cache accesses and C code (1)

```
int scaleFactor;

int scaleByFactor(int value) {
    return value * scaleFactor;
}
```

```
scaleByFactor:
    movl scaleFactor, %eax
    imull %edi, %eax
    ret
```

---

exericse: what data cache accesses does this function do?

cache accesses and C code (1)

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int scaleFactor;

int scaleByFactor(int value) {
    return value * scaleFactor;
}
```

```
scaleByFactor:
    movl scaleFactor, %eax
    imull %edi, %eax
    ret
```

---

exericse: what data cache accesses does this function do?

- 4-byte read of scaleFactor
- 8-byte read of return address

possible scaleFactor use

```
for (int i = 0; i < size; ++i) {
    array[i] = scaleByFactor(array[i]);
}
```

misses and code (2)

```
scaleByFactor:
    movl scaleFactor, %eax
    imull %edi, %eax
    ret
```

suppose each time this is called in the loop:

- return address located at address `0x7ffffffe43b8`
- scaleFactor located at address `0x6bc3a0`

with direct-mapped 32KB cache w/64 B blocks, what is their:

	return address	scaleFactor
tag		
index		
offset		

misses and code (2)

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```

suppose each time this is called in the loop:

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with direct-mapped 32KB cache w/64 B blocks, what is their:

	return address	scaleFactor
tag	0xffffffc	0xd7
index	0x10e	0x10e
offset	0x38	0x20

misses and code (2)

```
scaleByFactor:
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```

suppose each time this is called in the loop:

return address located at address `0x7ffffffe43b8`

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with direct-mapped 32KB cache w/64 B blocks, what is their:

	return address	scaleFactor
tag	0xffffffc	0xd7
index	0x10e	0x10e
offset	0x38	0x20

conflict miss coincidences?

obviously I set that up to have the same index

- have to use exactly the right amount of stack space…

but one of the reasons we'll want something better than direct-mapped cache

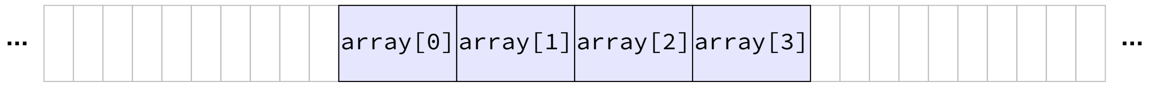
C and cache misses (warmup 1)

```
int array[4];
...
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
odd_sum += array[1];
even_sum += array[2];
odd_sum += array[3];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

How many data cache misses on a 1-set direct-mapped cache with 8B blocks?

some possiblities



Q1: how do cache blocks correspond to array elements?
not enough information provided!

aside: alignment

compilers and malloc/new implementations usually try align values

align = make address be multiple of something

most important reason: don't cross cache block boundaries

C and cache misses (warmup 2)

```
int array[4];
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
even_sum += array[2];
odd_sum += array[1];
odd_sum += array[3];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

Assume array[0] at beginning of cache block.

How many data cache misses on a 1-set direct-mapped cache with 8B blocks?

C and cache misses (warmup 3)

```
int array[8];
...
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
odd_sum += array[1];
even_sum += array[2];
odd_sum += array[3];
even_sum += array[4];
odd_sum += array[5];
even_sum += array[6];
odd_sum += array[7];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny), and array[0] at beginning of cache block.

How many data cache misses on a **2**-set direct-mapped cache with 8B blocks?

C and cache misses (warmup 4)

```
int array[8];
...
int even_sum = 0, odd_sum = 0;
even_sum += array[0];
even_sum += array[2];
even_sum += array[4];
even_sum += array[6];
odd_sum += array[1];
odd_sum += array[3];
odd_sum += array[5];
odd_sum += array[7];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

How many data cache misses on a **2**-set direct-mapped cache with 8B blocks?

arrays and cache misses (1)

```
int array[1024]; // 4KB array
int even_sum = 0, odd_sum = 0;
for (int i = 0; i < 1024; i += 2) {
    even_sum += array[i + 0];
    odd_sum +=  array[i + 1];
}
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

How many *data cache misses* on initially empty 2KB direct-mapped cache with 16B cache blocks?

arrays and cache misses (2)

```
int array[1024]; // 4KB array
int even_sum = 0, odd_sum = 0;
for (int i = 0; i < 1024; i += 2)
    even_sum += array[i + 0];
for (int i = 0; i < 1024; i += 2)
    odd_sum +=  array[i + 1];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

How many *data cache misses* on initially empty 2KB direct-mapped cache with 16B cache blocks?

