

## Equations for Exam #2

$$\begin{aligned}\tau_n &= \frac{1}{\alpha_r(n_0 + p_0)} \\ g_{op} &= \alpha_r [(n_0 + p_0) * \delta_n + \delta_n^2] \\ n_i^2 &= p_0 * n_0 \\ E_{F_n} - E_i &= kT \ln \frac{n_n}{n_i} \approx kT \ln \frac{N_D^-}{n_i} \\ E_{F_p} - E_i &= kT \ln \frac{p_p}{n_i} \approx kT \ln \frac{N_A^+}{n_i}\end{aligned}$$

For n-type sample:

$$\begin{aligned}F_n - E_i &= kT \ln \frac{n_n}{n_i}, n_n = n_{n0} + \delta_n \\ E_i - F_p &= kT \ln \frac{p_p}{n_i}, p_p = p_{p0} + \delta_p \\ \sigma_n &= q [\mu_p p_n + \mu_n n_n] \\ \text{For p-type sample:}\end{aligned}$$

$$\begin{aligned}F_n - E_i &= kT \ln \frac{n_p}{n_i}, n_p = n_{p0} + \delta_n \\ E_i - F_p &= kT \ln \frac{p_p}{n_i}, p_p = p_{p0} + \delta_p \\ \sigma_p &= q [\mu_p p_p + \mu_n n_p]\end{aligned}$$

$$\begin{aligned}J &= \sigma \vec{\varepsilon} \quad (\text{if } \vec{\varepsilon} > \varepsilon_c, J = q(n + p)v_{sat}) \\ D &= \frac{kT}{q}\mu, L = \sqrt{D\tau}\end{aligned}$$

$$qV_0 = (E_{F_n} - E_{F_p}) = kT \ln \frac{n_{n0}p_{n0}}{n_i^2}$$

$$\frac{p_p}{p_n} = \frac{n_n}{n_p} = e^{qV_0/kT}$$

$$\begin{aligned}\vec{\varepsilon}_0 &\equiv \text{Max Field at Junction} = -\frac{q}{\epsilon_s} N_D x_{n0} \\ &= -\frac{q}{\epsilon_s} N_A x_{p0}\end{aligned}$$

$$\begin{aligned}V_0 &= -\frac{1}{2\epsilon} * \frac{N_A N_D}{N_A + N_D} W^2 \\ W &= \left[ \frac{2\epsilon}{q} V_0 \left( \frac{1}{N_A} + \frac{1}{N_D} \right) \right]^{1/2} \\ &= \left[ \frac{2\epsilon}{q} (V_0 - V) \left( \frac{1}{N_A} + \frac{1}{N_D} \right) \right]^{1/2} \quad (\text{with bias})\end{aligned}$$

$$\epsilon_s = \epsilon_{r_s} \epsilon_0$$

$$x_{p0} = \frac{W}{1 + \frac{N_A}{N_D}}, \quad x_{n0} = \frac{W}{1 + \frac{N_D}{N_A}}$$

