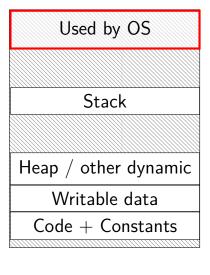
program memory

Used by OS
Stack
Heap / other dynamic
Writable data
Code + Constants

0xffff Ffff Ffff Ffff
0xffff 8000 0000 0000
0x7f...

0x0000 0000 0040 0000

program memory

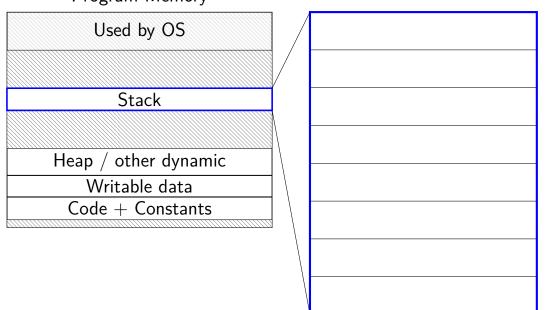


0xFFFF FFFF FFFF
0xFFFF 8000 0000 0000
0x7F...

0x0000 0000 0040 0000

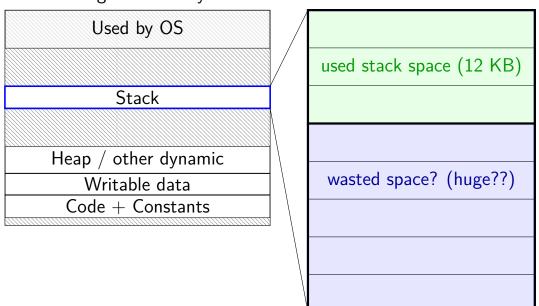
space on demand

Program Memory



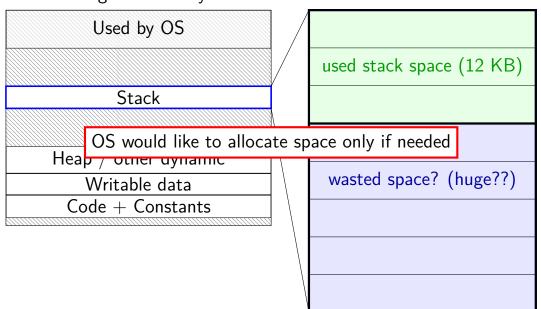
space on demand

Program Memory



space on demand

Program Memory



%rsp = 0x7FFFC000

```
...
// requires more stack space
A: pushq %rbx

B: movq 8(%rcx), %rbx
C: addq %rbx, %rax
...
```

VPN	valid?	physical
VIIN	valiu:	page
•••	•••	•••
0x7FFFB	0	
0x7FFFC	1	0x200DF
0x7FFFD	1	0x12340
0x7FFFE	1	0x12347
0x7FFFF	1	0x12345
•••	•••	•••

%rsp = 0x7FFFC000

```
// requires more stack space
A: pushq %rbx
page fault!
B: movq 8(%rcx), %rbx
C: addq %rbx, %rax
...
```

VPN	valid?	physical page
VIIV	valiu:	page
•••	•••	•••
0x7FFFB	0	
0x7FFFC	1	0x200DF
0x7FFFD	1	0x12340
0x7FFFE	1	0x12347
0x7FFFF	1	0x12345
•••	•••	•••

pushq triggers exception hardware says "accessing address 0x7FFBFF8" OS looks up what's should be there — "stack"

%rsp = 0x7FFFC000

```
// requires more stack space
A: pushq %rbx restarted

B: movq 8(%rcx), %rbx
C: addq %rbx, %rax
...
```

VPN	valid?	physical page
VEIN	valiu!	page
•••	•••	•••
0x7FFFB	1	0x200D8
0x7FFFC	1	0x200DF
0x7FFFD	1	0x12340
0x7FFFE	1	0x12347
0x7FFFF	1	0x12345
•••	•••	•••

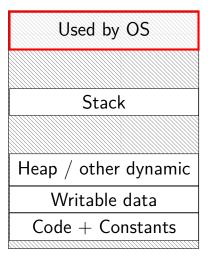
in exception handler, OS allocates more stack space OS updates the page table then returns to retry the instruction

note: the space doesn't have to be initially empty

only change: load from file, etc. instead of allocating empty page

loading program can be merely creating empty page table everything else can be handled in response to page faults no time/space spent loading/allocating unneeded space

program memory



0xFFFF FFFF FFFF

0xFFFF 8000 0000 0000

0x7F...

0x0000 0000 0040 0000

system calls, I/O events, etc. run OS code in kernel mode

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where in memory is this OS code?

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probably have a page table entry pointing to it marked not accessible in user mode

system calls, I/O events, etc. run OS code in kernel mode

where in memory is this OS code?

probably have a page table entry pointing to it marked not accessible in user mode

code better not be modified by user program otherwise: uncontrolled way to "escape" user mode

mmap

```
Linux/Unix has a function to "map" a file to memory
int file = open("somefile.dat", O_RDWR);
    // data is region of memory that represents file
char *data = mmap(..., file, 0);
   // read byte 6 from somefile.dat
char seventh_char = data[6];
   // modifies byte 100 of somefile.dat
data[100] = 'x';
    // can continue to use 'data' like an array
```

Linux maps: list of maps

```
$ cat /proc/self/maps
00400000-0040b000 r-xp 00000000 08:01 48328831
                                                         /bin/cat
0060a000-0060b000 r-p 0000a000 08:01 48328831
                                                         /bin/cat
0060b000-0060c000 rw-p 0000b000 08:01 48328831
                                                         /bin/cat
01974000-01995000 rw-p 00000000 00:00 0
                                                         [heap]
7f60c718b000-7f60c7490000 r-p 00000000 08:01 77483660
                                                         /usr/lib/locale/locale—archive
7f60c7490000-7f60c764e000 r-xp 00000000 08:01 96659129
                                                         /lib/x86_64-linux-gnu/libc-2.1
7f60c764e000-7f60c784e000 ----p 001be000 08:01 96659129
                                                         /lib/x86_64-linux-gnu/libc-2.1
7f60c784e000-7f60c7852000 r-p 001be000 08:01 96659129
                                                         /lib/x86_64-linux-gnu/libc-2.1
7f60c7852000-7f60c7854000 rw-p 001c2000 08:01 96659129
                                                         /lib/x86 64-linux-gnu/libc-2.1
7f60c7854000-7f60c7859000 rw-p 00000000 00:00 0
7f60c7859000-7f60c787c000 r-xp 00000000 08:01 96659109
                                                         /lib/x86_64-linux-gnu/ld-2.19.
7f60c7a39000-7f60c7a3b000 rw-p 00000000 00:00 0
7f60c7a7a000-7f60c7a7b000 rw-p 00000000 00:00 0
7f60c7a7b000-7f60c7a7c000 r-p 00022000 08:01 96659109
                                                         /lib/x86_64-linux-gnu/ld-2.19.
7f60c7a7c000-7f60c7a7d000 rw-p 00023000 08:01 96659109
                                                         /lib/x86_64-linux-gnu/ld-2.19.s
7f60c7a7d000-7f60c7a7e000 rw-p 00000000 00:00 0
7ffc5d2b2000-7ffc5d2d3000 rw-p 00000000 00:00 0
                                                         [stack]
7ffc5d3b0000-7ffc5d3b3000 r—p 00000000 00:00 0
                                                         [vvar]
7ffc5d3b3000-7ffc5d3b5000 r-xp 00000000 00:00 0
                                                         vdsol
fffffffff600000-ffffffffff601000 r-xp 00000000 00:00 0
                                                         [vsyscall]
```

Linux maps: list of maps

```
$ cat /proc/self/maps
00400000-0040b000 r-xp 00000000 08:01 48328831
                                                         /bin/cat
0060a000-0060b000 r-p 0000a000 08:01 48328831
                                                         /bin/cat
0060b000-0060c000 rw-p 0000b000 08:01 48328831
                                                         /bin/cat
01974000 - 01995000 \text{ rw-p} 00000000 00:00 0
                                                         [heap]
7f60c718b000_7f60c7490000
                                                         <u>usr/lib/locale/lo</u>cale—archive
7f60c74900 OS tracks list of struct vm_area_struct with:
                                                                          gnu/libc-2.1
7f60c764e0
                                                                          gnu/libc-2.1
          (shown in this output):
7f60c784e0
                                                                          gnu/libc-2.1
7f60c78520
                                                                          gnu/libc-2.1
             virtual address start, end
7f60c78540
                                                                          gnu/ld-2.19.s
7f60c78590
             permissions
7f60c7a390
7f60c7a7a0
             offset in backing file (if any)
7f60c7a7b0
                                                                          gnu/ld-2.19.s
7f60c7a7c0
             pointer to backing file (if any)
                                                                          gnu/ld-2.19.s
7f60c7a7d0
7ffc5d2b20
7ffc5d3b00
           (not shown):
7ffc5d3b30
ffffffffff
             info about sharing of non-file data
```

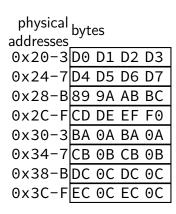
exercise setup

5-bit virtual addresses, 6-bit physical addresses, 8-byte pages

page table

virtual	valid?	physical
page #	valiu!	page #
00	1	010
01	1	111
10	0	000
11	1	000

physical addresses	byt	es		
0x00-3				
0x04-7	44	55	66	77
0x08-B	88	99	AA	ВВ
0x0C-F	C	DD	EE	FF
0x10-3	1A	2A	ЗА	4A
0x14-7	1В	2B	3B	4B
0x18-B				
0x1C-F	1C	2C	3C	4C



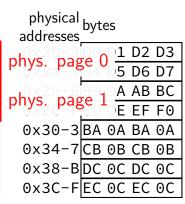
exercise setup

5-bit virtual addresses, 6-bit physical addresses, 8-byte pages

page table

virtual	valid?	physical
page #	valiu!	page #
00	1	010
01	1	111
10	0	000
11	1	000

physical addresses	bytes
	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C



5-bit virtual addresses, 6-bit physical addresses, 8-byte pages

```
(virtual addresses) 0x18 = ???; 0x03 = ???; 0x0A = ???; 0x13 = ???
```

page table

```
page # valid?
           010
    001
    01
           111
           000
    10
    11
           000
```

physical addresses	bytes
	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	byt	es		
0x20-3	D0	D1	D2	D3
0x24-7				
0x28-B 0x2C-F	89	9A	ΑB	ВС
0x2C-F	CD	DE	EF	F0
0x30-3	ВА	0A	ВА	0Α
0x34-7	СВ	0B	СВ	0B
0x38-B	DC	0C	DC	0C
0x3C-F	EC	0C	EC	0C

5-bit virtual addresses, 6-bit physical addresses, 8-byte pages

```
(virtual addresses) 0x18 = ; 0x03 = ???; 0x0A = ???; 0x13 = ???
```

page table

```
page # valid? _
    00
            010
    01
            111
            000
    10
            000
    11
```

physical addresses	bytes
addresses	
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
	CC DD EE FF
0x10-3	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical bytes addresses 0x20-3 D0 D1 D2 D3 0x24-7 D4 D5 D6 D7 0x28-B|89 9A AB BC 0x2C-FCD DE EF F0 0x30-3|BA 0A BA 0A 0x34-7 CB 0B CB 0B 0x38-BDC 0C DC 0C 0x3C-FEC 0C EC 0C