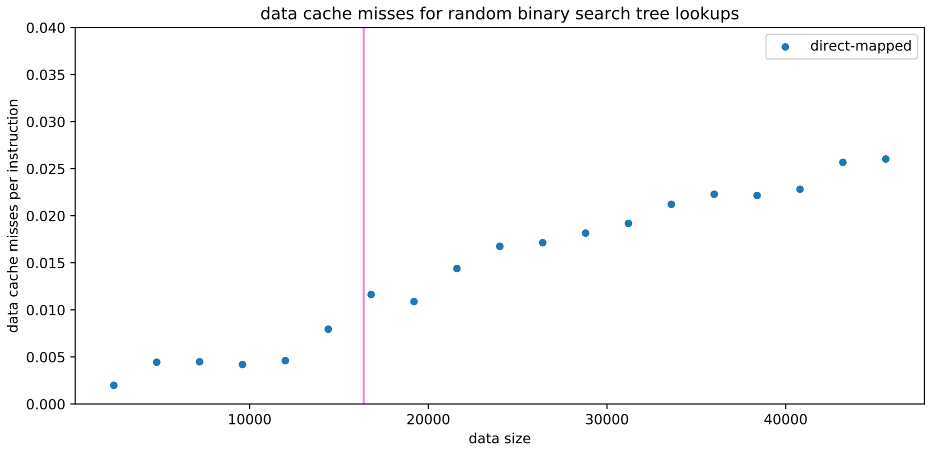
arrays and cache misses (2b)

```
int array[1024]; // 4KB array
int even_sum = 0, odd_sum = 0;
for (int i = 0; i < 1024; i += 2)
    even_sum += array[i + 0];
for (int i = 0; i < 1024; i += 2)
    odd_sum +=  array[i + 1];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

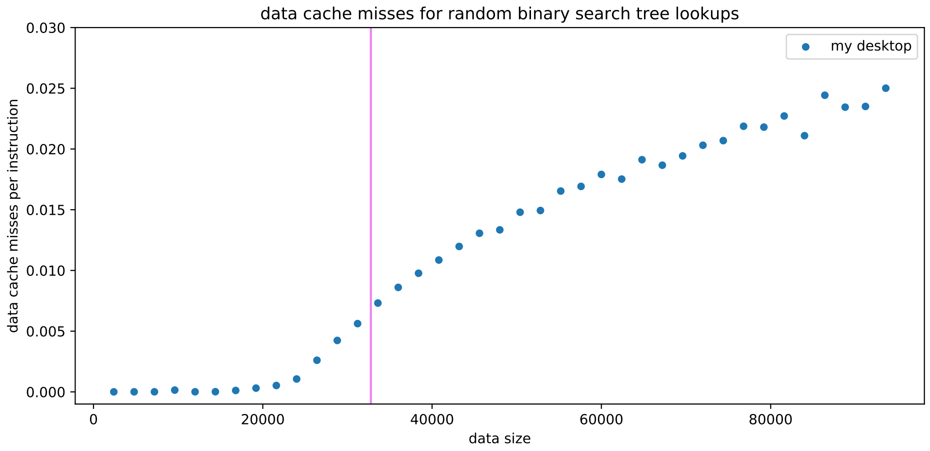
How many *data cache misses* on initially empty 4KB direct-mapped cache with 16B cache blocks?

simulated misses: BST lookups



(simulated 16KB direct-mapped data cache; excluding BST setup)

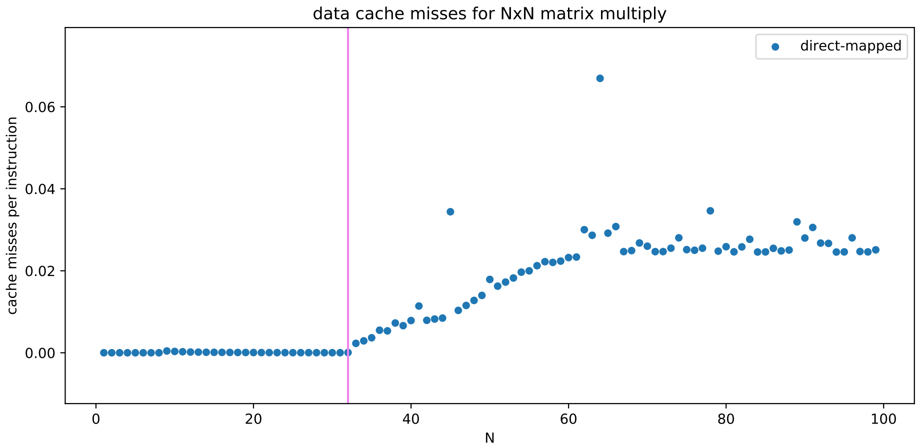
actual misses: BST lookups



(actual 32KB more complex data cache)

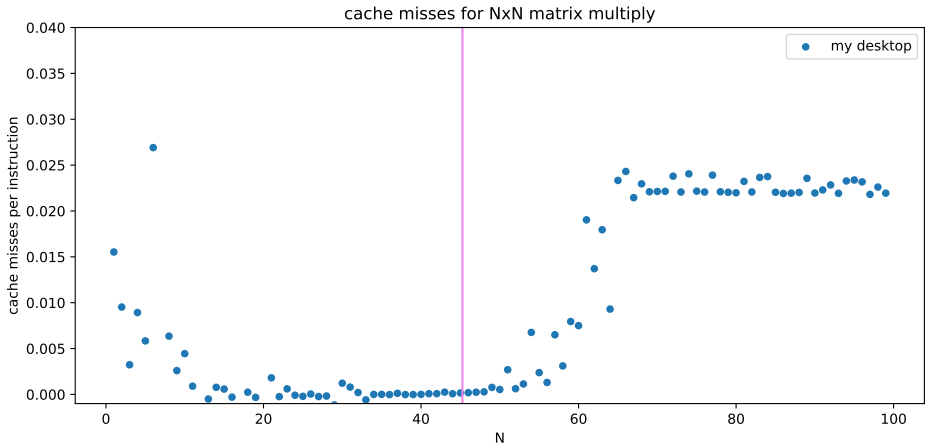
(only one set of measurements + other things on machine + excluding initial load)

simulated misses: matrix multiplies



(simulated 16KB direct-mapped data cache; excluding initial load)

actual misses: matrix multiplies



(actual 32KB more complex data cache; excluding matrix initial load)

(only one set of measurements + other things on machine)

misses with skipping

```
int array1[512]; int array2[512];
...
for (int i = 0; i < 512; i += 1)
    sum += array1[i] * array2[i];
}
```

Assume everything but `array1`, `array2` is kept in registers (and the compiler does not do anything funny).

About how many *data cache misses* on a 2KB direct-mapped cache with 16B cache blocks?
Hint: depends on relative placement of array1, array2

best/worst case

`array1[i]` and `array2[i]` always different sets:

- $=$ distance from array1 to array2 not multiple of # sets $\times$ bytes/set
- 2 misses every 4 `i`
- blocks of 4 array1[X] values loaded, then used 4 times before loading next block
- (and same for array2[X])

`array1[i]` and `array2[i]` same sets:

- $=$ distance from array1 to array2 is multiple of # sets $\times$ bytes/set
- 2 misses every `i`
- block of 4 array1[X] values loaded, one value used from it,
- then, block of 4 array2[X] values replaces it, one value used from it, …

worst case in practice?

two rows of matrix?

often sizeof(row) bytes apart

if the row size is multiple of number of sets $\times$ bytes per block, oops!

adding associativity

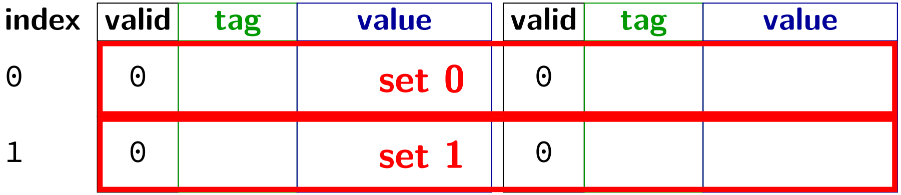
2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	0			0		
1	0			0		

multiple places to put values with same index
avoid misses from two active values using same set (“conflict misses”))

adding associativity

2-way set associative, 2 byte blocks, 2 sets



index	valid	tag	value	valid	tag	value
`0`	`0`		set 0	`0`		
`1`	`0`		set 1	`0`		

adding associativity

2-way set associative, 2 byte blocks, 2 sets

	way 0			way 1		
index	**valid**	**tag**	**value**	**valid**	**tag**	**value**
0	0			0		
1	0			0		

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	0			0		
1	0			0		

$m = 8$ bit addresses
$S = 2 = 2^s$ sets
$s = 1$ (set) index bits

$B = 2 = 2^b$ byte block size
$b = 1$ (block) offset bits
$t = m - (s + b) = 6$ tag bits

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	0		
1	0			0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	0		
1	0			0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	
01100001 (61)	
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
`0`	`1`	`000000`	`mem[0x00]` `mem[0x01]`	`0`		
`1`	`1`	`011000`	`mem[0x62]` `mem[0x63]`	`0`		

address (hex)	result
`00000000 (00)`	miss
`00000001 (01)`	hit
`01100011 (63)`	miss
`01100001 (61)`	
`01100010 (62)`	
`00000000 (00)`	
`01100100 (64)`	

tag index offset

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	
00000000 (00)	
01100100 (64)	

tag index offset

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	
01100100 (64)	

tag index offset

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	

tag index offset

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	result
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	miss

tag index offset

needs to replace block in set 0!

adding associativity

2-way set associative, 2 byte blocks, 2 sets

index	**valid**	**tag**	**value**	**valid**	**tag**	**value**
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]
1	1	011000	mem[0x62] mem[0x63]	0		

address (hex)	**result**
00000000 (00)	miss
00000001 (01)	hit
01100011 (63)	miss
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	miss

tag index offset

associative lookup possibilities

none of the blocks for the index are valid

none of the valid blocks for the index match the tag

- something else is stored there

one of the blocks for the index is valid and matches the tag

replacement policies

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value
0	1	`000000`	`mem[0x00]` `mem[0x01]`	1	`011000`	`mem[0x60]` `mem[0x61]`
1	1	`011000`	`mem[0x62]` `mem[0x63]`	0		

address (hex)	result
`000`	
`00000001 (01)`	hit
`01100011 (63)`	miss
`01100001 (61)`	miss
`01100010 (62)`	hit
`00000000 (00)`	hit
`01100100 (64)`	miss

how to decide where to insert 0x64?

replacement policies

2-way set associative, 2 byte blocks, 2 sets

index	valid	tag	value	valid	tag	value	LRU
0	1	000000	mem[0x00] mem[0x01]	1	011000	mem[0x60] mem[0x61]	1
1	1	011000	mem[0x62] mem[0x63]	0			1

address (hex)	result
00000000 (00)	mi
00000001 (01)	hit
01100011 (63)	mi
01100001 (61)	miss
01100010 (62)	hit
00000000 (00)	hit
01100100 (64)	miss

track which block was read least recently
updated on every access

example replacement policies

least recently used

- take advantage of temporal locality
- at least $\lceil \log_2(E!) \rceil$ bits per set for E-way cache
  - (need to store order of all blocks)

approximations of least recently used

- implementing least recently used is expensive
- really just need "avoid recently used" — much faster/simpler
- good approximations: E to $2E$ bits

first-in, first-out

- counter per set — where to replace next

(pseudo-)random

- no extra information!
- actually works pretty well in practice

associativity terminology

direct-mapped — one block per set

E-way set associative — E blocks per set

- E ways in the cache

fully associative — one set total (everything in one set)

Tag-Index-Offset formulas

m	memory addreses bits
E	number of blocks per set (“ways”)
$S = 2^s$	number of sets
s	(set) index bits
$B = 2^b$	block size
b	(block) offset bits
$t = m - (s + b)$	tag bits
$C = B \times S \times E$	cache size (excluding metadata)

arrays and cache misses (2)

