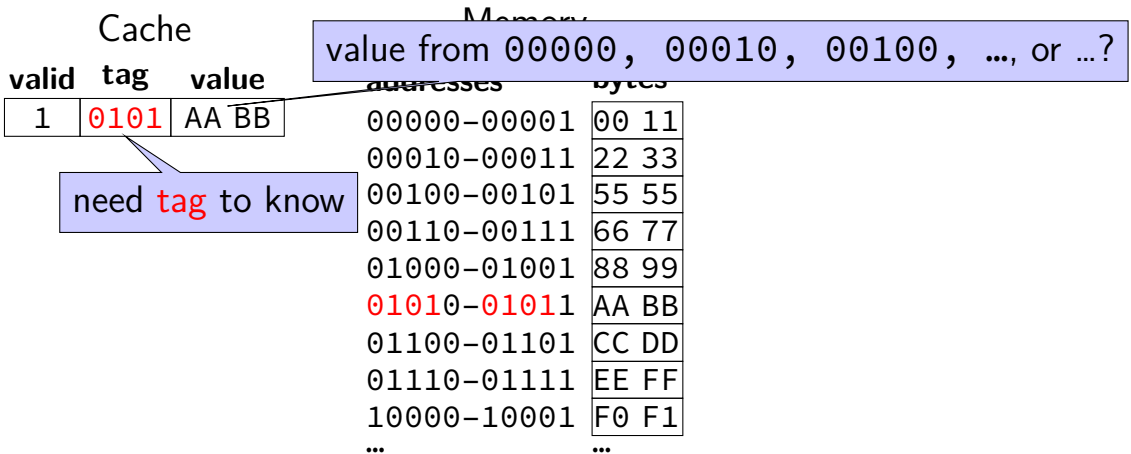
read byte at 01011?

invalid, fetch



one-block cache

read byte at 01011?



one-block cache

read byte at 01011?

Cache

valid	tag	value
1	0101	AA BB

Memory

addresses	bytes
00000–00001	00 11
00010–00011	22 33
00100–00101	55 55
00110–00111	66 77
01000–01001	88 99
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…	…

one-block cache

read byte at 01011?

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…	…

one-block cache

read byte at 01011?

Cache

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00000–00001	00 11
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01010–01011	AA BB
01100–01101	CC DD
01110–01111	EE FF
10000–10001	F0 F1
…	…

building a (direct-mapped) cache

Cache

value
00 00
00 00
00 00
00 00

cache block: 2 bytes

Memory

addresses	bytes
00000–00001	00 11
00010–00011	22 33
00100–00101	55 55
00110–00111	66 77
01000–01001	88 99
01010–01011	AA BB
01100–01101	CC DD
01110–01111	EE FF
10000–10001	F0 F1
…	…

building a (direct-mapped) cache

read byte at 01011?

Cache

value
00 00
00 00
00 00
00 00

cache block: 2 bytes

Memory

addresses	bytes
00000–00001	00 11
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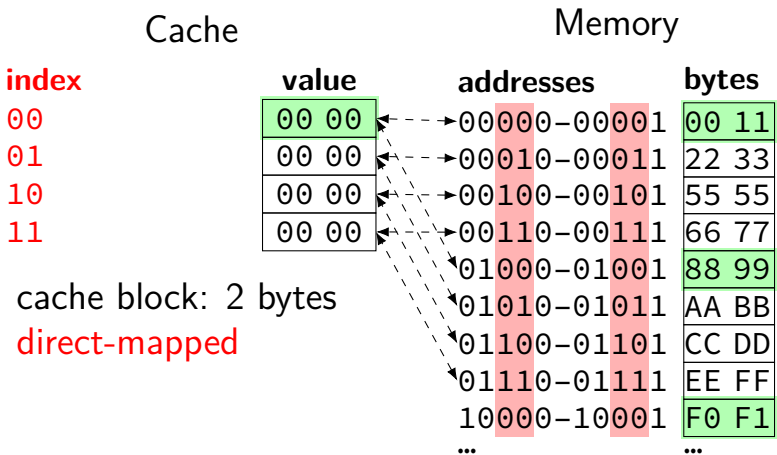
01000–01001	88 99
01010–01011	AA BB
01100–01101	CC DD
01110–01111	EE FF
10000–10001	F0 F1
…	…

building a (direct-mapped) cache

read byte at 01011?

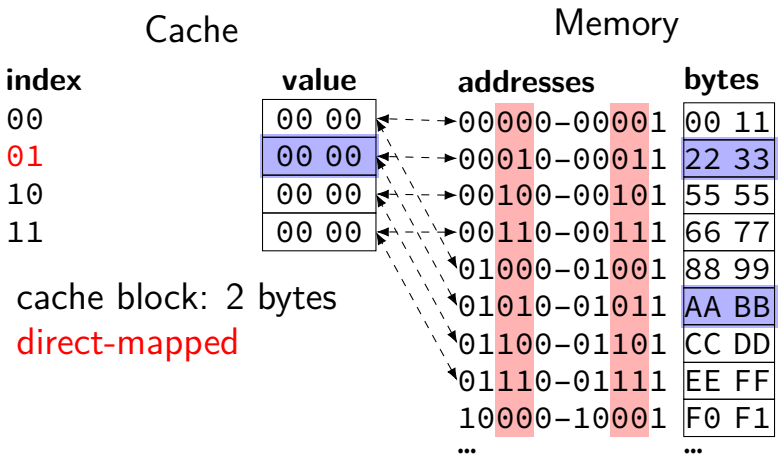
exactly one place for each address
spread out what can go in a block



building a (direct-mapped) cache

read byte at 01011?

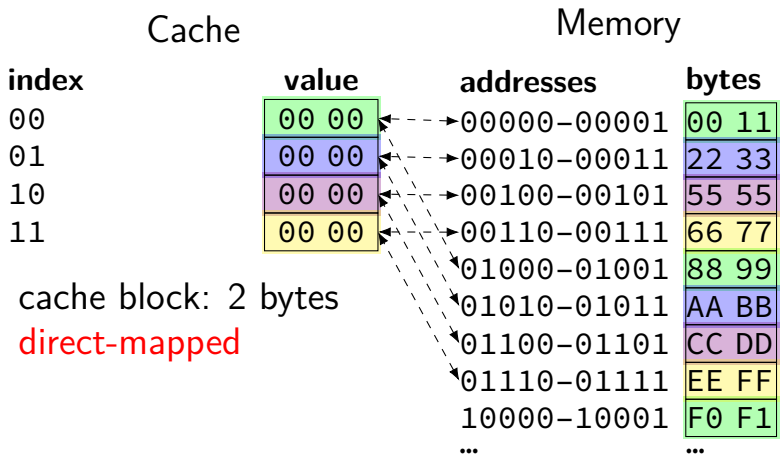
exactly one place for each address
spread out what can go in a block



building a (direct-mapped) cache

read byte at 01011?

exactly one place for each address
spread out what can go in a block

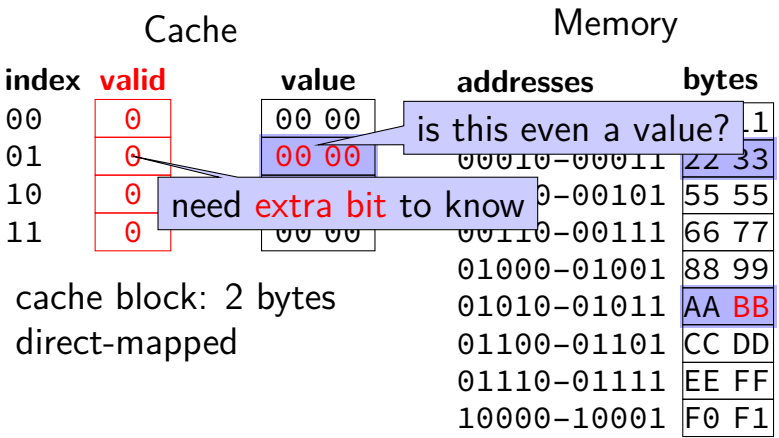


cache block: 2 bytes

direct-mapped

building a (direct-mapped) cache

read byte at 01011?



building a (direct-mapped) cache

read byte at 01011?

invalid, fetch

Cache

index	valid	value
00	0	00 00
01	1	AA BB
10	0	00 00
11	0	00 00

cache block: 2 bytes

direct-mapped

Memory

addresses	bytes
00000–00001	00 11
00010–00011	22 33
00100–00101	55 55
00110–00111	66 77
01000–01001	88 99
01010–01011	AA BB
01100–01101	CC DD
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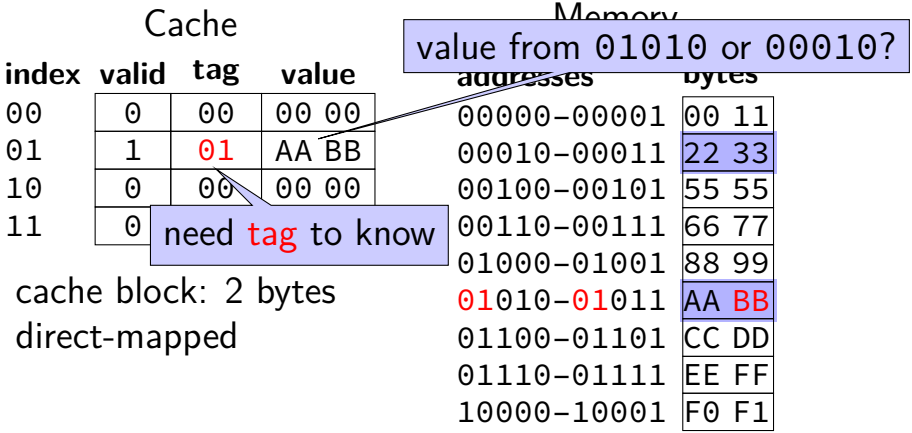
10000–10001	F0 F1
…	…

building a (direct-mapped) cache

read byte at 01011?

invalid, fetch



building a (direct-mapped) cache

read byte at 01011?

invalid, fetch

Cache

index	valid	tag	value
00	0	00	00 00
01	1	01	AA BB
10	0	00	00 00
11	0	00	00 00

cache block: 2 bytes

direct-mapped

Memory

addresses	bytes
00000–00001	00 11
00010–00011	22 33
00100–00101	55 55
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01000–01001	88 99
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01100–01101	CC DD
01110–01111	EE FF
10000–10001	F0 F1
…	…

terminology

row = set

preview: change how much is in a row

Tag-Index-Offset (TIO)

address `001111` (stores value `0xFF`)

cache	tag	index	offset
2 byte blocks, 4 sets			
2 byte blocks, 8 sets			
4 byte blocks, 2 sets			

2 byte blocks, 4 sets

index	valid	tag	value
00	1	000	00 11
01	1	001	AA BB
10	0	--	-- --
11	1	001	EE FF

4 byte blocks, 2 sets

index	valid	tag	value
0	1	000	00 11 22 33
1	1	001	CC DD EE FF

2 byte blocks, 8 sets

index	valid	tag	value
000	1	00	00 11
001	1	01	F1 F2
010	0	--	-- --
011	0	--	-- --
100	0	--	-- --
101	1	00	AA BB
110	0	--	-- --
111	1	00	EE FF

Tag-Index-Offset (TIO)

address `001111` (stores value `0xFF`)

cache	tag	index	offset
2 byte blocks, 4 sets			1
2 byte blocks, 8 sets			1
4 byte blocks, 2 sets			

2 byte blocks, 4 sets

index	valid	tag	value
00	1	000	00 11
01	1	001	AA BB
10	0	--	-- --
11	1	001	EE FF

4 byte blocks, 2 sets

index	valid	tag	value
0	1	000	00 11 22 33
1	1	001	CC DD EE FF

2 byte blocks, 8 sets

index	valid	tag	value
000	1	000	00 11
001	1	001	F1 F2
010	0	--	-- --
011	0	--	-- --
100	0	--	-- --
101	1	00	AA BB
110	0	--	-- --
111	1	00	EE FF

$2 = 2^1$ bytes in block
1 bit to say which byte

Tag-Index-Offset (TIO)

address `001111` (stores value `0xFF`)

cache	tag	index	offset
2 byte blocks, 4 sets			1
2 byte blocks, 8 sets			1
4 byte blocks, 2 sets			11

2 byte blocks, 4 sets

index	valid	tag	value
00	1	000	00 11
01	1	001	AA BB
10	0		
11	1		

2 byte blocks, 8 sets

index	valid	tag	value
000	1	00	00 11
001	1	01	F1 F2
0	--	-- --	
0	--	-- --	
0	--	-- --	
1	00	AA BB	
0	--	-- --	
1	00	EE FF	

$4 = 2^2$ bytes in block
2 bits to say which byte

4 byte blocks, 2 sets

index	valid	tag	value
0	1	000	00 11 22 33
1	1	001	CC DD EE FF

Tag-Index-Offset (TIO)

address `001111` (stores value `0xFF`)

cache	tag	index	offset
2 byte blocks, 4 sets		11	1
2 byte blocks, 8 sets			1
4 byte blocks, 2 sets		1	11

2 byte blocks, 4 sets

index	valid	tag	value
00	1	000	00 11
01	1	001	AA BB
10	0	--	-- --
11	1	001	EE FF

4 byte blocks, 2 sets

index	valid	tag	value
0	1	000	00 11 22 33
1	1	001	CC DD EE FF

2 byte blocks, 8 sets

index	valid	tag	value
000	1	00	00 11
001	1	00	F1 F2
010	0	--	-- --
011	0	--	-- --
100	0	--	-- --
101	1	00	AA BB
110	0	--	-- --
111	1	00	EE FF

$2^2 = 4$ sets
2 bits to index set

Tag-Index-Offset (TIO)

address `001111` (stores value `0xFF`)

cache	tag	index	offset
2 byte blocks, 4 sets		11	1
2 byte blocks, 8 sets		111	1
4 byte blocks, 2 sets		1	11

2 byte blocks, 4 sets

index	valid	tag	value
00	1	000	00 11
01	1	001	AA BB
10	0	--	-- --
11	1		

4 byte blocks, 2 sets

index	valid	tag	value
0	1	000	00 11 22 33
1	1	001	CC DD EE FF

$2^3 = 8$ sets

3 bits to index set

2 byte blocks, 8 sets

index	valid	tag	value
000	1	00	00 11
001	1	01	F1 F2
010	0	--	-- --
011	0	--	-- --
100	0	--	-- --
101	1	00	AA BB
110	0	--	-- --
111	1	00	EE FF

Tag-Index-Offset (TIO)

address `001111` (stores value `0xFF`)

cache	tag	index	offset
2 byte blocks, 4 sets		11	1
2 byte blocks, 8 sets		111	1
4 byte blocks, 2 sets		1	11

2 byte blocks, 4 sets

index	valid	tag	value
00	1	000	00 11
01	1	001	AA BB
10	0	--	-- --
11	1	001	EE FF

4 byte blocks, 2 sets

index	valid	tag	value
0	1	000	00 11 22 33
1	1	001	CC DD EE FF

2 byte blocks, 8 sets

index	valid	tag	value
000	1	00	00 11
001	1	01	F1 F2
010	0	--	-- --
01			--
10			--
10			BB
110	0	--	-- --
111	1	00	EE FF

$2^1 = 2$ sets

1 bit to index set

Tag-Index-Offset (TIO)

address `001111` (stores value `0xFF`)

cache	tag	index	offset
2 byte blocks, 4 sets	001	11	1
2 byte blocks, 8 sets	00	111	1
4 byte blocks, 2 sets	001	1	11

tag — whatever is left over

	valid	tag	value
00	1	000	00 11
01	1	001	AA BB
10	0	--	-- --
11	1	001	EE FF

4 byte blocks, 2 sets

index	valid	tag	value
0	1	000	00 11 22 33
1	1	001	CC DD EE FF

2 byte blocks, 8 sets

index	valid	tag	value
000	1	00	00 11
001	1	01	F1 F2
010	0	--	-- --
011	0	--	-- --
100	0	--	-- --
101	1	00	AA BB
110	0	--	-- --
111	1	00	EE FF

cache size

cache size = amount of *data* in cache

not included metadata (tags, valid bits, etc.)

