last time

storing page tables in memory

as array of page table entries

page table entries encoded as integer

page table base register — OS tells CPU base address of array

each program memory access = two real ones

preview: multi-level page table lookup

lab this week

no lab

a subset of TAs will be in Rice 130 to give office-hour-type help

anonymous feedback (1)

got this last Tuesday, missed addressing last Thursday (sorry!)

"Can you make the quizzes have more number of questions and/or each MCQ be worth less points? The percentage scores decreases drastically by making just one mistake. The quiz is also worth a huge portion of the final grade and being able to do better on it would help get a good grade."

probably should be some more questions, but I think I'd get more complaints if I really embraced more questions would like to use comments to give more naunce in quiz grades

quiz Q4

```
0x300010: movq %rax, (%rcx)
```

to execute:

```
access 0x300010 to read machine code — VPN 0x300 read %rax (no memory access) = 0x999000 read %rcx (no memory access) = 0x123450 write to 0x123450 to write %rax value — VPN 0x123
```

quiz Q5

```
accessing 0x30110 = 0x30000 + 0x110 = 0x30000 + 0x44 * 4
```

VPN = 0x44

page offset is 0x9433 (same in physical + virtual)

quiz Q6

usually I would say something that causes exception != can access

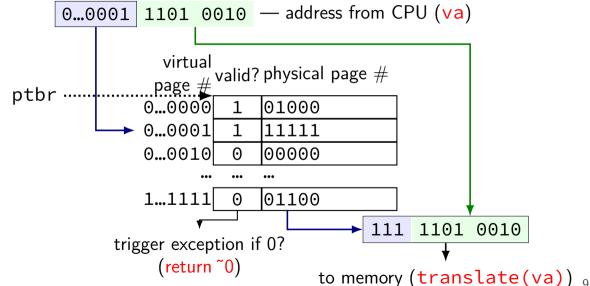
re: virtual/physical address bits could have most page table entries be invalid (in both)

anonymous feedback (2)

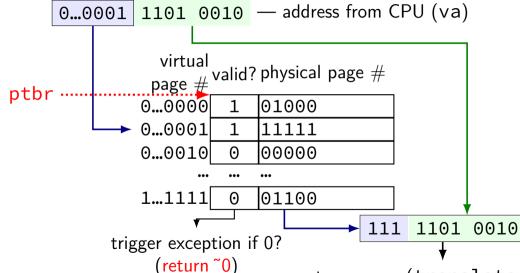
"I was hoping to have a little lecture time dedicated to explaining the nuances to the homework assignment, especially a clarification for what ptbr points to, and the difference between VPN and Physical page numbers in the context of this homework assignment"

"Do you mind re-visiting and explaining page_allocate()'s behavior?"

page table lookup (and translate())

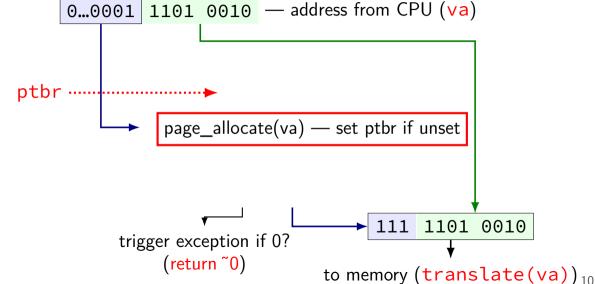


page table lookup (and translate())

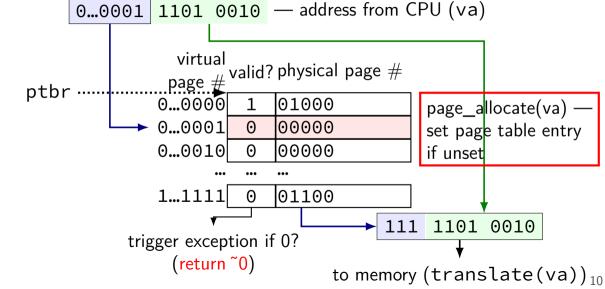


to memory (translate(va)) o

page table lookup (and allocate)



page table lookup (and allocate)



ptbr in assignment

```
size_t ptbr; points to beginning of (primary) page table initially 0 = doesn't point to anything
```

filled in by first call to page_allocate or by testing code

typical timings

task	typical time (order of magnitude)
empty function	nanosecond
getppid (syscall)	microsecond
system(/bin/true) (run program)	milliseconds
start signal handler	microseconds
signal ping/pong (context switch?)	tens of microseconds

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

top 16 bits of 64-bit addresses not used for translation

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: how many page table entries? (assuming page table like shown before)

exercise: how large are physical page numbers?

my desktop: 39-bit physical addresses; 48-bit virtual addresses

4096 byte pages

exercise: how many page table entries? (assuming page table like shown before) $2^{48}/2^{12}=2^{36}$ entries

exercise: how large are physical page numbers? 39 - 12 = 27 bits

my desktop: 39-bit physical addresses; 48-bit virtual addresses 4096 byte pages

exercise: how many page table entries? (assuming page table like shown before) $2^{48}/2^{12}=2^{36}$ entries

exercise: how large are physical page numbers? 39-12=27 bits page table entries are 8 bytes (room for expansion, metadata) trick: power of two size makes table lookup faster

would take up 2^{39} bytes?? (512GB??)

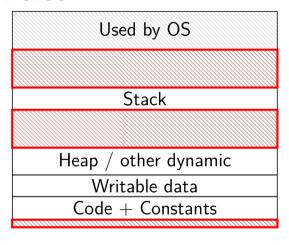
huge page tables

huge virtual address spaces!

impossible to store PTE for every page

how can we save space?

holes



most pages are invalid

saving space

basic idea: don't store (most) invalid page table entries
use a data structure other than a flat array
 want a map — lookup key (virtual page number), get value (PTE)
options?

saving space

```
basic idea: don't store (most) invalid page table entries
use a data structure other than a flat array
    want a map — lookup key (virtual page number), get value (PTE)
options?
```

hashtable

actually used by some historical processors but never common

saving space

basic idea: don't store (most) invalid page table entries
use a data structure other than a flat array
want a map — lookup key (virtual page number), get value (PTE)

options?

hashtable actually used by some historical processors

but never common

tree data structure

but not quite a search tree

search tree tradeoffs

lookup usually implemented in hardware

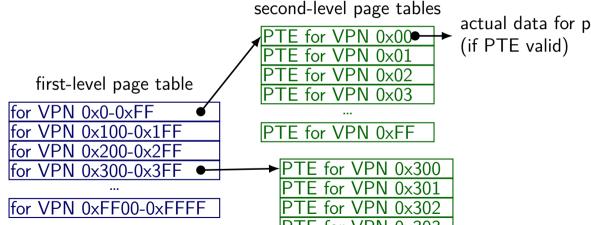
lookup should be simple solution: lookup splits up address bits (no complex calculations)

lookup should not involve many memory accesses

doing two memory accesses is already very slow solution: tree with many children from each node

(far from binary tree's left/right child)

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)



LONG OFF

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)

second-level page tables

PTE for VPN 0x00

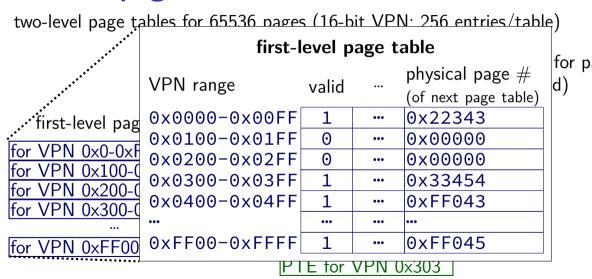
PTE for VPN 0x01

PTE for VPN 0x02

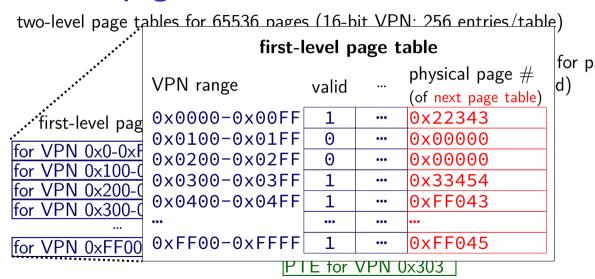
PTE for VPN 0x02

PTE for VPN 0x03

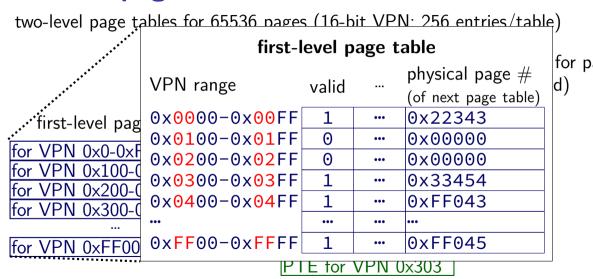
for VPN 0x0-0xFF VPN 0x100-0x1FF invalid entries represent big holes 0x200-0x2FFVPN 0x300 for VPN 0x300-0x3FF VPN 0x301 for VPN 0xFF00-0xFFFF LONG OFF



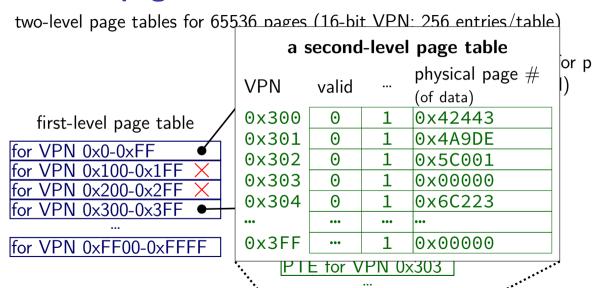
V/DNI A AFE



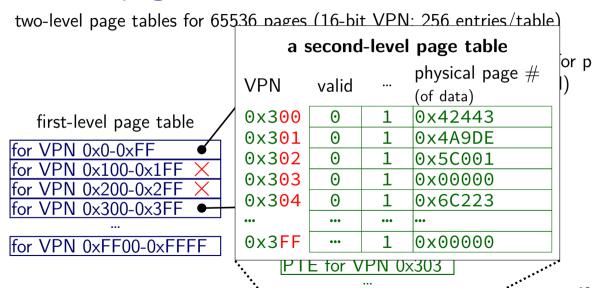
V/DNI A AFF



V/DNI A AFE

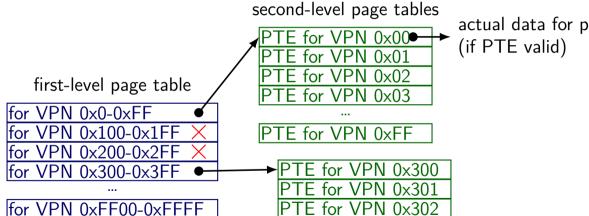


V/DNI A AFE



V/DNI A AFE

two-level page tables for 65536 pages (16-bit VPN; 256 entries/table)



LONG OFF

two-level page table lookup

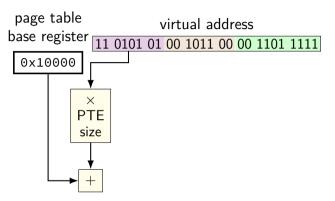
virtual address

11 0101 01 00 1011 00 00 1101 1111

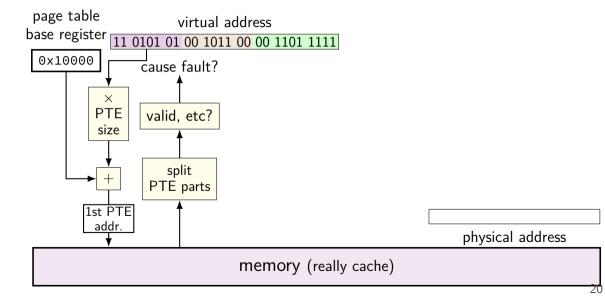
VPN — split into two parts (one per level)