5-bit virtual addresses, 6-bit physical addresses, 8-byte pages

```
(virtual addresses) 0x18 = ; 0x03 = ; 0x0A = ???; 0x13 = ??? page table
```

```
virtual physical page # valid? page # 00 1 010 010 01 111 110 0 000 11 1 1000
```

physical addresses	bytes
	00 11 22 33
0x04-7	44 55 66 77
	88 99 AA BB
0x0C-F	CC DD EE FF
	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	byt	es		
0x20-3	D0	D1		
0x24-7				
0x28-B				
0x2C-F	CD	DE	EF	F0
0x30-3	ВА	0A	ВА	0A
0x34-7	СВ	0B	СВ	0B
0x38-B				
0x3C-F	EC	0C	EC	0C

5-bit virtual addresses, 6-bit physical addresses, 8-byte pages

```
(virtual addresses) 0x18 = ; 0x03 = ; 0x0A = ; 0x13 = ??? page table
```

```
virtual physical page # valid? page # page # 00 1 010 011 111 10 0 000 11 1 1 1 000
```

physical addresses	bytes
	00 11 22 33
0x04-7	44 55 66 77
	88 99 AA BB
0x0C-F	CC DD EE FF
	1A 2A 3A 4A
0x14-7	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical addresses	byt	es		
0x20-3	D0	D1		
0x24-7				
0x28-B	89	9A	ΑB	ВС
0x2C-F	CD	DE	EF	F0
0x30-3	ВА	0A	ВА	0A
0x34-7	СВ	0B	CB	0B
0x38-B	DC	0C	DC	0C
0x3C-F	EC	0C	EC	0C

5-bit virtual addresses, 6-bit physical addresses, 8-byte pages

```
(virtual addresses) 0x18 = ; 0x03 = ; 0x0A = ; 0x13 = page table
```

```
virtual physical page # valid? page # 00 1 010 010 010 1111 10 0 000 11 1 1000
```

physical addresses	bytes
addresses	5,000
0x00-3	00 11 22 33
0x04-7	44 55 66 77
0x08-B	88 99 AA BB
0x0C-F	CC DD EE FF
0x10-3	1A 2A 3A 4A
	1B 2B 3B 4B
0x18-B	1C 2C 3C 4C
0x1C-F	1C 2C 3C 4C

physical bytes addresses 0x20-3 D0 D1 D2 D3 0x24-7 D4 D5 D6 D7 0x28-B|89 9A AB BC 0x2C-FCD DE EF F0 0x30-3|BA 0A BA 0A 0x34-7 CB 0B CB 0B 0x38-BDC 0C DC 0C 0x3C-FEC 0C EC 0C

do we really need a complete copy?

bash	new copy of bash
Used by OS	Used by OS
Stack	Stack
Heap / other dynamic	Heap / other dynamic
Writable data	Writable data
Code + Constants	Code + Constants

do we really need a complete copy?

bash	new copy of bash
Used by OS	Used by OS
Stack	Stack
Heap / other dynamic	Heap / other dynamic
Writable data	Writable data
Code + Constants	Code + Constants

shared as read-only

do we really need a complete copy?

bash	new copy of bash
Used by OS	Used by OS
Stack	Stack
Heap / other dynamic	Heap $/$ other dynamic
Writable data	Writable data
Code + Constants can't be	shared? Code + Constants

trick for extra sharing

```
sharing writeable data is fine — until either process modifies it example: default value of global variables might typically not change (or OS might have preloaded executable's data anyways)
```

can we detect modifications?

trick for extra sharing

```
sharing writeable data is fine — until either process modifies it example: default value of global variables might typically not change (or OS might have preloaded executable's data anyways)
```

can we detect modifications?

trick: tell CPU (via page table) shared part is read-only processor will trigger a fault when it's written

VPN

valid? write?

•••

0x00601 0x00602 0x00603 0x00604 0x00605

		Page
•••	•••	•••
1	1	0x12345
1	1	0x12347
1	1	0x12340
1	1	0x200DF
1	1	0x200AF
•••	•••	•••

VPN	
•••	
0x00601	
0x00602	
0x00603	
0x00604	
0x00605	
•••	

valid? write?		
vallu	write:	page
•••	•••	•••
1	0	0x12345
1	0	0x12347
1	0	0x12340
1	0	0x200DF
1	0	0x200AF
•••	•••	•••

•••
0x00601
0x00602
0x00603
0x00604
0x00605

VPN

valid?	write?	physical page

•••	•••	•••
1	0	0x12345
1	0	0x12347
1	0	0x12340
1	0	0x200DF
1	0	0x200AF
•••	•••	•••

copy operation actually duplicates page table both processes share all physical pages but marks pages in both copies as read-only

			•				
VPN	valid?	write?	physical page	VPN	valid?	write?	physical page
•••	•••	•••	•••	•••	•••	•••	•••
0x00601	1	0	0x12345	0x00601	1	0	0x1234
0x00602	1	0	0x12347	0x00602	1	0	0x1234
0x00603	1	0	0x12340	0x00603	1	0	0x1234
0x00604	1	0	0x200DF	0x00604	1	0	0x200D
0x00605	1	0	0x200AF	0x00605	1	0	0x200A
•••	•••	•••	•••	•••	•••	•••	•••

when either process tries to write read-only page triggers a fault — OS actually copies the page

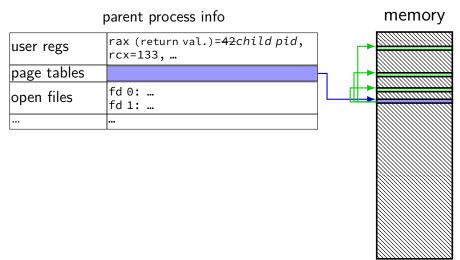
0x12345

0x200AF

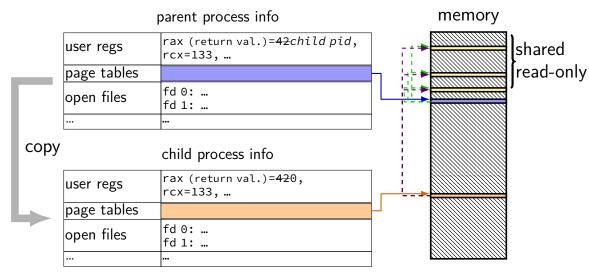
VPN	valid? write? page		physical	VPN	valid?	valid? write?			
VIIN	valiu:	WIILE	page	V I I I I	valiu:	WIILE:	page		
•••	•••	•••	•••	•••	•••	•••	•••		
0x00601	1	0	0x12345	0x00601	1	0	0x12345		
0x00602	1	0	0x12347	0x00602	1	0	0x12347		
0x00603	1	0	0x12340	0x00603	1	0	0x12340		
0x00604	1	0	0x200DF	0x00604	1	0	0x200DF		
0x00605	1	0	0x200AF	0x00605	1	1	0x300FD		
•••	•••	•••	•••	•••	•••	•••	•••		

after allocating a copy, OS reruns the write instruction

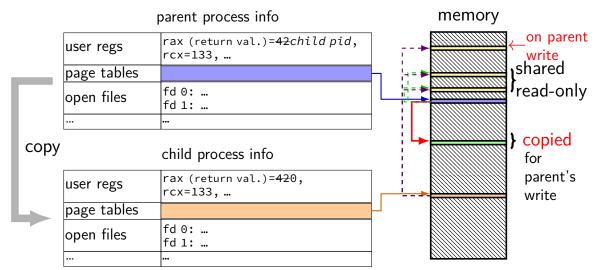
fork (w/ copy-on-write, if parent writes first)



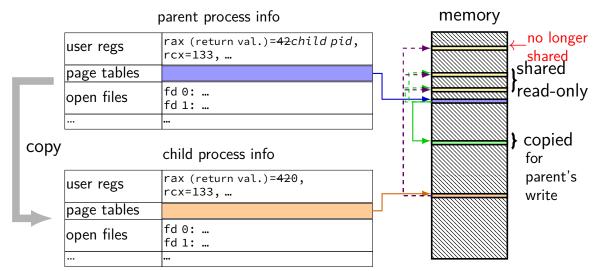
fork (w/ copy-on-write, if parent writes first)



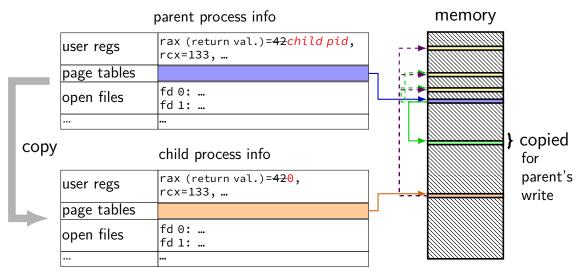
fork (w/ copy-on-write, if parent writes first)



fork (w/ copy-on-write, if parent writes first)



fork (w/ copy-on-write, if parent writes first)



page tricks generally

deliberately make program trigger page/protection fault

but don't assume page/protection fault is an error

have seperate data structures represent logically allocated memory e.g. "addresses 0x7FFF8000 to 0x7FFFFFFFF are the stack"

page table is for the hardware and not the OS

example page table tricks

allocating space on demand

loading code/data from files on disk on demand

saving data temporarily to disk, reloading to memory on demand "swapping"

stopping in a debugger when a variable is modified detecting whether memory was read/written recently sharing memory between programs on two different machines

"copy-on-write" (later)

hardware help for page table tricks

information about the address causing the fault
e.g. special register with memory address accessed
harder alternative: OS disassembles instruction, look at registers

(by default) rerun faulting instruction when returning from exception

precise exceptions: no side effects from faulting instruction or after e.g. pushq that caused did not change %rsp before fault e.g. can't notice if instructions were executed in parallel

where can processor store megabytes of page tables? in memory

page table entry layout (chosen by processor)

valid (bit 15)|physical page # (bits 4–14)|other bits and/or unused (bit 0-3)|

where can processor store megabytes of page tables? in memory

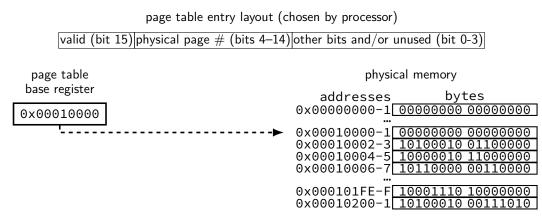
page table entry layout (chosen by processor)

valid (bit 15) physical page # (bits 4–14) other bits and/or unused (bit 0-3)