Tag-Index-Offset formulas (direct-mapped)

(formulas derivable from prior slides)

$S = 2^s$	number of sets
s	(set) index bits
$B = 2^b$	block size
b	(block) offset bits
m	memory addreses bits
$t = m - (s + b)$	tag bits
$C = B \times S$	cache size (if direct-mapped)

Tag-Index-Offset formulas (direct-mapped)

(formulas derivable from prior slides)

$S = 2^s$	number of sets
s	(set) index bits
$B = 2^b$	block size
b	(block) offset bits
m	memory addreses bits
$t = m - (s + b)$	tag bits
$C = B \times S$	cache size (if direct-mapped)

TIO: exercise

64-byte blocks, 128 set cache

stores $64 \times 128 = 8192$ bytes (of data)

if addresses 32-bits, then how many tag/index/offset bits?

which bytes are stored in the same block as byte from `0x1037`?

A. byte from `0x1011`
B. byte from `0x1021`
C. byte from `0x1035`
D. byte from `0x1041`

example access pattern (1)

address (hex)	result
00000000 (00)	
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

2 byte blocks, 4 sets

index	valid	tag	value
00	0		
01	0		
10	0		
11	0		

example access pattern (1)

address (hex)	result
00000000 (00)	
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

2 byte blocks, 4 sets

index	valid	tag	value
00	0		
01	0		
10	0		
11	0		

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	0		
01	0		
10	0		
11	0		

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	miss
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	1	00000	mem[0x00] mem[0x01]
01	0		
10	0		
11	0		

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	1	00000	mem[0x00] mem[0x01]
01	0		
10	0		
11	0		

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01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

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$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	1	00000	mem[0x00] mem[0x01]
01	1	01100	mem[0x62] mem[0x63]
10	0		
11	0		

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	1	01100	mem[0x60] mem[0x61]
01	1	01100	mem[0x62] mem[0x63]
10	0		
11	0		

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	
01100100 (64)	

tag index offset

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	1	01100	mem[0x60] mem[0x61]
01	1	01100	mem[0x62] mem[0x63]
10	0		
11	0		

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	miss
01100100 (64)	

tag index offset

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	1	00000	mem[0x00] mem[0x01]
01	1	01100	mem[0x62] mem[0x63]
10	0		
11	0		

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	miss
01100100 (64)	miss

tag index offset

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	1	00000	mem[0x00] mem[0x01]
01	1	01100	mem[0x62] mem[0x63]
10	1	01100	mem[0x64] mem[0x65]
11	0		

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	miss
01100100 (64)	miss

tag index offset

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

2 byte blocks, 4 sets

index	valid	tag	value
00	1	00000	mem[0x00] mem[0x01]
01	1	01100	mem[0x62] mem[0x63]
10	1	01100	mem[0x64] mem[0x65]
11	0		

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

example access pattern (1)

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	miss
01100100 (64)	miss

tag index offset

2 byte blocks, 4 sets

index	valid	tag	value
00	1	00000	mem[0x00] mem[0x01]
01	1	01100	mem[0x62] mem[0x63]
10	1	01100	mem[0x64] mem[0x65]
11	0		

miss caused by conflict

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

$m = 8$ bit addresses
$t = m - (s + b) = 5$ tag bits

exercise

address (hex)	result
00000000 (00)	
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

4 byte blocks, 4 sets

index	valid	tag	value
00			
01			
10			
11			

exercise

address (hex)	result
00000000 (00)	
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

4 byte blocks, 4 sets

index	valid	tag	value
00			
01			
10			
11			

how is the 8-bit address 61 (01100001) split up into tag/index/offset?

b block offset bits;
$B = 2^b$ byte block size;
s set index bits; $S = 2^s$ sets ;
$t = m - (s + b)$ tag bits (lefto

exercise

address (hex)	result
00000000 (00)	
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

4 byte blocks, 4 sets

index	valid	tag	value
00			
01			
10			
11			

$B = 4 = 2^b$ byte block size
$b = 2$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

$m = 8$ bit addresses
$t = m - (s + b) = 4$ tag bits

exercise

address (hex)	result
00000000 (00)	
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

$B = 4 = 2^b$ byte block size
$b = 2$ (block) offset bits
$S = 4 = 2^s$ sets
$s = 2$ (set) index bits

4 byte blocks, 4 sets

index	valid	tag	value
00			
01			
10			
11			

$m = 8$ bit addresses
$t = m - (s + b) = 4$ tag bits

exercise

address (hex)	result
00000000 (00)	
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

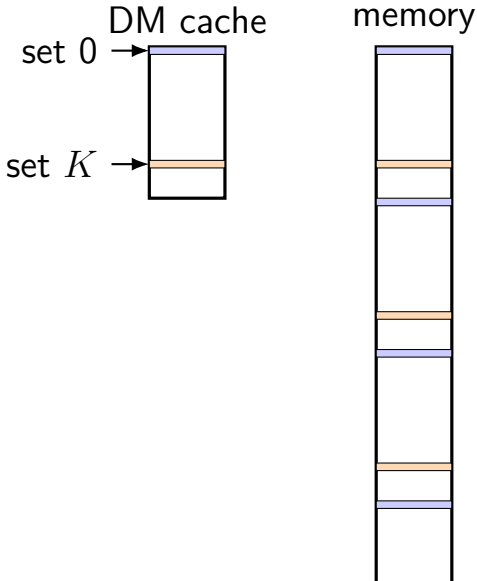
tag index offset

4 byte blocks, 4 sets

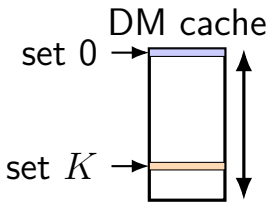
index	valid	tag	value
00			
01			
10			
11			

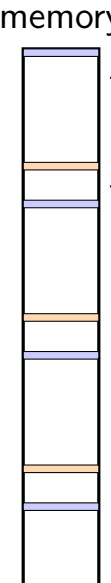
exercise: which accesses are hits?

mapping of sets to memory (direct-mapped)



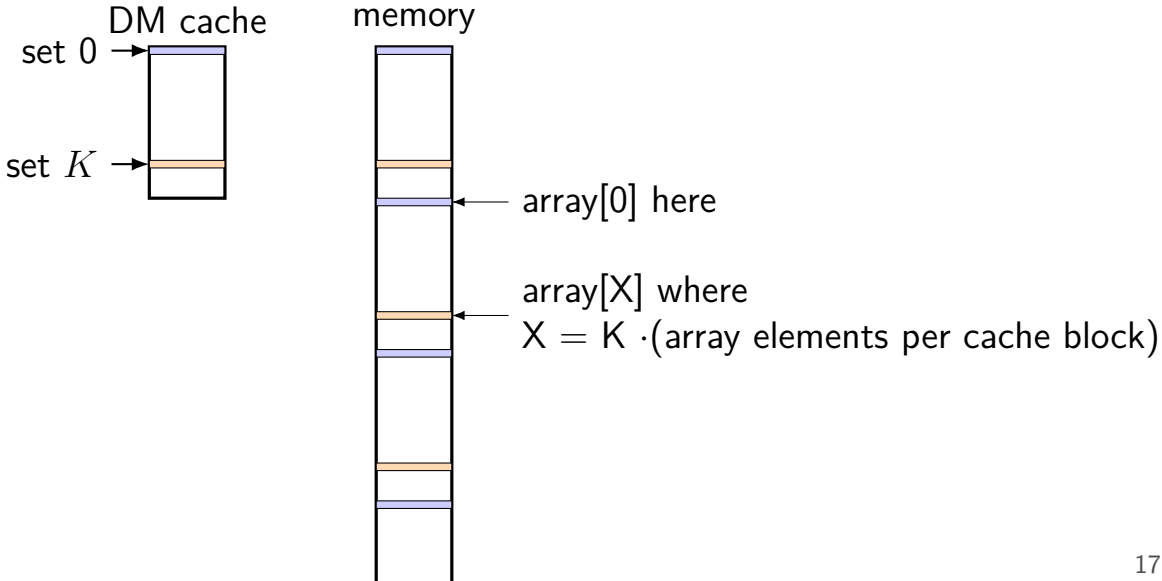
mapping of sets to memory (direct-mapped)



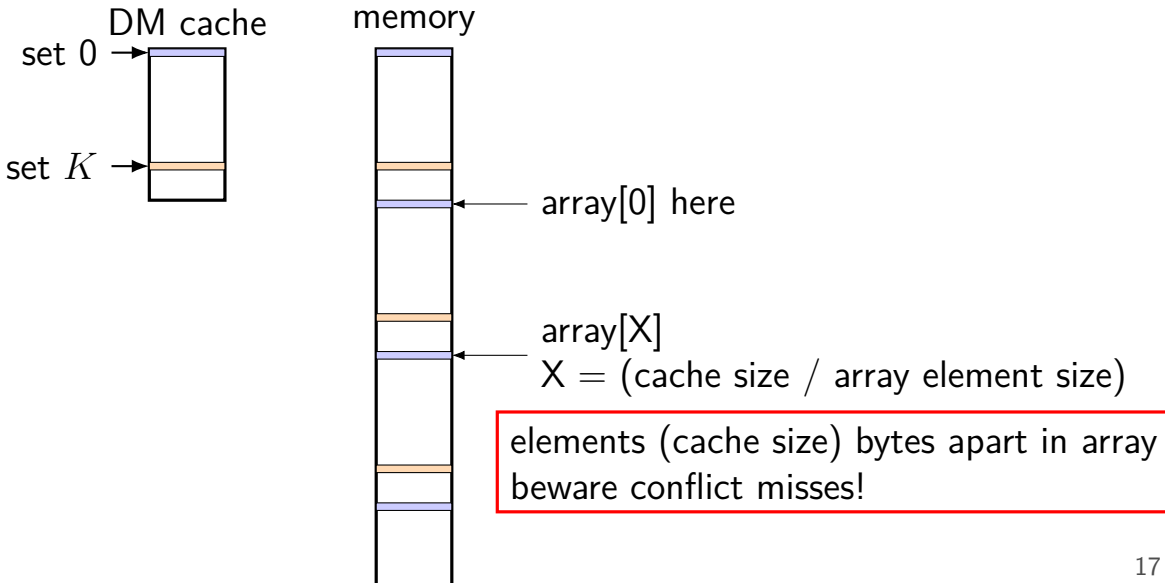


values which would be stored in same set (cache size) bytes apart

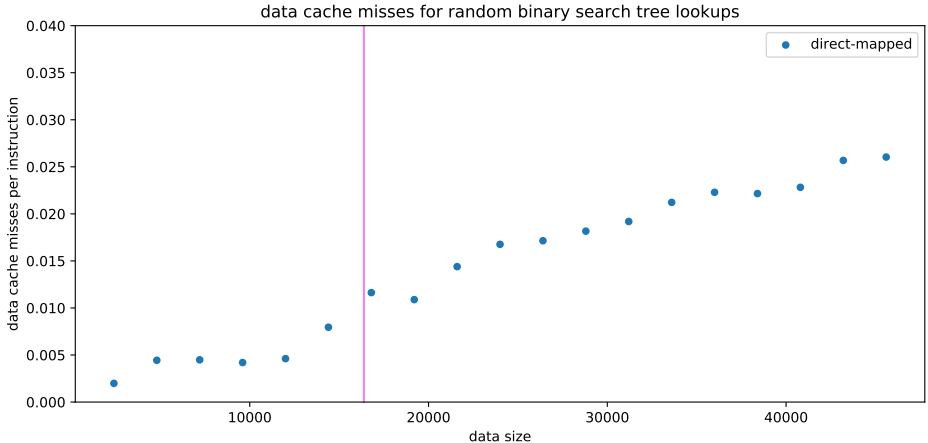
mapping of sets to memory (direct-mapped)



mapping of sets to memory (direct-mapped)

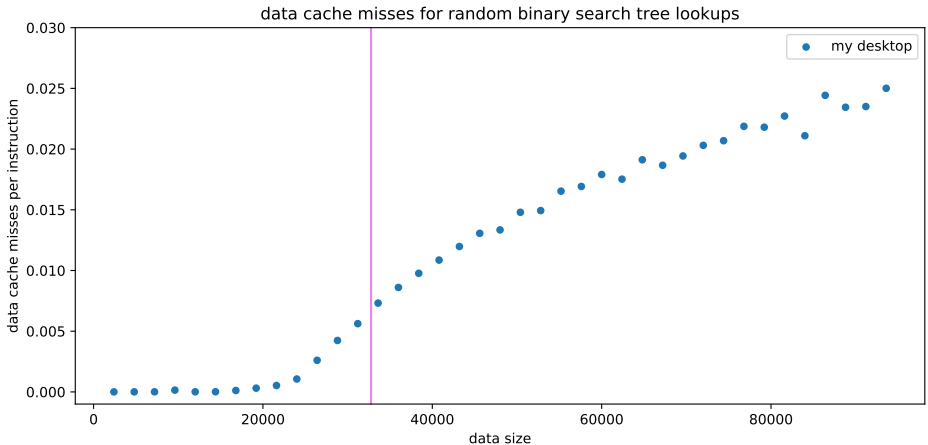


simulated misses: BST lookups



(simulated 16KB direct-mapped data cache; excluding BST setup)