```
int array[1024]; // 4KB array
int even_sum = 0, odd_sum = 0;
for (int i = 0; i < 1024; i += 2)
    even_sum += array[i + 0];
for (int i = 0; i < 1024; i += 2)
    odd_sum +=  array[i + 1];
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

How many *data cache misses* on initially empty 2KB direct-mapped cache with 16B cache blocks? Would a set-associative cache be better?

explanation

2-way, 2KB set associative cache, 16B blocks

4 offset bits, 6 index bits

so addresses multiples 2^{10} bytes apart differ only in tag bits

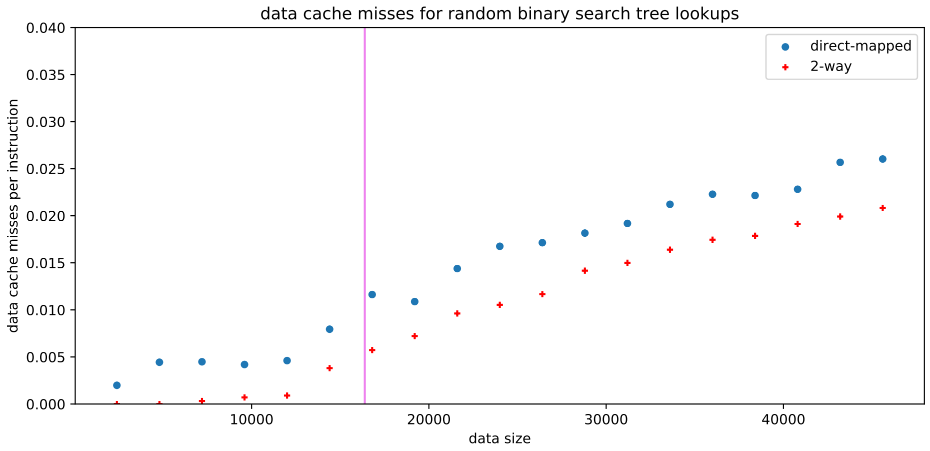
example: array[0→3], array[256→259], array[512→515], array[768→771]

those all use the same set

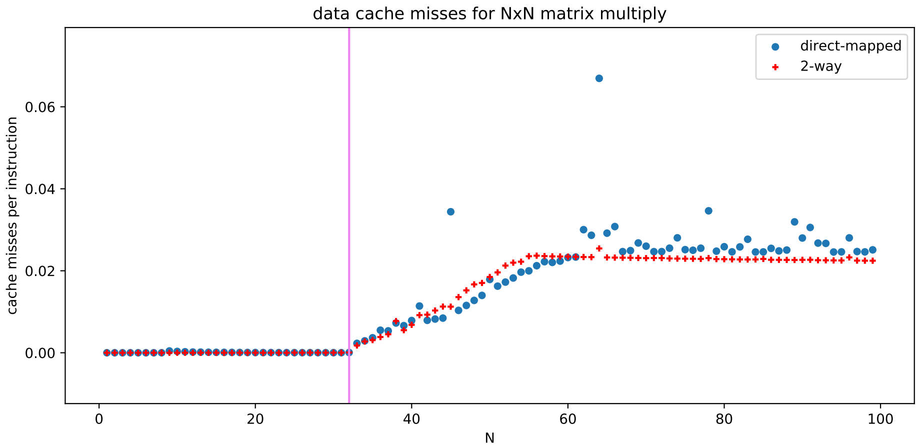
but sets only holds 2 things

all misses

simulated misses: BST lookups



simulated misses: matrix multiplies



handling writes

what about writing to the cache?

two decision points:

if the value is not in cache, do we add it?

- if yes: need to load rest of block
- if no: missing out on locality?

if value is in cache, when do we update next level?

- if immediately: extra writing
- if later: need to remember to do so

allocate on write?

processor writes less than whole cache block

block not yet in cache

two options:

write-allocate

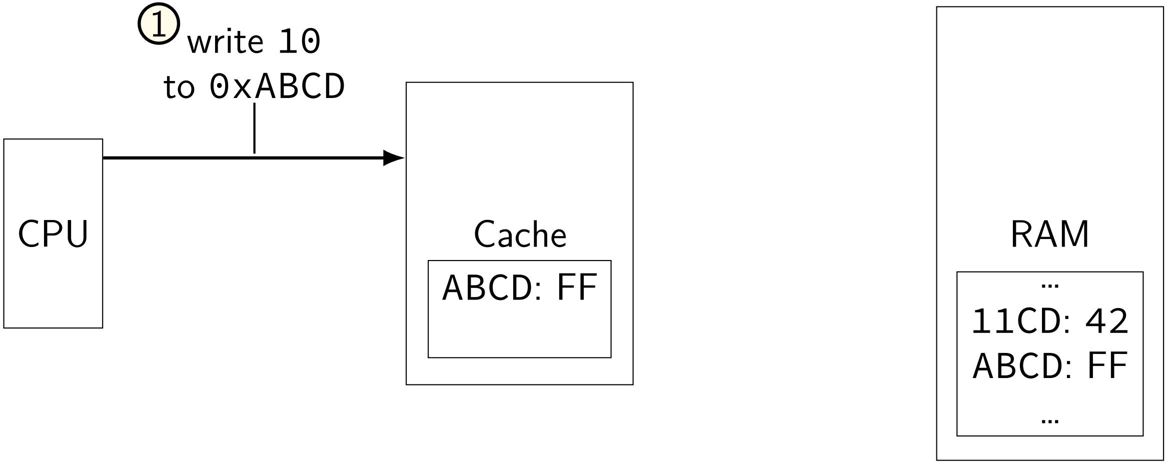
- fetch rest of cache block, replace written part
- (then follow write-through or write-back policy)

write-no-allocate

- don't use cache at all (send write to memory *instead*)
- guess: not read soon?