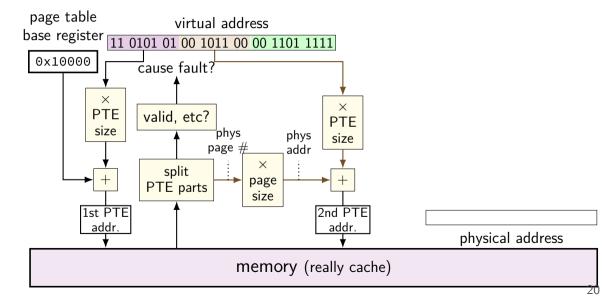
this example: parts equal sized — common, but not required

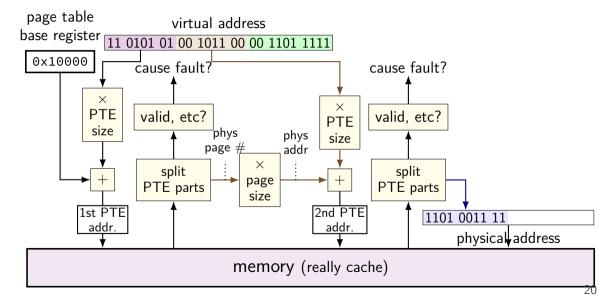
two-level page table lookup

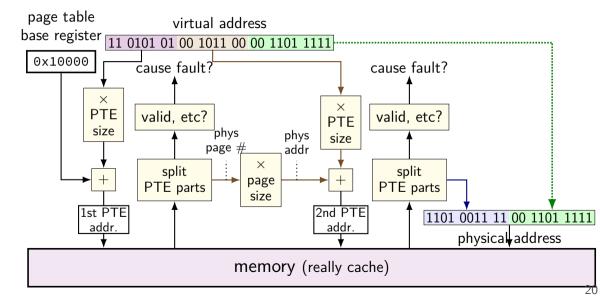


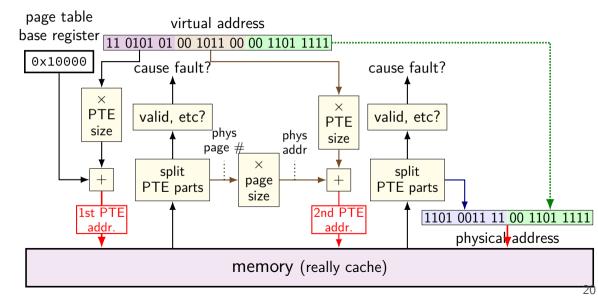
two-level page table lookup

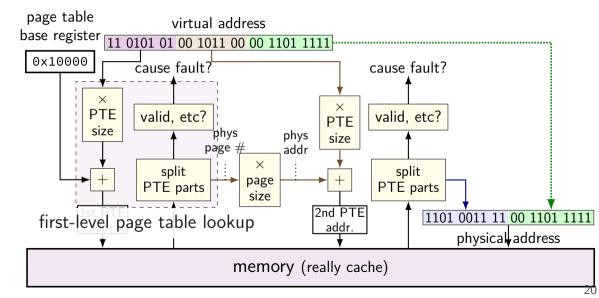


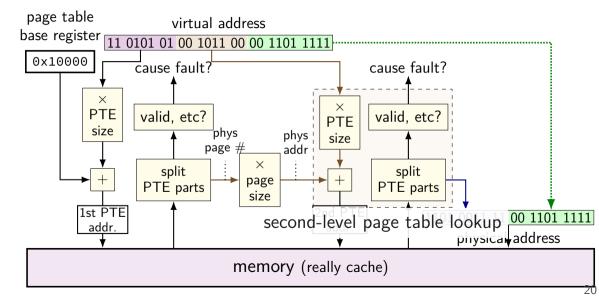


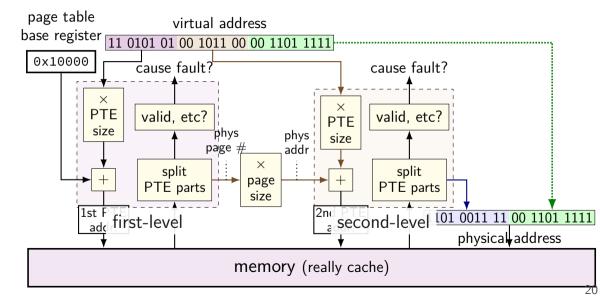


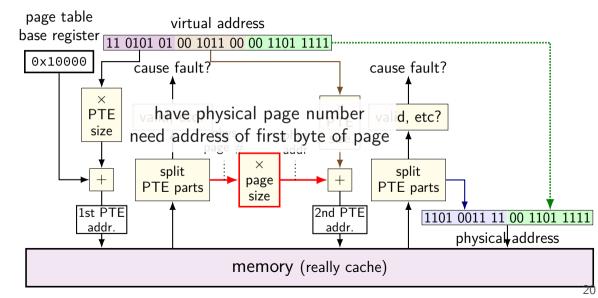


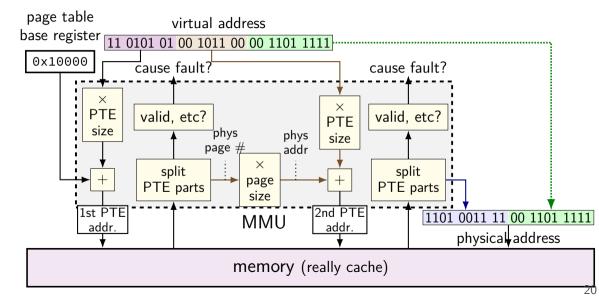




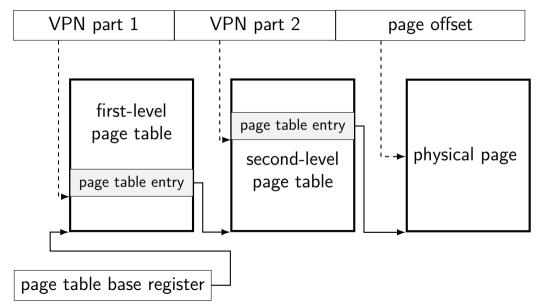








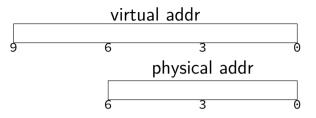
another view



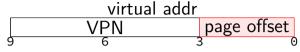
2

9-bit virtual address

6-bit physical address



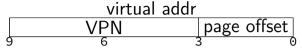
- 9-bit virtual address
- 6-bit physical address
- 8-byte pages \rightarrow 3-bit page offset (bottom) $\frac{1}{6}$
- 9-bit VA: 6 bit VPN + 3 bit PO
- 6-bit PA: 3 bit PPN + 3 bit PO



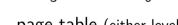
physical addr

page offset

- 9-bit virtual address
- 6-bit physical address
- 8-byte pages \rightarrow 3-bit page offset (bottom)
- 9-bit VA: 6 bit VPN + 3 bit PO
- 6-bit PA: 3 bit PPN + 3 bit PO
- O-BILLIA. S BILLIAN | S BILLIO
- 1 page page tables w/ 1 byte entry \rightarrow 8 entry PTs



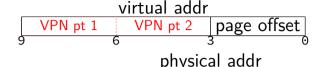


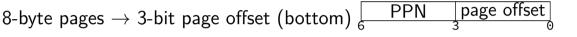


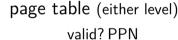
- page table (either level)
 - valid? PPN
 - 0 | |
 -

- 9-bit virtual address
- 6-bit physical address
- 9-bit VA: 6 bit VPN + 3 bit PO
- 6-bit PA: 3 bit PPN + 3 bit PO
- 0-bit FA. 3 bit FFN + 3 bit FO
- 8 entry page tables \rightarrow 3-bit VPN parts
- 9-bit VA: 3 bit VPN part 1; 3 bit VPN part 2

1 page page tables w/ 1 byte entry \rightarrow 8 entry PTs









9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x20; translate virtual address 0x129

physical addresses	bytes				physical bytes addresses				
addresses					addresses				
0x00-3			22	33	0x20-3	00	91	72	13
0x04-7	44	55	66	77	0x24-7	F4	Α5	36	07
0x08-B	88	99	AΑ	ВВ	0x28-B	89	9A	ΑB	ВС
0x0C-F	CC	DD	ΕE	FF	0x2C-F	CD	DE	EF	F0
0x10-3	1A	2A	ЗА	4A	0x30-3	ВА	0Α	ВА	0Α
0x14-7	1B	2B	3B	4B	0x34-7	DB	0B	DB	0B
0x18-B	10	2C	3C	4C	0x38-B	EC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C-F	ΑC	DC	DC	0C

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x20; translate virtual address 0x129

```
physical bytes
                                                0x129 = 1 0010 1001
addresses
                                                0x20 + 0x4 \times 1 = 0x24
0 \times 00 - 3 | 00 \ 11 \ 22 \ 33
                         0x20-3|00 91 72 13
                                                PTE 1 value:
0 \times 04 - 7 | 44 55 66 77
                         0x24-7|_{F4} A5 36 07
                                                0xF4 = 1111 0100
                         0x28-Bl89 9A AB BC
0x08-Bl88 99 AA BB
                                                PPN 111. valid 1
0x0C-FCC DD EE FF
                         0x2C-FCD DE EF F0
                         0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
0x14-7|1B 2B 3B 4B
                         0x34-7DB 0B DB 0B
0x18-Bl1C 2C 3C 4C
                         0x38-BIEC 0C EC 0C
0x1C-F|1C 2C 3C 4C
                         0x3C-FIAC DC DC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

```
physical bytes
                                                  0 \times 129 = 1 \ 0010 \ 1001
addresses
                                                  0x20 + 0x4 \times 1 = 0x24
0 \times 00 - 3 | 00 \ 11 \ 22 \ 33
                          0x20-3|00 91 72 13
                                                  PTE 1 value:
                          0x24-7|F4 A5 36 07
0 \times 04 - 7 | 44 55 66 77
                                                  0xF4 = 1111 0100
                          0x28-Bl89 9A AB BC
0x08-Bl88 99 AA BB
                                                  PPN 111. valid 1
0x0C-FCC DD EE FF
                          0x2C-FCD DE EF F0
                                                  PTE 2 addr:
                          0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                                   111 \ 000 + 101 \times 1 = 0 \times 3D
                          0x34-7DB 0B DB 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                                   PTE 2 value: 0xDC
0x18-Bl1C 2C 3C 4C
                          0x38-BIEC 0C EC 0C
0×1C-F|1C 2C 3C 4C
                          0x3C-FIAC DC DC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x20; translate virtual address 0x129

```
physical bytes
                            physical <sub>bytes</sub>
                                                      0 \times 129 = 1 \ 0010 \ 1001
addresses
                            addresses
                                                      0x20 + 0x4 \times 1 = 0x24
0x00-3|00 11 22 33
                            0 \times 20 - 3 | 00 \ 91 \ 72 \ 13
                                                      PTE 1 value:
0 \times 04 - 7 | 44 55 66 77
                            0x24-7|F4 A5 36 07
                                                      0 \times F4 = 1111 \ 0100
                            0x28-B|89 9A AB BC
0x08-Bl88 99 AA BB
                                                      PPN 111. valid 1
0x0C-FCC DD EE FF
                            0x2C-FCD DE EF F0
                                                      PTE 2 addr:
0 \times 10 - 3 | 1A 2A 3A 4A
                            0x30-3|BA 0A BA 0A
                                                      111 \ 000 + 101 \times 1 = 0x3D
                                                      PTE 2 value: 0xDC
0 \times 14 - 7 | 1B 2B 3B 4B
                            0 \times 34 - 7 \mid DB \mid 0B \mid DB \mid 0B
                            0x38-BIEC 0C EC 0C
                                                      PPN 110; valid 1
0x18-Bl1C 2C 3C 4C
                                                      M[110 \ 001 \ (0x31)] = 0x0A
0x1C-F|1C 2C 3C 4C
                            0x3C-FAC DC DC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