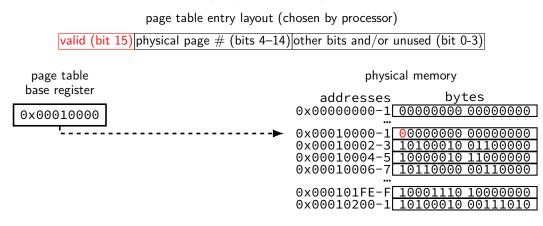
page table base register

0x00010000

where can processor store megabytes of page tables? in memory



where can processor store megabytes of page tables? in memory



where can processor store megabytes of page tables? in memory

page table entry layout (chosen by processor) valid (bit 15) physical page # (bits 4–14) other bits and/or unused (bit 0-3) physical memory page table base register addresses bytes 0x00000000-1 00000000 00000000 0x00010000 0x00010000-1 00000000 $0 \times 00010002 - 3 10100010$ $0 \times 00010004 - 5\Gamma$ 0x00010006-7 0x000101FE-F 10001110 0x00010200-1 10100010 0011101

where can processor store megabytes of page tables? in memory

page table entry layout (chosen by processor) valid (bit $\overline{15}$) physical page # (bits 4–14) other bits and/or unused (bit 0-3) physical memory page table base register addresses bytes 0x00000000-1 00000000 00000000 0x00010000 0x00010000-1 00000000 00000000 $0 \times 00010002 - 3 10100010$ $0 \times 00010004 - 5\Gamma$ 10000010 0x00010006-7 10110000 0x000101FE-F 10001110 0x00010200-1 10100010 0011101

where can processor store megabytes of page tables? in memory

valid (bit 15) physical page # (bits 4–14) other bits and/or unused (bit 0-3) page table physical memory base register addresses bytes 0x00000000-1 00000000 00000000 0x00010000 0x00010000-1 00000000 00000000 $0 \times 00010002 - 3$ page table (logically) 0x00010004-5 10000010 0x00010006-7 10110000 00110000 virtual page # valid? physical page # 0000 0000 0000 0000 0x000101FE-F 10001110 0000 0001 0x00010200-1 10100010 00111010 0000 0010 0000 0011 0000 0011 1111 1111 00 1110 1000

page table entry layout (chosen by processor)

where can processor store megabytes of page tables? in memory

valid (bit 15) physical page # (bits 4–14) other bits and/or unused (bit 0-3) page table physical memory base register addresses bytes 0x00000000-1 00000000 00000000 0x00010000 0x00010000-1 00000000 00000000 0x00010002-3 page table (logically) 0x00010004-5 0000010 0x00010006-7 0110000 00110000 virtual page # valid? physical page # 0000 0000 0000 0000 0x000101FE-F 10001110 0000 0001 0x00010200-1 10100010 00111010 0000 0010 0000 0011 0000 0011 1111 1111 00 1110 1000

page table entry layout (chosen by processor)

where can processor store megabytes of page tables? in memory

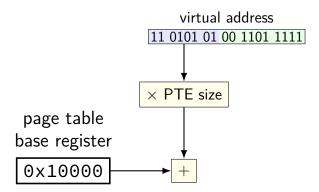
page table entry layout (chosen by processor) valid (bit 15) physical page # (bits 4–14) other bits and/or unused (bit 0-3) page table physical memory base register addresses bytes 0x00000000-1 00000000 00000000 0x00010000 0x00010000-1 00000000 $0 \times 00010002 - 3$ page table (logically) 0x00010004-5 0x00010006-7 virtual page # valid? physical page # 0000 0000 0x000101FE-F 10001 0000 0001 0x00010200-1 10100010 001 0000 0010 0000 0011 0000 001 1111 1111 1110 1000

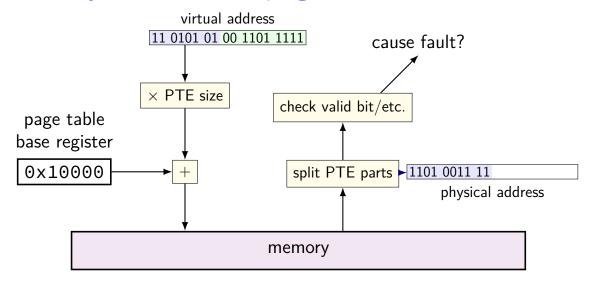
where can processor store megabytes of page tables? in memory

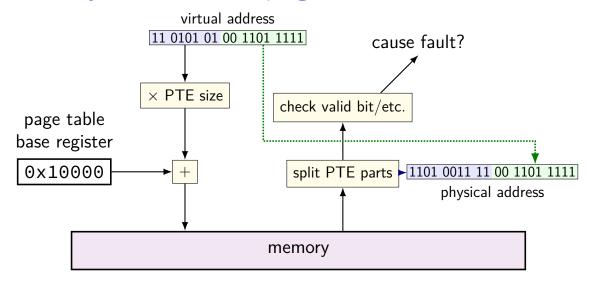
page table entry layout (chosen by processor) valid (bit 15) physical page # (bits 4–14) other bits and/or unused (bit 0-3) page table physical memory base register addresses bytes 0x00000000-1 00000000 00000000 0x00010000 0x00010000-1 00000000 000000000 $0 \times 00010002 - 3$ page table (logically) 0x00010004-5 10000010 0x00010006-7 10110000 001 virtual page # valid? physical page # 0000 0000 0000 0000 0x000101FE-F 10001110 0000 0001 0x00010200-1 10100010 00111010 0000 0010 0000 0011 0000 0011 1111 1111 00 1110 1000

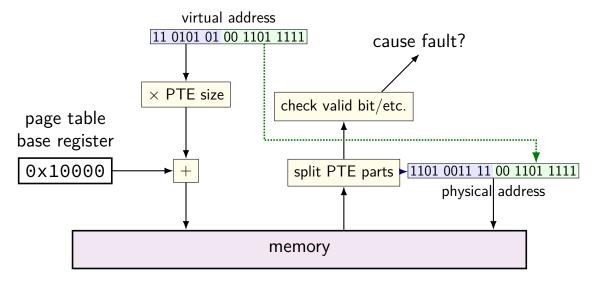
virtual address

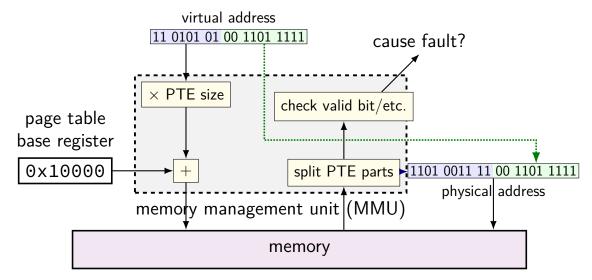
11 0101 01 00 1101 1111

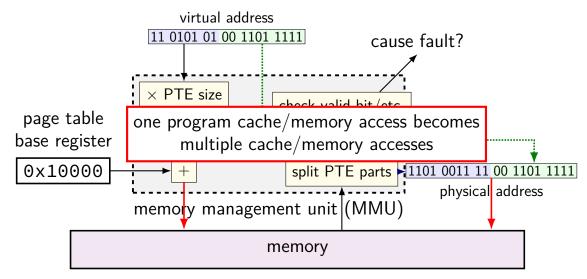


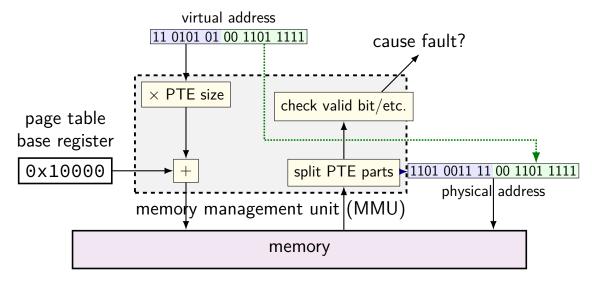












physical addresses	byte	es			phys addres	ical sses	byt	es		
0x00-3			22	33	0x20				D2	D3
0x04-7	44	55	66	77	0x24	-7	E4	E5	F6	07
0x08-B	88	99	AΑ	ВВ	0x28	В-В	89	9A	ΑB	ВС
0x0C-F	CC	DD	EE	FF	0x20	:-F	CD	DE	EF	F0
0x10-3	1A	2A	3A	4A	0x30)-3	ВА	0A	ВА	0Α
0x14-7	1B	2B	3B	4B	0x34	<u>-7</u>	СВ	0B	СВ	0B
0x18-B	1C	2C	3C	4C	0x38	В-В	DC	0C	DC	0C
0x1C-F	1C	2C	3C	4C	0x30	-F	EC	0C	EC	0C

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other;

```
physical bytes
                       physical bytes
                                           0x31 = 11 0001
                      addresses
addresses
                                           PTE addr:
0x00-3|00 11 22 33
                      0x20-3|D0 D1 D2 D3
                                           0x20 + 110 \times 1 = 0x26
0x04-7|44 55 66 77
                      0x24-7|E4 E5 F6 07
0x08-B|88 99 AA BB
                      0x28-B|89 9A AB BC
                                          PTE value:
                      0x2C-FCD DE EF F0
0x0C-FICC DD EE FF
                                           0xF6 = 1111 0110
0x10-3|1A 2A 3A 4A
                      0x30-3|BA 0A BA 0A
                                           PPN 111, valid 1
0x14-7|1B 2B 3B 4B
                      0x34-7|CB 0B CB 0B
                                           M[111 \ 001] = M[0x39]
                      0x38-BDC 0C DC 0C
0x18-B|1C 2C 3C 4C
                                           \rightarrow 0x0C
0x1C-F|1C 2C 3C 4C
                      0x3C-FEC 0C EC 0C
```

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other;

physical bytes addresses	physical bytes addresses	0x31 = 11 0001
addresses 0x00-300 11 22 33	addresses 0x20-3D0 D1 D2 D3	PTE addr:
0x04-744 55 66 77	0x24-7E4 E5 F6 07	$0x20 + 110 \times 1 = 0x26$
0x08-B <mark>88 99 AA BB</mark>	0x28-B89 9A AB BC	PTE value:
0x0C-FCC DD EE FF	0x2C-FCD DE EF F0	0xF6 = 1111 0110
0x10-3 1A 2A 3A 4A	0x30-3BA 0A BA 0A	PPN 111 , valid 1
0×14-7 1B 2B 3B 4B	0x34-7 CB 0B CB 0B	
0×18-B 1C 2C 3C 4C	0x38-BDC 0C DC 0C	M[111 001] = M[0x39]
0x1C-F1C 2C 3C 4C	0x3C-FEC 0C EC 0C	ightarrow 0x0C

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other;

```
physical bytes
                       physical bytes
                                           0x31 = 11 \ 0001
                      addresses
addresses
                                           PTE addr:
0x00-3|00 11 22 33
                      0x20-3|D0 D1 D2 D3
                                           0x20 + 110 \times 1 = 0x26
0x04-7|44 55 66 77
                      0x24-7|E4 E5 F6 07
0x08-B|88 99 AA BB
                      0x28-B|89 9A AB BC
                                          PTE value:
                      0x2C-FCD DE EF F0
0x0C-FICC DD EE FF
                                           0xF6 = 1111 0110
0x10-3|1A 2A 3A 4A
                      0x30-3|BA 0A BA 0A
                                           PPN 111, valid 1
0x14-7|1B 2B 3B 4B
                      0x34-7|CB 0B CB 0B
                                           M[111 \ 001] = M[0x39]
                      0x38-BDC 0C DC 0C
0x18-B|1C 2C 3C 4C
                                           \rightarrow 0x0C
0x1C-F|1C 2C 3C 4C
                      0x3C-FEC 0C EC 0C
```