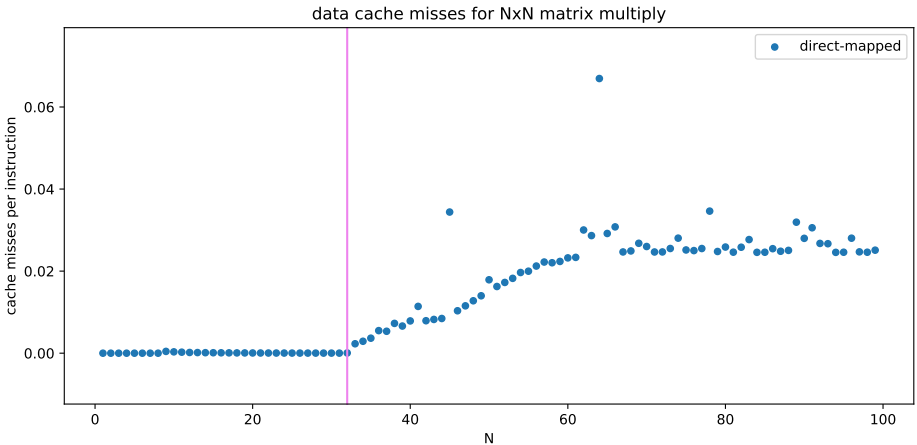
actual misses: BST lookups



(actual 32KB more complex data cache)

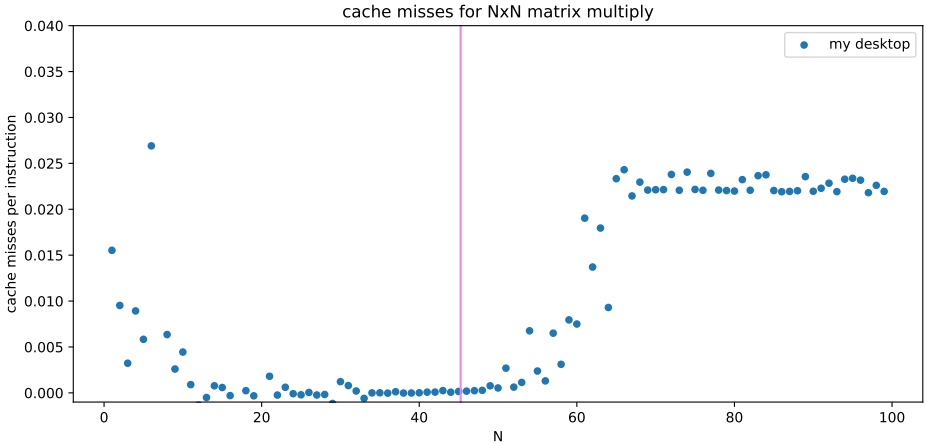
(only one set of measurements + other things on machine + excluding initial load)

simulated misses: matrix multiplies



(simulated 16KB direct-mapped data cache; excluding initial load)

actual misses: matrix multiplies



(actual 32KB more complex data cache; excluding matrix initial load)
(only one set of measurements + other things on machine)

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	0			0		
1	0			0		

multiple places to put values with same index
avoid misses from two active values using same set
("conflict misses")

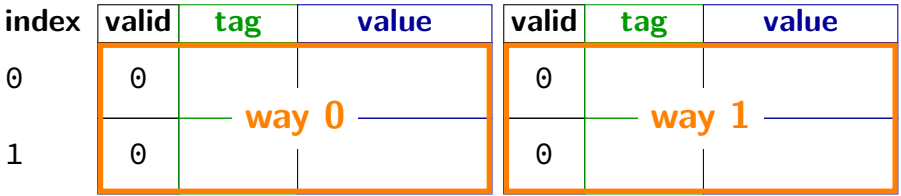
adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	0		set 0	0		
1	0		set 1	0		

adding associativity

2-way set associative, 2 byte blocks, 2 sets



adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	0			0		
1	0			0		

$m = 8$ bit addresses
$S = 2 = 2^s$ sets
$s = 1$ (set) index bits

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$t = m - (s + b) = 6$ tag bits

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	0		
1	0			0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	0		
1	0			0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	0		
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	
00000000 (00)	
01100100 (64)	

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	
01100100 (64)	

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	miss

needs to replace block in set 0!

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	miss

associative lookup possibilities

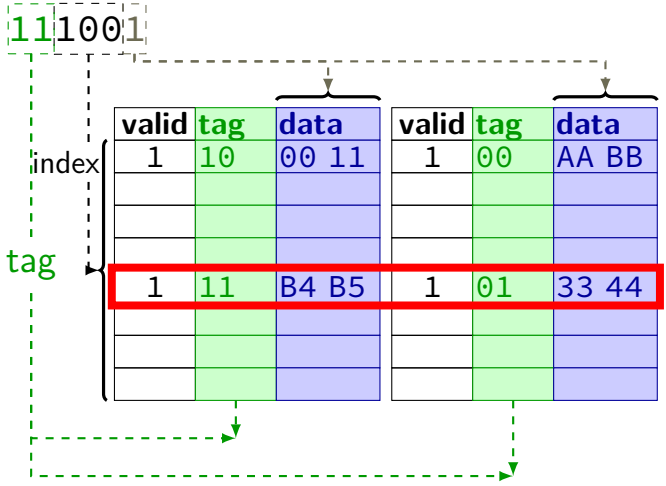
none of the blocks for the index are valid

none of the valid blocks for the index match the tag

- something else is stored there

one of the blocks for the index is valid and matches the tag

cache operation (associative)



replacement policies

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
000	
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	miss

how to decide where to insert 0x64?

replacement policies

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value	LRU
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]	1
1	1	011000	mem[0x62] mem[0x63]	0			1

address (hex)	result
00000000 (00)	mi
00000001 (01)	hit
01100011 (63)	mi
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	miss

track which block was read least recently
updated on every access

example replacement policies

least recently used

- take advantage of temporal locality
- at least $\lceil \log_2(E!) \rceil$ bits per set for E-way cache
  - (need to store order of all blocks)

approximations of least recently used

- implementing least recently used is expensive
- really just need "avoid recently used" — much faster/simpler
- good approximations: E to $2E$ bits

first-in, first-out

- counter per set — where to replace next

(pseudo-)random

- no extra information!
- actually works pretty well in practice

associativity terminology

direct-mapped — one block per set

E-way set associative — E blocks per set

E ways in the cache

fully associative — one set total (everything in one set)

Tag-Index-Offset formulas

m	memory addreses bits
E	number of blocks per set (“ways”)
$S = 2^s$	number of sets
s	(set) index bits
$B = 2^b$	block size
b	(block) offset bits
$t = m - (s + b)$	tag bits
$C = B \times S \times E$	cache size (excluding metadata)

cache accesses and C code (1)

```
int scaleFactor;

int scaleByFactor(int value) {
    return value * scaleFactor;
}
```

```
scaleByFactor:
    movl scaleFactor, %eax
    imull %edi, %eax
    ret
```

---

exericse: what data cache accesses does this function do?

cache accesses and C code (1)

```
int scaleFactor;

int scaleByFactor(int value) {
    return value * scaleFactor;
}
```

```
scaleByFactor:
    movl scaleFactor, %eax
    imull %edi, %eax
    ret
```

---

exericse: what data cache accesses does this function do?

- 4-byte read of scaleFactor
- 8-byte read of return address

possible scaleFactor use

```
for (int i = 0; i < size; ++i) {
    array[i] = scaleByFactor(array[i]);
}
```

misses and code (2)

```
scaleByFactor:
    movl scaleFactor, %eax
    imull %edi, %eax
    ret
```

suppose each time this is called in the loop:

return address located at address `0x7ffffffe43b8`

scaleFactor located at address `0x6bc3a0`

with direct-mapped 32KB cache w/64 B blocks, what is their:

	return address	scaleFactor
tag		
index		
offset		

misses and code (2)

```
scaleByFactor:
    movl scaleFactor, %eax
    imull %edi, %eax
    ret
```

suppose each time this is called in the loop:

return address located at address `0x7ffffffe43b8`

scaleFactor located at address `0x6bc3a0`

with direct-mapped 32KB cache w/64 B blocks, what is their:

	return address	scaleFactor
tag	0xffffffc	0xd7
index	0x10e	0x10e
offset	0x38	0x20

misses and code (2)

```
scaleByFactor:
    movl scaleFactor, %eax
    imull %edi, %eax
    ret
```

suppose each time this is called in the loop:

return address located at address `0x7ffffffe43b8`

scaleFactor located at address `0x6bc3a0`

with direct-mapped 32KB cache w/64 B blocks, what is their:

	return address	scaleFactor
tag	0xffffffc	0xd7
index	0x10e	0x10e
offset	0x38	0x20

conflict miss coincidences?

obviously I set that up to have the same index

- have to use exactly the right amount of stack space...

but one of the reasons we'll want something better than direct-mapped cache

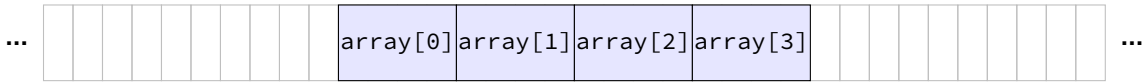
C and cache misses (warmup 1)

```
int array[4];
...
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
odd_sum += array[1];
even_sum += array[2];
odd_sum += array[3];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

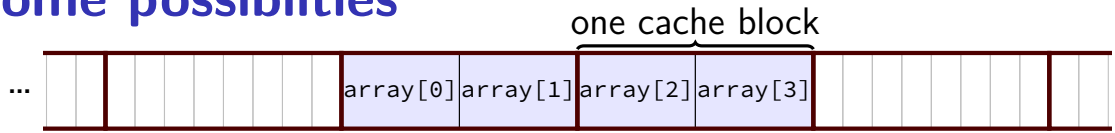
How many data cache misses on a 1-set direct-mapped cache with 8B blocks?

some possiblities



Q1: how do cache blocks correspond to array elements?
not enough information provided!

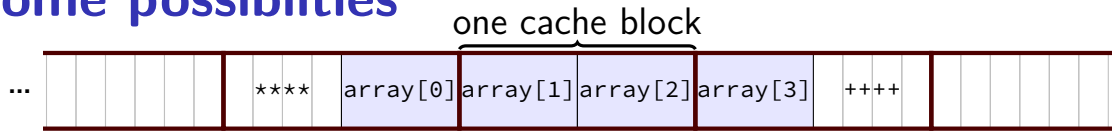
some possiblities



if array[0] starts at beginning of a cache block...
array split across two cache blocks

memory access	**cache contents afterwards**
—	`(empty)`
read `array[0]` (miss)	`{array[0], array[1]}`
read `array[1]` (hit)	`{array[0], array[1]}`
read `array[2]` (miss)	`{array[2], array[3]}`
read `array[3]` (hit)	`{array[2], array[3]}`

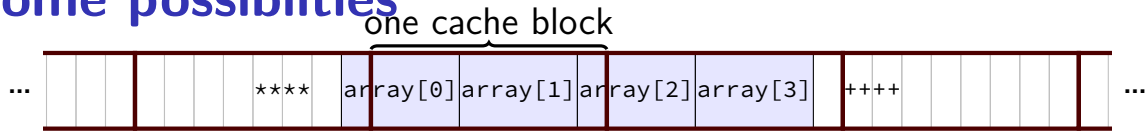
some possiblities



if array[0] starts right in the middle of a cache block
array split across three cache blocks

memory access	**cache contents afterwards**
—	(empty)
read `array[0]` (miss)	{****, `array[0]`}
read `array[1]` (miss)	{`array[1]`, `array[2]`}
read `array[2]` (hit)	{`array[1]`, `array[2]`}
read `array[3]` (miss)	{`array[3]`, ++++}

some possiblities



if array[0] starts at an odd place in a cache block,
need to read two cache blocks to get most array elements

memory access	cache contents afterwards
—	(empty)
read `array[0]` byte 0 (miss)	{ ****, array[0] byte 0 }
read `array[0]` byte 1-3 (miss)	{ array[0] byte 1-3, array[2], array[3] byte 0 }
read `array[1]` (hit)	{ array[0] byte 1-3, array[2], array[3] byte 0 }
read `array[2]` byte 0 (hit)	{ array[0] byte 1-3, array[2], array[3] byte 0 }
read `array[2]` byte 1-3 (miss)	{part of array[2], array[3], ++++}
read `array[3]` (hit)	{part of array[2], array[3], ++++}

aside: alignment

compilers and malloc/new implementations usually try align values

align = make address be multiple of something

most important reason: don't cross cache block boundaries

C and cache misses (warmup 2)

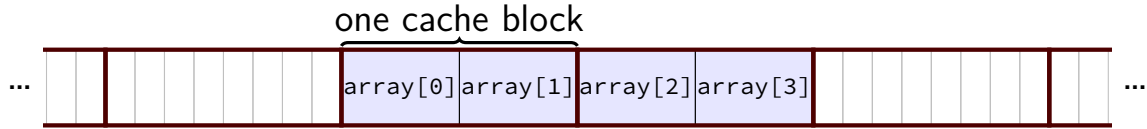
```
int array[4];
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
even_sum += array[2];
odd_sum += array[1];
odd_sum += array[3];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

Assume array[0] at beginning of cache block.

How many data cache misses on a 1-set direct-mapped cache with 8B blocks?

exercise solution



memory access	cache contents afterwards
—	(empty)
read array[0] (miss)	{array[0], array[1]}
read array[2] (miss)	{array[2], array[3]}
read array[1] (miss)	{array[0], array[1]}
read array[3] (miss)	{array[2], array[3]}

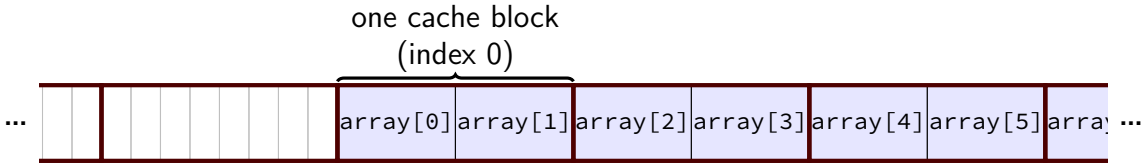
C and cache misses (warmup 3)

```
int array[8];
...
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
odd_sum += array[1];
even_sum += array[2];
odd_sum += array[3];
even_sum += array[4];
odd_sum += array[5];
even_sum += array[6];
odd_sum += array[7];
```

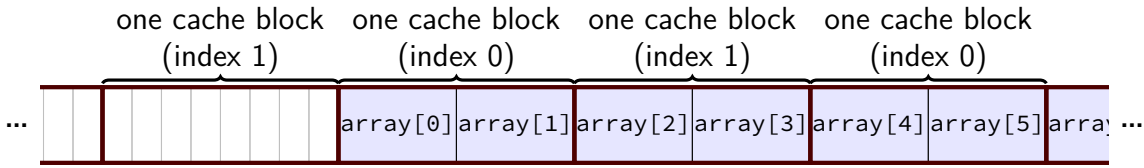
Assume everything but `array` is kept in registers (and the compiler does not do anything funny), and array[0] at beginning of cache block.

How many data cache misses on a **2**-set direct-mapped cache with 8B blocks?