```
physical bytes
                            physical <sub>bytes</sub>
                                                      0 \times 129 = 1 \ 0010 \ 1001
addresses
                            addresses
                                                      0x20 + 0x4 \times 1 = 0x24
0x00-3|00 11 22 33
                            0 \times 20 - 3 | 00 \ 91 \ 72 \ 13
                                                      PTE 1 value:
0 \times 04 - 7 | 44 55 66 77
                            0x24-7|F4 A5 36 07
                                                      0 \times F4 = 1111 \ 0100
                            0x28-B|89 9A AB BC
0x08-Bl88 99 AA BB
                                                      PPN 111. valid 1
0x0C-FCC DD EE FF
                            0x2C-FCD DE EF F0
                                                      PTE 2 addr:
0 \times 10 - 3 | 1A 2A 3A 4A
                            0x30-3|BA 0A BA 0A
                                                      111 \ 000 + 101 \times 1 = 0x3D
                                                      PTE 2 value: 0xDC
0 \times 14 - 7 | 1B 2B 3B 4B
                            0 \times 34 - 7 \mid DB \mid 0B \mid DB \mid 0B
                            0x38-BIEC 0C EC 0C
                                                      PPN 110; valid 1
0x18-Bl1C 2C 3C 4C
                                                      M[110 \ 001 \ (0x31)] = 0x0A
0x1C-F|1C 2C 3C 4C
                            0x3C-FAC DC DC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x20; translate virtual address 0x129

```
physical bytes
                             physical <sub>bytes</sub>
                                                      0 \times 129 = 1 \quad 0010 \quad 1001
addresses
                            addresses
                                                      0x20 + 0x4 \times 1 = 0x24
0x00-3|00 11 22 33
                            0 \times 20 - 3 | 00 \ 91 \ 72 \ 13
                                                      PTE 1 value:
0 \times 04 - 7 | 44 55 66 77
                            0x24-7|F4 A5 36 07
                                                      0 \times F4 = 1111 \ 0100
                            0x28-B|89 9A AB BC
0x08-Bl88 99 AA BB
                                                      PPN 111. valid 1
0x0C-FCC DD EE FF
                            0x2C-FCD DE EF F0
                                                      PTE 2 addr:
0 \times 10 - 3 | 1A 2A 3A 4A
                            0x30-3|BA 0A BA 0A
                                                       111 000 + 101 \times 1 = 0x3D
                                                      PTE 2 value: 0xDC
0 \times 14 - 7 | 1B 2B 3B 4B
                            0 \times 34 - 7 \mid DB \mid 0B \mid DB \mid 0B
                            0x38-BIEC 0C EC 0C
                                                      PPN 110; valid 1
0x18-Bl1C 2C 3C 4C
                                                      M[110 \ 001 \ (0x31)] = 0x0A
0x1C-F|1C 2C 3C 4C
                            0x3C-FAC DC DC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused; page table base register 0x08; translate virtual address 0x0FB

```
physical bytes
addresses
0 \times 00 - 3 | 00 \ 11 \ 22 \ 33
                          0x20-3|D0 D1 D2 D3
0 \times 04 - 7 | 44 55 66 77
                          0x24-7D4 D5 D6 D7
                          0x28-Bl89 9A AB BC
0x08-Bl88 99 AA BB
0x0C-FCC DD EE FF
                          0x2C-FCD DE EF F0
                          0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                          0x34-7DB 0B DB 0B
0 \times 14 - 7 | 1B 2B 3B 4B
0x18-Bl1C 2C 3C 4C
                          0x38-BIEC 0C EC 0C
0x1C-F|1C 2C 3C 4C
                          0x3C-FIFC 0C FC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

```
physical bytes
                         physical <sub>bytes</sub>
addresses
                                                0 \times 0 = 011 \ 111 \ 011
0x00-3|00 11 22 33
                         0x20-3|D0 D1 D2 D3
                                                (PTE 1 addr: 0x08 +
                         0x24-7D4 D5 D6 D7
0x04-7|44 55 66 77
                                                PTE size times 011 (3))
0x08-B|88 99 AA BB
                         0x28-B|89 9A AB BC
                                                PTE 1: 0xBB at 0x0B
0x0C-FCC DD EE FF
                         0x2C-FCD DE EF F0
                                                PTE 1: PPN 101 (5) valid 1
0x10-3|1A 2A 3A 4A
                         0x30-3|BA 0A BA 0A
                                                PTE 2: 0xF0 at 0x2F
                         0 \times 34 - 7 | DB | 0B | DB | 0B
0x14-7|1B 2B 3B 4B
                                                PTE 2: PPN 111 (7) valid 1
0x18-Bl1C 2C 3C 4C
                         0x38-BIEC 0C EC 0C
                                                111 \ 011 = 0x3B \rightarrow 0x0C
0x1C-F|1C 2C 3C 4C
                         0x3C-FIFC 0C FC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

```
physical bytes
                         physical <sub>bytes</sub>
addresses
                                                0 \times 0 = 011 \ 111 \ 011
0x00-3|00 11 22 33
                         0x20-3|D0 D1 D2 D3
                                                (PTE 1 addr: 0x08 +
                         0x24-7D4 D5 D6 D7
0x04-7|44 55 66 77
                                                PTE size times 011 (3))
0x08-B|88 99 AA BB
                         0x28-B|89 9A AB BC
                                                PTE 1: 0xBB at 0x0B
0x0C-FCC DD EE FF
                         0x2C-FCD DE EF F0
                                                PTE 1: PPN 101 (5) valid 1
0x10-3|1A 2A 3A 4A
                         0x30-3|BA 0A BA 0A
                                                PTE 2: 0xF0 at 0x2F
                         0 \times 34 - 7 | DB | 0B | DB | 0B
0x14-7|1B 2B 3B 4B
                                                PTE 2: PPN 111 (7) valid 1
0x18-Bl1C 2C 3C 4C
                         0x38-BIEC 0C EC 0C
                                                111 \ 011 = 0x3B \rightarrow 0x0C
0x1C-F|1C 2C 3C 4C
                         0x3C-FIFC 0C FC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

```
physical bytes
                         physical <sub>bytes</sub>
addresses
                                                0 \times 0 = 011 \ 111 \ 011
0x00-3|00 11 22 33
                         0x20-3|D0 D1 D2 D3
                                                (PTE 1 addr: 0x08 +
                         0x24-7D4 D5 D6 D7
0x04-7|44 55 66 77
                                                PTE size times 011 (3))
0x08-B|88 99 AA BB
                         0x28-B|89 9A AB BC
                                                PTE 1: 0xBB at 0x0B
0x0C-FCC DD EE FF
                         0x2C-FCD DE EF F0
                                                PTE 1: PPN 101 (5) valid 1
0x10-3|1A 2A 3A 4A
                         0x30-3|BA 0A BA 0A
                                                PTE 2: 0xF0 at 0x2F
                         0 \times 34 - 7 | DB | 0B | DB | 0B
0x14-7|1B 2B 3B 4B
                                                PTE 2: PPN 111 (7) valid 1
0x18-Bl1C 2C 3C 4C
                         0x38-BIEC 0C EC 0C
                                                111 \ 011 = 0x3B \rightarrow 0x0C
0x1C-F|1C 2C 3C 4C
                         0x3C-FIFC 0C FC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

```
physical bytes
                         physical <sub>bytes</sub>
addresses
                                                0 \times 0 = 011 \ 111 \ 011
0x00-3|00 11 22 33
                         0x20-3|D0 D1 D2 D3
                                                (PTE 1 addr: 0x08 +
                         0x24-7D4 D5 D6 D7
0x04-7|44 55 66 77
                                                PTE size times 011 (3))
0x08-B|88 99 AA BB
                         0x28-B|89 9A AB BC
                                                PTE 1: 0xBB at 0x0B
0x0C-FCC DD EE FF
                         0x2C-FCD DE EF F0
                                                PTE 1: PPN 101 (5) valid 1
0x10-3|1A 2A 3A 4A
                         0x30-3|BA 0A BA 0A
                                                PTE 2: 0xF0 at 0x2F
                         0 \times 34 - 7 | DB | 0B | DB | 0B
0x14-7|1B 2B 3B 4B
                                                PTE 2: PPN 111 (7) valid 1
0x18-Bl1C 2C 3C 4C
                         0x38-BIEC 0C EC 0C
                                                111 \ 011 = 0x3B \rightarrow 0x0C
0x1C-F|1C 2C 3C 4C
                         0x3C-FIFC 0C FC 0C
```

multi-level page tables

VPN split into pieces for each level of page table

top levels: page table entries point to next page table usually using physical page number of next page table

bottom level: page table entry points to destination page

validity checks at each level

note on VPN splitting

indexes used for lookup parts of the virtual page number (there are not multiple VPNs)

splitting addresses

```
if:
```

256-byte (2⁸ byte) pages 4-byte page table entries 3 levels of page tables page tables take up 1 page

Q1: page offset size (bits)

A. <= 4 B. 5-7 C. 8-11 D. 12-15 E. >15

Q2: virtual page number size (bits)

A. <=4 B. 5-7 C. 8-11 D. 12-15 E. >15

Q3: split address 0x1234

backup slides

x86-64 page table splitting

48-bit virtual address

12-bit page offset (4KB pages)

36-bit virtual page number, split into four 9-bit parts

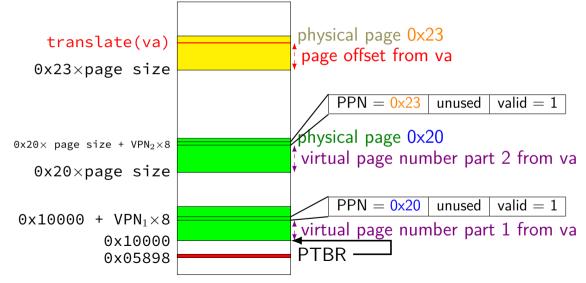
page tables at each level: 2^9 entries, 8 bytes/entry page tables take up 4KB (1 page)

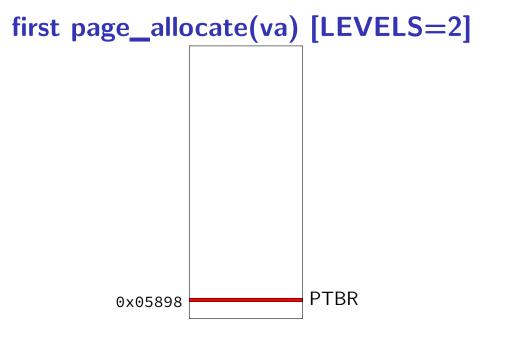
assignment part 2/3

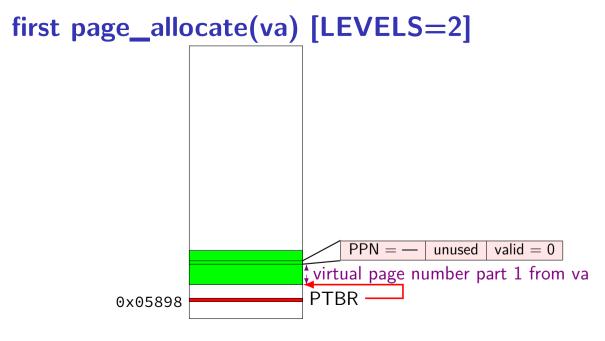
supporting arbitrary numbers of LEVELS, POBITS

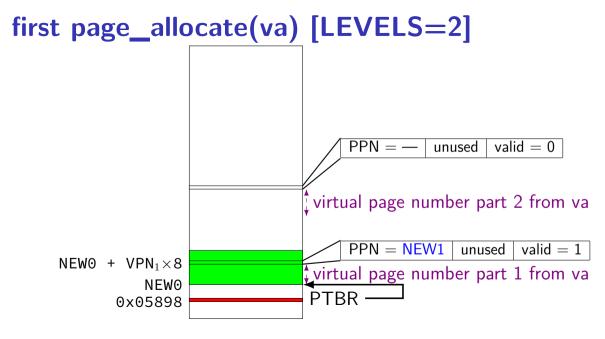
code review in lab after reading days limited allowed collaboration

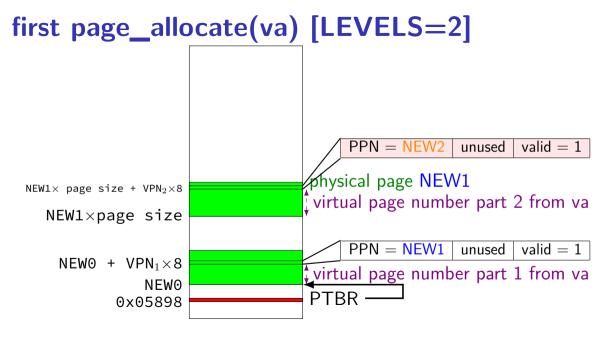
pa = translate(va) [LEVELS=2]

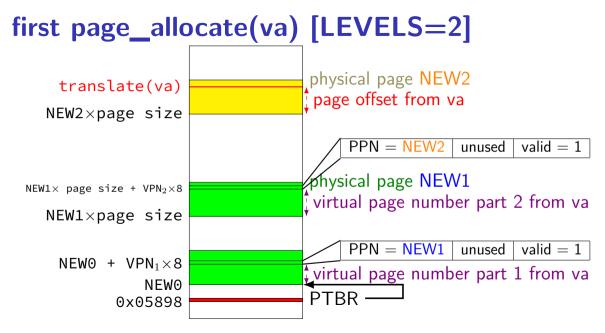












later page allocates?

some of those allocations done earlier e.g. ptbr already set

should reuse existing allocation then

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused; page table base register 0x10; translate virtual address 0x109

physical addresses	byte	es			physica addresses	l byt	es		
addresses					addresse	s			
0x00-3	00	11	22	33	0x20-3	3 D0	D1	D2	D3
0x04-7	44	55	66	77	0x24-7	'D4	D5	D6	D7
0x08-B	88	99	AA	ВВ	0x28-E	89	9A	ΑB	ВС
0x0C-F	CC	DD	EE	FF	0x2C-F	CD	DE	EF	F0
0x10-3	1A	2A	5A	4A	0x30-3	BA	0A	ВА	0Α
0x14-7	1В	2B	3B	4B	0x34-7	DB	0B	DB	0B
0x18-B	1C	2C	3C	4C	0x38-E	BEC	0C	EC	0C
0x1C-F	1C	2C	3C	4C	0x3C-F	FC	0C	FC	0C

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