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other;

```
physical bytes
                       physical bytes
                                           0x31 = 11 0001
                      addresses
addresses
                                           PTE addr:
0x00-3|00 11 22 33
                      0x20-3|D0 D1 D2 D3
                                           0x20 + 110 \times 1 = 0x26
0x04-7|44 55 66 77
                      0x24-7|E4 E5 F6 07
0x08-B|88 99 AA BB
                      0x28-B|89 9A AB BC
                                          PTE value:
                      0x2C-FCD DE EF F0
0x0C-FICC DD EE FF
                                           0xF6 = 1111 0110
0x10-3|1A 2A 3A 4A
                      0x30-3|BA 0A BA 0A
                                           PPN 111, valid 1
0x14-7|1B 2B 3B 4B
                      0x34-7|CB 0B CB 0B
                                           M[111 \ 001] = M[0x39]
                      0x38-BDC 0C DC 0C
0x18-B|1C 2C 3C 4C
                                           \rightarrow 0x0C
0x1C-F|1C 2C 3C 4C
                      0x3C-F|EC 0C EC 0C
```

physical bytes addresses		physical addresses	byte	25		
addresses		addresses	-) -			
0x00-300 11 22	2 33	0x20-3	Α0	E2	D1	F3
0x04-744 55 66	6 77	0x24-7	E4	E5	F6	07
0x08-B88 99 A	A BB	0x28-B	89	9A	AB	ВС
0x0C-FCC DD EI	E FF	0x2C-F	CD	DE	EF	F0
0x10-3 1A 2A 3/	4 4A	0x30-3	ВА	0Α	ВА	0Α
0x14-7 1B 2B 3B	3 4B	0x34-7	СВ	0B	СВ	0B
0x18-B1C 2C 30	C 4C	0x38-B	DC	0C	DC	0C
0x1C-F1C 2C 30	C 4C	0x3C-F	EC	0C	EC	0C

```
physical bytes
                       physical bytes
                                            0x12 = 01 0010
                      addresses
addresses
                                            PTE addr:
                      0x20-3|A0 E2 D1 F3
0x00-3|00 11 22 33
                                           0x20 + 2 \times 1 = 0x22
0x04-7|44 55 66 77
                      0x24-7|E4 E5 F6 07
0x08-B|88 99 AA BB
                      0x28-B|89 9A AB BC
                                           PTE value:
                      0x2C-FCD DE EF F0
0x0C-FICC DD EE FF
                                            0 \times D1 = 1101 0001
0x10-3|1A 2A 3A 4A
                      0x30-3|BA 0A BA 0A
                                           PPN 110, valid 1
0x14-7|1B 2B 3B 4B
                      0x34-7|CB 0B CB 0B
                                           M[110 \ 001] = M[0x32]
                       0x38-BDC 0C DC 0C
0x18-B|1C 2C 3C 4C
                                           \rightarrow 0xBA
0x1C-F|1C 2C 3C 4C
                      0x3C-FEC 0C EC 0C
```

```
physical bytes
                       physical bytes
                                            0 \times 12 = 01 \ 0.010
                      addresses
addresses
                                            PTE addr:
0x00-3|00 11 22 33
                       0x20-3|A0 E2 D1 F3
                                            0x20 + 2 \times 1 = 0x22
0x04-7|44 55 66 77
                       0x24-7|E4 E5 F6 07
0x08-B|88 99 AA BB
                       0x28-B|89 9A AB BC
                                           PTE value:
                       0x2C-FCD DE EF F0
0x0C-FICC DD EE FF
                                            0xD1 = 1101 0001
0x10-3|1A 2A 3A 4A
                       0x30-3|BA 0A BA 0A
                                            PPN 110, valid 1
0x14-7|1B 2B 3B 4B
                       0x34-7|CB 0B CB 0B
                                            M[110 \ 001] = M[0x32]
                       0x38-BDC 0C DC 0C
0x18-B|1C 2C 3C 4C
                                            \rightarrow 0xBA
0x1C-F|1C 2C 3C 4C
                       0x3C-FEC 0C EC 0C
```

```
physical bytes
                       physical bytes
                                            0 \times 12 = 01 \ 0010
                      addresses
addresses
                                            PTE addr:
0x00-3|00 11 22 33
                       0x20-3|A0 E2 D1 F3
                                            0x20 + 2 \times 1 = 0x22
0x04-7|44 55 66 77
                       0x24-7|E4 E5 F6 07
0x08-B|88 99 AA BB
                       0x28-B|89 9A AB BC
                                           PTE value:
                       0x2C-FCD DE EF F0
0x0C-FICC DD EE FF
                                            0xD1 = 1101 0001
0x10-3|1A 2A 3A 4A
                       0x30-3|BA 0A BA 0A
                                            PPN 110, valid 1
0x14-7|1B 2B 3B 4B
                       0x34-7|CB 0B CB 0B
                                            M[110 \ 001] = M[0x32]
                       0x38-BDC 0C DC 0C
0x18-B|1C 2C 3C 4C
                                            \rightarrow 0xBA
0x1C-F|1C 2C 3C 4C
                       0x3C-FEC 0C EC 0C
```

6-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 other page table base register 0x20; translate virtual address 0x12

physical bytes physical bytes $0 \times 12 = 01 \ 0.010$ addresses addresses PTE addr: 0x20-3 A0 E2 D1 F3 0x00-3|00 11 22 33 $0x20 + 2 \times 1 = 0x22$ 0x04-7|44 55 66 77 0x24-7|E4 E5 F6 07 0x08-B|88 99 AA BB 0x28-B|89 9A AB BC PTE value: 0x2C-FCD DE EF F0 0x0C-FICC DD EE FF 0xD1 = 1101 00010x10-3|1A 2A 3A 4A 0x30-3|BA 0A BA 0A PPN 110, valid 1 0x14-7|1B 2B 3B 4B 0x34-7|CB 0B CB 0B $M[110 \ 001] = M[0x32]$ 0x38-BDC 0C DC 0C 0x18-B|1C 2C 3C 4C \rightarrow 0xBA 0x1C-F|1C 2C 3C 4C 0x3C-FEC 0C EC 0C

pagetable assignment

```
pagetable assignment
```

simulate page tables (on top of normal program memory) alternately: implement another layer of page tables on top of the existing system's

in assignment:

virtual address \sim arguments to your functions

physical address \sim your program addresses (normal pointers)

pagetable assignment API

```
/* configuration parameters */
#define POBITS ...
#define LEVELS /* later /
size_t ptbr; // page table base register
    // points to page table (array of page table entries)
// lookup "virtual" address 'va' in page table ptbr points to
// return (void*) (~0L) if invalid
void *translate(size t va);
// make it so 'va' is valid, allocating one page for its data
// if it isn't already
void page_allocate(size_t va)
```

translate()

with POBITS=12, LEVELS=1:

ptbr = GetPointerToTable(

١
)

VDN valid2 physical

```
\begin{array}{l} translate(0x0FFF) == (void^*) ~0L \\ translate(0x1000) == (void^*) ~0x9999000 \\ translate(0x1001) == (void^*) ~0x9999001 \\ translate(0x2000) == (void^*) ~0L \\ translate(0x2001) == (void^*) ~0L \\ translate(0x3000) == (void^*) ~0x3333000 \\ \end{array}
```

translate()

with POBITS=12, LEVELS=1:

 $\mathsf{ptbr} = \mathsf{GetPointerToTable}($

valia !	pnysicai	
0		
1	0x9999	١
0)
1	0x3333	
	0 1 0 1 	0 —

1/DM - 1:12 mby/size1

```
\begin{array}{l} translate(0x0FFF) == (void^*) ~0L \\ translate(0x1000) == (void^*) ~0x9999000 \\ translate(0x1001) == (void^*) ~0x9999001 \\ translate(0x2000) == (void^*) ~0L \\ translate(0x2001) == (void^*) ~0L \\ translate(0x3000) == (void^*) ~0x3333000 \\ \end{array}
```

page_allocate()

```
with POBITS=12, LEVELS=1:  ptbr == 0 \\ page\_allocate(0x1000) \ or \ page\_allocate(0x1001) \ or \ ...
```

page_allocate()

```
with POBITS=12, LEVELS=1: 
 ptbr == 0 page\_allocate(0x1000) \ or \ page\_allocate(0x1001) \ or \ ...
```

 $\mathsf{ptbr}\ \mathit{now} == \mathsf{GetPointerToTable}($

VEIN	vanu :	priyan	Cai	
0	0			
1	1	(new))	١
2	0	_)
3	1			

V/DNI valid2 physical

allocated with posix_memalign

page_allocate()

```
with POBITS=12, LEVELS=1: 
 ptbr == 0 page\_allocate(0x1000) \ or \ page\_allocate(0x1001) \ or \ ...
```

 $ptbr\ \textit{now} == \mathsf{GetPointerToTable}($

VPN	valid?	physical
0	0	

allocated with posix_memalign

posix_memalign

```
void *result;
error code =
     posix_memalign(&result, alignment, size);
allocate size bytes
choosing address that is multiple of alignment
    can make sure allocation starts at beginning of page
error_code indicates if out-of-memory, etc.
fills in result (passed via pointer)
```

posix_memalign

```
void *result;
error code =
     posix_memalign(&result, alignment, size);
allocate size bytes
choosing address that is multiple of alignment
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posix_memalign

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void *result;
error code =
     posix_memalign(&result, alignment, size);
allocate size bytes
choosing address that is multiple of alignment
    can make sure allocation starts at beginning of page
error_code indicates if out-of-memory, etc.
fills in result (passed via pointer)
```

parts

```
part 1 (next week): LEVELS=1, POBITS=12 and
    translate() OR
     page_allocate()
part 2: all LEVELS, both functions
    in preparation for code review
     originally scheduled for lab on the 27th
    will move to lab just after reading day
     (might mean I need to cancel lab one week)
part 3: final submission
     Friday after code review
     most of grade based on this
     will test previous parts again
```

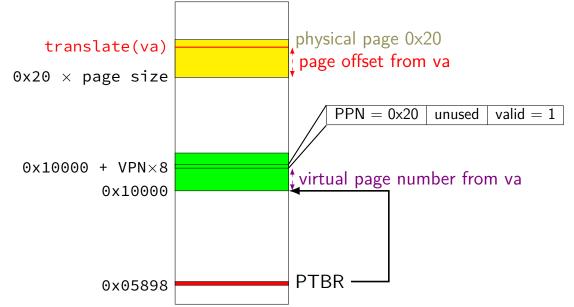
address/page table entry format

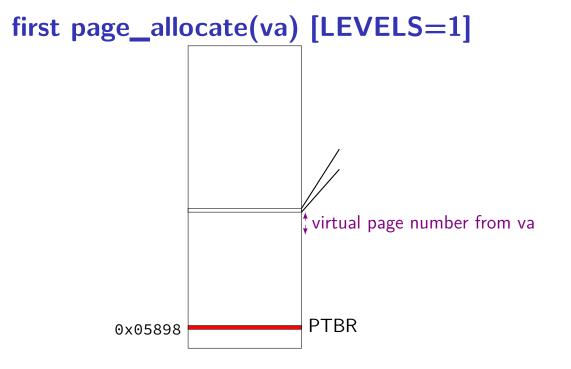
(with POBITS=12, LEVELS=1)

	bits 63–21	bits 20–12	bits 11–1	bit 0
page table entry	physical page number		unused	valid bit
virtual address	unused	virtual page number	page offset	
physical address	physical page number		page offset	