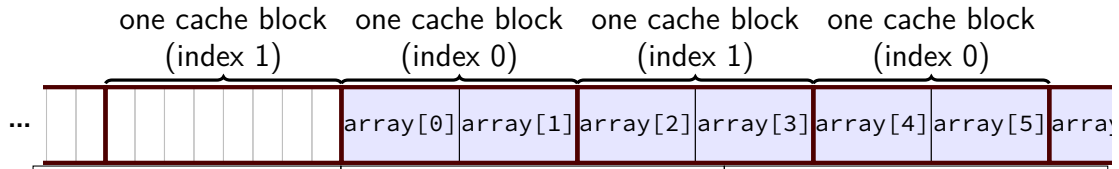
exercise solution



exercise solution

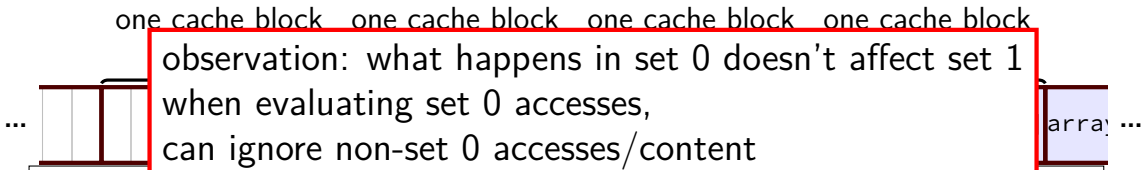


exercise solution



memory access	set 0 afterwards	set 1 afterwards
—	(empty)	(empty)
read array[0] (miss)	{array[0], array[1]}	(empty)
read array[1] (hit)	{array[0], array[1]}	(empty)
read array[2] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[3] (hit)	{array[0], array[1]}	{array[2], array[3]}
read array[4] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[5] (hit)	{array[4], array[5]}	{array[2], array[3]}
read array[6] (miss)	{array[4], array[5]}	{array[6], array[7]}
read array[7] (hit)	{array[4], array[5]}	{array[6], array[7]}

exercise solution



observation: what happens in set 0 doesn't affect set 1
when evaluating set 0 accesses,
can ignore non-set 0 accesses/content

memory access	set 0 afterwards	set 1 afterwards
—	(empty)	(empty)
read array[0] (miss)	{array[0], array[1]}	(empty)
read array[1] (hit)	{array[0], array[1]}	(empty)
read array[2] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[3] (hit)	{array[0], array[1]}	{array[2], array[3]}
read array[4] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[5] (hit)	{array[4], array[5]}	{array[2], array[3]}
read array[6] (miss)	{array[4], array[5]}	{array[6], array[7]}
read array[7] (hit)	{array[4], array[5]}	{array[6], array[7]}

exercise solution

one cache block | one cache block | one cache block | one cache block

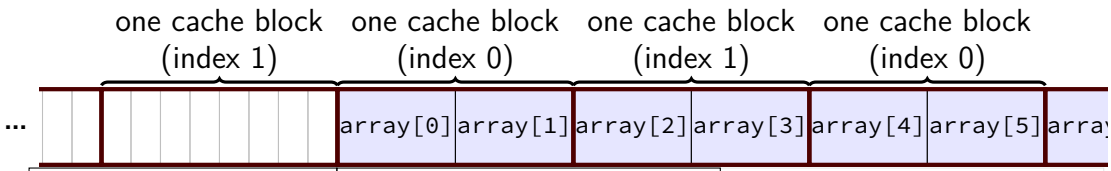
observation: what happens in set 0 doesn't affect set 1

when evaluating set 0 accesses,

can ignore non-set 0 accesses/content

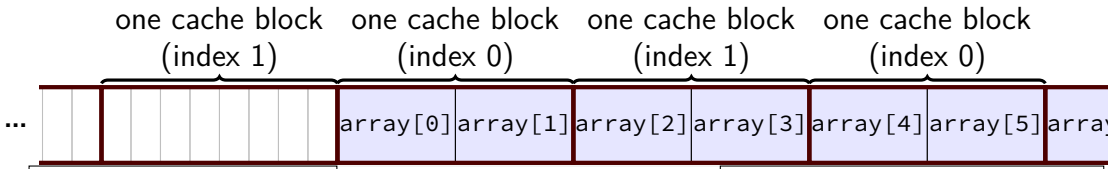
memory access	set 0 afterwards	set 1 afterwards
—	(empty)	(empty)
read array[0] (miss)	{array[0], array[1]}	(empty)
read array[1] (hit)	{array[0], array[1]}	(empty)
read array[2] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[3] (hit)	{array[0], array[1]}	{array[2], array[3]}
read array[4] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[5] (hit)	{array[4], array[5]}	{array[2], array[3]}
read array[6] (miss)	{array[4], array[5]}	{array[6], array[7]}
read array[7] (hit)	{array[4], array[5]}	{array[6], array[7]}

exercise solution



memory access	set 0 afterwards	set 1 afterwards
—	(empty)	(empty)
read array[0] (miss)	{array[0], array[1]}	(empty)
read array[1] (hit)	{array[0], array[1]}	(empty)
read array[2] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[3] (hit)	{array[0], array[1]}	{array[2], array[3]}
read array[4] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[5] (hit)	{array[4], array[5]}	{array[2], array[3]}
read array[6] (miss)	{array[4], array[5]}	{array[6], array[7]}
read array[7] (hit)	{array[4], array[5]}	{array[6], array[7]}

exercise solution



memory access	set 0 afterwards	set 1 afterwards
—	(empty)	(empty)
read array[0] (miss)	{array[0], array[1]}	(empty)
read array[1] (hit)	{array[0], array[1]}	(empty)
read array[2] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[3] (hit)	{array[0], array[1]}	{array[2], array[3]}
read array[4] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[5] (hit)	{array[4], array[5]}	{array[2], array[3]}
read array[6] (miss)	{array[4], array[5]}	{array[6], array[7]}
read array[7] (hit)	{array[4], array[5]}	{array[6], array[7]}

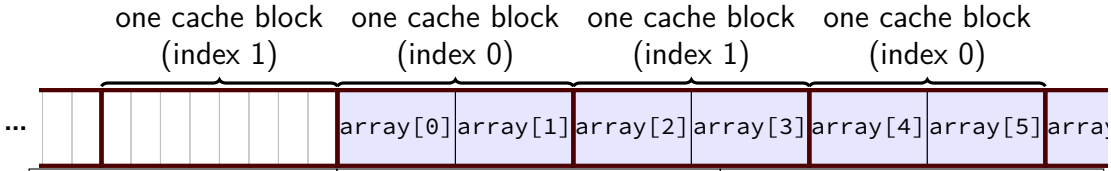
C and cache misses (warmup 4a)

```
int array[8]; /* assume aligned */
...
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
even_sum += array[2];
even_sum += array[4];
even_sum += array[6];
odd_sum += array[1];
odd_sum += array[3];
odd_sum += array[5];
odd_sum += array[7];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

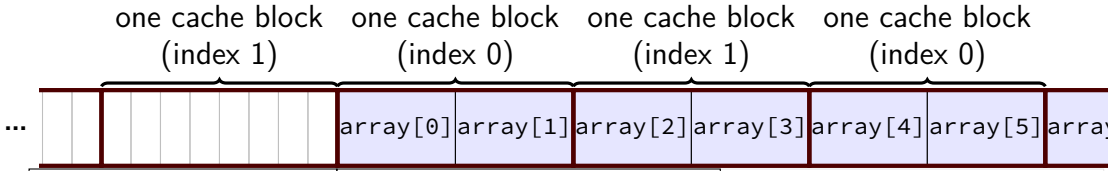
How many data cache misses on a **2**-set direct-mapped cache with 8B blocks?

exercise solution



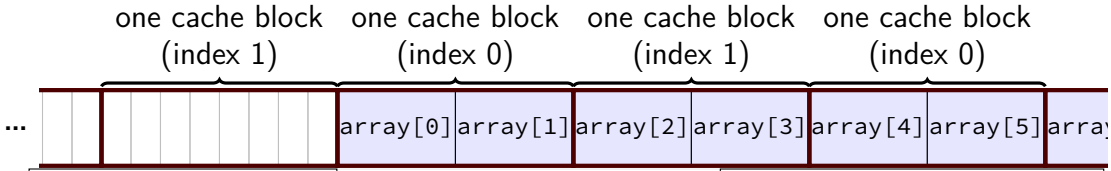
memory access	set 0 afterwards	set 1 afterwards
—	(empty)	(empty)
read array[0] (miss)	{array[0], array[1]}	(empty)
read array[2] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[4] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[6] (miss)	{array[4], array[5]}	{array[6], array[7]}
read array[1] (miss)	{array[0], array[1]}	{array[6], array[7]}
read array[3] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[5] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[7] (miss)	{array[4], array[5]}	{array[6], array[7]}

exercise solution



memory access	set 0 afterwards	set 1 afterwards
—	(empty)	(empty)
read array[0] (miss)	{array[0], array[1]}	(empty)
read array[2] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[4] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[6] (miss)	{array[4], array[5]}	{array[6], array[7]}
read array[1] (miss)	{array[0], array[1]}	{array[6], array[7]}
read array[3] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[5] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[7] (miss)	{array[4], array[5]}	{array[6], array[7]}

exercise solution



memory access	set 0 afterwards	set 1 afterwards
—	(empty)	(empty)
read array[0] (miss)	{array[0], array[1]}	(empty)
read array[2] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[4] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[6] (miss)	{array[4], array[5]}	{array[6], array[7]}
read array[1] (miss)	{array[0], array[1]}	{array[6], array[7]}
read array[3] (miss)	{array[0], array[1]}	{array[2], array[3]}
read array[5] (miss)	{array[4], array[5]}	{array[2], array[3]}
read array[7] (miss)	{array[4], array[5]}	{array[6], array[7]}

C and cache misses (warmup 4b)

```
int array[8]; /* assume aligned */
...
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
odd_sum += array[3];
even_sum += array[6];
odd_sum += array[1];
even_sum += array[4];
odd_sum += array[7];
even_sum += array[2];
odd_sum += array[5];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

How many data cache misses on a **2**-set direct-mapped cache with 8B blocks?

C and cache misses (warmup 5)

```
int array[1024]; /* assume aligned */ int even = 0, odd = 0;
even += array[0];
even += array[2];
even += array[512];
even += array[514];
odd += array[1];
odd += array[3];
odd += array[511];
odd += array[513];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

observation: array[0] and array[512] exactly 2KB apart

How many data cache misses on a 2KB direct mapped cache with 16B blocks?

C and cache misses (warmup 6)

```
int array[1024]; /* assume aligned */ int even = 0, odd = 0;
even += array[0];
even += array[2];
even += array[500];
even += array[502];
odd += array[1];
odd += array[3];
odd += array[501];
odd += array[503];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

How many data cache misses on a 2KB direct mapped cache with 16B blocks?

misses with skipping

```
int array1[512]; int array2[512];
...
for (int i = 0; i < 512; i += 1)
    sum += array1[i] * array2[i];
}
```

Assume everything but `array1`, `array2` is kept in registers (and the compiler does not do anything funny).

About how many *data cache misses* on a 2KB direct-mapped cache with 16B cache blocks?
Hint: depends on relative placement of array1, array2

best/worst case

`array1[i]` and `array2[i]` always different sets:

= distance from array1 to array2 not multiple of # sets × bytes/set

2 misses every 4 `i`

blocks of 4 array1[X] values loaded, then used 4 times before loading next block

(and same for array2[X])

`array1[i]` and `array2[i]` same sets:

= distance from array1 to array2 is multiple of # sets × bytes/set

2 misses every `i`

block of 4 array1[X] values loaded, one value used from it,

then, block of 4 array2[X] values replaces it, one value used from it, ...

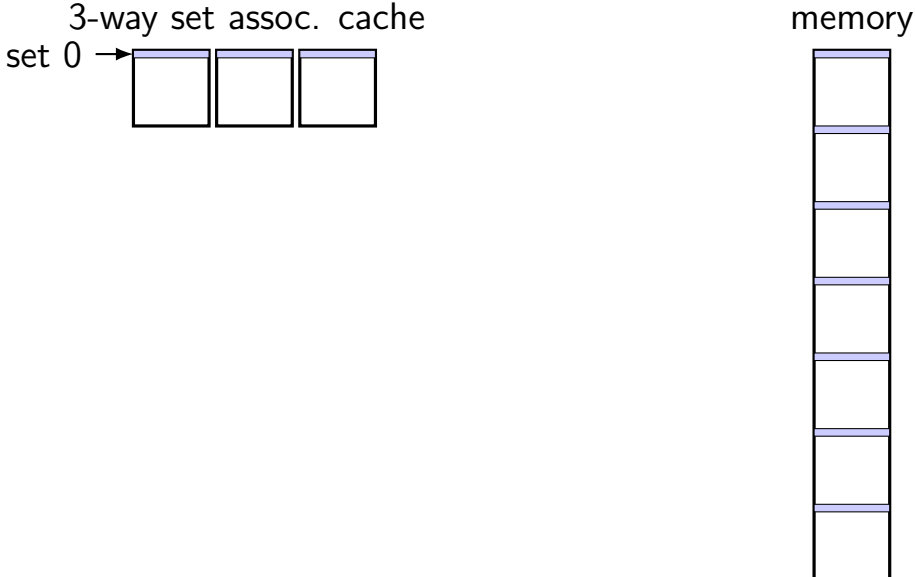
worst case in practice?

two rows of matrix?

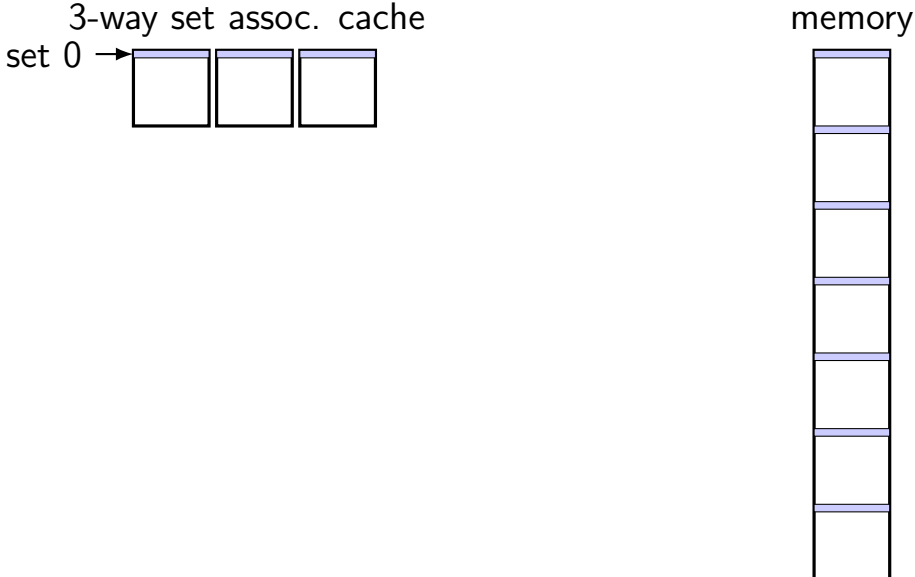
often sizeof(row) bytes apart

if the row size is multiple of number of sets $\times$ bytes per block, oops!