```
page table base register 0x10; translate virtual address 0x109 physical bytes physical bytes 0x109 = 100 011 001
```

 $0 \times 00 - 3 00 \ 11 \ 22 \ 33$ $0 \times 20 - 3 \ D0 \ D1 \ D2 \ D3$ $0 \times 10 + PTE \ size \ times \ 4 \ (100)$

0x0C-F CC DD EE FF
0x10-3 1A 2A 5A 4A
0x14-7 1B 2B 3B 4B
0x2C-F CD DE EF F0
0x30-3 BA 0A BA 0A
0x34-7 DB 0B DB 0B
0x34-7 DB 0B DB 0B DB 0B
0x34-7 DB 0B DB 0B DB 0B
0

 $0 \times 14 - 7$ 1B 2B 3B 4B $0 \times 34 - 7$ DB 0B DB 0B PTE 2: 0×33 at 0×03 $0 \times 18 - B$ 1C 2C 3C 4C $0 \times 38 - B$ EC 0C EC 0C PTE 2: PPN 001 (1) valid 1 $0 \times 1C - F$ 1C 2C 3C 4C $0 \times 3C - F$ FC 0C FC 0C 001 $001 = 0 \times 09 \rightarrow 0 \times 99$

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

```
page table base register 0 \times 10; translate virtual address 0 \times 109
```

physical bytes physical _{bytes} $0 \times 109 = 100 \ 011 \ 001$ addresses (PTE 1 at: 0x00-300 11 22 33 0x20-3|D0 D1 D2 D3

0x10 + PTE size times 4 (100)) 0x04-7|44 55 66 77 0x24-7D4 D5 D6 D7

PTE 1: 0x1B at 0x14 0x08-B|88 99 AA BB 0x28-B|89 9A AB BC PTE 1: PPN 000 (0) valid 1 0x0C-FCC DD EE FF 0x2C-FCD DE EF F0 (second table at:

0x10-3|1A 2A 5A 4A 0x30-3|BA 0A BA 0A 0 (000) times page size = 0×00) 0x14-7|1B 2B 3B 4B $0 \times 34 - 7 \mid DB \mid 0B \mid DB \mid 0B$ PTE 2: 0x33 at 0x03 0x18-Bl1C 2C 3C 4C 0x38-BIEC 0C EC 0C PTE 2: PPN 001 (1) valid 1 $001 \ 001 = 0x09 \rightarrow 0x99$ 0x1C-F|1C 2C 3C 4C 0x3C-FIFC 0C FC 0C

0x1C-F|1C 2C 3C 4C

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

```
page table base register 0 \times 10; translate virtual address 0 \times 109
```

physical bytes physical _{bytes} $0 \times 109 = 100 \ 011 \ 001$ addresses (PTE 1 at:

0x00-300 11 22 33 0x20-3|D0 D1 D2 D3 0x10 + PTE size times 4 (100)) 0x04-7|44 55 66 77 0x24-7D4 D5 D6 D7

PTF 1: 0x1B at 0x14 0x08-B|88 99 AA BB 0x28-B|89 9A AB BC PTE 1: PPN 000 (0) valid 1 0x0C-FCC DD EE FF 0x2C-FCD DE EF F0 (second table at:

0x10-3|1A 2A 5A 4A 0x30-3|BA 0A BA 0A 0 (000) times page size = 0×00) 0x14-7|1B 2B 3B 4B $0 \times 34 - 7 \mid DB \mid 0B \mid DB \mid 0B$ PTF 2: 0x33 at 0x03 0x18-Bl1C 2C 3C 4C 0x38-BIEC 0C EC 0C PTE 2: PPN 001 (1) valid 1 $001 \ 001 = 0x09 \rightarrow 0x99$

0x3C-FIFC 0C FC 0C

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE

page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused;

```
page table base register 0x10; translate virtual address 0x109
```

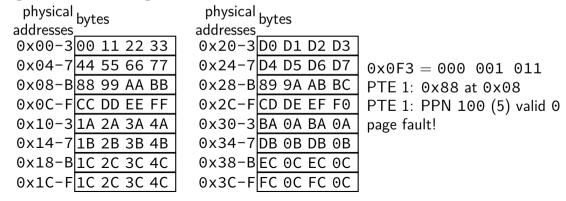
physical bytes addresses physical bytes addresses $0 \times 0 = 100 \$

0x08-B 88 99 AA BB
0x0C-F CC DD EE FF
0x10-3 1A 2A 5A 4A
0x24-7 D4 D3 D6 D7
PTE 1: 0x1B at 0x14
PTE 1: 0x1B at 0x14
PTE 1: PPN 000 (0) valid 1
(second table at:
0x30-3 BA 0A BA 0A
0 (000) times page size = 0x00

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x08; translate virtual address 0x00B

physical bytes addresses $0 \times 00 - 3 | 00 \ 11 \ 22 \ 33$ 0x20-3|D0 D1 D2 D3 0x04-7|44 55 66 77 0x24-7D4 D5 D6 D7 0x28-Bl89 9A AB BC 0x08-Bl88 99 AA BB 0x0C-FCC DD EE FF 0x2C-FCD DE EF F0 0x30-3|BA 0A BA 0A $0 \times 10 - 3 | 1A 2A 3A 4A$ 0x34-7DB 0B DB 0B $0 \times 14 - 7 | 1B 2B 3B 4B$ 0x18-Bl1C 2C 3C 4C 0x38-BIEC 0C EC 0C 0x1C-F|1C 2C 3C 4C 0x3C-FIFC 0C FC 0C

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x08; translate virtual address 0x00B



9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x08; translate virtual address 0x00B

```
physical bytes
addresses
0x00-3|00 11 22 33
                        0x20-3 D0 D1 D2 D3
0x04-7|44 55 66 77
                        0x24-7D4 D5 D6 D7
                                              0 \times 0 = 000 001 011
0x08-B|88 99 AA BB
                        0x28-Bl89 9A AB BC
                                              PTE 1: 0x88 at 0x08
0x0C-FCC DD EE FF
                        0x2C-FCD DE EF F0
                                              PTE 1: PPN 100 (5) valid 0
                        0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                              page fault!
                        0x34-7DB 0B DB 0B
0 \times 14 - 7 | 1B 2B 3B 4B
0x18-Bl1C 2C 3C 4C
                        0x38-BIEC 0C EC 0C
0x1C-F|1C 2C 3C 4C
                        0x3C-FIFC 0C FC 0C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x08; translate virtual address 0x1CB

physical bytes addresses $0 \times 00 - 3 | 00 \ 11 \ 22 \ 33$ 0x20-3|D0 D1 D2 D3 0x04-7|44 55 66 77 0x24-7D4 D5 D6 D7 0x28-Bl89 9A AB BC 0x08-Bl88 99 AA BB 0x0C-FCC DD EE FF 0x2C-FCD DE EF F0 0x30-3|BA 0A BA 0A $0 \times 10 - 3 | 1A 2A 3A 4A$ 0x34-7DB 0B DB 0B $0 \times 14 - 7 | 1B 2B 3B 4B$ 0x18-Bl1C 2C 3C 4C 0x38-BIEC 0C EC 0C 0x1C-F|1C 2C 3C 4C 0x3C-FIFC 0C FC 0C

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9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

```
physical bytes
                         physical <sub>bytes</sub>
addresses
0x00-3|00 11 22 33
                        0x20-3|D0 D1 D2 D3
                                               0 \times 1 CB = 111 001 011
                        0x24-7D4 D5 D6 D7
0x04-7|44 55 66 77
                                               PTE 1: 0xFF at 0x0F
0x08-B|88 99 AA BB
                        0x28-B|89 9A AB BC
                                               PTE 1: PPN 111 (7) valid 1
0x0C-FCC DD EE FF
                        0x2C-FCD DE EF F0
                                               PTE 2: 0x0C at 0x39
0x10-3|1A 2A 3A 4A
                        0x30-3|BA 0A BA 0A
                                               PTE 2: PPN 000 (0) valid 0
                        0x34-7DB 0B DB 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                               page fault!
                        0x38-BIEC 0C EC 0C
0x18-Bl1C 2C 3C 4C
                        0x3C-F|FC 0C FC 0C
0x1C-F|1C 2C 3C 4C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused page table base register 0x08; translate virtual address 0x1CB

```
physical bytes
                         physical <sub>bytes</sub>
addresses
0x00-3|00 11 22 33
                        0x20-3|D0 D1 D2 D3
                                               0 \times 1 CB = 111 001 011
                        0x24-7D4 D5 D6 D7
0x04-7|44 55 66 77
                                               PTE 1: 0xFF at 0x0F
0x08-B|88 99 AA BB
                        0x28-B|89 9A AB BC
                                               PTE 1: PPN 111 (7) valid 1
0x0C-FCC DD EE FF
                        0x2C-FCD DE EF F0
                                               PTE 2: 0x0C at 0x39
0x10-3|1A 2A 3A 4A
                        0x30-3|BA 0A BA 0A
                                               PTE 2: PPN 000 (0) valid 0
                        0x34-7DB 0B DB 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                               page fault!
                        0x38-BIEC 0C EC 0C
0x18-Bl1C 2C 3C 4C
                        0x3C-F|FC 0C FC 0C
0x1C-F|1C 2C 3C 4C
```

9-bit virtual addresses, 6-bit physical; 8 byte pages, 1 byte PTE page tables 1 page; PTE: 3 bit PPN (MSB), 1 valid bit, 4 unused

page table base register 0x08; translate virtual address 0x1CB physical bytes physical bytes