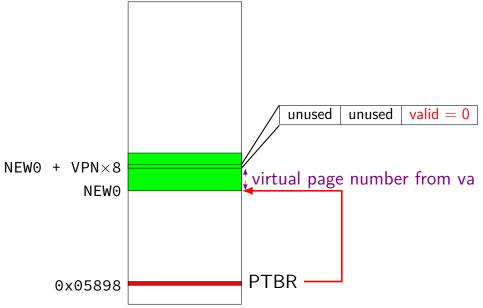
in assignment: value from posix_memalign = physical address

pa = translate(va) [LEVELS=1]

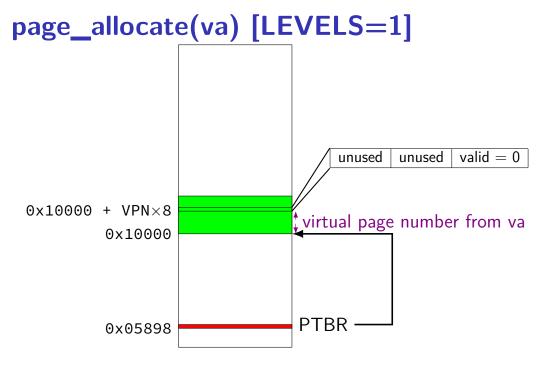


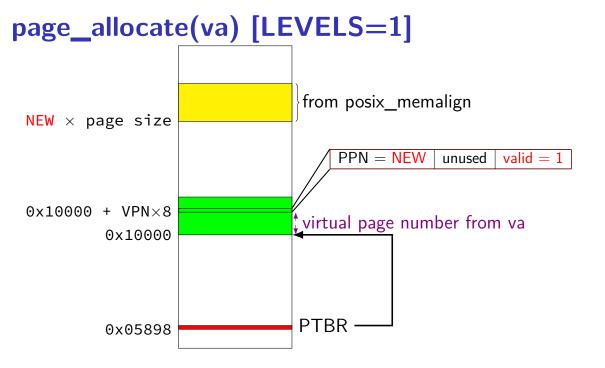


first page_allocate(va) [LEVELS=1]

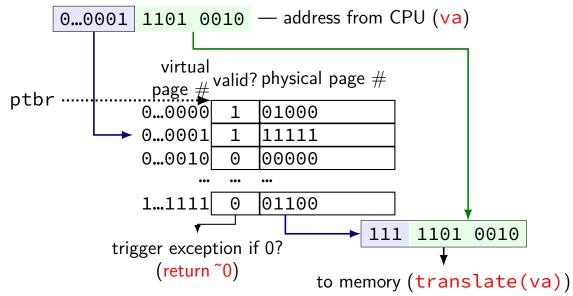


first page_allocate(va) [LEVELS=1] from posix_memalign $NEW1 \times page size$ PPN = NEW1valid = 1unused NEW0 + VPN×8 ‡virtual page number from va NEW₀ **PTBR** 0x05898

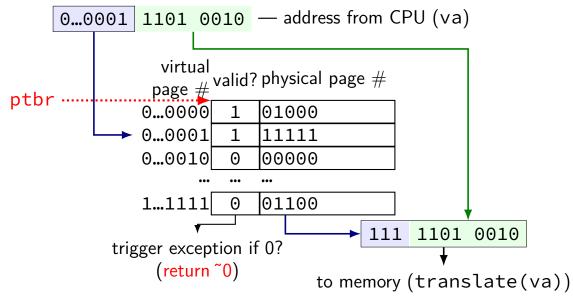




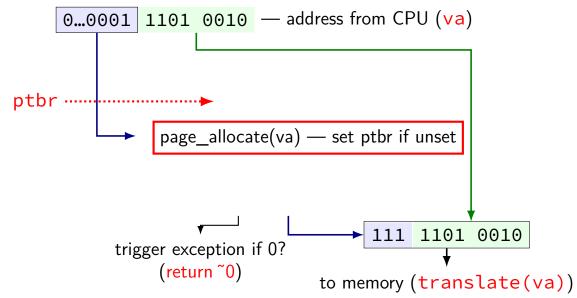
page table lookup (and translate())



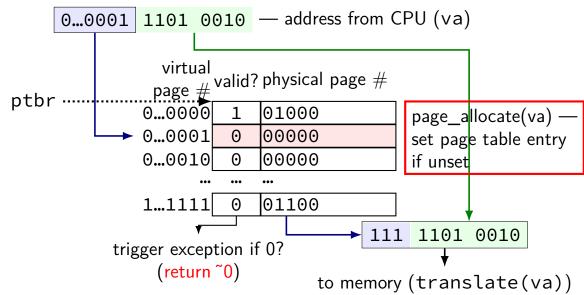
page table lookup (and translate())



page table lookup (and allocate)



page table lookup (and allocate)



my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

top 16 bits of 64-bit addresses not used for translation

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: how many page table entries? (assuming page table like shown before)

exercise: how large are physical page numbers?

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: how many page table entries? (assuming page table like shown before)

exercise: how large are physical page numbers?

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: how many page table entries? (assuming page table like shown before)

exercise: how large are physical page numbers?

page table entries are 8 bytes (room for expansion, metadata) trick: power of two size makes table lookup faster

would take up 2^{39} bytes?? (512GB??)

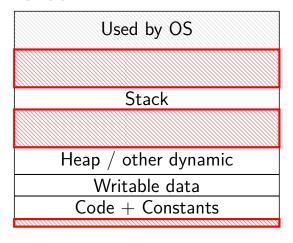
huge page tables

huge virtual address spaces!

impossible to store PTE for every page

how can we save space?

holes



most pages are invalid

saving space

basic idea: don't store (most) invalid page table entries
use a data structure other than a flat array
 want a map — lookup key (virtual page number), get value (PTE)
options?

saving space

```
basic idea: don't store (most) invalid page table entries
use a data structure other than a flat array
want a map — lookup key (virtual page number), get value (PTE)
options?
```

hashtable

actually used by some historical processors but never common

saving space

```
basic idea: don't store (most) invalid page table entries
use a data structure other than a flat array
    want a map — lookup key (virtual page number), get value (PTE)
options?
```

hashtable

actually used by some historical processors but never common

tree data structure

but not quite a search tree

search tree tradeoffs

lookup usually implemented in hardware

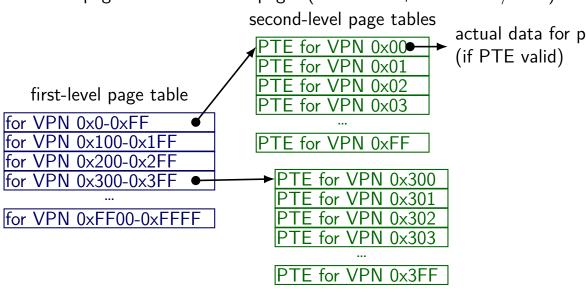
lookup should be simple solution: lookup splits up address bits (no complex calculations)

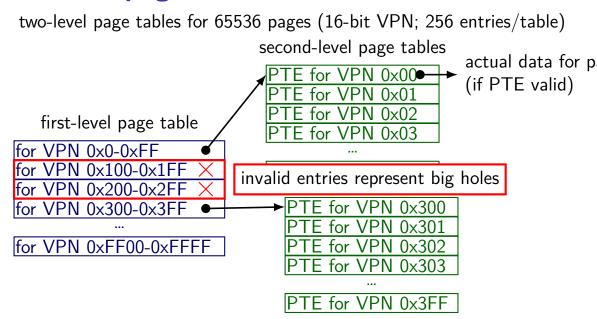
lookup should not involve many memory accesses

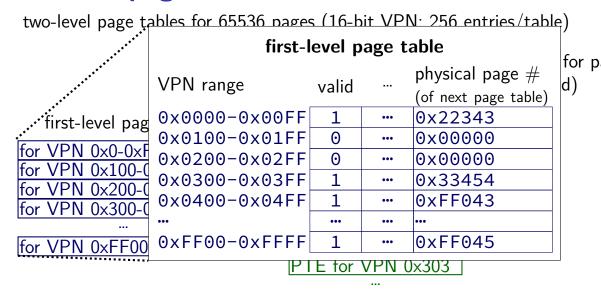
doing two memory accesses is already very slow solution: tree with many children from each node

(far from binary tree's left/right child)

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)

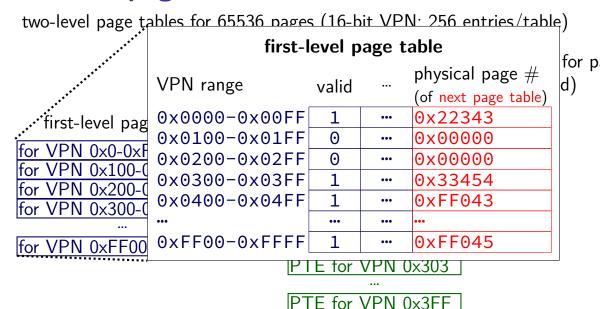


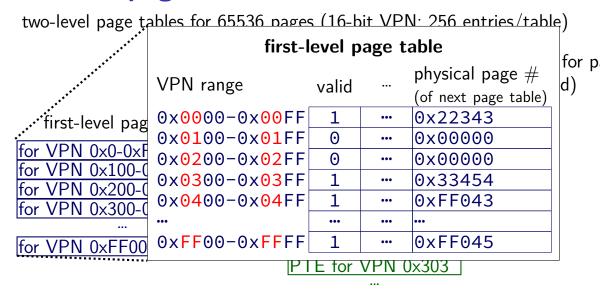




TE for VPN 0x3FF

41

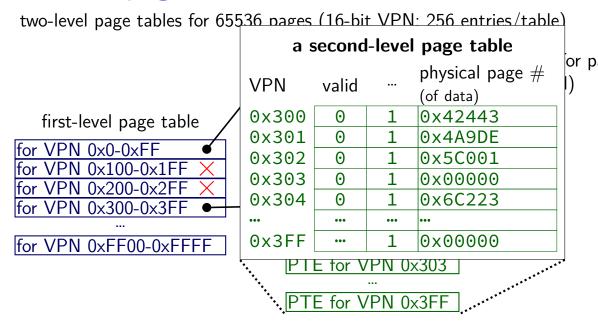




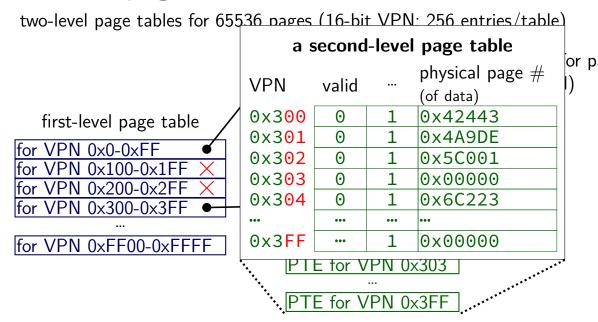
TE for VPN 0x3FF

41

two-level page tables

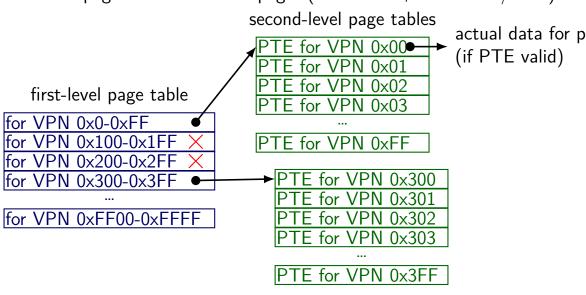


two-level page tables



two-level page tables

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)