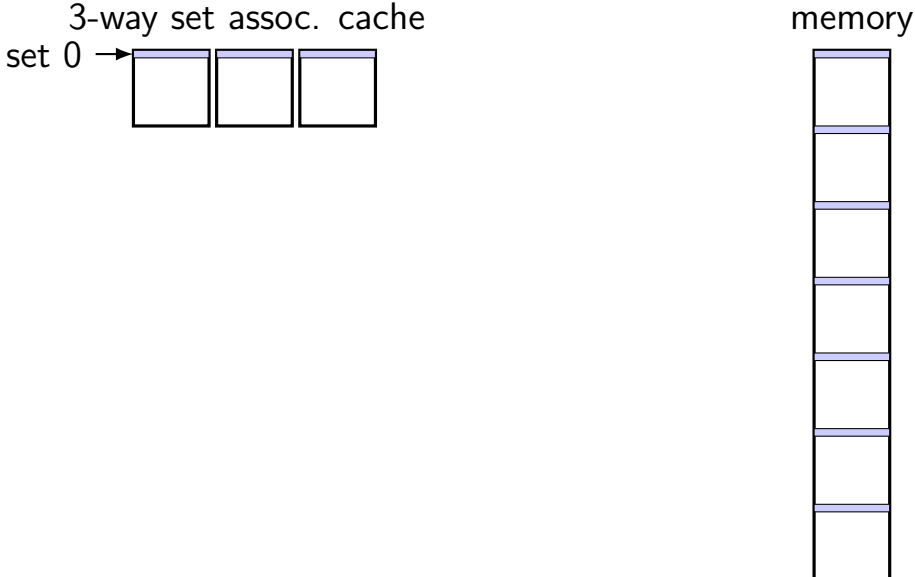
mapping of sets to memory (3-way)



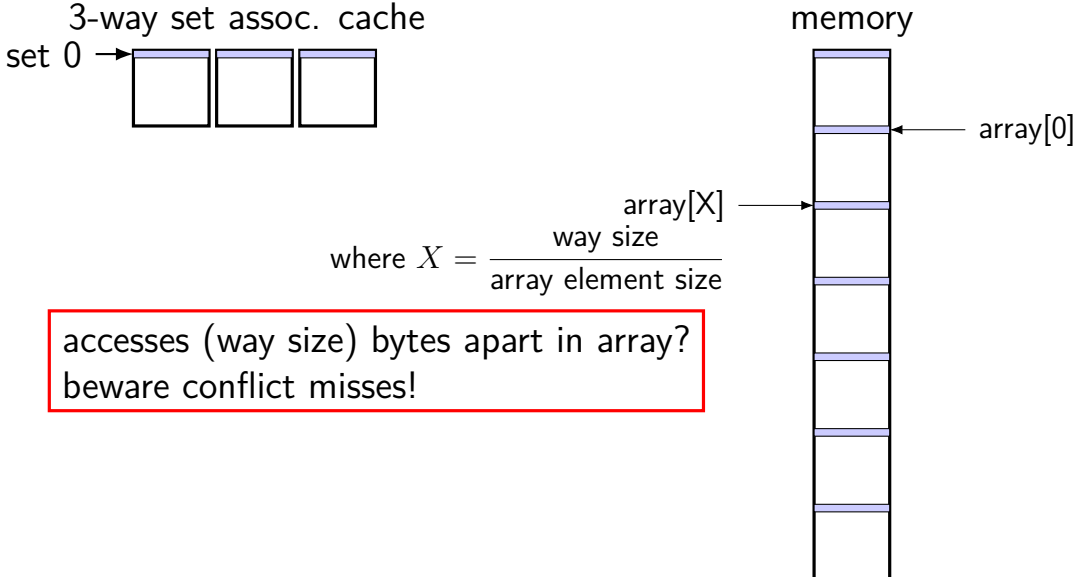
mapping of sets to memory (3-way)



mapping of sets to memory (3-way)



mapping of sets to memory (3-way)



accesses (way size) bytes apart in array?
beware conflict misses!

misses with skipping

```
int array1[512]; int array2[512];
...
for (int i = 0; i < 512; i += 1)
    sum += array1[i] * array2[i];
}
```

Assume everything but `array1`, `array2` is kept in registers (and the compiler does not do anything funny).

About how many *data cache misses* on a 2KB direct-mapped cache with 16B cache blocks?
Hint: depends on relative placement of array1, array2

How about on a two-way set associative cache?

C and cache misses (assoc)

```
int array[1024]; /* assume aligned */
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
even_sum += array[2];
even_sum += array[512];
even_sum += array[514];
odd_sum += array[1];
odd_sum += array[3];
odd_sum += array[511];
odd_sum += array[513];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

opbservation: array[0], array[256], array[512], array[768] in same set

How many data cache misses on a 2KB 2-way set associative cache with 16B blocks

C and cache misses (assoc)

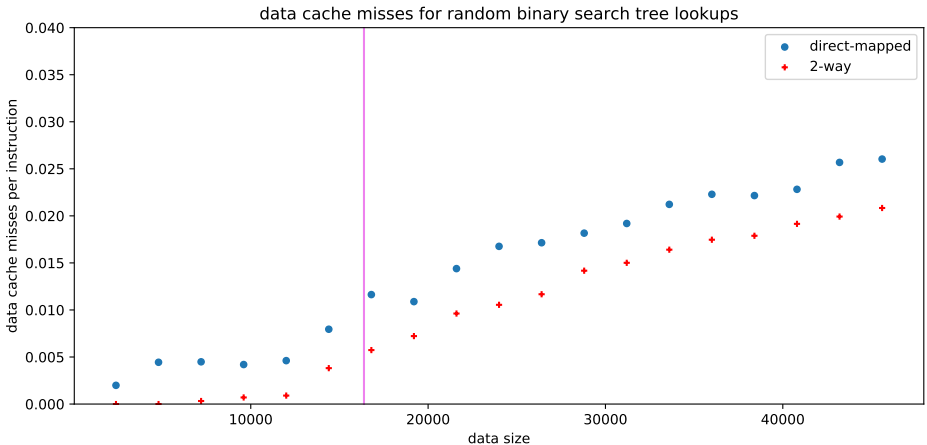
```
int array[1024]; /* assume aligned */
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
even_sum += array[256];
even_sum += array[512];
even_sum += array[768];
odd_sum += array[1];
odd_sum += array[257];
odd_sum += array[513];
odd_sum += array[769];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

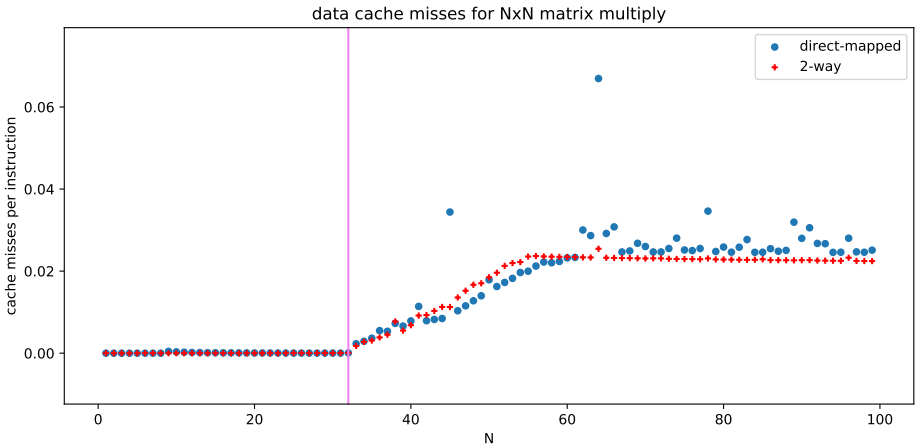
observation: array[0], array[256], array[512], array[768] in same set

How many data cache misses on a 2KB 2-way set associative cache with 16B blocks?

simulated misses: BST lookups



simulated misses: matrix multiplies



handling writes

what about writing to the cache?

two decision points:

if the value is not in cache, do we add it?

- if yes: need to load rest of block — *write-allocate*
- if no: missing out on locality? *write-no-allocate*

if value is in cache, when do we update next level?

- if immediately: extra writing *write-through*
- if later: need to remember to do so *write-back*

allocate on write?

processor writes less than whole cache block

block not yet in cache

two options:

write-allocate

fetch rest of cache block, replace written part
(then follow write-through or write-back policy)

write-no-allocate

don't use cache at all (send write to memory *instead*)
guess: not read soon?

allocate on write?

processor writes less than whole cache block

block not yet in cache

two options:

write-allocate

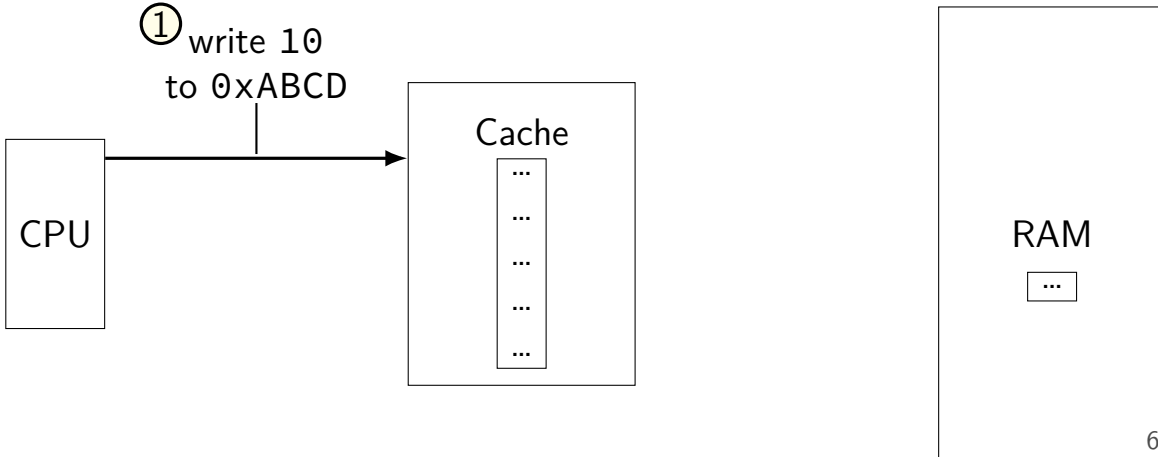
fetch rest of cache block, replace written part
(then follow write-through or write-back policy)

write-no-allocate

don't use cache at all (send write to memory *instead*)
guess: not read soon?