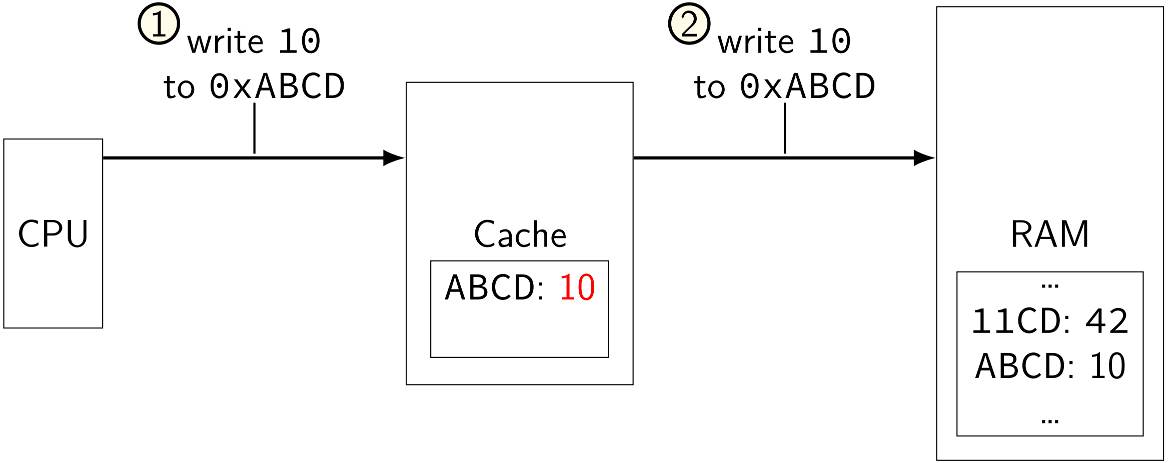
write-through v. write-back

option 1: write-through



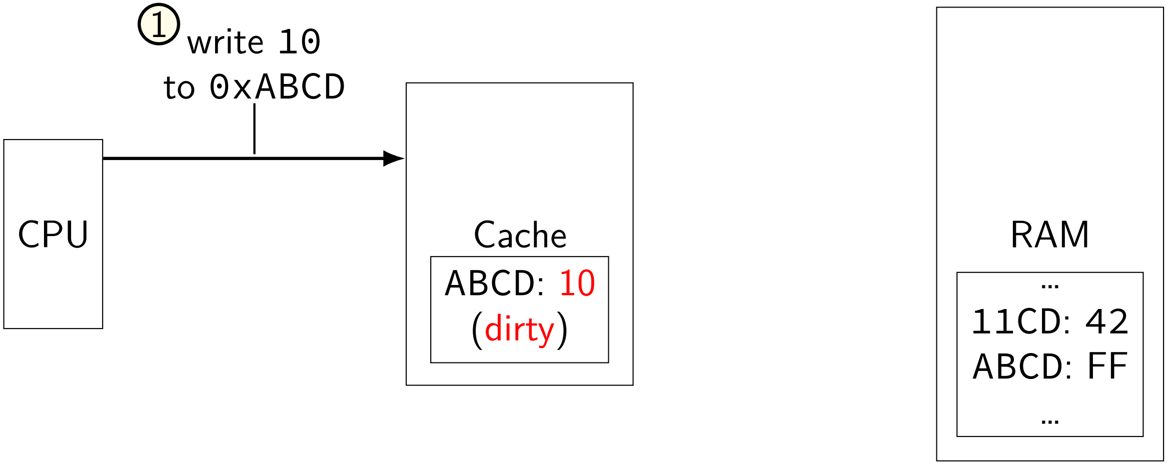
write-through v. write-back

option 1: write-through



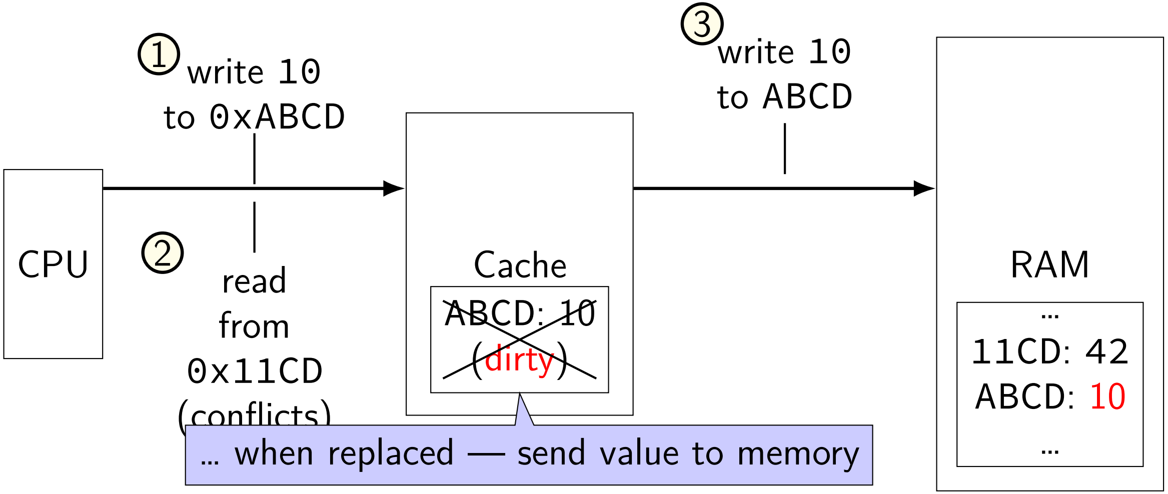
write-through v. write-back

option 2: write-back

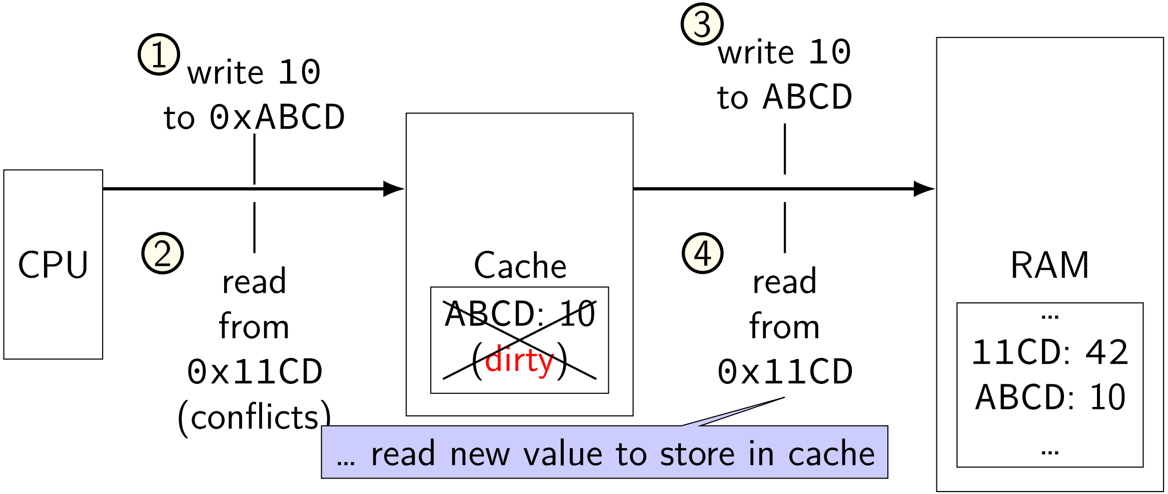


write-through v. write-back

option 2: write-back



write-through v. write-back



writeback policy

changed value!