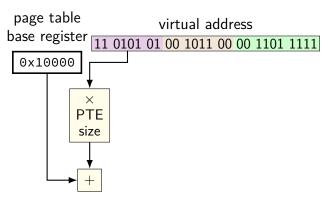


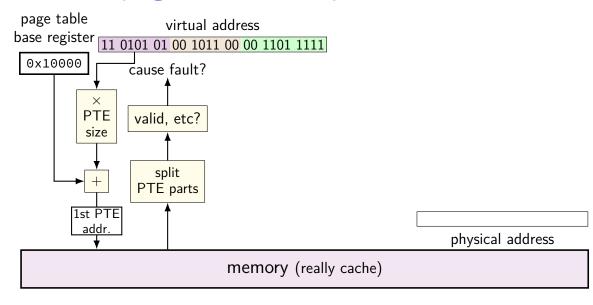
virtual address

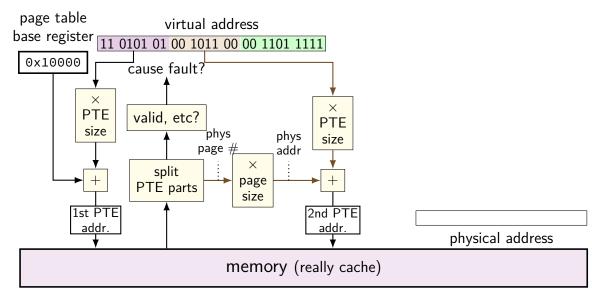
11 0101 01 00 1011 00 00 1101 1111

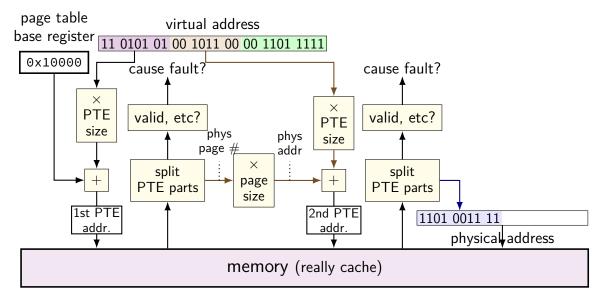
VPN — split into two parts (one per level)

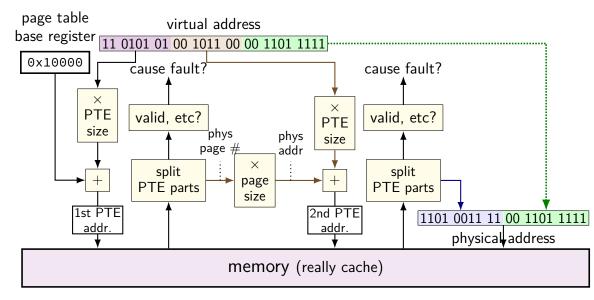
this example: parts equal sized — common, but not required

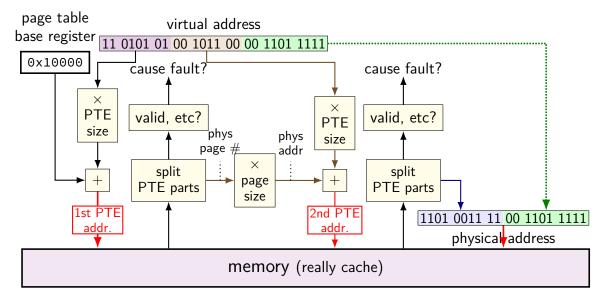


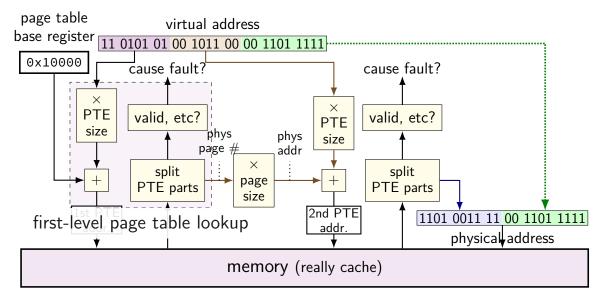


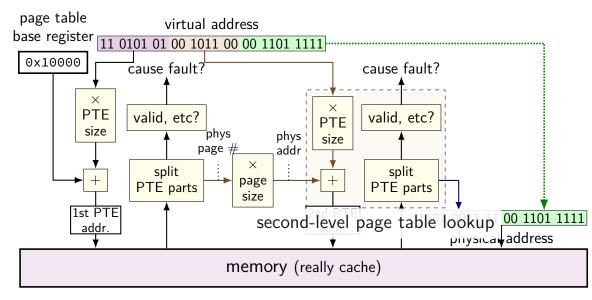


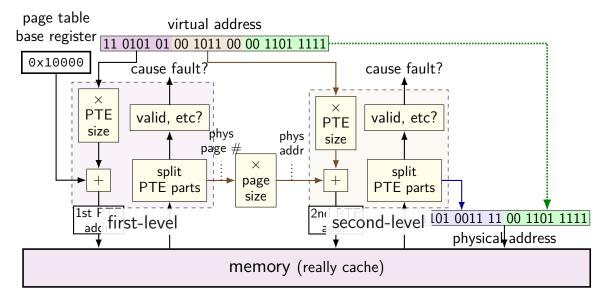


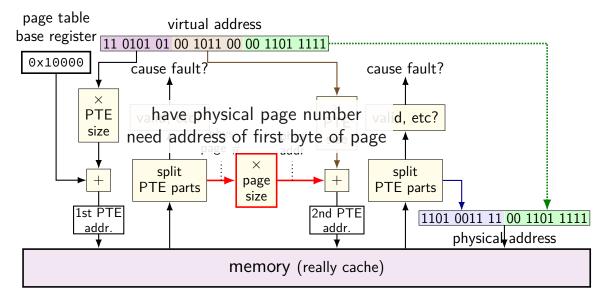


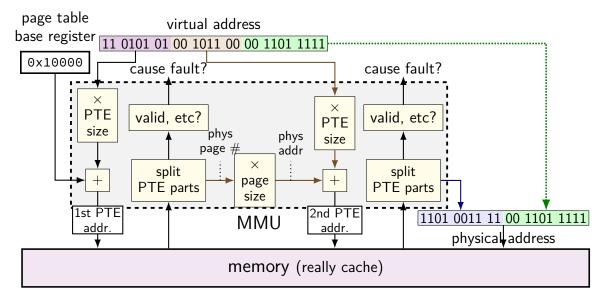












another view



multi-level page tables

VPN split into pieces for each level of page table

top levels: page table entries point to next page table usually using physical page number of next page table

bottom level: page table entry points to destination page

validity checks at each level

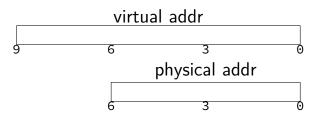
note on VPN splitting

indexes used for lookup parts of the virtual page number (there are not multiple VPNs)

assignment

9-bit virtual address

6-bit physical address



9-bit virtual address

virtual addr

VPN page offset

9 6 3

6-bit physical address

- physical addr
 PPN page offset
- 8-byte pages \rightarrow 3-bit page offset (bottom) ⁶
- 9-bit VA: 6 bit VPN + 3 bit PO
- 6-bit PA: 3 bit PPN + 3 bit PO

9-bit virtual address

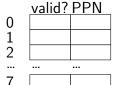
virtual addr
VPN page offset
9 6 3

physical addr

6-bit physical address

- phy PPN
- page offset

- 8-byte pages \rightarrow 3-bit page offset (bottom) ⁶
- 9-bit VA: 6 bit VPN + 3 bit PO
- 6-bit PA: 3 bit PPN + 3 bit PO
- 1 page page tables w/ 1 byte entry \rightarrow 8 entry PTs



page table (either level)

9-bit virtual address

virtual addr page offset VPN pt 1 VPN pt 2

PPN

- 6-bit physical address
- 8-byte pages \rightarrow 3-bit page offset (bottom) ⁶
- page table (either level)

page offset

physical addr

- 9-bit VA: 6 bit VPN + 3 bit PO
- 6-bit PA: 3 bit PPN + 3 bit PO
- 1 page page tables w/ 1 byte entry \rightarrow 8 entry PTs
- valid? PPN

- 8 entry page tables \rightarrow 3-bit VPN parts
- 9-bit VA: 3 bit VPN part 1; 3 bit VPN part 2

physical addresses	byte	es			physica addresses	byt	es		
0x00-3	00	11	22	33	0x20-3			72	13
0x04-7	44	55	66	77	0x24-7	F4	Α5	36	07
0x08-B	88	99	AΑ	ВВ	0x28-E	89	9A	ΑB	ВС
0x0C-F	CC	DD	EE	FF	0x2C-F	CD	DE	EF	F0
0x10-3	1A	2A	ЗА	4A	0x30-3	ВА	0A	ВА	0A
0x14-7	1B	2B	3B	4B	0x34-7	DB	0B	DB	0B
0x18-B	1C	2C	3C	4C	0x38-E	EC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C-F	AC	DC	DC	0C

physical addresses	byt	es		
0x00-3				
0x04-7	44	55	66	77
0x08-B	88	99	AΑ	ВВ
0x0C-F	CC	DD	ΕE	FF
0x10-3	1A	2A	3A	4A
0x14-7	1В	2B	3B	4B
0x18-B	1C	2C	3C	4C
0x1C-F	1C	2C	3C	4C

physical addresses	byt	es		
0x20-3	00	91		
0x24-7				
0x28-B				
0x2C-F	CD	DE	EF	F0
0x30-3	ВА	0A	ВА	0A
0x34-7				
0x38-B	EC	0C	EC	0C
0x3C-F	AC	DC	DC	0C

physical addresses	bytes	
	00 11 22 33	7
	44 55 66 77	
0x08-B	88 99 AA BB	
0x0C-F	CC DD EE FF	1
0x10-3	1A 2A 3A 4A	
0x14-7	1B 2B 3B 4B	
0x18-B	1C 2C 3C 4C	
0x1C-F	1C 2C 3C 4C	

physical addresses	byt	es		
0x20-3	00	91	72	13
0x24-7				
0x28-B	89	9A	AB	ВС
0x2C-F	CD	DE	EF	F0
0x30-3	ВА	0A	ВА	ΘΑ
0x34-7	DB	0B	DB	0B
0x38-B	EC	0C	EC	0C
0x3C-F	AC.	DC	DC.	0C