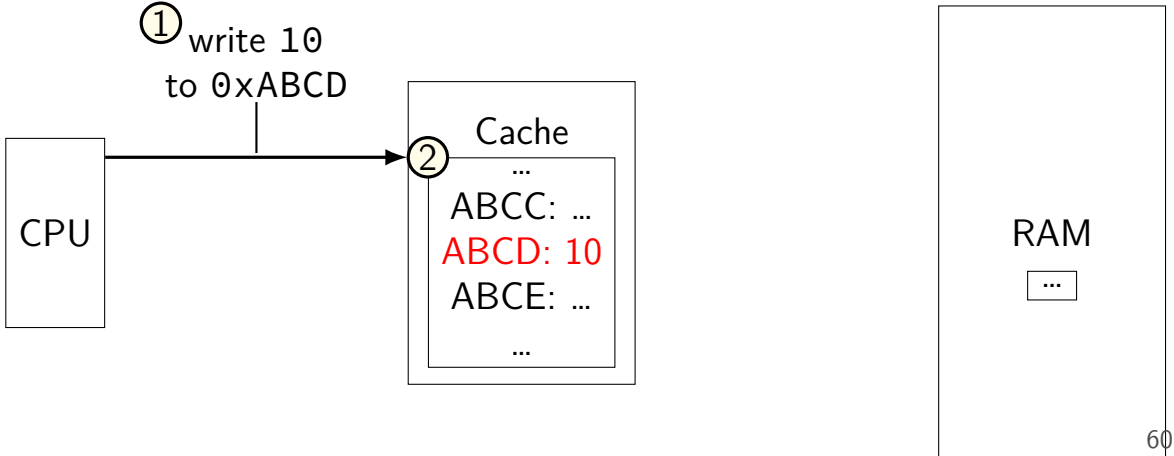
write-allocate v. write-no-allocate

option 1: write-allocate

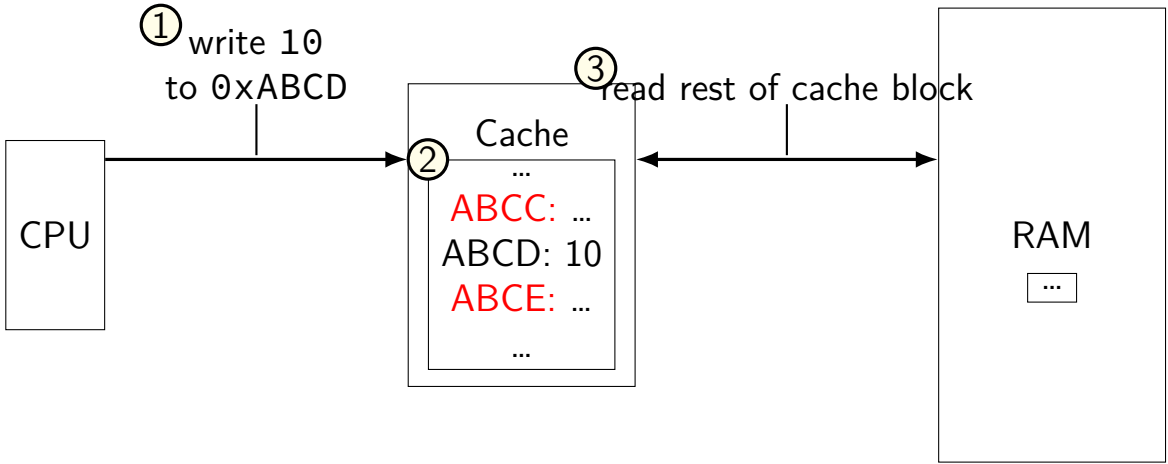


write-allocate v. write-no-allocate

option 1: write-allocate

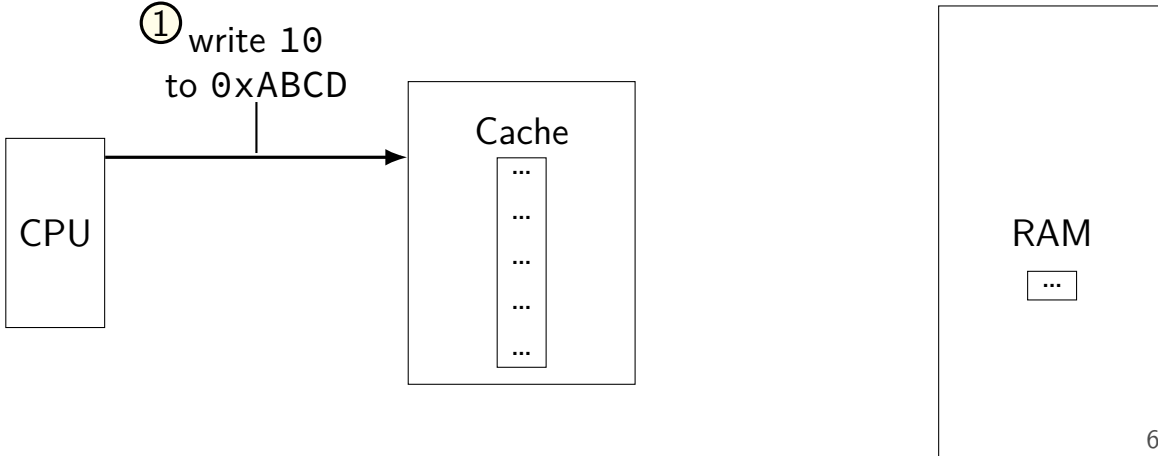


write-allocate v. write-no-allocate



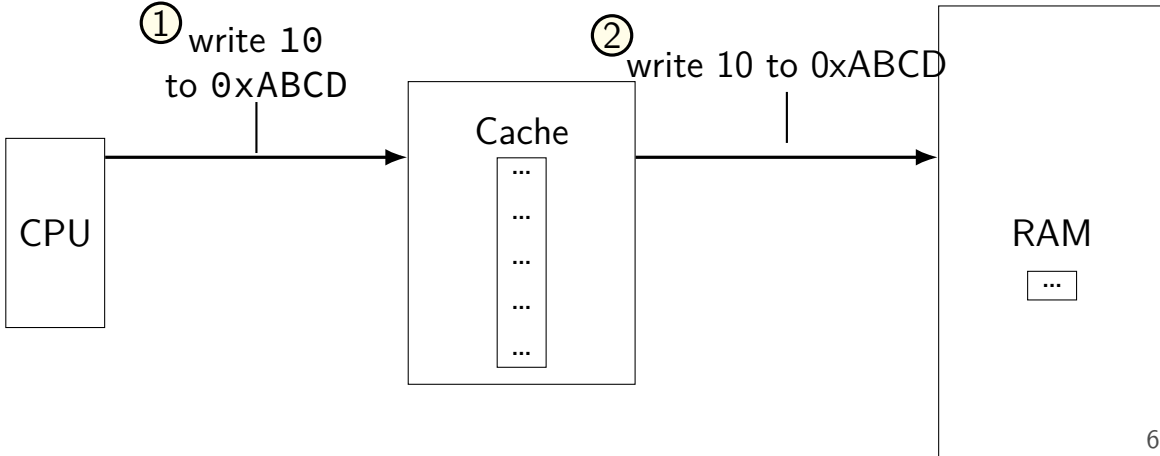
write-allocate v. write-no-allocate

option 2: write-no-allocate



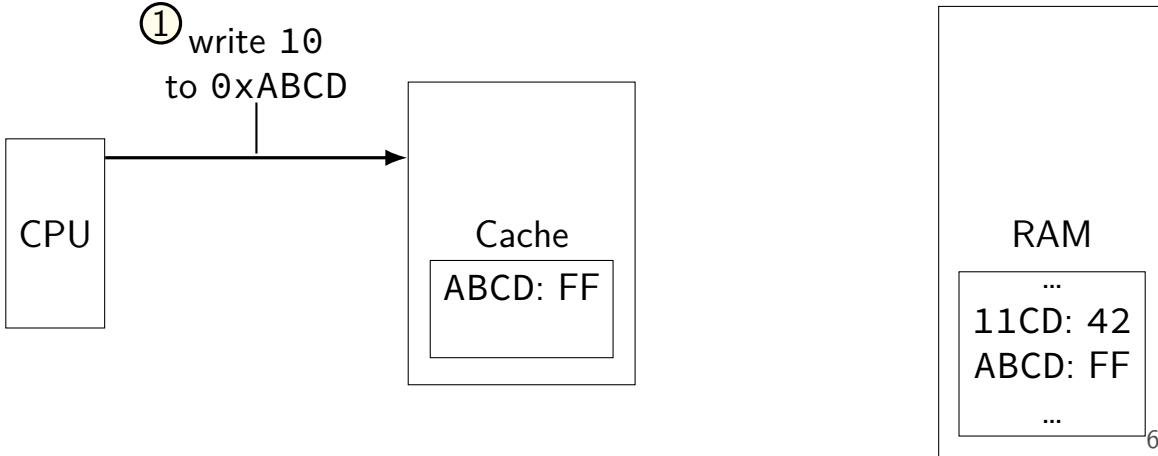
write-allocate v. write-no-allocate

option 2: write-no-allocate



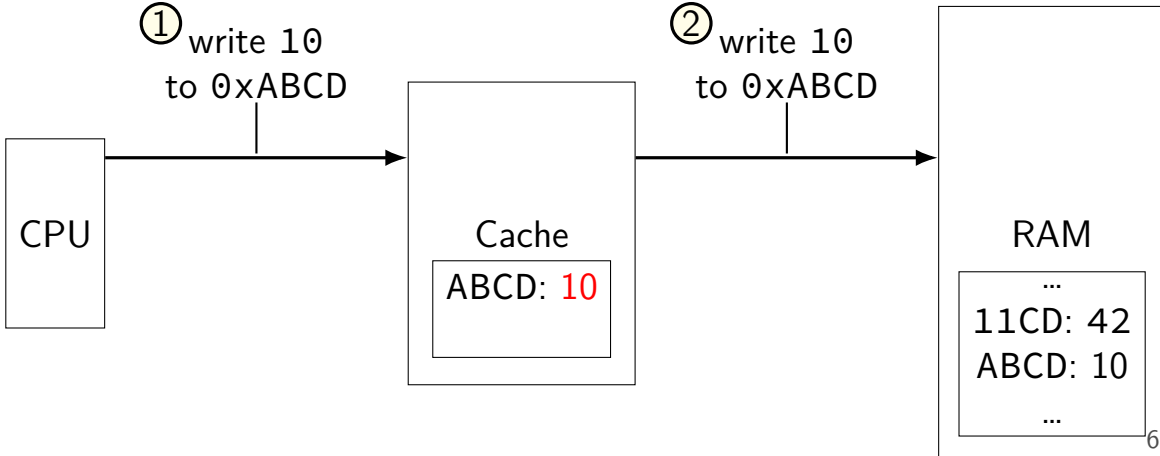
write-through v. write-back

option 1: write-through



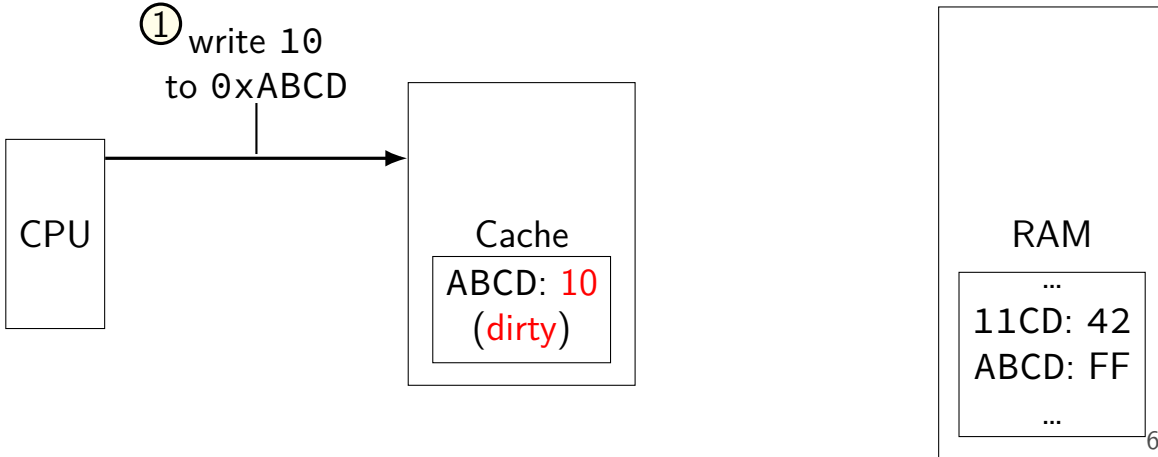
write-through v. write-back

option 1: write-through



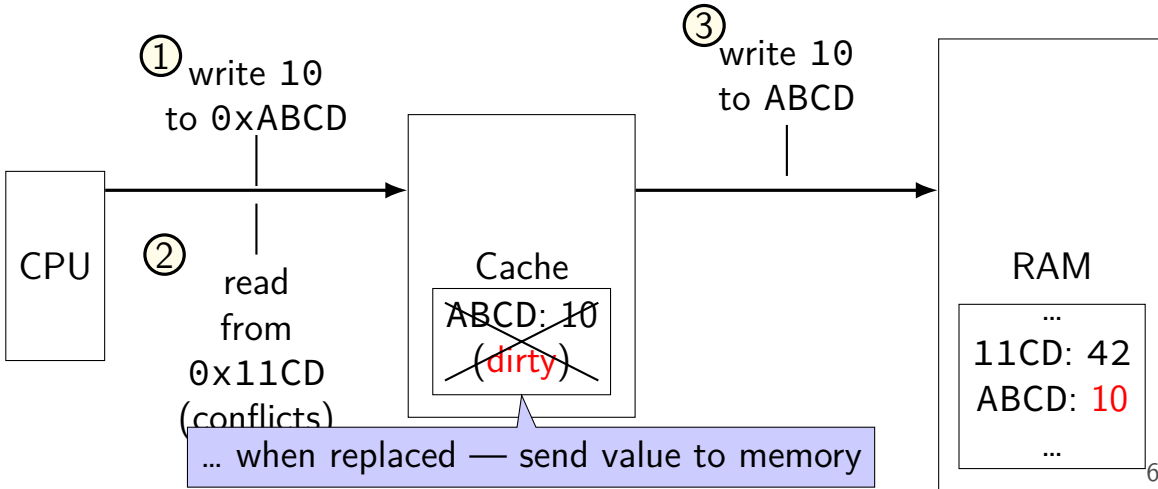
write-through v. write-back

option 2: write-back

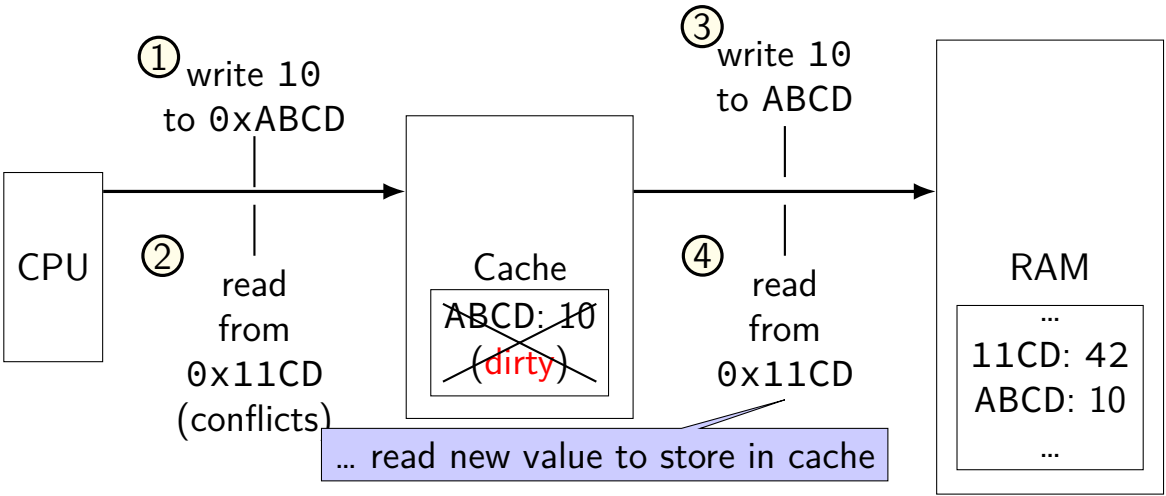


write-through v. write-back

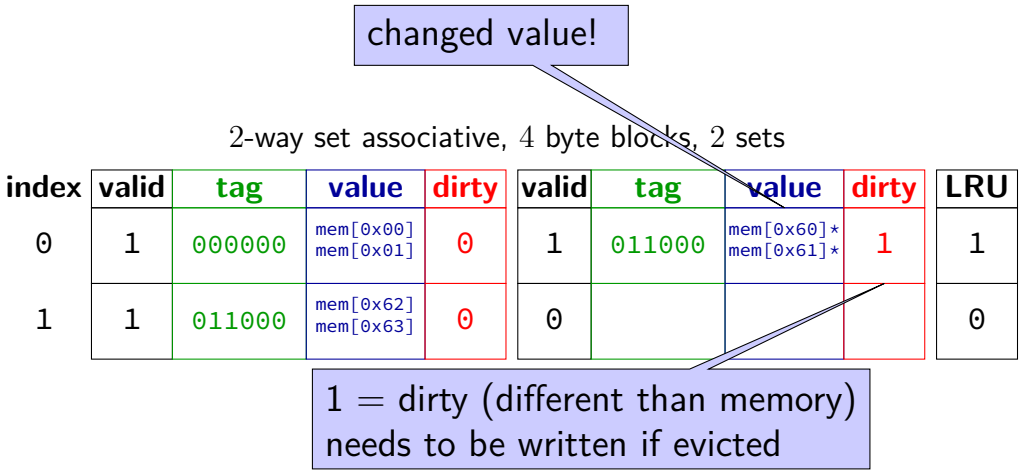
option 2: write-back



write-through v. write-back



writeback policy



write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing $\widehat{0}$xFF into address 0x04?

index 0, tag 000001

write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing $\widehat{0}$xFF into address 0x04?

index 0, tag 000001

step 1: find least recently used block

write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	~~1~~	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing $\widehat{0}$xFF into address 0x04?

index 0, tag 000001

step 1: find least recently used block

step 2: possibly writeback old block

write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	000001	0xFF mem[0x05]	1	0
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing $\widehat{0}$xFF into address 0x04?

index 0, tag 000001

step 1: find least recently used block

step 2: possibly writeback old block

step 3a: read in new block – to get mem[0x05]

step 3b: update LRU information

write-no-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing $\widehat{0}$xFF into address 0x04?

step 1: is it in cache yet?

step 2: no, just send it to memory

exercise (1)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	001100	mem[0x30] mem[0x31]	0	1	010000	mem[0x40]* mem[0x41]*	1	0
1	1	011000	mem[0x62] mem[0x63]	0	1	001100	mem[0x32]* mem[0x33]*	1	1

for each of the following accesses, performed alone, would it require (a) reading a value from memory (or next level of cache) and (b) writing a value to the memory (or next level of cache)?