2-way set associative, 4 byte blocks, 2 sets

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

$1 =$ dirty (different than memory)
needs to be written if evicted

write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address `0x04`?

index 0, tag 000001

write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	`000000`	`mem[0x00]` `mem[0x01]`	0	1	`011000`	`mem[0x60]`* `mem[0x61]`*	1	1
1	1	`011000`	`mem[0x62]` `mem[0x63]`	0	0				0

writing 0xFF into address `0x04`?

index 0, tag 000001

step 1: find least recently used block

write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	~~1~~	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address `0x04`?

index 0, tag 000001

step 1: find least recently used block

step 2: possibly writeback old block

write-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	000001	0xFF mem[0x05]	1	0
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address `0x04`?

index 0, tag 000001

step 1: find least recently used block

step 2: possibly writeback old block

step 3a: read in new block – to get mem[0x05]

step 3b: update LRU information

write-no-allocate + write-back

2-way set associative, LRU, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	000000	mem[0x00] mem[0x01]	0	1	011000	mem[0x60]* mem[0x61]*	1	1
1	1	011000	mem[0x62] mem[0x63]	0	0				0

writing 0xFF into address 0x04?

step 1: is it in cache yet?

step 2: no, just send it to memory

exercise (1)

2-way set associative, LRU, write-allocate, writeback

index	valid	tag	value	dirty	valid	tag	value	dirty	LRU
0	1	001100	mem[0x30] mem[0x31]	0	1	010000	mem[0x40]* mem[0x41]*	1	0
1	1	011000	mem[0x62] mem[0x63]	0	1	001100	mem[0x32]* mem[0x33]*	1	1

for each of the following accesses, performed alone, would it require (a) reading a value from memory (or next level of cache) and (b) writing a value to the memory (or next level of cache)?

writing 1 byte to 0x33
reading 1 byte from 0x52
reading 1 byte from 0x50

exercise (2)

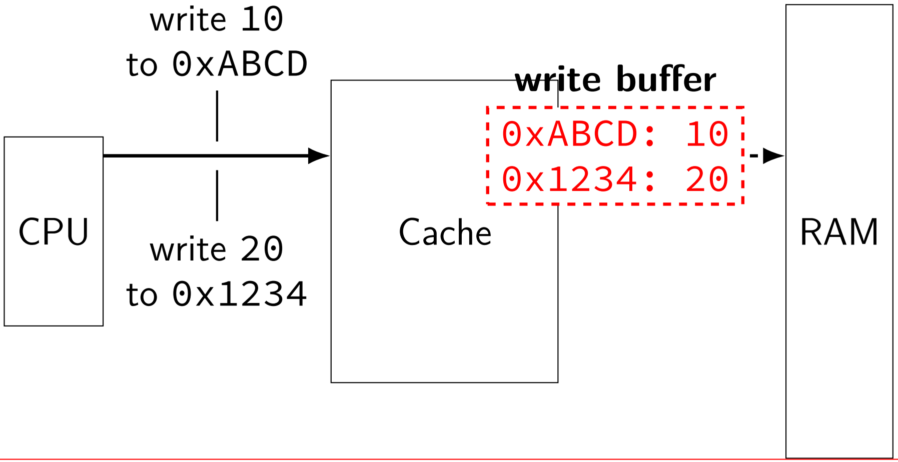
2-way set associative, LRU, write-no-allocate, write-through

index	valid	tag	value	valid	tag	value	LRU
0	1	001100	mem[0x30] mem[0x31]	1	010000	mem[0x40] mem[0x41]	0
1	1	011000	mem[0x62] mem[0x63]	1	001100	mem[0x32] mem[0x33]	1

for each of the following accesses, performed alone, would it require (a) reading a value from memory and (b) writing a value to the memory?

writing 1 byte to 0x33
reading 1 byte from 0x52
reading 1 byte from 0x50

fast writes



write appears to complete immediately when placed in buffer
memory can be much slower

cache miss types

common to categorize misses:

- roughly "cause" of miss assuming cache block size fixed

compulsory (or *cold*) — first time accessing something

- adding more sets or blocks/set wouldn't change

conflict — sets aren't big/flexible enough

- a fully-associtive (1-set) cache of the same size would have done better

capacity — cache was not big enough

coherence — from sync'ing cache with other caches

- only issue with multiple cores

making any cache look bad

1. access enough blocks, to fill the cache
2. access an additional block, replacing something
3. access last block replaced
4. access last block replaced
5. access last block replaced

…

but — typical real programs have locality

cache optimizations

(assuming typical locality + keeping cache size constant if possible...)

	miss rate	hit time	miss penalty
increase cache size	better	worse	—
increase associativity	better	worse	worse?
increase block size	depends	worse	worse
add secondary cache	—	—	better
write-allocate	better	—	?
writeback	—	—	?
LRU replacement	better	?	worse?
prefetching	better	—	—

prefetching = guess what program will use, access in advance

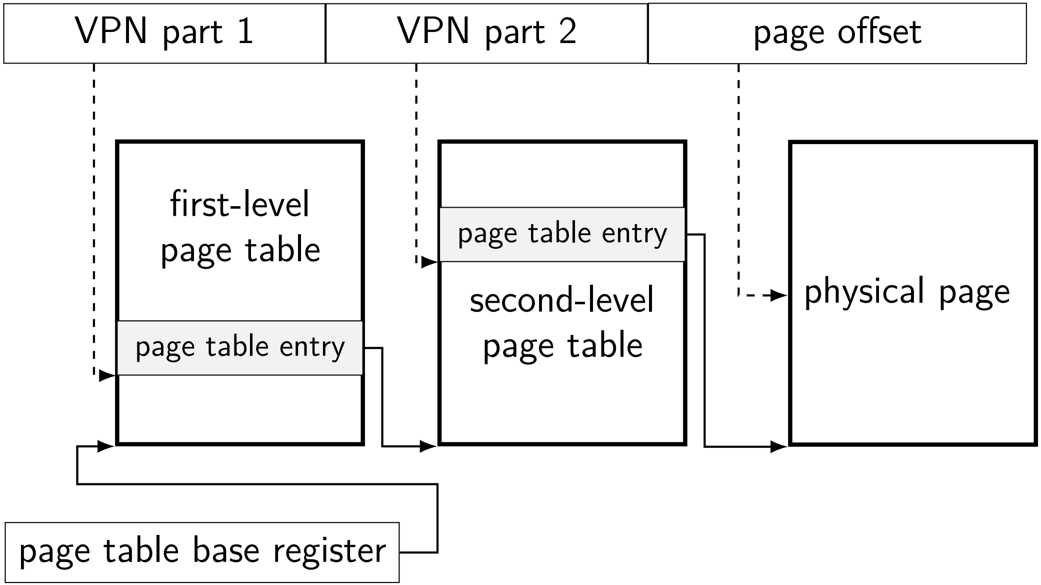
$$\text{average time} = \text{hit time} + \text{miss rate} \times \text{miss penalty}$$