```
addresses
0x00-3|00 11 22 33
                        0x20-3|D0 D1 D2 D3
                                               0 \times 1 CB = 111 001 011
                        0x24-7D4 D5 D6 D7
0x04-7|44 55 66 77
                                               PTE 1: 0xFF at 0x0F
0x08-B|88 99 AA BB
                        0x28-B|89 9A AB BC
                                               PTE 1: PPN 111 (7) valid 1
0x0C-FCC DD EE FF
                        0x2C-FCD DE EF F0
                                               PTE 2: 0 \times 0 C at 0 \times 39
0x10-3|1A 2A 3A 4A
                        0x30-3|BA 0A BA 0A
                                               PTE 2: PPN 000 (0) valid 0
                        0x34-7DB 0B DB 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                               page fault!
                        0x38-BIEC 0C EC 0C
0x18-Bl1C 2C 3C 4C
                        0x3C-F|FC 0C FC 0C
0x1C-F|1C 2C 3C 4C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

```
page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused
```

physical baddresses_		physical	byt	e s					
addresses_	ytes			physical _{bytes} addresses					
0×00-30	0 11	22	33	(9x20-3	D0	E1	D2	D3
0×04-74	4 55	66	77	(9x24-7	D4	E5	D6	E7
0x08-B8	8 99	AA	ВВ	(9x28-B	89	9A	ΑB	ВС
0×0C-FC	C DD	EE	FF	(9x2C−F	CD	DE	EF	F0
0x10-3	.A 2A	ЗА	4A	(9x30-3	ВА	0Α	ВА	0Α
0×14-7	B 2B	3B	4B	(9x34-7	DB	0B	DB	0B
0x18-B	.C 2C	3C	4C	(9х38-В	EC	0C	EC	0C
0x1C-FA	C BC	DC	EC	(9x3C−F	FC	0C	FC	0C

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

```
physical bytes
addresses
                                                    0 \times 376 = 110 \ 111 \ 0110
0 \times 00 - 3 \mid 00 \ 11 \ 22 \ 33
                           0x20-3|D0 E1 D2 D3
                                                    PTE 1: 0x10 + 6 \times 2 = 0x1C:
0 \times 04 - 7 | 44 55 66 77
                           0x24-7D4 E5 D6 E7
                                                    AC BC
0x08-Bl88 99 AA BB
                           0x28-Bl89 9A AB BC
                                                    PTF 1: PPN 10 valid 1
0x0C-FCC DD EE FF
                           0x2C-FCD DE EF F0
                                                    PTE 2: 0x20 + 7 \times 2 = 0x2E:
                           0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                                    FF F0
                           0 \times 34 - 7 | DB | 0B | DB | 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                                    PTE 2: PPN 11 valid 1
0x18-Bl1C 2C 3C 4C
                           0x38-BIEC 0C EC 0C
                                                    11 0110 = 0x36 \rightarrow DB
0×1C-FAC BC DC EC
                           0x3C-F|FC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

```
physical bytes
addresses
                                                    0 \times 376 = 110 \ 111 \ 0110
0 \times 00 - 3 \mid 00 \ 11 \ 22 \ 33
                           0x20-3|D0 E1 D2 D3
                                                    PTE 1: 0x10 + 6 \times 2 = 0x1C:
0 \times 04 - 7 | 44 55 66 77
                           0x24-7D4 E5 D6 E7
                                                    AC BC
0x08-Bl88 99 AA BB
                           0x28-Bl89 9A AB BC
                                                    PTF 1: PPN 10 valid 1
0x0C-FCC DD EE FF
                           0x2C-FCD DE EF F0
                                                    PTE 2: 0x20 + 7 \times 2 = 0x2E:
                           0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                                    FF F0
                           0 \times 34 - 7 | DB | 0B | DB | 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                                    PTE 2: PPN 11 valid 1
0x18-Bl1C 2C 3C 4C
                           0x38-BIEC 0C EC 0C
                                                    11 0110 = 0x36 \rightarrow DB
0×1C-FAC BC DC EC
                           0x3C-F|FC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

```
physical bytes
addresses
                                                    0 \times 376 = 110 \ 111 \ 0110
0 \times 00 - 3 | 00 \ 11 \ 22 \ 33
                           0x20-3|D0 E1 D2 D3
                                                    PTE 1: 0x10 + 6 \times 2 = 0x1C:
0 \times 04 - 7 | 44 55 66 77
                           0x24-7D4 E5 D6 E7
                                                    AC BC
                           0x28-Bl89 9A AB BC
0x08-Bl88 99 AA BB
                                                    PTF 1: PPN 10 valid 1
0x0C-FCC DD EE FF
                           0x2C-FCD DE EF F0
                                                    PTE 2: 0x20 + 7 \times 2 = 0x2E:
                           0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                                    EF F0
                           0 \times 34 - 7 | DB | 0B | DB | 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                                    PTE 2: PPN 11 valid 1
0x18-Bl1C 2C 3C 4C
                           0x38-BIEC 0C EC 0C
                                                    11 0110 = 0x36 \rightarrow DB
0x1C-FAC BC DC EC
                           0x3C-FIFC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

```
physical bytes
addresses
                                                    0 \times 376 = 110 \ 111 \ 0110
0 \times 00 - 3 \mid 00 \ 11 \ 22 \ 33
                           0x20-3|D0 E1 D2 D3
                                                    PTE 1: 0x10 + 6 \times 2 = 0x1C:
0 \times 04 - 7 | 44 55 66 77
                           0x24-7D4 E5 D6 E7
                                                    AC BC
0x08-Bl88 99 AA BB
                           0x28-Bl89 9A AB BC
                                                    PTF 1: PPN 10 valid 1
0x0C-FCC DD EE FF
                           0x2C-FCD DE EF F0
                                                    PTE 2: 0x20 + 7 \times 2 = 0x2E:
                           0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                                    EF F0
                           0 \times 34 - 7 | DB | 0B | DB | 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                                    PTE 2: PPN 11 valid 1
0x18-Bl1C 2C 3C 4C
                           0x38-BIEC 0C EC 0C
                                                    11 0110 = 0x36 \rightarrow DB
0×1C-FAC BC DC EC
                           0x3C-F|FC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

```
physical bytes
addresses
                                                    0 \times 376 = 110 \ 111 \ 0110
0 \times 00 - 3 \mid 00 \ 11 \ 22 \ 33
                           0x20-3|D0 E1 D2 D3
                                                    PTE 1: 0x10 + 6 \times 2 = 0x1C:
0 \times 04 - 7 | 44 55 66 77
                           0x24-7D4 E5 D6 E7
                                                    AC BC
0x08-Bl88 99 AA BB
                           0x28-Bl89 9A AB BC
                                                    PTF 1: PPN 10 valid 1
0x0C-FCC DD EE FF
                           0x2C-FCD DE EF F0
                                                     PTE 2: 0x20 + 7 \times 2 = 0x2E:
                           0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                                    FF FO
                           0 \times 34 - 7 | DB | 0B | DB | 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                                     PTE 2: PPN 11 valid 1
0x18-Bl1C 2C 3C 4C
                           0x38-BIEC 0C EC 0C
                                                     11 0110 = 0x36 \rightarrow DB
0×1C-FAC BC DC EC
                           0x3C-FIFC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

```
page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused
```

```
physical bytes
addresses
                                                    0 \times 376 = 110 \ 111 \ 0110
0 \times 00 - 3 \mid 00 \ 11 \ 22 \ 33
                           0x20-3|D0 E1 D2 D3
                                                    PTE 1: 0x10 + 6 \times 2 = 0x1C:
0 \times 04 - 7 | 44 55 66 77
                           0x24-7D4 E5 D6 E7
                                                    AC BC
0x08-Bl88 99 AA BB
                           0x28-Bl89 9A AB BC
                                                    PTF 1: PPN 10 valid 1
0x0C-FCC DD EE FF
                           0x2C-FCD DE EF F0
                                                    PTE 2: 0x20 + 7 \times 2 = 0x2E:
                           0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                                    EF F0
                           0 \times 34 - 7 | DB | 0B | DB | 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                                    PTE 2: PPN 11 valid 1
0x18-Bl1C 2C 3C 4C
                           0x38-BIEC 0C EC 0C
                                                    11 0110 = 0x36 \rightarrow DB
0×1C-FAC BC DC EC
                           0x3C-FIFC 0C FC 0C
```

10-bit virtual addresses, 6-bit physical; 16 byte pages, 2 byte PTE

page tables 1 page; PTE 1st byte: (MSB) 2-bit PPN, valid bit; rest unused

```
physical bytes
addresses
                                                   0 \times 376 = 110 \ 111 \ 0110
0 \times 00 - 3 \mid 00 \ 11 \ 22 \ 33
                          0x20-3|D0 E1 D2 D3
                                                   PTE 1: 0x10 + 6 \times 2 = 0x1C:
0 \times 04 - 7 | 44 55 66 77
                          0x24-7D4 E5 D6 E7
                                                   AC BC
0x08-Bl88 99 AA BB
                          0x28-Bl89 9A AB BC
                                                   PTF 1: PPN 10 valid 1
0x0C-FCC DD EE FF
                          0x2C-FCD DE EF F0
                                                   PTE 2: 0x20 + 7 \times 2 = 0x2E:
                          0x30-3|BA 0A BA 0A
0 \times 10 - 3 | 1A 2A 3A 4A
                                                   EF F0
                          0x34-7DB 0B DB 0B
0 \times 14 - 7 | 1B 2B 3B 4B
                                                   PTE 2: PPN 11 valid 1
0x18-Bl1C 2C 3C 4C
                          0x38-BIEC 0C EC 0C
                                                   11 0110 = 0x36 \rightarrow DB
0×1C-FAC BC DC EC
                          0x3C-F|FC 0C FC 0C
```

x86-64 page table entries (1)

		5 5 5 5 5 5 5 8 7 6 5 4 3 2	M -	M-1 2 1 0 9 8 7 6 5 4 3 2 1 0 9 8 7 6 5 4 3 2 1 0 9 8 7 6 5 4 3 2 1	0			
X D	Prot. Key ⁴	Ignored	Rsvd.	Address of 4KB page frame	1	PTE: 4KB page		
	Ignored <u>O</u>							

```
present = valid
```

```
R/W = writes allowed?
```

```
U/S = user-mode allowed? ("user/supervisor")
```

XD = execute-disable?

 $\mathsf{A} = \mathsf{accessed?} \ (\mathsf{MMU} \ \mathsf{sets} \ \mathsf{to} \ \mathsf{1} \ \mathsf{on} \ \mathsf{page} \ \mathsf{read/write})$

D = dirty? (MMU sets to 1 on page write)

x86-64 page table entries (1)

		5 5 5 5 5 5 5 8 7 6 5 4 3 2	M -	M-1 2 1 0 9 8 7 6 5 4 3 2 1 0 9 8 7 6 5 4 3 2 1 0 9 8 7 6 5 4 3 2 1	0			
X D	Prot. Key ⁴	Ignored	Rsvd.	Address of 4KB page frame	1	PTE: 4KB page		
	Ignored <u>O</u>							

```
present = valid
```

```
R/W = writes allowed?
```

$$U/S = user-mode allowed?$$
 ("user/supervisor")

XD = execute-disable?

$$A = accessed?$$
 (MMU sets to 1 on page read/write)

D = helps support replacement policies for swapping

x86-64 page table entries (1)

```
| Frot | Ignored | Rsvd. | Address of 4KB page frame | Ign. | Ign
```

```
present = valid
```

```
R/W = writes allowed?
```

$$U/S = user-mode allowed?$$
 ("user/supervisor")

```
XD = execute-disable?
```

D = dirty? (MMU sets to 1 on page write)

1 1 1 1 1 1 1

x86-64 page table entries (2)

	-		5 5 5 5 5 5 5 8 7 6 5 4 3 2	M -	M-1 3 3 3 2 2 2 2 2 2 2 2 2 2 1 1 1 1 1 1	0	
X	(Prot. Key ⁴	Ignored	Rsvd.	Address of 4KB page frame Ign. G P D A C W J S W	1	PTE: 4KB page
	Ignored						

G = global? (shared between all page tables)