physical addresses	byt	es		
0x00-3		11	22	33
0x04-7	44	55	66	77
0x08-B	88	99	AA	ВВ
0x0C-F	CC	DD	ΕE	FF
0x10-3	1A	2A	ЗА	4A
0x14-7	1В	2B	3B	4B
0x18-B	1C	2C	3C	4C
0x1C-F	1C	2C	3C	4C

physical addresses	byt	es		
0x20-3	00	91	72	13
0x24-7				
0x28-B				
0x2C-F	CD	DE	EF	F0
0x30-3	ВА	0A	ВА	0A
0x34-7				
0x38-B	EC	0C	EC	0C
0x3C-F	AC	DC	DC	0C

physical addresses	byt	es			physical addresses	byt	es		
0x00-3	00	11	22	33	0x20-3	00	91	72	13
0x04-7	44	55	66	77	0x24-7	F4	Α5	36	07
0x08-B	88	99	AΑ	ВВ	0x28-B	89	9A	ΑB	ВС
0x0C-F	CC	DD	ΕE	FF	0x2C-F	CD	DE	EF	F0
0x10-3	1A	2A	ЗА	4A	0x30-3	ВА	0A	ВА	0A
0x14-7	1В	2B	3B	4B	0x34-7	DB	0B	DB	0B
0x18-B	1C	2C	3C	4C	0x38-B	EC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C-F	AC	DC	DC	0C

physical addresses	byte	es			physical addresses	byt	es		
0x00-3	00	11	22	33	0x20-3			D2	D3
0x04-7	44	55	66	77	0x24-7	D4	D5	D6	D7
0x08-B	88	99	AΑ	ВВ	0x28-B	89	9A	ΑB	ВС
0x0C-F	CC	DD	EE	FF	0x2C-F	CD	DE	EF	F0
0x10-3	1A	2A	ЗА	4A	0x30-3	ВА	0A	ВА	0A
0x14-7	1B	2B	3B	4B	0x34-7	DB	0B	DB	0B
0x18-B	1C	2C	3C	4C	0x38-B	EC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C-F	FC	0C	FC	0C

physical addresses	byte	es			physical addresses	byt	es		
0x00-3			22	33	0x20-3	D0	D1	D2	D3
0x04-7	44	55	66	77	0x24-7	D4	D5	D6	D7
0x08-B	88	99	AΑ	ВВ	0x28-B	89	9A	ΑB	ВС
0x0C-F	CC	DD	EE	FF	0x2C-F	CD	DE	EF	F0
0x10-3	1A	2A	ЗА	4A	0x30-3	ВА	0Α	ВА	0Α
0x14-7	1В	2B	3B	4B	0x34-7	DB	0B	DB	0B
0x18-B	1C	2C	3C	4C	0x38-B	EC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C-F	FC	0C	FC	0C

physical addresses	bytes		physic address
0x00-3	00 11 22	2 33	0x20-
0x04-7	44 55 66	3 77	0x24-
0x08-B	88 99 A <i>i</i>	A BB	0x28-
0x0C-F	CC DD EI	E FF	0x2C-
0x10-3	1A 2A 3	4 4 A	0x30-
0x14-7	1B 2B 3	3 4B	0x34-
0x18-B	1C 2C 30	C 4C	0x38-
0x1C-F	1C 2C 30	C 4C	0x3C-

physical addresses	byt	es		
0x20-3	D0	D1	D2	D3
0x24-7	D4	D5	D6	D7
0x28-B				
0x2C-F	CD	DE	EF	F0
0x30-3	ВА	0A	ВА	0A
0x34-7	DB	0B	DB	0B
0x38-B	EC	0C	EC	0C
0x3C-F	FC.	0C	FC.	0C

2 D3
5 D7
BC
F0
\ 0A
3 0B
0C
0C
1

physical addresses	byte	es			physic address	al es	byt	es		
0x00-3			22	33	0x20-				D2	D3
0x04-7	44	55	66	77	0x24-	-7[D4	D5	D6	D7
0x08-B	88	99	AΑ	ВВ	0x28-	-B[89	9A	ΑB	ВС
0x0C-F	CC	DD	EE	FF	0x2C-	-F[CD	DE	EF	F0
0x10-3	1A	2A	3A	4A	0x30-	-3[ВА	0Α	ВА	0Α
0x14-7	1B	2B	3B	4B	0x34-	-7[DB	0B	DB	0B
0x18-B	1C	2C	3C	4C	0x38-	-в[EC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C-	-F[FC	0C	FC	0C

physical bytes addresses ox00-3 00 11 22 33 physical bytes addresses ox20-3 D0 D1 D2 D	
)3
0x04-744 55 66 77 0x24-7D4 D5 D6 D	7
0x08-B88 99 AA BB 0x28-B89 9A AB B	3C
0x0C-FCC DD EE FF 0x2C-FCD DE EF F	-0
0x10-3 1A 2A 5A 4A 0x30-3 BA 0A BA 0	λ
0x14-7 1B 2B 3B 4B)B
0x18-B 1C 2C 3C 4C 0x38-B EC 0C EC 0)C
0x1C-F1C 2C 3C 4C 0x3C-FFC 0C FC 0)C

physical addresses	byte	es			physic address	cal ses	byte	es		
0x00-3			22	33	0x20-				D2	D3
0x04-7	44	55	66	77	0x24-	-7	D4	D5	D6	D7
0x08-B	88	99	AΑ	ВВ	0x28-	-в	89	9A	ΑB	ВС
0x0C-F	CC	DD	EE	FF	0x2C-	-F	CD	DE	EF	F0
0x10-3	1A	2A	3A	4A	0x30-	-3	ВА	0Α	ВА	0A
0x14-7	1B	2B	3B	4B	0x34-	-7	DB	0B	DB	0B
0x18-B	1C	2C	3C	4C	0x38-	-В	EC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C-	-F	FC	0C	FC	0C

physical bytes addresses							
0x00-3			22	33			
0x04-7	44	55	66	77			
0x08-B							
0x0C-F	CC	DD	EE	FF			
0x10-3	1A	2A	ЗА	4A			
0x14-7							
0x18-B							
0x1C-F	1C	2C	3C	4C			

physical addresses	byt	es		
0x20-3	D0	D1	D2	D3
0x24-7	D4	D5	D6	D7
0x28-B				
0x2C-F				
0x30-3	ВА	0A	ВА	0A
0x34-7	DB	0B	DB	0B
0x38-B	EC	0C	EC	0C
0x3C-F	FC.	0 C	FC.	0C

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x08; translate virtual address 0x00B

physical addresses	byte	es			physiaddress	cal ses	byt	es		
0x00-3	00	11	22	33	0x20				D2	D3
0x04-7	44	55	66	77	0x24	-7	D4	D5	D6	D7
0x08-B	88	99	AA	ВВ	0x28	-B	89	9A	ΑB	ВС
0x0C-F	CC	DD	EE	FF	0x2C	-F	CD	DE	EF	F0
0x10-3	1A	2A	ЗА	4A	0x30	-3	ВА	0A	ВА	0A
0x14-7	1B	2B	3B	4B	0x34	-7	DB	0B	DB	0B
0x18-B	1C	2C	3C	4C	0x38	-B	EC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C	-F	FC	0C	FC	0C

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x08; translate virtual address 0x1CB

physical addresses	byt	es		
0x00-3		11	22	33
0x04-7	44	55	66	77
0x08-B	88	99	AA	ВВ
0x0C-F	CC	DD	ΕE	FF
0x10-3	1A	2A	ЗА	4A
0x14-7	1В	2B	3B	4B
0x18-B	1C	2C	3C	4C
0x1C-F	1C	2C	3C	4C

physical addresses	byt	es		
0x20-3			D2	D3
0x24-7	D4	D5	D6	D7
0x28-B	89	9A	ΑB	ВС
0x2C-F	CD	DE	EF	F0
0x30-3	ВА	0Α	ВА	0A
0x34-7				
0x38-B	EC	0C	EC	0C
0x3C-F	FC	0C	FC	0C

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

physical addresses	byt	es		
0x00-3				
0x04-7	44	55	66	77
0x08-B				
0x0C-F	CC	DD	EE	FF
0x10-3	1A	2A	3A	4A
0x14-7				
0x18-B	1C	2C	3C	4C
0x1C-F	AC	ВС	DC	EC

```
physical bytes addresses 0x20-3 D0 E1 D2 D3 0x24-7 D4 E5 D6 E7 0x28-B 89 9A AB BC 0x2C-F CD DE EF F0 0x30-3 BA 0A BA 0A 0x34-7 DB 0B DB 0B 0x38-B EC 0C EC 0C 0x3C-F FC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

physical addresses	byt	es		
0x00-3			22	33
0x04-7	44	55	66	77
0x08-B				
0x0C-F	CC	DD	EE	FF
0x10-3	1A	2A	3A	4A
0x14-7				
0x18-B	1C	2C	3C	4C
0x1C-F	AC	ВС	DC	EC

```
physical addresses

0x20-3 D0 E1 D2 D3

0x24-7 D4 E5 D6 E7

0x28-B 89 9A AB BC

0x2C-F CD DE EF F0

0x30-3 BA 0A BA 0A

0x34-7 DB 0B DB 0B

0x38-B EC 0C EC 0C

0x3C-F FC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

physical addresses	byt	es		
0x00-3			22	33
0x04-7	44	55	66	77
0x08-B				
0x0C-F	CC	DD	EE	FF
0x10-3	1A	2A	3A	4A
0x14-7				
0x18-B	1C	2C	3C	4C
0x1C-F	AC	ВС	DC	EC

```
physical addresses

0x20-3 D0 E1 D2 D3

0x24-7 D4 E5 D6 E7

0x28-B 89 9A AB BC

0x2C-F CD DE EF F0

0x30-3 BA 0A BA 0A

0x34-7 DB 0B DB 0B

0x38-B EC 0C EC 0C

0x3C-F FC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

physical addresses	byt	es		
0x00-3	00	11	22	33
0x04-7	44	55	66	77
0x08-B	88	99	AΑ	ВВ
0x0C-F	CC	DD	EE	FF
0x10-3	1A	2A	3A	4A
0x14-7	1В	2B	3B	4B
0x18-B	1C	2C	3C	4C
0x1C-F	AC	ВС	DC	EC

```
physical bytes
addresses
0x20-3D0 E1 D2 D3
0x24-7D4 E5 D6 E7
0x28-Bl89 9A AB BC
0x2C-FCD DE EF F0
0x30-3|BA 0A BA 0A
0x34-7DB 0B DB 0B
0x38-B|EC 0C EC 0C
0x3C-FIFC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

physical addresses	byt	es		
0x00-3			22	33
0x04-7	44	55	66	77
0x08-B				
0x0C-F	CC	DD	EE	FF
0x10-3	1A	2A	3A	4A
0x14-7				
0x18-B	1C	2C	3C	4C
0x1C-F	AC	ВС	DC	EC

```
physical addresses

0x20-3 D0 E1 D2 D3

0x24-7 D4 E5 D6 E7

0x28-B 89 9A AB BC

0x2C-F CD DE EF F0

0x30-3 BA 0A BA 0A

0x34-7 DB 0B DB 0B

0x38-B EC 0C EC 0C

0x3C-F FC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

physical addresses	byt	es		
0x00-3			22	33
0x04-7	44	55	66	77
0x08-B	88	99	AΑ	ВВ
0x0C-F	CC	DD	EE	FF
0x10-3	1A	2A	3A	4A
0x14-7	1В	2B	3B	4B
0x18-B				
0x1C-F	AC	ВС	DC	EC