cache optimizations by miss type

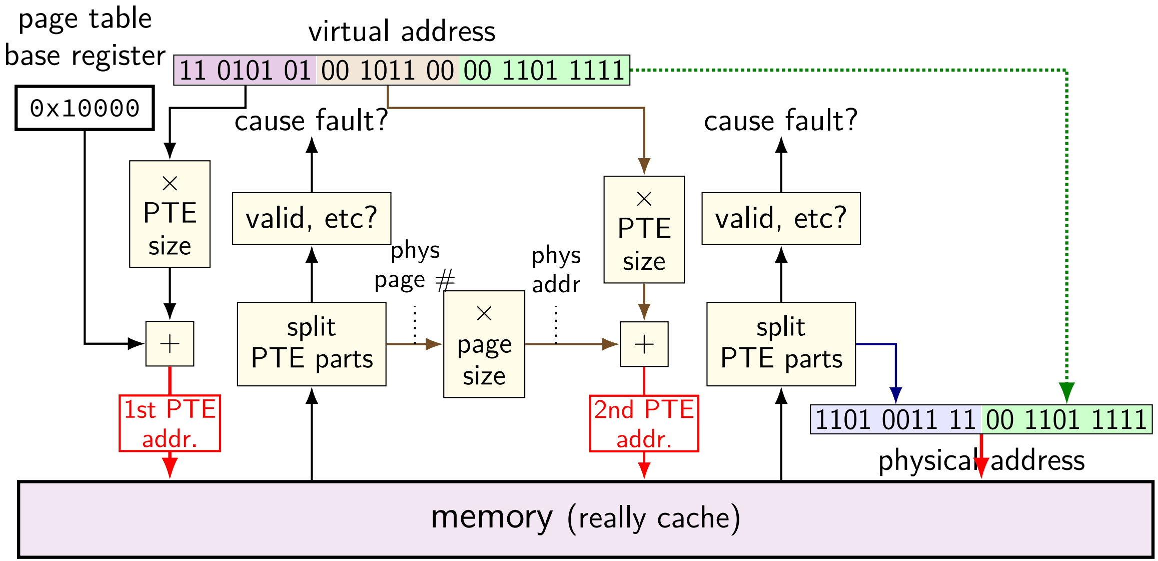
(assuming other listed parameters remain constant)

	capacity	conflict	compulsory
increase cache size	fewer misses	fewer misses	—
increase associativity	—	fewer misses	—
increase block size	more misses?	more misses?	fewer misses
LRU replacement	—	fewer misses	—
prefetching	—	—	fewer misses

another view



two-level page table lookup



cache accesses and multi-level PTs

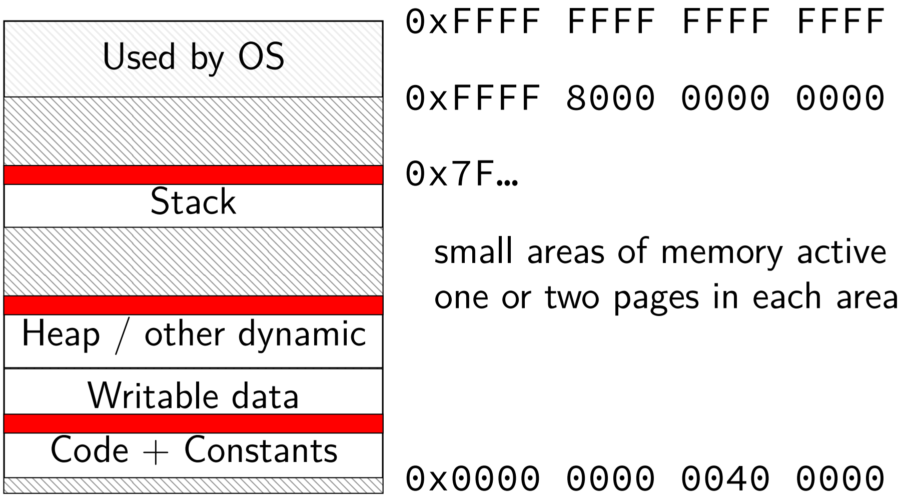
four-level page tables — five cache accesses per program memory access

L1 cache hits — typically a couple cycles each?

so add 8 cycles to each program memory access?

not acceptable

program memory active sets



small areas of memory active at a time

one or two pages in each area?

page table entries and locality

page table entries have excellent temporal locality

typically one or two pages of the stack active

typically one or two pages of code active

typically one or two pages of heap/globals active

each page contains whole functions, arrays, stack frames, etc.

page table entries and locality

page table entries have excellent temporal locality

typically one or two pages of the stack active

typically one or two pages of code active

typically one or two pages of heap/globals active

each page contains whole functions, arrays, stack frames, etc.

needed page table entries are very small

page table entry cache

caled a **TLB** (translation lookaside buffer)

very small cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

page table entry cache

caled a **TLB** (translation lookaside buffer)

very small cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

only caches the page table lookup itself
(generally) just entries from the last-level page tables

page table entry cache

caled a **TLB** (translation lookaside buffer)

very small cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

not much spatial locality between page table entries
(they're used for kilobytes of data already)
(and if spatial locality, maybe use larger page size?)

page table entry cache

caled a **TLB** (translation lookaside buffer)

very small cache of page table entries

L1 cache	TLB
physical addresses	virtual page numbers
bytes from memory	page table entries
tens of bytes per block	one page table entry per block
usually thousands of blocks	usually tens of entries

