BIOS 6301: Assignment 3

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Due Tuesday, 26 September, 1:00 PM

50 points total.

Add your name as `author` to the file's metadata section.

Submit a single knitr file (named `homework3.rmd`) by email to marisa.h.blackman@vanderbilt.edu. Place your R code in between the appropriate chunks for each question. Check your output by using the `Knit HTML` button in RStudio.

$5^{n=day}$ points taken off for each day late.

Question 1

15 points

Write a simulation to calculate the power for the following study design. The study has two variables, treatment group and outcome. There are two treatment groups (0, 1) and they should be assigned randomly with equal probability. The outcome should be a random normal variable with a mean of 60 and standard deviation of 20. If a patient is in the treatment group, add 5 to the outcome. 5 is the true treatment effect. Create a linear model for the outcome by the treatment group, and extract the p-value (hint: see assignment1). Test if the p-value is less than or equal to the alpha level, which should be set to 0.05.

The p-value is greater than 0.05

```
n <- 25
treatment <- rbinom(n, size = 1, prob = 0.5)
outcome <- rnorm(n, 60, 20)
outcome_2 <- ifelse(treatment == 1, outcome+5, outcome)

model <- lm(outcome_2 ~ treatment)
summary(model)
```

```
##
## Call:
## lm(formula = outcome_2 ~ treatment)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -25.671  -8.359   0.161  12.288  36.476
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept)   46.219      5.835   7.921 5.08e-08 ***
## treatment     14.629      6.876   2.127   0.0443 *
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 15.44 on 23 degrees of freedom
## Multiple R-squared:  0.1644, Adjusted R-squared:  0.1281
## F-statistic: 4.526 on 1 and 23 DF,  p-value: 0.04432
```

```
model.c <- coef(summary(model))
p <- (pt(model.c[2,3],8,lower.tail = FALSE))*2
p
```

```
## [1] 0.06605293
```

```
p < 0.05
```

```
## [1] FALSE
```

Repeat this procedure 1000 times. The power is calculated by finding the percentage of times the p-value is less than or equal to the alpha level. Use the `set.seed` command so that the professor can reproduce your results.

1. Find the power when the sample size is 100 patients. (10 points)

```
set.seed(1)

n <- 100
mean(replicate(1000, {
  treatment <- rbinom(n, size = 1, prob = 0.5)
  outcome <- rnorm(n, 60, 20)
  outcome_2 <- ifelse(treatment == 1, outcome+5, outcome)

  model <- lm(outcome_2 ~ treatment)
  model.c <- coef(summary(model))
  p <- (pt(model.c[2,3],8,lower.tail = FALSE))*2
}) < 0.05 )
```

```
## [1] 0.19
```

1. Find the power when the sample size is 1000 patients. (5 points)

```
set.seed(2)

n <- 1000
mean(replicate(1000, {
  treatment <- rbinom(n, size = 1, prob = 0.5)
  outcome <- rnorm(n, 60, 20)
  outcome_2 <- ifelse(treatment == 1, outcome+5, outcome)

  model <- lm(outcome_2 ~ treatment)
  model.c <- coef(summary(model))
  p <- (pt(model.c[2,3],8,lower.tail = FALSE))*2
}) < 0.05 )
```

```
## [1] 0.951
```

Question 2

14 points

Obtain a copy of the football-values lecture. Save the `2023/proj_wr23.csv` file in your working directory. Read in the data set and remove the first two columns.

```
library(readr)
df <- read_csv("~/Desktop/BIOS 6301 - Introduction to Statistical Computing/datasets//proj_wr23.csv")
```

```
## Rows: 256 Columns: 10
## -- Column specification --------------------------------------------------------
## Delimiter: ","
## chr (2): PlayerName, Team
## dbl (8): rec_att, rec_yds, rec_tds, rush_att, rush_yds, rush_tds, fumbles, fpts
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

```
head(df)
```

```
## # A tibble: 6 x 10
##   PlayerName    Team  rec_att rec_yds rec_tds rush_att rush_yds rush_tds fumbles
##   <chr>         <chr>   <dbl>   <dbl>   <dbl>    <dbl>    <dbl>    <dbl>   <dbl>
## 1 Justin Jeffe~ MIN     110.    1529.     8        3.7     18.1      0.3     0.4
## 2 Ja'Marr Chase CIN     107     1377.    10.1      5.2     24.6      0.1     1.1
## 3 Cooper Kupp   LAR     104.    1325.     8.7      7.1     74.7      0.9     0.6
## 4 Tyreek Hill   MIA     106.    1402.     7.8      9.5     57.1      0.6     0.5
## 5 CeeDee Lamb   DAL      99.7   1307.     7.9      8.5     55.4      0.2     0.5
## 6 Stefon Diggs  BUF      96.8   1286.     8.5      0.8      3.9      0       0.6
## # i 1 more variable: fpts <dbl>
```