```
PWT, PCD, PAT = control how caches work when accessing physical page: can disable using the cache entirely can disable write-back (use write-through instead) multicore-related cache settings (and some other settings)
```

x86-64 page table entries (2)

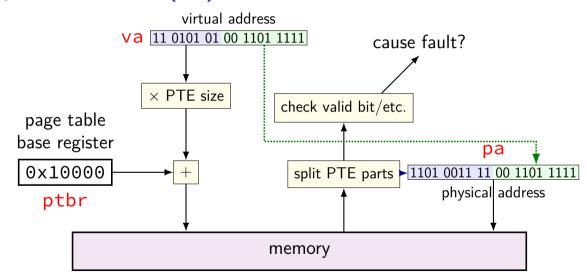
		5 5 5 5 5 5 8 7 6 5 4 3 2	M -	M-1 2 1 0 9 8 7 6 5 4 3 2 1 0 9 8 7 6 5 4 3 2 1 0 9 8 7 6 5 4 3 2 1	0			
X D	Prot. Key ⁴	Ignored	Rsvd.	Address of 4KB page frame	1	PTE: 4KB page		
	Ignored							

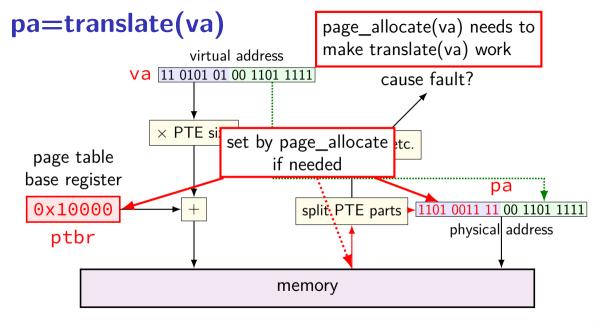
G = global? (shared between all page tables)

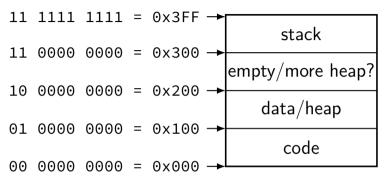
P CPU won't evict TLB entries on most page table base registers changes

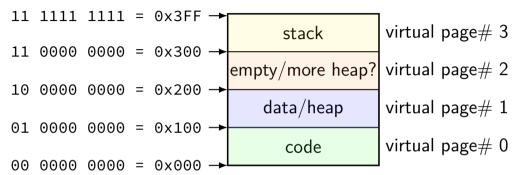
can disable using the cache entirely can disable write-back (use write-through instead) multicore-related cache settings (and some other settings)

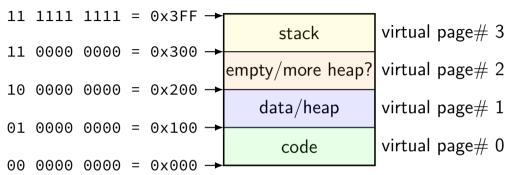
pa=translate(va)



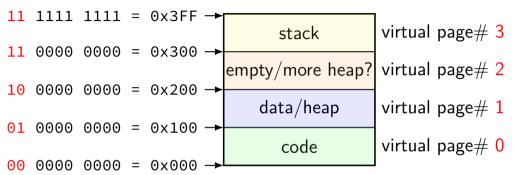




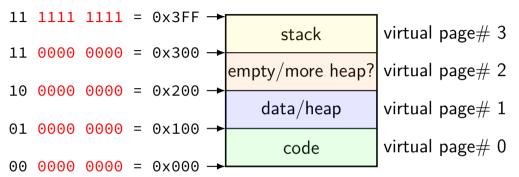




divide memory into pages (2^8 bytes in this case) "virtual" = addresses the program sees



page number is upper bits of address (because page size is power of two)



rest of address is called page offset

toy physical memory

program memory virtual addresses

11	0000	0000	to	
11	1111	1111		
10	0000	0000	to	
10	1111	1111		
01	0000	0000	to	Ī
01	1111	1111		
00	0000	0000	to	
00	1111	1111		

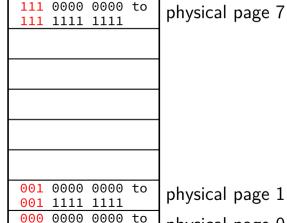
real memory physical addresses

, ,			
111	0000	0000	to
111	1111	1111	
001	0000	0000	to
001	1111	1111	
000	0000	0000	to
000	1111	1111	

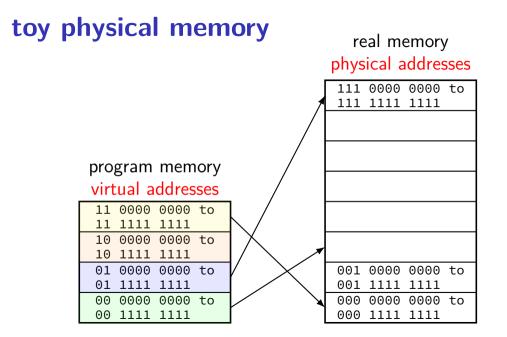
toy physical memory

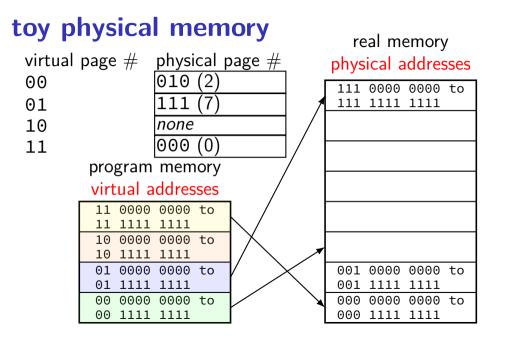
real memory physical addresses

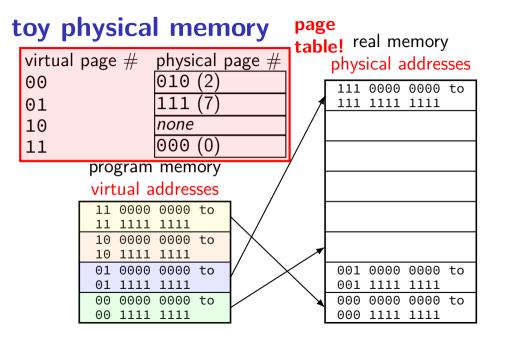
program memory virtual addresses 0000 0000 to 1111 0000 to 0000 1111 0000 0000 to 1111 0000 to 0000 1111



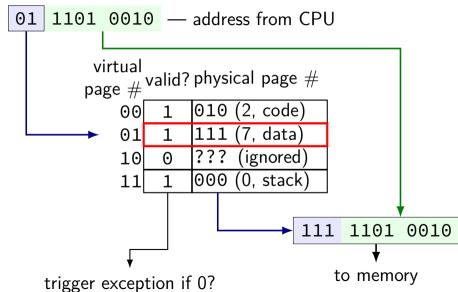
physical page 1 physical page 0

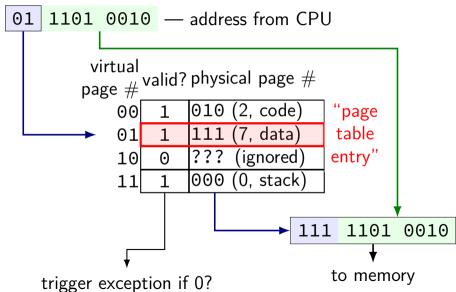






```
virtual page # valid? physical page # 00 1 010 (2, code) 01 1 111 (7, data) 10 0 ??? (ignored) 11 1 000 (0, stack)
```





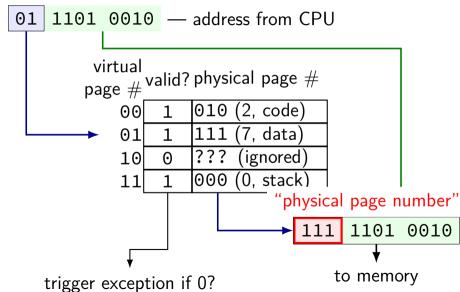
43

t "virtual page number" ookup 1101 0010 — address from CPU virtual page # valid? physical page #010 (2, code) 00data 01 10 0 (ignored) 000 (0, stack) 1101 0010

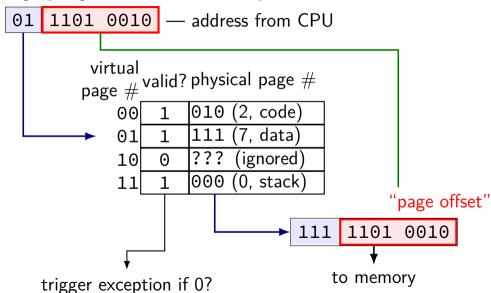
trigger exception if 0?

to memory

43



toy pag "page offset" ookup



exit statuses

```
int main() {
    return 0;  /* or exit(0); */
}
```

the status

```
#include <sys/wait.h>
 waitpid(child pid, &status, 0);
  if (WIFEXITED(status)) {
    printf("main returned or exit called with %d\n",
           WEXITSTATUS(status));
  } else if (WIFSIGNALED(status)) {
    printf("killed by signal %d\n", WTERMSIG(status));
  } else {
```

"status code" encodes both return value and if exit was abnormal W* macros to decode it

the status

```
#include <sys/wait.h>
 waitpid(child pid, &status, 0);
  if (WIFEXITED(status)) {
    printf("main returned or exit called with %d\n",
           WEXITSTATUS(status));
  } else if (WIFSIGNALED(status)) {
    printf("killed by signal %d\n", WTERMSIG(status));
  } else {
```

"status code" encodes both return value and if exit was abnormal W* macros to decode it

program

operating system

46

program

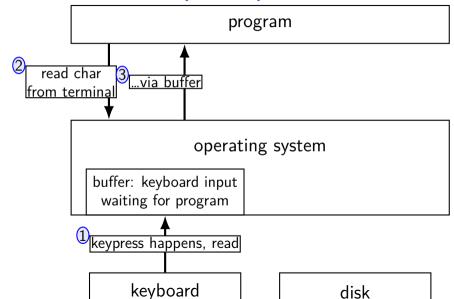
operating system

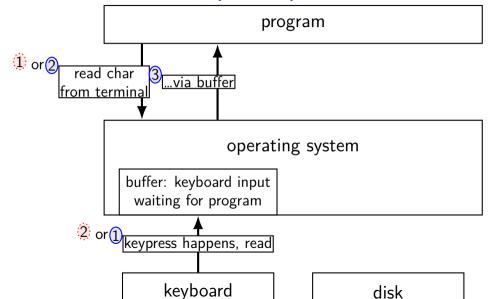
buffer: keyboard input waiting for program

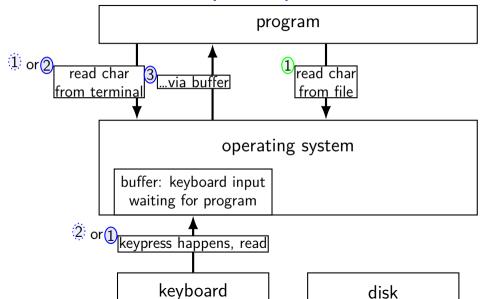
keypress happens, read

disk

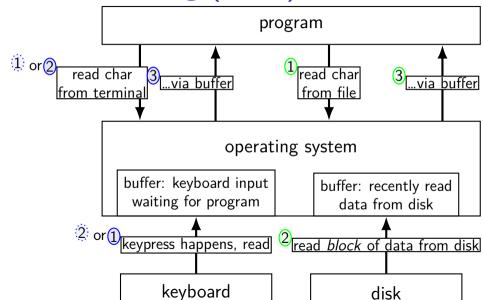
keyboard







46



46

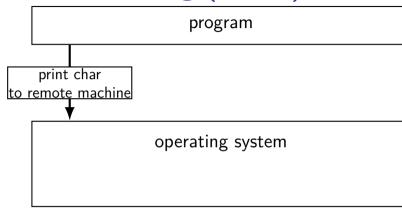
program

operating system

network

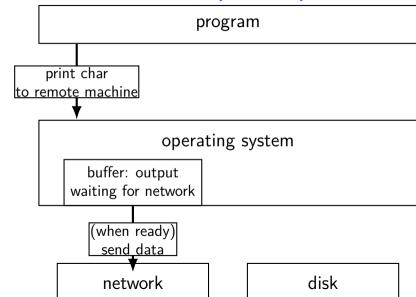
disk

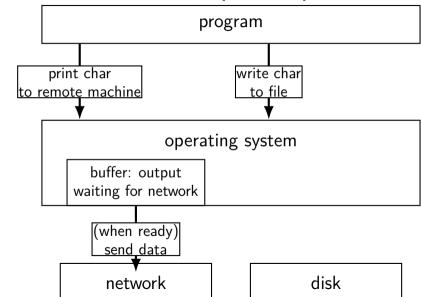
network

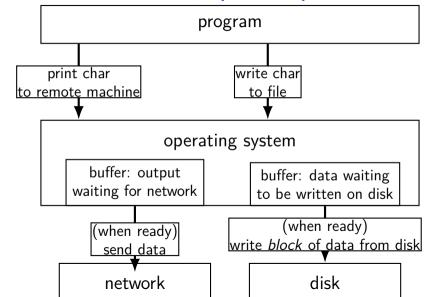


disk

4





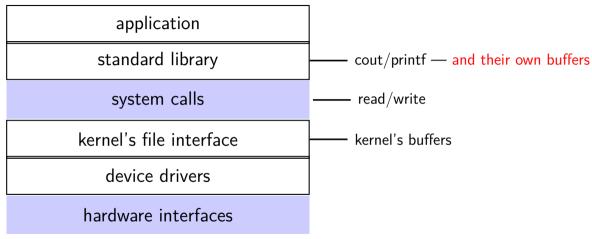


read/write operations