few active page table entries at a time
enables highly associative cache designs

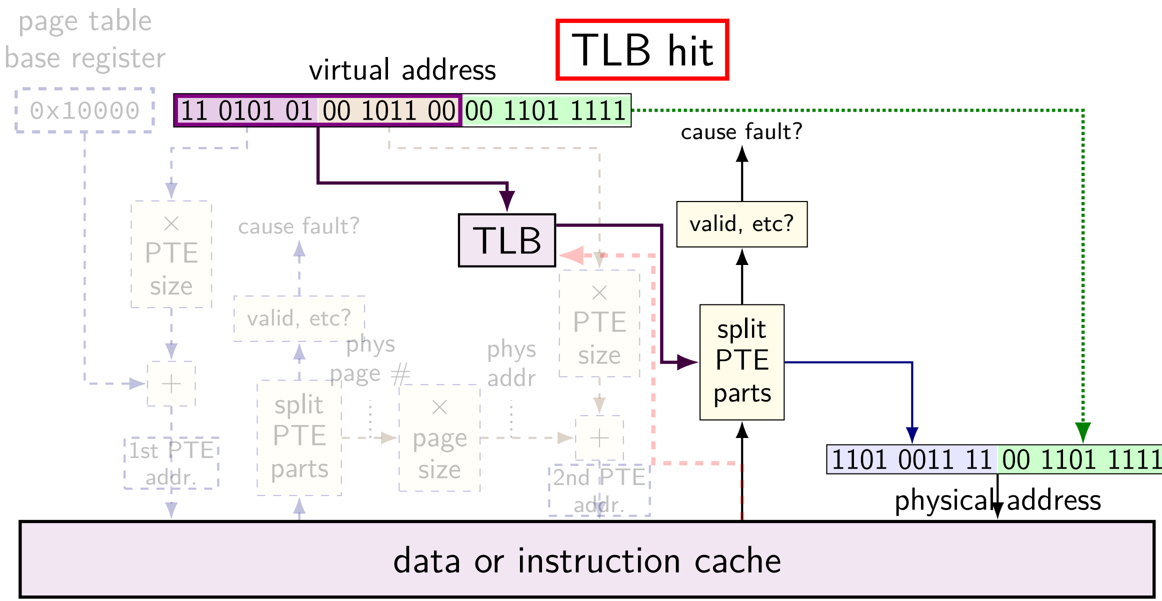
TLB and multi-level page tables

TLB caches valid last-level page table entries

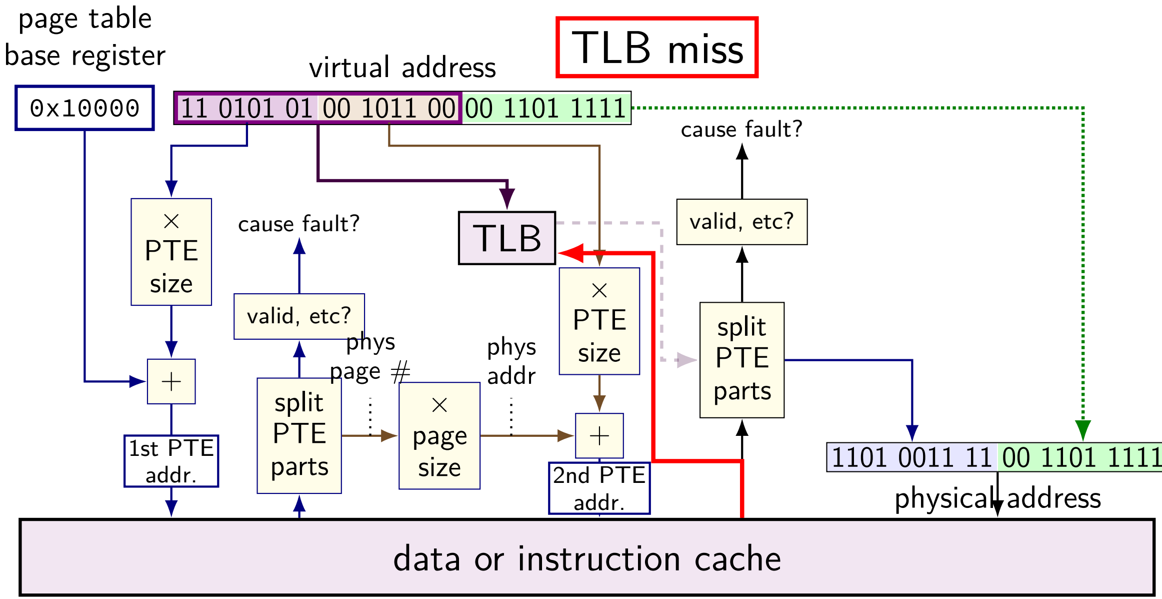
doesn't matter which last-level page table

means TLB output can be used directly to form address

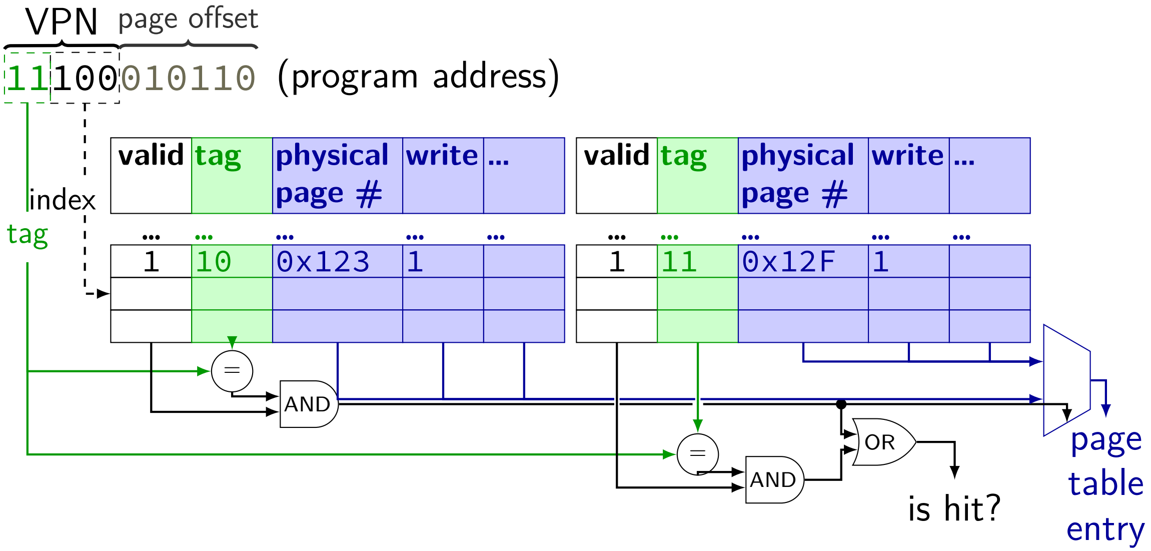
TLB and two-level lookup



TLB and two-level lookup



TLB organization (2-way set associative)



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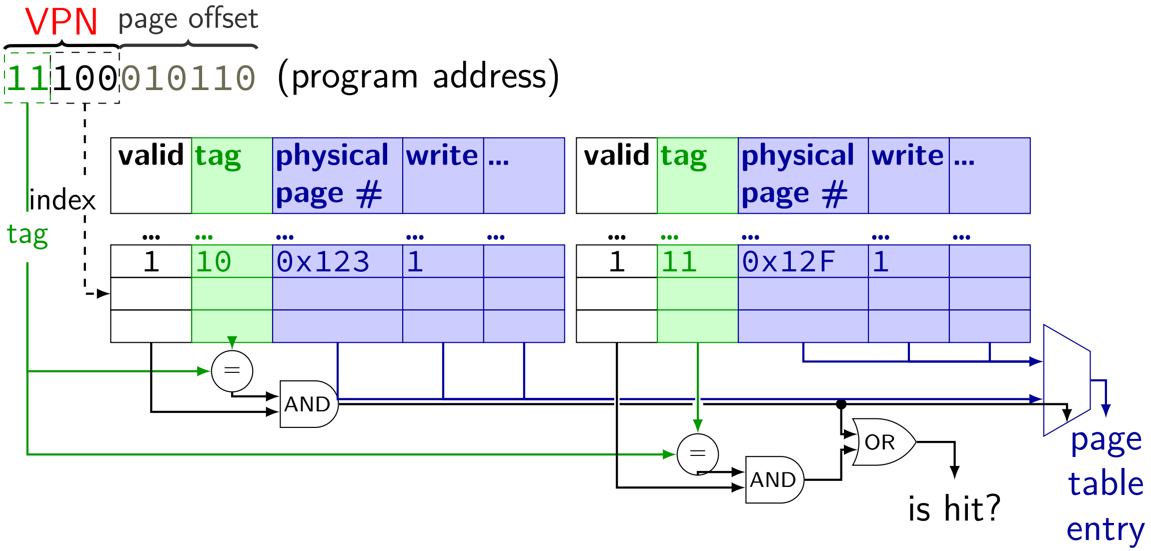