```
wr23.df <- df[-c(1,2)]
head(wr23.df)
```

```
## # A tibble: 6 x 8
##   rec_att rec_yds rec_tds rush_att rush_yds rush_tds fumbles  fpts
##     <dbl>   <dbl>   <dbl>    <dbl>    <dbl>    <dbl>   <dbl> <dbl>
## 1   110.    1529.     8        3.7     18.1      0.3     0.4  204.
## 2   107     1377.    10.1      5.2     24.6      0.1     1.1  199.
## 3   104.    1325.     8.7      7.1     74.7      0.9     0.6  196.
## 4   106.    1402.     7.8      9.5     57.1      0.6     0.5  195.
## 5    99.7   1307.     7.9      8.5     55.4      0.2     0.5  184.
## 6    96.8   1286.     8.5      0.8      3.9      0       0.6  179.
```

1. Show the correlation matrix of this data set. (4 points)

```
wr23.corr <- cor(wr23.df)
wr23.corr
```

```
##            rec_att   rec_yds   rec_tds  rush_att  rush_yds  rush_tds   fumbles
## rec_att  1.0000000 0.9751004 0.9632402 0.3472074 0.3268797 0.2727289 0.6500961
```

```
## rec_yds  0.9751004 1.0000000 0.9690563 0.3275376 0.3063227 0.2651483 0.6464774
## rec_tds  0.9632402 0.9690563 1.0000000 0.2656168 0.2542211 0.2277144 0.6148910
## rush_att 0.3472074 0.3275376 0.2656168 1.0000000 0.9527671 0.8333155 0.3881654
## rush_yds 0.3268797 0.3063227 0.2542211 0.9527671 1.0000000 0.8994103 0.3619078
## rush_tds 0.2727289 0.2651483 0.2277144 0.8333155 0.8994103 1.0000000 0.3048482
## fumbles  0.6500961 0.6464774 0.6148910 0.3881654 0.3619078 0.3048482 1.0000000
## fpts     0.9777955 0.9961858 0.9791021 0.3704589 0.3565869 0.3183841 0.6445244
##              fpts
## rec_att  0.9777955
## rec_yds  0.9961858
## rec_tds  0.9791021
## rush_att 0.3704589
## rush_yds 0.3565869
## rush_tds 0.3183841
## fumbles  0.6445244
## fpts     1.0000000
```

1. Generate a data set with 30 rows that has a similar correlation structure. Repeat the procedure 1,000 times and return the mean correlation matrix. (10 points)

```
library(MASS)

var.wr23.df <- var(wr23.df)
mean.wr23.df <- colMeans(wr23.df)

sim <- mvrnorm(30, mu = mean.wr23.df, Sigma = var.wr23.df)
sim.df <- as.data.frame(sim)

sim.matrix <- cor(sim.df)
sim.matrix
```

```
##            rec_att   rec_yds   rec_tds  rush_att  rush_yds  rush_tds   fumbles
## rec_att  1.0000000 0.9765594 0.9768014 0.5541054 0.5206232 0.4359737 0.6444594
## rec_yds  0.9765594 1.0000000 0.9711872 0.4753867 0.4329781 0.3949890 0.6293757
## rec_tds  0.9768014 0.9711872 1.0000000 0.4358826 0.4097618 0.3541964 0.5966012
## rush_att 0.5541054 0.4753867 0.4358826 1.0000000 0.9491220 0.8128254 0.5538708
## rush_yds 0.5206232 0.4329781 0.4097618 0.9491220 1.0000000 0.9100954 0.5390258
## rush_tds 0.4359737 0.3949890 0.3541964 0.8128254 0.9100954 1.0000000 0.5206031
## fumbles  0.6444594 0.6293757 0.5966012 0.5538708 0.5390258 0.5206031 1.0000000
## fpts     0.9861085 0.9964053 0.9821103 0.5122496 0.4800669 0.4365000 0.6318189
##              fpts
## rec_att  0.9861085
## rec_yds  0.9964053
## rec_tds  0.9821103
## rush_att 0.5122496
## rush_yds 0.4800669
## rush_tds 0.4365000
## fumbles  0.6318189
## fpts     1.0000000
```