```
read()/write(): move data into/out of buffer
possibly wait if buffer is empty (read)/full (write)
```

actual I/O operations — wait for device to be ready trigger process to stop waiting if needed

layering



why the extra layer

```
better (but more complex to implement) interface:
     read line
     formatted input (scanf, cin into integer, etc.)
     formatted output
less system calls (bigger reads/writes) sometimes faster
     buffering can combine multiple in/out library calls into one system call
more portable interface
     cin. printf. etc. defined by C and C++ standards
```

exercise

```
pid_t p = fork();
int pipe_fds[2];
pipe(pipe fds);
if (p == 0) { /* child */
  close(pipe_fds[0]);
  char c = 'A';
 write(pipe_fds[1], &c, 1);
  exit(0):
} else { /* parent */
  close(pipe_fds[1]);
  char c;
  int count = read(pipe_fds[0], &c, 1);
  printf("read %d bytes\n", count);
```

The child is trying to send the character A to the parent, but the above code outputs read 0 bytes instead of read 1 bytes. What happened?

exercise solution

pipe() is after fork — two pipes, one in child, one in parent

} else { /* fork error */ }

```
int pipe fd[2];
if (pipe(pipe fd) < 0)</pre>
    handle error(); /* e.g. out of file descriptors */
int read fd = pipe fd[0];
int write_fd = pipe_fd[1];
child_pid = fork();
if (child pid == 0) {
   /* in child process, write to pipe */
    close(read fd);
    write_to_pipe(write_fd); /* function not shown */
    exit(EXIT SUCCESS);
} else if (child pid > 0) {
    /* in parent process, read from pipe */
    close(write fd):
    read_from_pipe(read_fd); /* function not shown */
    waitpid(child_pid, NULL, 0);
    close(read fd):
```

'standard' pattern with fork() int pipe fd[2]; if (pipe(pipe fd) < 0)</pre> handle error(); /* e.g. out of file descriptors */ int read fd = pipe fd[0]; int write_fd = pipe_fd[1]; child_pid = fork(); if (child pid == 0) { /* in child process, write to pipe */ close(read fd); write_to_pipe(write_fd); /* function not shown */ exit(EXIT SUCCESS);

} else if (child pid > 0) { /* in parent process, read from pipe */ close(write fd): read_from_pipe(read_fd); /* function not shown */ waitpid(child_pid, NULL, 0); close(read fd): } else { /* fork error */ }

```
read() will not indicate
int pipe fd[2];
                                            end-of-file if write fd is open
if (pipe(pipe fd) < 0)</pre>
    handle_error(); /* e.g. out of file | (any copy of it)
int read fd = pipe fd[0];
int write_fd = pipe_fd[1];
child_pid = fork();
if (child pid == 0) {
    /* in child process, write to pipe */
    close(read fd);
    write_to_pipe(write_fd); /* function not shown */
    exit(EXIT SUCCESS);
```

} else if (child pid > 0) { /* in parent process, read from pipe */ close(write fd); read_from_pipe(read_fd); /* function not shown */ waitpid(child_pid, NULL, 0); close(read fd): } else { /* fork error */ }

close(read_fd);

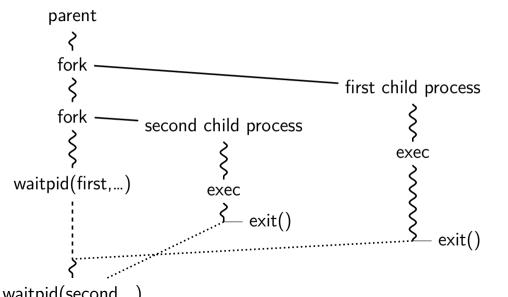
else { /* fork error */ }

```
have habit of closing
int pipe fd[2];
                                        to avoid 'leaking' file descriptors
if (pipe(pipe fd) < 0)</pre>
    handle_error(); /* e.g. out of fi you can run out
int read fd = pipe fd[0];
int write_fd = pipe_fd[1];
child_pid = fork();
if (child pid == 0) {
    /* in child process, write to pipe */
   close(read fd);
    write_to_pipe(write_fd); /* function not shown */
    exit(EXIT SUCCESS);
} else if (child pid > 0) {
    /* in parent process, read from pipe */
    close(write fd):
    read_from_pipe(read_fd); /* function not shown */
    waitpid(child_pid, NULL, 0);
```

pipe() and blocking

```
BROKEN example:
int pipe fd[2];
if (pipe(pipe fd) < 0)</pre>
    handle error();
int read fd = pipe fd[0];
int write fd = pipe fd[1];
write(write fd, some buffer, some big size);
read(read fd, some buffer, some big size);
This is likely to not terminate. What's the problem?
```

pattern with multiple?



this class: focus on Unix

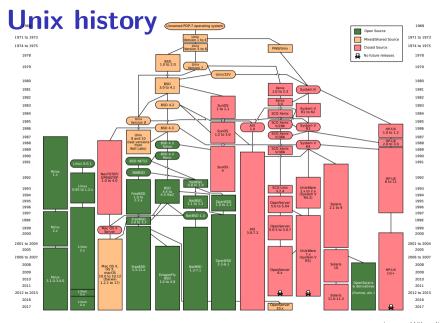
Unix-like OSes will be our focus

we have source code

used to from 2150, etc.?

have been around for a while

xv6 imitates Unix



POSIX: standardized Unix

Portable Operating System Interface (POSIX) "standard for Unix"

```
current version online:
https://pubs.opengroup.org/onlinepubs/9699919799/
(almost) followed by most current Unix-like OSes
...but OSes add extra features
```

...and POSIX doesn't specify everything

what POSIX defines

POSIX specifies the library and shell interface source code compatibility

doesn't care what is/is not a system call...

doesn't specify binary formats...

idea: write applications for POSIX, recompile and run on all implementations

this was a very important goal in the 80s/90s at the time, no dominant Unix-like OS (Linux was very immature)

getpid

```
pid_t my_pid = getpid();
printf("my pid is %ld\n", (long) my_pid);
```

process ids in ps

read/write

```
ssize_t read(int fd, void *buffer, size_t count);
ssize t write(int fd, void *buffer, size_t count);
read/write up to count bytes to/from buffer
returns number of bytes read/written or -1 on error
    ssize_t is a signed integer type
    error code in errno
read returning 0 means end-of-file (not an error)
    can read/write less than requested (end of file, broken I/O device, ...)
```

read'ing one byte at a time

```
string s;
ssize t amount read;
char c:
/* cast to void * not needed in C */
while ((amount_read = read(STDIN_FILENO, (void*) &c, 1)) > 0)
    /* amount read must be exactly 1 */
    s += c;
if (amount read == -1) {
    /* some error happened */
    perror("read"); /* print out a message about it */
} else if (amount read == 0) {
   /* reached end of file */
```

write example

```
/* cast to void * optional in C */
write(STDOUT_FILENO, (void *) "Hello, World!\n", 14);
```

read/write

```
ssize_t read(int fd, void *buffer, size_t count);
ssize t write(int fd, void *buffer, size_t count);
read/write up to count bytes to/from buffer
returns number of bytes read/written or -1 on error
    ssize_t is a signed integer type
    error code in errno
read returning 0 means end-of-file (not an error)
    can read/write less than requested (end of file, broken I/O device, ...)
```

read'ing a fixed amount

```
ssize t offset = 0;
const ssize t amount to read = 1024;
char result[amount to read];
do {
    /* cast to void * optional in C */
    ssize t amount read =
        read(STDIN FILENO,
             (void *) (result + offset),
             amount to read - offset);
    if (amount read < 0) {</pre>
        perror("read"); /* print error message */
        ... /* abort??? */
    } else {
        offset += amount read;
```

partial reads

on regular file: read reads what you request

but otherwise: usually gives you what's known to be available after waiting for something to be available

partial reads

on regular file: read reads what you request

but otherwise: usually gives you what's known to be available after waiting for something to be available

reading from network — what's been received

reading from keyboard — what's been typed

write example (with error checking)

```
const char *ptr = "Hello, World!\n";
ssize t remaining = 14;
while (remaining > 0) {
    /* cast to void * optional in C */
    ssize t amount written = write(STDOUT FILENO.
                                     ptr,
                                     remaining);
    if (amount_written < 0) {</pre>
        perror("write"); /* print error message */
        ... /* abort??? */
    } else {
        remaining -= amount_written;
        ptr += amount_written;
```

partial writes

usually only happen on error or interruption

but can request "non-blocking" (interruption: via signal)

usually: write waits until it completes

= until remaining part fits in buffer in kernel does not mean data was sent on network, shown to user yet, etc.

aside: environment variables (1)

key=value pairs associated with every process:

\$ printenv

PWD=/zf14/cr4bd

```
MODULE VERSION STACK=3.2.10
MANPATH=:/opt/puppetlabs/puppet/share/man
XDG_SESSION_ID=754
HOSTNAME=labsrv01
SELINUX ROLE REOUESTED=
TFRM=screen
SHELL=/bin/bash
HISTSIZE=1000
SSH CLIENT=128.143.67.91 58432 22
SELINUX_USE_CURRENT_RANGE=
QTDIR=/usr/lib64/at-3.3
OLDPWD=/zf14/cr4bd
QTINC=/usr/lib64/qt-3.3/include
SSH_TTY=/dev/pts/0
OT GRAPHICSSYSTEM_CHECKED=1
USFR=cr4hd
LS COLORS=rs=0:di=01;34:ln=01;36:mh=00:pi=40;33:so=01;35:do=01;35:bd=40;33;01:cd=40;33;01:or
MODULE VERSION=3.2.10
MAIL=/var/spool/mail/cr4bd
```

PATH=/zf14/cr4bd/.cargo/bin:/zf14/cr4bd/bin:/usr/lib64/qt-3.3/bin:/usr/local/bin:/usr/bin:/u

aside: environment variables (2)

```
environment variable library functions:
    getenv("KEY") \rightarrow value
    putenv("KEY=value") (sets KEY to value)
    setenv("KEY", "value") (sets KEY to value)
int execve(char *path, char **argv, char **envp)
    char *envp[] = { "KEY1=value1", "KEY2=value2", NULL };
    char *argv[] = { "somecommand", "some arg", NULL };
    execve("/path/to/somecommand", argv, envp);
```

normal exec versions — keep same environment variables

aside: environment variables (3)

interpretation up to programs, but common ones...

```
PATH=/bin:/usr/bin
to run a program 'foo', look for an executable in /bin/foo, then
/usr/bin/foo
```

```
HOME=/zf14/cr4bd current user's home directory is '/zf14/cr4bd'
```

```
TERM=screen-256color your output goes to a 'screen-256color'-style terminal
```

--

multiple processes?