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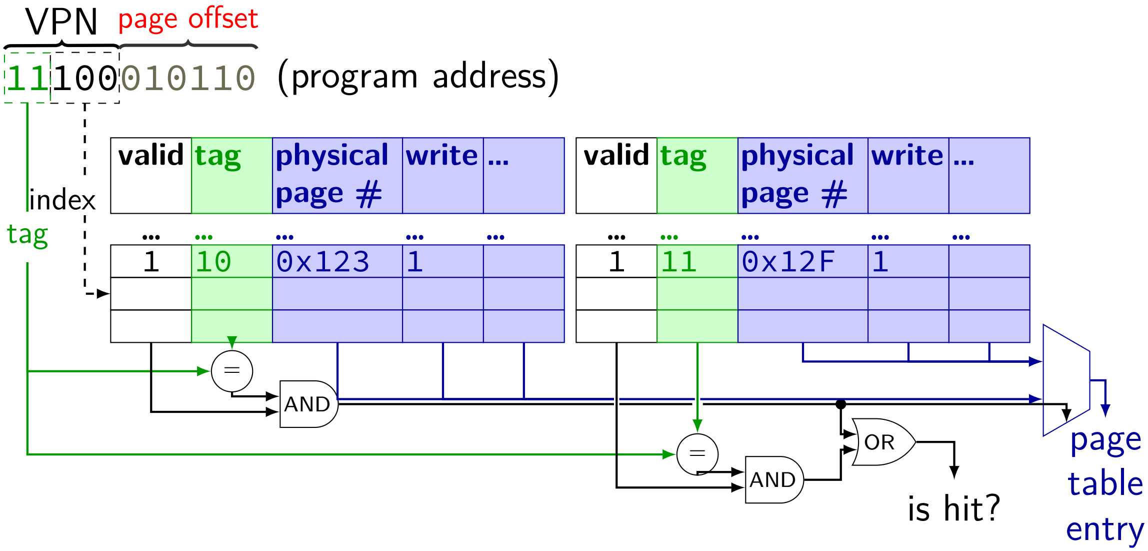

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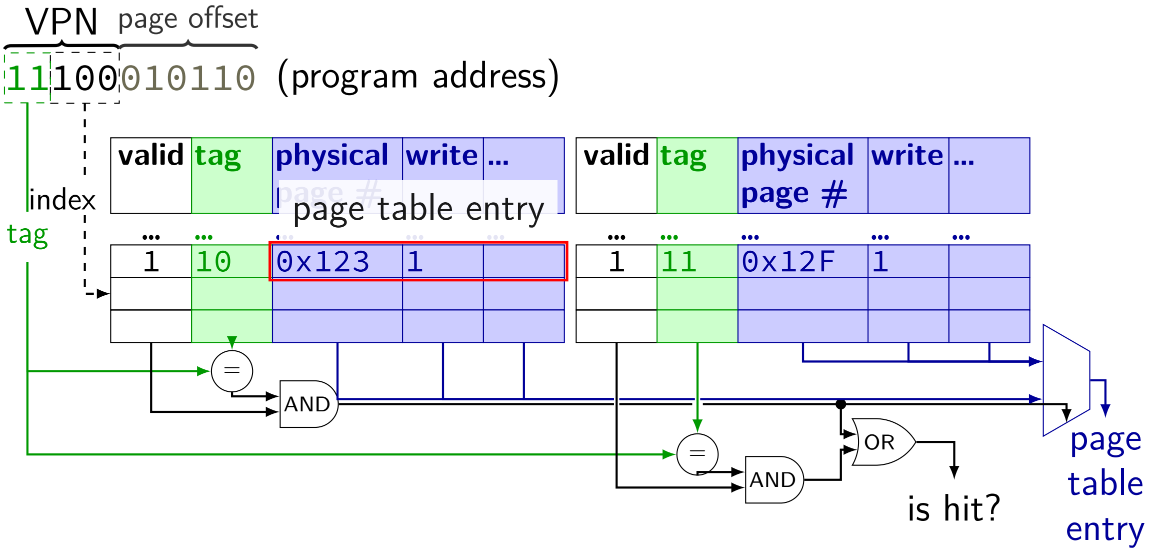
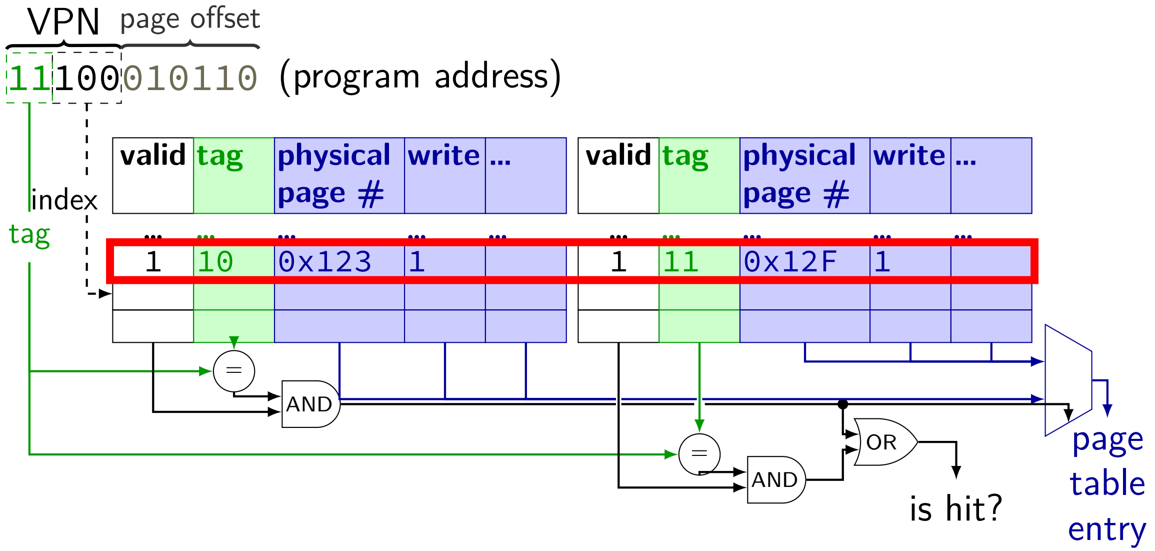


TLB organization (2-way set associative)



exercise: TLB access pattern (setup)

4-entry, 2-way TLB, LRU replacement policy, initially empty

4096 byte pages

how many index bits?

TLB index of virtual address 0x12345?

exercise: TLB access pattern

4-entry, 2-way TLB, LRU replacement policy, initially empty

4096 byte pages

type	virtual	physical
`read`	`0x440030`	`0x554030`
`write`	`0x440034`	`0x554034`
`read`	`0x7FFFE008`	`0x556008`
`read`	`0x7FFFE000`	`0x556000`
`read`	`0x7FFFDFF8`	`0x5F8FF8`
`read`	`0x664080`	`0x5F9080`
`read`	`0x440038`	`0x554038`
`write`	`0x7FFFDFF0`	`0x5F8FF0`

which are TLB hits? which are TLB misses? final contents of TLB?

backup slides

arrays and cache misses (3)

```
int sum; int array[1024]; // 4KB array
for (int i = 8; i < 1016; i += 1) {
    int local_sum = 0;
    for (int j = i - 8; j < i + 8; j += 1) {
        local_sum += array[i] * (j - i);
    }
    sum += (local_sum - array[i]);
}
```

Assume everything but `array` is kept in registers (and the compiler does not do anything funny).

How many *data cache misses* on initially empty 2KB direct-mapped cache with 16B cache blocks?