```
keep.1=0
loops=1000
```

```
for (i in 1:loops){
      sim2 <- mvrnorm(30, mu = mean.wr23.df, Sigma = var.wr23.df)
      sim2.matrix <- keep.1+cor(sim2)/loops
}

sim2.matrix
```

```
##                rec_att       rec_yds       rec_tds     rush_att     rush_yds
## rec_att   1.000000e-03  9.748363e-04  9.733791e-04 9.366844e-05 7.517513e-05
## rec_yds   9.748363e-04  1.000000e-03  9.756412e-04 9.123550e-05 6.484852e-05
## rec_tds   9.733791e-04  9.756412e-04  1.000000e-03 4.090452e-05 1.094207e-05
## rush_att  9.366844e-05  9.123550e-05  4.090452e-05 1.000000e-03 9.494793e-04
## rush_yds  7.517513e-05  6.484852e-05  1.094207e-05 9.494793e-04 1.000000e-03
## rush_tds -1.873136e-05 -2.522219e-05 -8.317690e-05 8.313376e-04 9.092258e-04
## fumbles   7.718322e-04  7.675817e-04  7.273057e-04 1.974602e-04 1.746754e-04
## fpts      9.782027e-04  9.967942e-04  9.813811e-04 1.439216e-04 1.208035e-04
##                rush_tds      fumbles         fpts
## rec_att  -1.873136e-05 7.718322e-04 9.782027e-04
## rec_yds  -2.522219e-05 7.675817e-04 9.967942e-04
## rec_tds  -8.317690e-05 7.273057e-04 9.813811e-04
## rush_att  8.313376e-04 1.974602e-04 1.439216e-04
## rush_yds  9.092258e-04 1.746754e-04 1.208035e-04
## rush_tds  1.000000e-03 7.903137e-05 2.776676e-05
## fumbles   7.903137e-05 1.000000e-03 7.642516e-04
## fpts      2.776676e-05 7.642516e-04 1.000000e-03
```

Question 3

21 points

Here's some code:

```
nDist <- function(n = 100) {
    df <- 10
    prob <- 1/3
    shape <- 1
    size <- 16
    list(
        beta = rbeta(n, shape1 = 5, shape2 = 45),
        binomial = rbinom(n, size, prob),
        chisquared = rchisq(n, df),
        exponential = rexp(n),
        f = rf(n, df1 = 11, df2 = 17),
        gamma = rgamma(n, shape),
        geometric = rgeom(n, prob),
        hypergeometric = rhyper(n, m = 50, n = 100, k = 8),
        lognormal = rlnorm(n),
        negbinomial = rnbinom(n, size, prob),
        normal = rnorm(n),
        poisson = rpois(n, lambda = 25),
        t = rt(n, df),
        uniform = runif(n),
        weibull = rweibull(n, shape)
```

```
    )
}
```

1. What does this do? (3 points)

```
round(sapply(nDist(500), mean), 2)
```

```
##           beta       binomial     chisquared    exponential              f
##           0.10           5.34           9.79           1.05           1.14
##          gamma      geometric hypergeometric      lognormal    negbinomial
##           1.01           2.02           2.64           1.72          31.49
##         normal        poisson              t        uniform        weibull
##          -0.03          25.06          -0.03           0.50           1.00
```

Here, 'sapply' is running the nDist function (defined above) on the value of 500. Further, we have specified that 'sapply' return the mean values of each output (e.g., beta, binomial, chisquared) and round the numerical value to 2 decimal places.

2. What about this? (3 points)

```
sort(apply(replicate(20, round(sapply(nDist(10000), mean), 2)), 1, sd))
```

```
##           beta        uniform              t              f hypergeometric
##    0.000000000    0.002236068    0.006958524    0.007451598    0.009445132
##         normal        weibull    exponential          gamma       binomial
##    0.009880869    0.010208356    0.011367081    0.011367081    0.018750439
##      lognormal      geometric     chisquared        poisson    negbinomial
##    0.018890265    0.026051568    0.043585971    0.053692595    0.085075818
```

We are using 'sapply' to run the nDist function on the value of 10000 and specifying it return the mean values of each output rounded to 2 decimal places. Additionally, we are asking this command to be replicated 20 times and to sort the outputted means in a matrix. Finally, we are asking to find the standard deviation of each mean, then sort the results from lowest to highest.

In the output above, a small value would indicate that `N=10,000` would provide a sufficent sample size as to estimate the mean of the distribution. Let's say that a value *less than 0.02* is "close enough".

3. For each distribution, estimate the sample size required to simulate the distribution's mean. (15 points)

```
#sizeDist = c()
#n=100000
#
#   while(length(sizeDist) != 15){
#    sdDist = rowMeans(replicate(100, {
#                                  apply(replicate(20, round(sapply(nDist(n), mean), 2)), 1, sd)
#                                      }))
#    x = sdDist[which(sdDist < 0.02)]
#    sizeDist[setdiff(names(x), names(sizeDist))]= n
#    n=n+1000
#  }

#sizeDist
```

Don't worry about being exact. It should already be clear that N < 10,000 for many of the distributions. You don't have to show your work. Put your answer to the right of the vertical bars (|) below.

distribution	N
beta	100
binomial	8,000
chisquared	50,000
exponential	2,500
f	1,200
gamma	2,500
geometric	15,000
hypergeometric	4,300
lognormal	12,000
negbinomial	200,000
normal	2,500
poisson	70,000
t	3,000
uniform	300
weibull	2,600