writing 1 byte to 0x33
reading 1 byte from 0x52
reading 1 byte from 0x50

exercise (1, solution)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	001100	mem[0x30] mem[0x31]	0	1	010000	mem[0x40]* mem[0x41]*	1	0
1	1	011000	mem[0x62] mem[0x63]	0	1	001100	mem[0x32]* mem[0x33]*	1	1

writing 1 byte to 0x33: (set 1, offset 1) no read or write

reading 1 byte from 0x52:

reading 1 byte from 0x50:

exercise (1, solution)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	001100	mem[0x30] mem[0x31]	0	1	010000	mem[0x40]* mem[0x41]*	1	0
1	1	011000	mem[0x62] mem[0x63]	0	1	001100	mem[0x32]* mem[0x33]*	1	~~1~~0

writing 1 byte to 0x33: (set 1, offset 1) no read or write

reading 1 byte from 0x52:

reading 1 byte from 0x50:

exercise (1, solution)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	001100	mem[0x30] mem[0x31]	0	1	010000	mem[0x40]* mem[0x41]*	1	0
1	1	011000	mem[0x62] mem[0x63]	0	1	001100	mem[0x32]* mem[0x33]*	1	1

writing 1 byte to 0x33: (set 1, offset 1) no read or write

reading 1 byte from 0x52: (set 1, offset 0) **write** back 0x32-0x33; **read** 0x52-0x53

reading 1 byte from 0x50:

exercise (1, solution)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	001100	mem[0x30] mem[0x31]	0	1	010000	mem[0x40]* mem[0x41]*	1	0
1	1	011000	mem[0x62] mem[0x63]	0	1	101000	mem[0x52] mem[0x53]	~~1~~0	~~1~~0

writing 1 byte to 0x33: (set 1, offset 1) no read or write

reading 1 byte from 0x52: (set 1, offset 0) **write** back 0x32-0x33; **read** 0x52-0x53

reading 1 byte from 0x50:

exercise (1, solution)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	001100	mem[0x30] mem[0x31]	0	1	010000	mem[0x40]* mem[0x41]*	1	0
1	1	011000	mem[0x62] mem[0x63]	0	1	001100	mem[0x32]* mem[0x33]*	1	1

writing 1 byte to 0x33: (set 1, offset 1) no read or write

reading 1 byte from 0x52: (set 1, offset 0) **write** back 0x32-0x33; **read** 0x52-0x53

reading 1 byte from 0x50: (set 0, offset 0) replace 0x30-0x31 (no write back); **read** 0x50-0x51

exercise (1, solution)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	101000	mem[0x50] mem[0x51]	0	1	010000	mem[0x40]* mem[0x41]*	1	~~0~~1
1	1	011000	mem[0x62] mem[0x63]	0	1	001100	mem[0x32]* mem[0x33]*	1	1

writing 1 byte to 0x33: (set 1, offset 1) no read or write

reading 1 byte from 0x52: (set 1, offset 0) **write** back 0x32-0x33; **read** 0x52-0x53

reading 1 byte from 0x50: (set 0, offset 0) replace 0x30-0x31 (no write back); **read** 0x50-0x51

exercise (2)

2-way set associative, LRU, write-no-allocate, write-through

index	valid	tag	value	valid	tag	value	LRU
0	1	001100	mem[0x30] mem[0x31]	1	010000	mem[0x40] mem[0x41]	0
1	1	011000	mem[0x62] mem[0x63]	1	001100	mem[0x32] mem[0x33]	1

for each of the following accesses, performed alone, would it require (a) reading a value from memory and (b) writing a value to the memory?

writing 1 byte to 0x33
reading 1 byte from 0x52
reading 1 byte from 0x50

exercise (2, solution)

2-way set associative, LRU, write-no-allocate, write-through

index	valid	tag	value	valid	tag	value	LRU
0	1	001100	mem[0x30] mem[0x31]	1	010000	mem[0x40] mem[0x41]	0
1	1	011000	mem[0x62] mem[0x63]	1	001100	mem[0x32] mem[0x33]	1

writing 1 byte to 0x33: (set 1, offset 1) write-through 0x33 modification

reading 1 byte from 0x52:

reading 1 byte from 0x50:

exercise (2, solution)

2-way set associative, LRU, write-no-allocate, write-through

index	valid	tag	value	valid	tag	value	LRU
0	1	001100	mem[0x30] mem[0x31]	1	010000	mem[0x40] mem[0x41]	0
1	1	011000	mem[0x62] mem[0x63]	1	001100	mem[0x32] mem[0x33]	~~10~~

writing 1 byte to 0x33: (set 1, offset 1) write-through 0x33 modification

reading 1 byte from 0x52:

reading 1 byte from 0x50:

exercise (2, solution)

2-way set associative, LRU, write-no-allocate, write-through

index	valid	tag	value	valid	tag	value	LRU
0	1	001100	mem[0x30] mem[0x31]	1	010000	mem[0x40] mem[0x41]	0
1	1	011000	mem[0x62] mem[0x63]	1	001100	mem[0x32] mem[0x33]	1

writing 1 byte to 0x33: (set 1, offset 1) write-through 0x33 modification

reading 1 byte from 0x52: (set 1, offset 0) replace 0x32-0x33; **read** 0x52-0x53

reading 1 byte from 0x50:

exercise (2, solution)

2-way set associative, LRU, write-no-allocate, write-through

index	valid	tag	value	valid	tag	value	LRU
0	1	001100	mem[0x30] mem[0x31]	1	010000	mem[0x40] mem[0x41]	0
1	1	011000	mem[0x62] mem[0x63]	1	101000	mem[0x52] mem[0x53]	~~1~~0

writing 1 byte to 0x33: (set 1, offset 1) write-through 0x33 modification

reading 1 byte from 0x52: (set 1, offset 0) replace 0x32-0x33; **read** 0x52-0x53

reading 1 byte from 0x50:

exercise (2, solution)

2-way set associative, LRU, write-no-allocate, write-through

index	valid	tag	value	valid	tag	value	LRU
0	1	001100	mem[0x30] mem[0x31]	1	010000	mem[0x40] mem[0x41]	0
1	1	011000	mem[0x62] mem[0x63]	1	001100	mem[0x32] mem[0x33]	1

writing 1 byte to 0x33: (set 1, offset 1) write-through 0x33 modification

reading 1 byte from 0x52: (set 1, offset 0) replace 0x32-0x33; **read** 0x52-0x53

reading 1 byte from 0x50: (set 0, offset 0) replace 0x30-0x31; **read** 0x50-0x51

exercise (2, solution)

2-way set associative, LRU, write-no-allocate, write-through

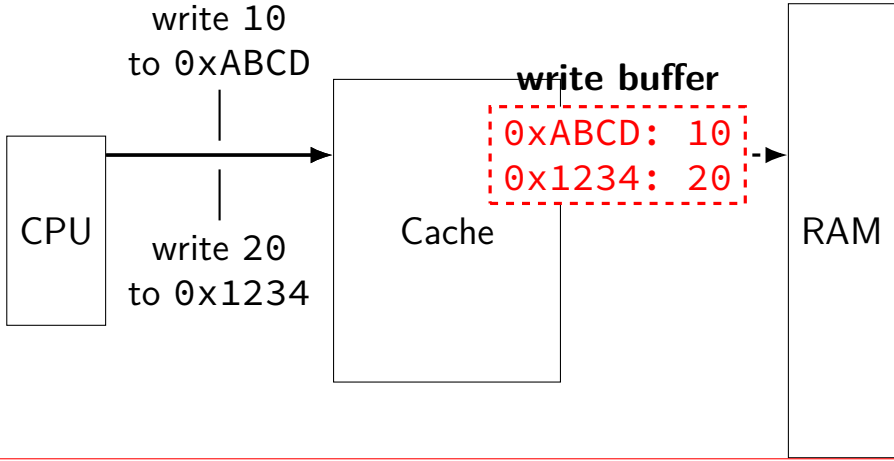
index	valid	tag	value	valid	tag	value	LRU
0	1	101000	mem[0x50] mem[0x51]	1	010000	mem[0x40] mem[0x41]	~~01~~
1	1	011000	mem[0x62] mem[0x63]	1	001100	mem[0x32] mem[0x33]	1

writing 1 byte to 0x33: (set 1, offset 1) write-through 0x33 modification

reading 1 byte from 0x52: (set 1, offset 0) replace 0x32-0x33; **read** 0x52-0x53

reading 1 byte from 0x50: (set 0, offset 0) replace 0x30-0x31; **read** 0x50-0x51

fast writes



write appears to complete immediately when placed in buffer
memory can be much slower

cache tradeoffs briefly

deciding cache size, associativity, etc.?

lots of tradeoffs:

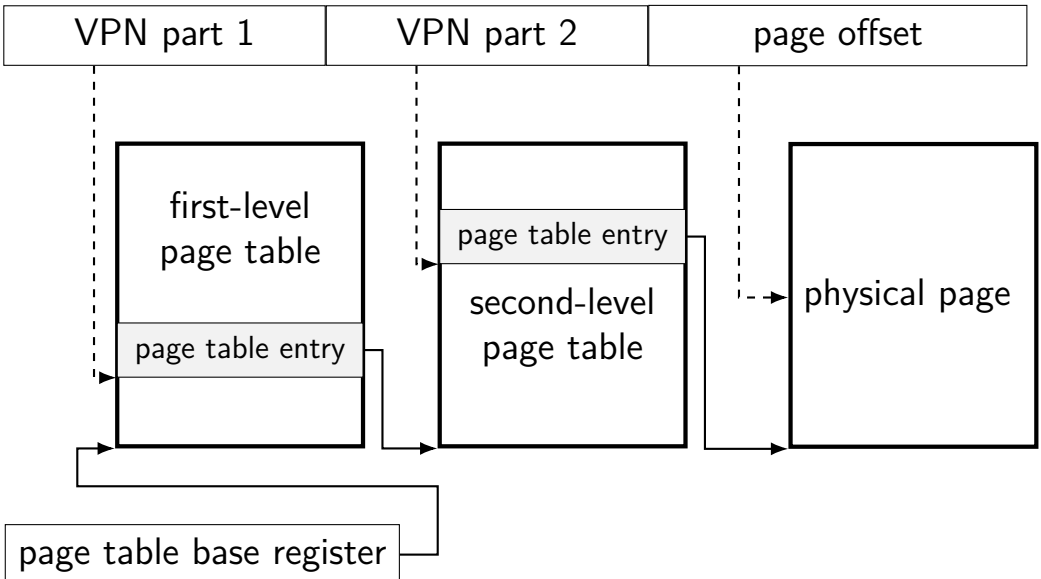
- more cache hits v. slower cache hits?
- faster cache hits v. fewer cache hits?
- more cache hits v. slower cache misses?
- ...

details depend on programs run

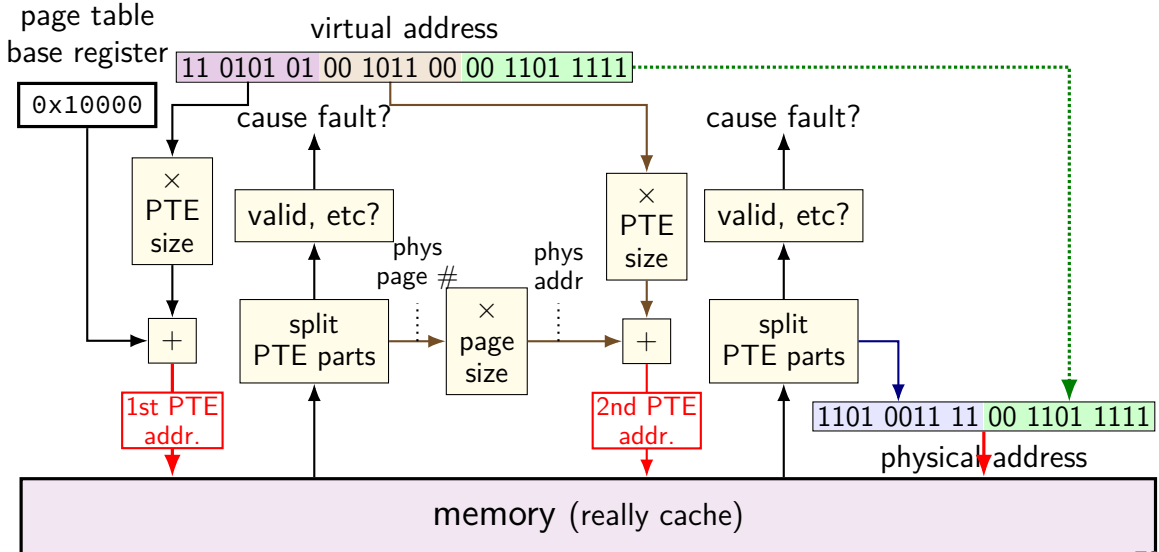
- how often is same block used again?
- how often is same index bits used?

simulation to assess impact of designs

another view



two-level page table lookup



cache accesses and multi-level PTs

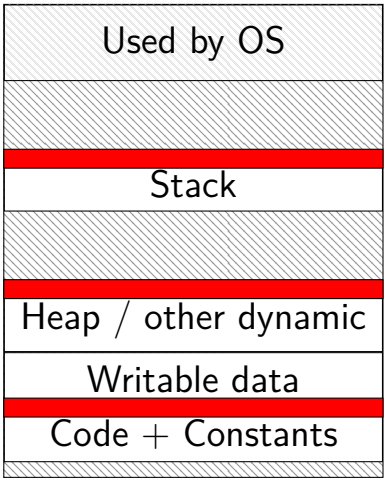
four-level page tables — five cache accesses per program memory access

L1 cache hits — typically a couple cycles each?

so add 8 cycles to each program memory access?

not acceptable

program memory active sets



0xFFFF FFFF FFFF FFFF

0xFFFF 8000 0000 0000

0x7F...

small areas of memory active at a time
one or two pages in each area?