```
physical bytes
addresses
0x20-3D0 E1 D2 D3
0x24-7D4 E5 D6 E7
0x28-Bl89 9A AB BC
0x2C-FCD DE EF F0
0x30-3|BA 0A BA 0A
0x34-7DB 0B DB 0B
0x38-B|EC 0C EC 0C
0x3C-FIFC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

physical addresses	byt	es		
0x00-3			22	33
0x04-7	44	55	66	77
0x08-B				
0x0C-F	CC	DD	EE	FF
0x10-3	1A	2A	3A	4A
0x14-7				
0x18-B	1C	2C	3C	4C
0x1C-F	AC	ВС	DC	EC

```
physical addresses

0x20-3 D0 E1 D2 D3

0x24-7 D4 E5 D6 E7

0x28-B 89 9A AB BC

0x2C-F CD DE EF F0

0x30-3 BA 0A BA 0A

0x34-7 DB 0B DB 0B

0x38-B EC 0C EC 0C

0x3C-F FC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

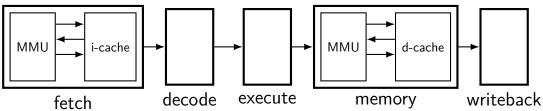
page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

physical addresses	byt	es		
0x00-3	00	11	22	33
0x04-7	44	55	66	77
0x08-B	88	99	AΑ	ВВ
0x0C-F				
0x10-3	1A	2A	3A	4A
0x14-7	1В	2B	3B	4B
0x18-B			3C	
0x1C-F	AC	ВС	DC	EC

```
physical bytes addresses 0x20-3 D0 E1 D2 D3 0x24-7 D4 E5 D6 E7 0x28-B 89 9A AB BC 0x2C-F CD DE EF F0 0x30-3 BA 0A BA 0A 0x34-7 DB 0B DB 0B 0x38-B EC 0C EC 0C 0x3C-F FC 0C FC 0C
```

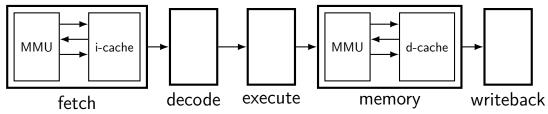
backup slides

MMUs in the pipeline



up to four memory accesses per instruction

MMUs in the pipeline



up to four memory accesses per instruction challenging to make this fast (topic for a future date)

do we really need a complete copy?

basn
Used by OS
Stack
Heap / other dynamic
Writable data

hach

new copy of bash Used by OS Stack Heap / other dynamic Writable data Code + Constants

do we really need a complete copy?

bash	new copy of bash			
Used by OS	Used by OS			
Stack	Stack			
Heap / other dynamic	Heap / other dynamic			
Writable data	Writable data			
Code + Constants	Code + Constants			

shared as read-only

do we really need a complete copy?

bash	new copy of bash		
Used by OS	Used by OS		
Stack	Stack		
Heap / other dynamic	Heap / other dynamic		
Writable data	Writable data		
Code + Constants can't be shared? Code + Constants			

trick for extra sharing

sharing writeable data is fine — until either process modifies it example: default value of global variables might typically not change (or OS might have preloaded executable's data anyways)

can we detect modifications?

trick for extra sharing

```
sharing writeable data is fine — until either process modifies it example: default value of global variables might typically not change (or OS might have preloaded executable's data anyways)
```

can we detect modifications?

trick: tell CPU (via page table) shared part is read-only processor will trigger a fault when it's written

VPN

... 0x00601 0x00602 0x00603 0x00604 0x00605 valid? write?

		page
•••	•••	•••
1	1	0x12345
1	1	0x12347
1	1	0x12340
1	1	0x200DF
1	1	0x200AF
•••	•••	•••

VPN
•••
0x00601
0x00602
0x00603 0x00604
$0 \times 0 0 6 0 4$ $0 \times 0 0 6 0 5$

physical valid? write? page				
•••	•••	•••		
1	0	0x12345		
1	0	0x12347		
1	0	0x12340		
1	0	0x200DF		
1	0	0x200AF		
•••	•••	•••		

•••
0x00601
0x00602
0x00603
0x00604
0x00605

VPN

valid? w	write?	physical page
vana.	vviice.	page

•••	•••	•••
1	0	0x12345
1	0	0x12347
1	0	0x12340
1	0	0x200DF
1	0	0x200AF
•••	•••	•••

copy operation actually duplicates page table both processes share all physical pages but marks pages in both copies as read-only

physical

VPN	valid? write? page				
VIIV	vana.	page			
•••	•••	•••	•••		
0x00601	1	0	0x12345		
0x00602	1	0	0x12347		
0x00603	1	0	0x12340		
0x00604	1	0	0x200DF		
0x00605	1	0	0x200AF		
•••	•••	•••	•••		

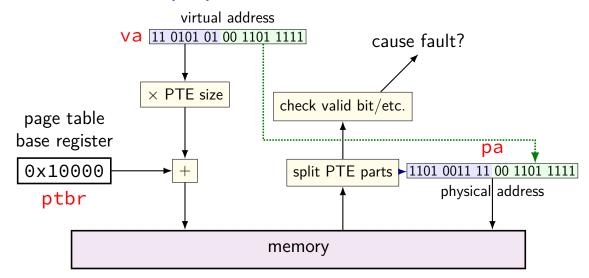
VPN	valid?	write	pnysicai page
•••	•••	•••	
0x00601	1	0	0x12345
0x00602	1	0	0x12347
0x00603	1	0	0x12340
0x00604	1	0	0x200DF
0x00605	1	0	0x200AF
•••	•••	•••	•••

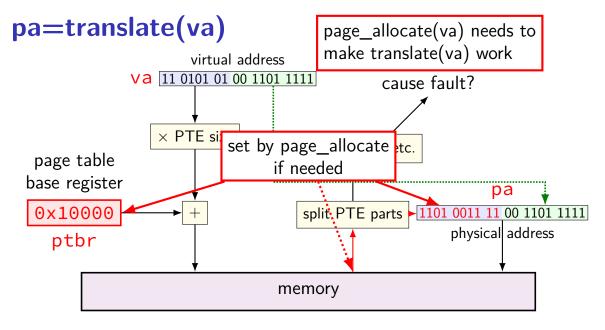
when either process tries to write read-only page triggers a fault — OS actually copies the page

VPN	valid?	writo	physical Page	VPN	valid?	writo	physical page
VIIN	vallu:	WIILE	[:] page	VIIN	valiu:	wille:	page
•••	•••	•••	•••	•••	•••	•••	•••
0x00601	1	0	0x12345	0x00601	1	0	0x12345
0x00602	1	0	0x12347	0x00602	1	0	0x12347
0x00603	1	0	0x12340	0x00603	1	0	0x12340
0x00604	1	0	0x200DF	<u>0x00604</u>	1	0	0x200DF
0x00605	1	0	0x200AF	0x00605	1	1	0x300FD
•••	•••	•••	•••	•••	•••	•••	•••

after allocating a copy, OS reruns the write instruction

pa=translate(va)





swapping

early motivation for virtual memory: swapping

using disk (or SSD, ...) as the next level of the memory hierarchy how our textbook and many other sources presents virtual memory

OS allocates program space on disk own mapping of virtual addresses to location on disk

DRAM is a cache for disk

swapping

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swapping components

```
"swap in" a page — exactly like allocating on demand!

OS gets page fault — invalid in page table
check where page actually is (from virtual address)
read from disk
eventually restart process

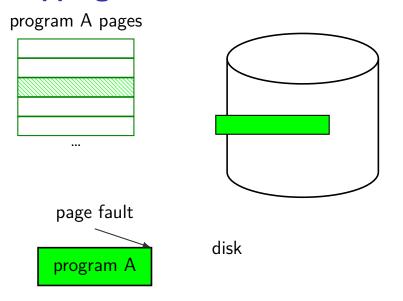
"swap out" a page
OS marks as invalid in the page table(s)
copy to disk (if modified)
```

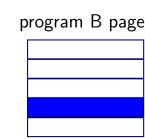
HDD reads and writes: milliseconds to tens of milliseconds minimum size: 512 bytes writing tens of kilobytes basically as fast as writing 512 bytes

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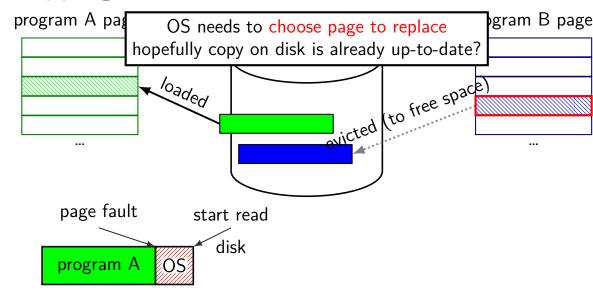
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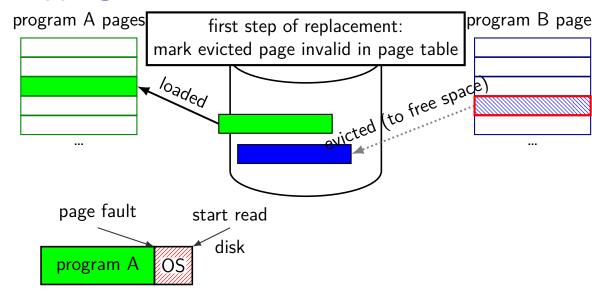
HDD reads and writes: milliseconds to tens of milliseconds minimum size: 512 bytes writing tens of kilobytes basically as fast as writing 512 bytes

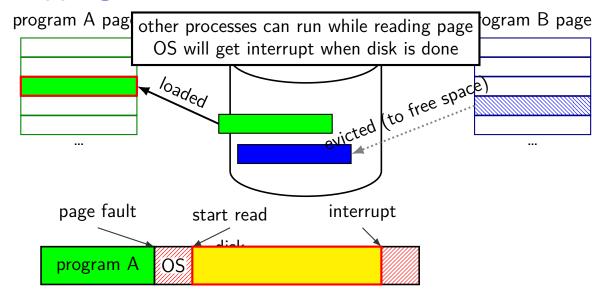


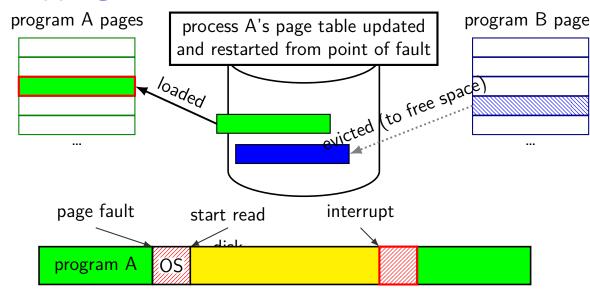


...









swapping almost mmap

```
access mapped file for first time, read from disk (like swapping when memory was swapped out)
```

```
write "mapped" memory, write to disk eventually (like writeback policy in swapping) use "dirty" bit
```

extra detail: other processes should see changes all accesses to file use same physical memory