```
while (...) {
    pid = fork();
    if (pid == 0) {
        exec ...
    } else if (pid > 0) {
        pids.push back(pid);
/* retrieve exit statuses in order */
for (pid t pid : pids) {
    waitpid(pid, ...);
```

waiting for all children

```
#include <sys/wait.h>
 while (true) {
    pid t child pid = waitpid(-1, &status, 0);
    if (child_pid == (pid_t) -1) {
      if (errno == ECHILD) {
        /* no child process to wait for */
        break;
      } else {
       /* some other error */
    /* handle child_pid exiting */
```

multiple processes?

```
while (...) {
    pid = fork();
    if (pid == 0) {
        exec ...
    } else if (pid > 0) {
        pids.push back(pid);
/* retrieve exit statuses as processes finish */
while ((pid = waitpid(-1, \ldots)) != -1) {
    handleProcessFinishing(pid);
```

'waiting' without waiting

```
#include <sys/wait.h>
...
pid_t return_value = waitpid(child_pid, &status, WNOHANG);
if (return_value == (pid_t) 0) {
    /* child process not done yet */
} else if (child_pid == (pid_t) -1) {
    /* error */
} else {
    /* handle child_pid exiting */
}
```

parent and child processes

every process (but process id 1) has a parent process
(getppid())

this is the process that can wait for it

creates tree of processes (Linux pstree command):

```
init(1)-+-ModemManager(919)-+-{ModemManager}(972)
                                                                           -mongod(1336)-+-(mongod)(1556)
                               - (ModenManager) (1864)
                                                                                         I-(mongod)(1557)
          -NetworkManager(1160)-+-dhclient(1755)
                                  I-dosmaso(1985)
                                   (NetworkManager)(1188)
                                   -{NetworkManager}(1194)
                                   (NetworkManager)(1195)
         -accounts-daemon(1649)-+-(accounts-daemon)(1757)
                                   -{accounts-daemon}(1758)
          -acpid(1338)
                                                                           -mosh-server(19898)---bash(19891)---tmux(5442)
          -apache2(3165)-+-apache2(4125)-+-(apache2)(4126)
                                                                           -mosh-server(21996)---bash(21997)
                                             {apache2}(4127)
                                                                           -mosh-server(22533)---bash(22534)---tmux(22588)
                           -apache2(28920)-+-{apache2}(28926)
                                                                           -nm-applet(2588)-+-{nm-applet}(2739
                                              -{apache2}(28960)
                                                                                             (ng.applet)(2743)
                           -apache2(28921)-+-{apache2}(28927)
                                                                           -nnbd(2224)
                                                                           -ntpd(3891)
                                              . [anache2](28963)
                                                                           -polkitd(1197)-+-(polkitd)(1239)
                           -apache2(28922)-+-{apache2}(28928)
                                                                                          -{polkitd}(1240
                                              - (anache2)(28961)
                                                                            -pulseaudio(2563)-+-{pulseaudio}(2617)
                           apache2(28923)-+-(apache2)(28936)
                                                                                             -{pulseaudio}(2623)
                                             -{apache2}(28962)
                                                                            puppet(2373) --- (puppet)(32455)
                           apache2(28925)-+-{apache2}(28958)
                                                                           -rpc.idmapd(875)
                                             -{apache23(28965)
                                                                           -rpc.statd(954)
                           -apache2(32165)-+-{apache2}(32166)
                                                                           -rpcbind(884)
                                              -{apache2}(32167)
                                                                           -rserver(1501)-+-(rserver)(1786)
                                                                                          -{rserver}(1787)
          -at-spi-bus-laun(2252)-+-dbus-daemon(2269)
                                                                            rsysload(1090)-+-{rsysload}(1092)
                                  |-{at-spi-bus-laun}(2266)
                                                                                           1-{rsysload}(1893)
                                    -{at-spi-bus-laun}(2268)
                                                                                            [reveload](1894)
                                    (at-spi-bus-laun)(2270)
                                                                           -rtkit-daenon(2565)-+-(rtkit-daenon)(2566
          -at-spi2-registr(2275)---{at-spi2-registr}(2282)
                                                                                               -{rtkit-daenon}(2567)
         -atd(1633)
                                                                           -sd cicero(2852)-+-sd cicero(2853)
         -automount(13454)-+-{automount}(13455)
                                                                                             {sd cicero}(2854)
                              - (automount)(13456)
                                                                                              [sd_c1ceco](2855)
                                                                           -sd dummy(2849)-+-(sd dummy)(2850)
                              (automount)(13461)
                              - (automount)(13464)
                                                                           -sd espeak(2749)-+-{sd espeak}(2845)
                              -{automount}(13465)
```

parent and child questions...

```
what if parent process exits before child?
     child's parent process becomes process id 1 (typically called init)
what if parent process never waitpid()s (or equivalent) for child?
     child process stays around as a "zombie"
     can't reuse pid in case parent wants to use waitpid()
what if non-parent tries to waitpid() for child?
     waitpid fails
```

program

operating system

keyboard disk

program

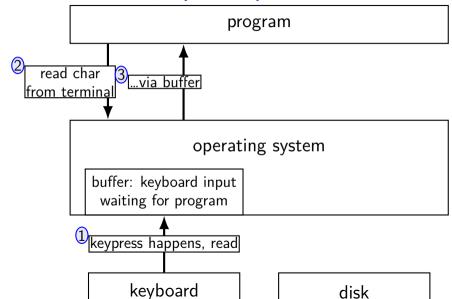
operating system

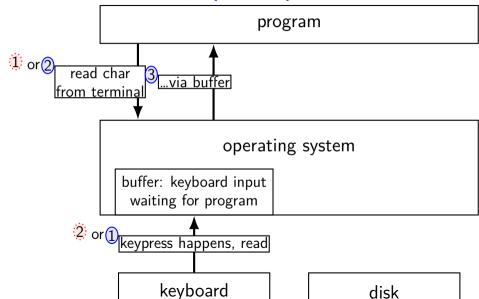
buffer: keyboard input waiting for program

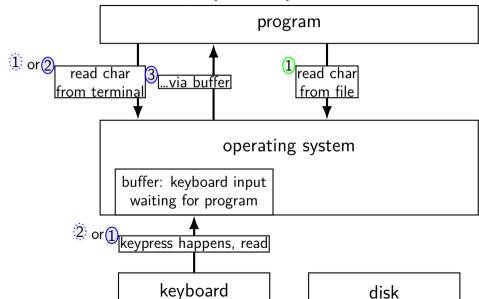
temperating system

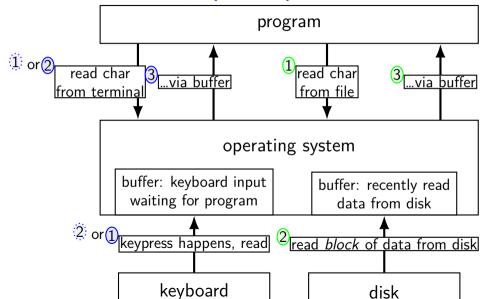
disk

keyboard







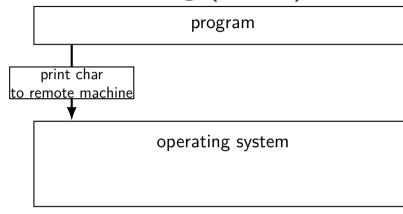


program

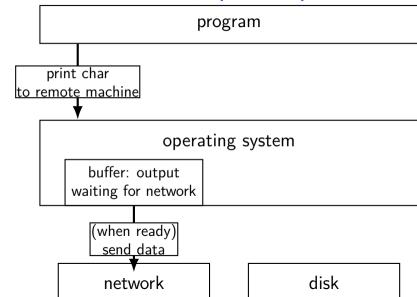
operating system

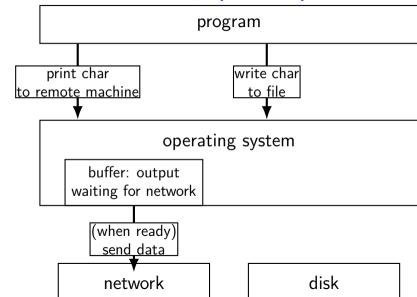
network

disk

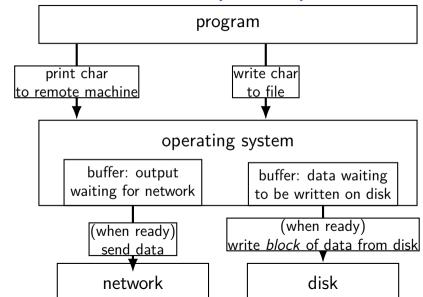


network disk





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read/write operations

```
read()/write(): move data into/out of buffer
possibly wait if buffer is empty (read)/full (write)
```

actual I/O operations — wait for device to be ready trigger process to stop waiting if needed

filesystem abstraction

```
regular files — named collection of bytes also: size, modification time, owner, access control info, ...
```

directories — folders containing files and directories
hierarchical naming: /net/zf14/cr4bd/fall2018/cs4414
mostly contains regular files or directories

open

```
int open(const char *path, int flags);
int open(const char *path, int flags, int mode);
int read fd = open("dir/file1", 0 RDONLY);
int write_fd = open("/other/file2",
        O_WRONLY | O_CREAT | O_TRUNC, 0666);
int rdwr fd = open("file3", O RDWR);
```

open

```
int open(const char *path, int flags, int mode);
path = filename
e.g. "/foo/bar/file.txt"
    file.txt in
    directory bar in
    directory foo in
    "the root directory"
e.g. "quux/other.txt
    other txt in
    directory quux in
    "the current working directory" (set with chdir())
```

int open(const char *path, int flags);

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open: file descriptors

```
int open(const char *path, int flags);
int open(const char *path, int flags, int mode);
return value = file descriptor (or -1 on error)
index into table of open file descriptions for each process
used by system calls that deal with open files
```

POSIX: everything is a file

```
the file: one interface for
devices (terminals, printers, ...)
regular files on disk
networking (sockets)
local interprocess communication (pipes, sockets)
```

basic operations: open(), read(), write(), close()

exercise

```
int pipe_fds[2]; pipe(pipe_fds);
pid_t p = fork();
if (p == 0) {
  close(pipe_fds[0]);
  for (int i = 0; i < 10; ++i) {
    char c = '0' + i;
   write(pipe fds[1], &c, 1);
  exit(0):
close(pipe fds[1]);
char buffer[10];
ssize t count = read(pipe fds[0], buffer, 10);
for (int i = 0; i < count; ++i) {
  printf("%c", buffer[i]);
Which of these are possible outputs (if pipe, read, write, fork don't fail)?
 A. 0123456789 B. 0
                                   C. (nothing)
```

E. A and C F. A. B. and C

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D. A and B

exercise

```
int pipe_fds[2]; pipe(pipe_fds);
pid_t p = fork();
if (p == 0) {
  close(pipe_fds[0]);
  for (int i = 0; i < 10; ++i) {
    char c = '0' + i;
   write(pipe fds[1], &c, 1);
  exit(0):
close(pipe fds[1]);
char buffer[10];
ssize t count = read(pipe fds[0], buffer, 10);
for (int i = 0; i < count; ++i) {
  printf("%c", buffer[i]);
Which of these are possible outputs (if pipe, read, write, fork don't fail)?
 A. 0123456789 B. 0
                                   C. (nothing)
```

E. A and C F. A. B. and C

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D. A and B

empirical evidence

partial reads

read returning 0 always means end-of-file by default, read always waits *if no input available yet* but can set read to return *error* instead of waiting

read can return less than requested if not available e.g. child hasn't gotten far enough

pipe: closing?

```
if all write ends of pipe are closed can get end-of-file (read() returning 0) on read end exit()ing closes them
```

 \rightarrow close write end when not using

generally: limited number of file descriptors per process

→ good habit to close file descriptors not being used
 (but probably didn't matter for read end of pipes in example)

swapping almost mmap

```
access mapped file for first time, read from disk (like swapping when memory was swapped out)
```

write "mapped" memory, write to disk eventually (like writeback policy in swapping) use "dirty" bit

extra detail: other processes should see changes all accesses to file use same physical memory