0x0000 0000 0040 0000

page table entries and locality

page table entries have excellent temporal locality

typically one or two pages of the stack active

typically one or two pages of code active

typically one or two pages of heap/globals active

each page contains whole functions, arrays, stack frames, etc.

page table entries and locality

page table entries have excellent temporal locality

typically one or two pages of the stack active

typically one or two pages of code active

typically one or two pages of heap/globals active

each page contains whole functions, arrays, stack frames, etc.

needed page table entries are very small

page table entry cache

caled a **TLB** (translation lookaside buffer)

(usually very small) cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

page table entry cache

caled a **TLB** (translation lookaside buffer)

(usually very small) cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

only caches the page table lookup itself
(generally) just entries from the last-level page tables

page table entry cache

caled a **TLB** (translation lookaside buffer)

(usually very small) cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

virtual page number divided into index + tag

page table entry cache

caled a **TLB** (translation lookaside buffer)

(usually very small) cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

not much spatial locality between page table entries
(they're used for kilobytes of data already)

page table entry cache

caled a **TLB** (translation lookaside buffer)

(usually very small) cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

0 block offset bits

page table entry cache

caled a **TLB** (translation lookaside buffer)

(usually very small) cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

few active page table entries at a time
enables highly associative cache designs

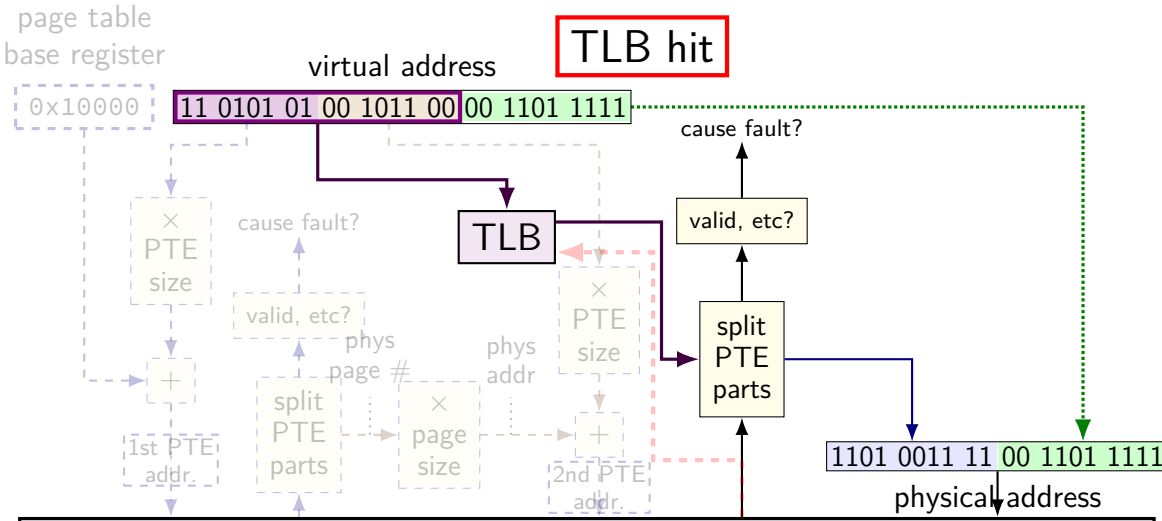
TLB and multi-level page tables

TLB caches valid last-level page table entries

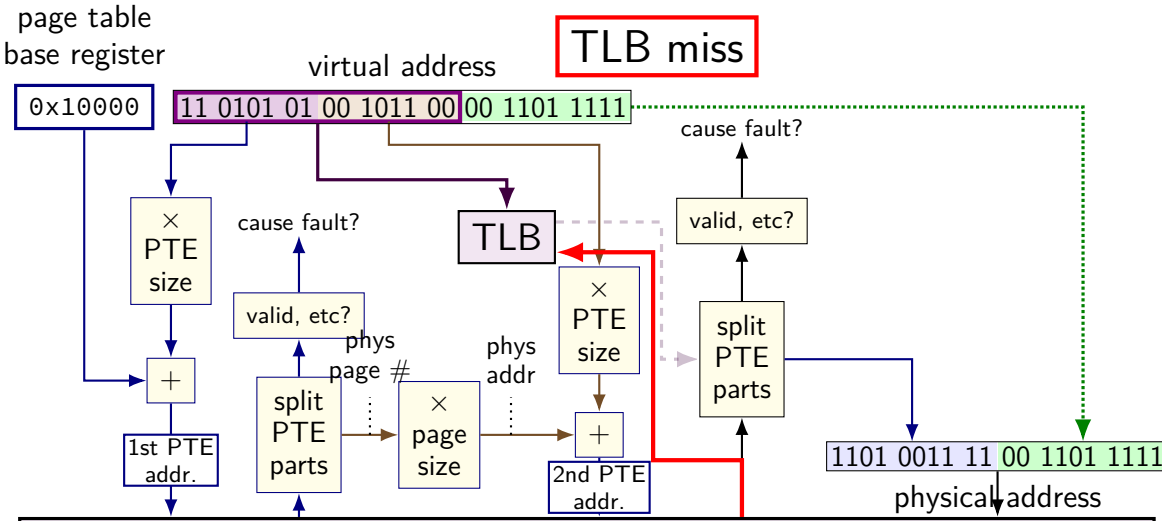
doesn't matter which last-level page table

means TLB output can be used directly to form address

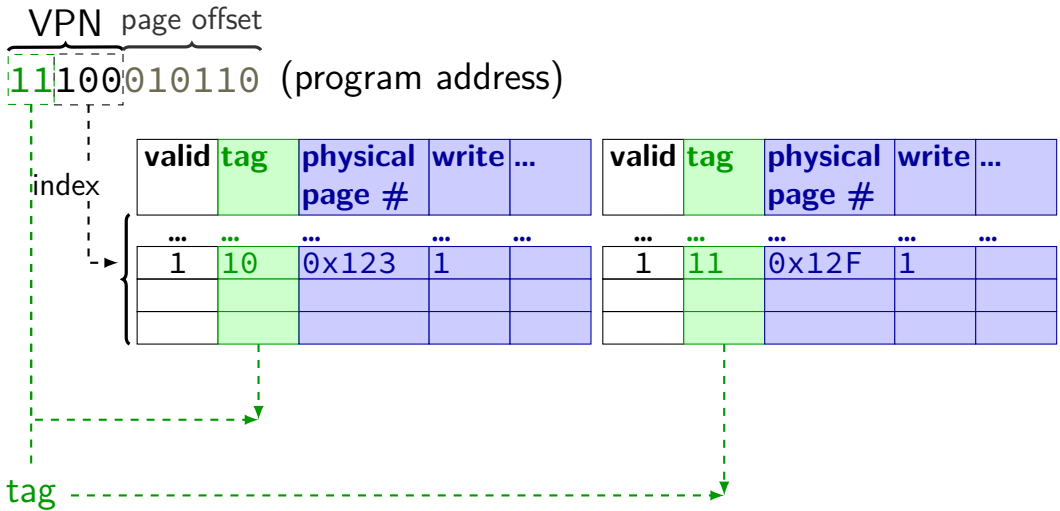
TLB and two-level lookup



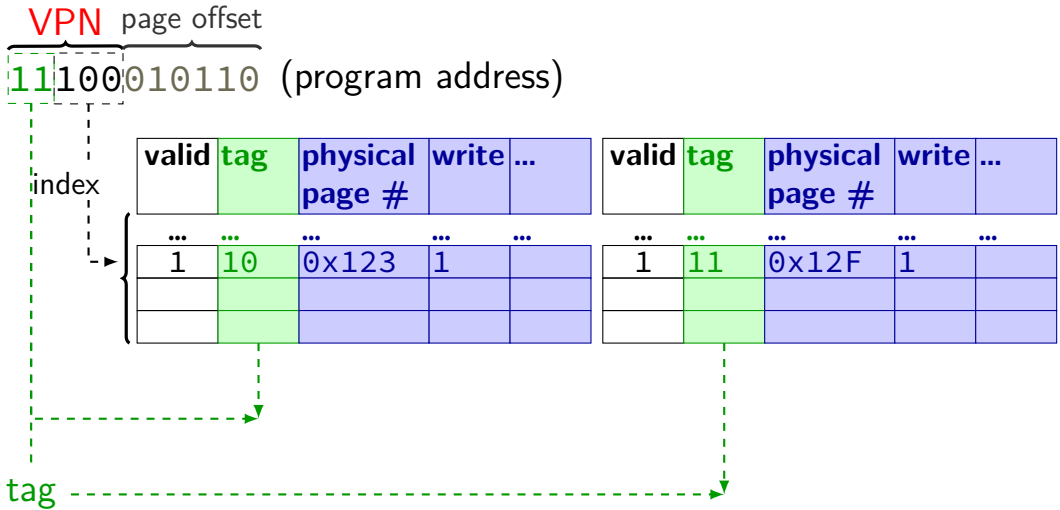
TLB and two-level lookup



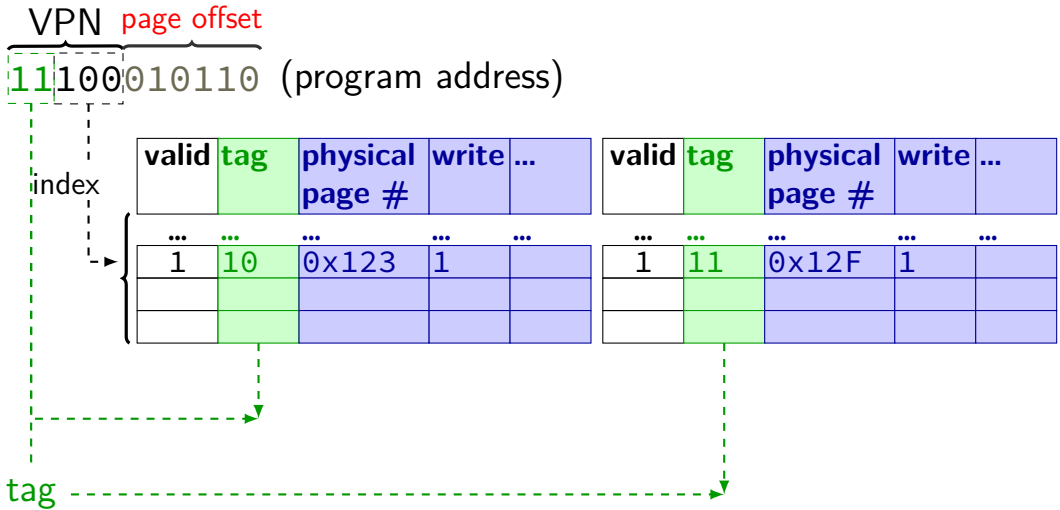
TLB organization (2-way set associative)



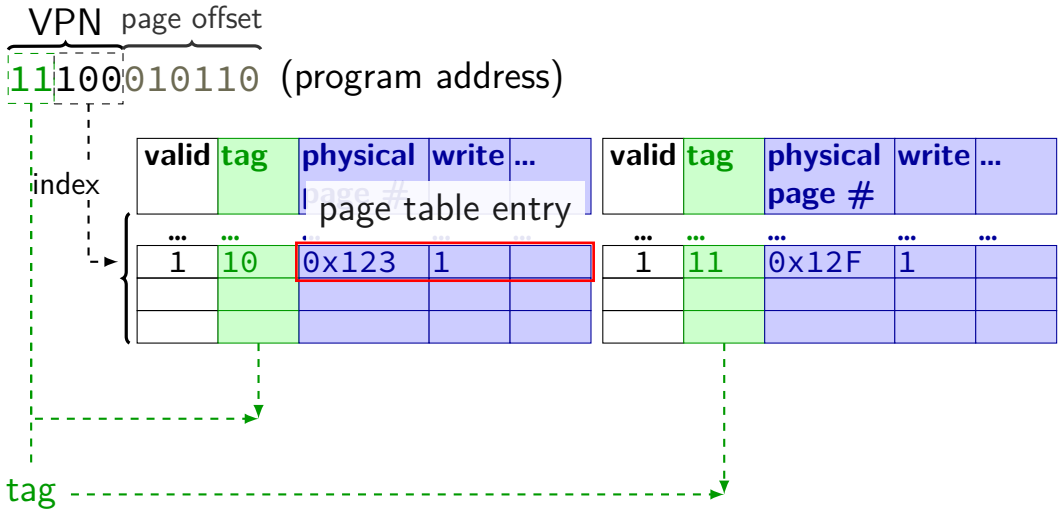
TLB organization (2-way set associative)



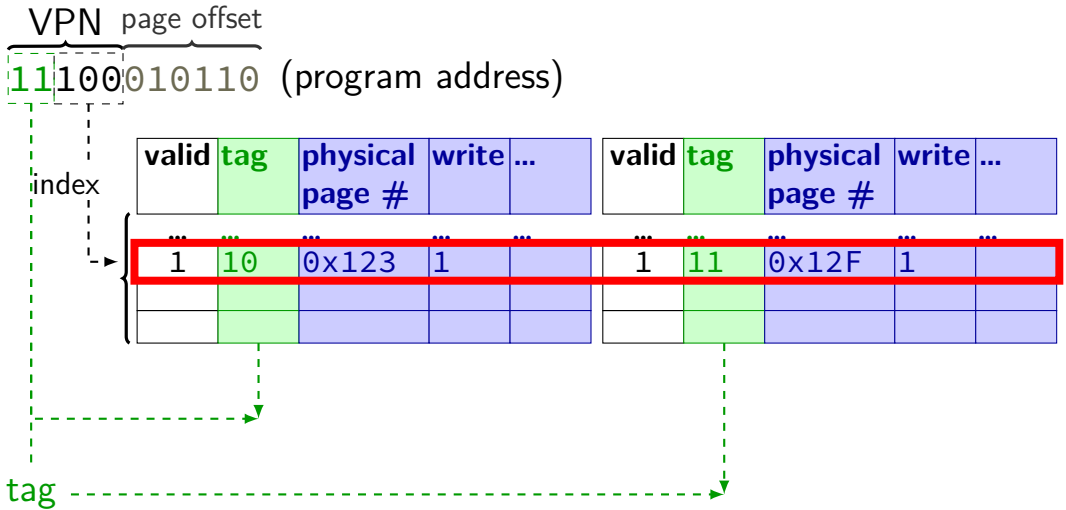
TLB organization (2-way set associative)



TLB organization (2-way set associative)



TLB organization (2-way set associative)



exercise: TLB access pattern (setup)

4-entry, 2-way TLB, LRU replacement policy, initially empty

4096 byte pages

how many index bits?

TLB index of virtual address 0x12345?

exercise: TLB access pattern

4-entry, 2-way TLB, LRU replacement policy, initially empty

4096 byte pages

type	virtual	physical
read	0x440030	0x554030
write	0x440034	0x554034
read	0x7FFFE008	0x556008
read	0x7FFFE000	0x556000
read	0x7FFFDFF8	0x5F8FF8
read	0x664080	0x5F9080
read	0x440038	0x554038
write	0x7FFFDFF0	0x5F8FF0

which are TLB hits? which are TLB misses? final contents of TLB?

exercise: TLB access pattern

4-entry, 2-way TLB, LRU replacement policy, initially empty

4096 byte pages

				VPNs of PTEs held in TLB	
type	virtual	physical	result	set 0	set 1
`read`	`0x440030`	`0x554030`	miss	0x440	
`write`	`0x440034`	`0x554034`	hit	0x440	
`read`	`0x7FFFE008`	`0x556008`	miss	0x440	
`read`	`0x7FFFE000`	`0x556000`	hit	0x440, 0x7FFFE	
`read`	`0x7FFFDFF8`	`0x5F8FF8`	miss	0x440, 0x7FFFE	0x7FFFD
`read`	`0x664080`	`0x5F9080`	miss	0x664, 0x7FFFE	0x7FFFD
`read`	`0x440038`	`0x554038`	miss	0x664, 0x440	0x7FFFD
`write`	`0x7FFFDFF0`	`0x5F8FF0`	hit	0x664, 0x440	0x7FFFD

which are TLB hits? which are TLB misses? final contents of TLB?

exercise: TLB access pattern

4-entry, 2-way TLB, LRU replacement policy, initially empty

4096 byte pages

set idx	V	tag	physical page	write?	user?	...	LRU?
0	1	0x00220 (0x440 ≫ 1)	0x554	1	1	...	no
	1	0x00332 (0x00664 ≫ 1)	0x5F9	1	1	...	yes
1	1	0x3FFFF (0x7FFFD ≫ 1)	0x5F8	1	1	...	no
	0	---	---	–	–	...	yes

type					
read	0x440038	0x554038	miss	0x664, 0x440	0x7FFFD
write	0x7FFFDFF0	0x5F8FF0	hit	0x664, 0x440	0x7FFFD

which are TLB hits? which are TLB misses? final contents of TLB?