$$C_j = \frac{\epsilon_s}{W} (F/cm^2)$$

$$I = I_0 (e^{V/V_T} - 1); V_T = \frac{kT}{q}$$

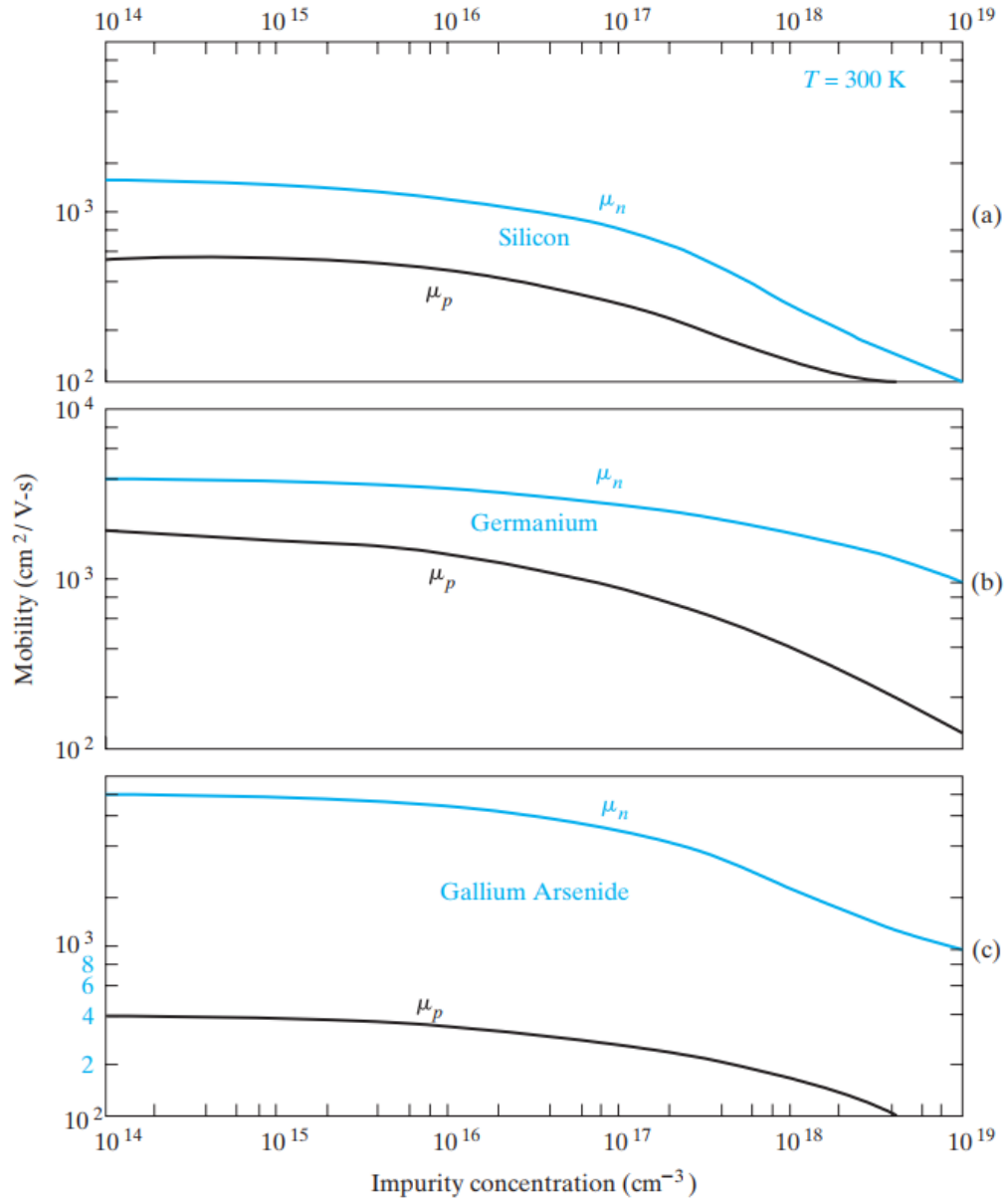
$$I_0 = qA \left[ \frac{D_p p_n}{L_p} + \frac{D_n n_p}{L_n} \right]$$

$$\begin{aligned}Q_+ &= qA x_{n0} N_D = qA x_{p0} N_A \\ \delta n(x_p) &= \Delta n_p e^{-x_p/L_n} = n_p (e^{V/V_T} - 1) e^{-x_p/L_n} \\ \delta p(x_n) &= \Delta p_n e^{-x_n/L_p} = p_n (e^{V/V_T} - 1) e^{-x_n/L_p}\end{aligned}$$

$$\begin{aligned}x_{p0} &= \left[ \frac{2\epsilon}{q} V_0 \left( \frac{N_D}{N_A(N_A + N_D)} \right) \right]^{1/2} \\ x_{n0} &= \left[ \frac{2\epsilon}{q} V_0 \left( \frac{N_A}{N_D(N_A + N_D)} \right) \right]^{1/2}\end{aligned}$$

Constants:

$$\begin{aligned}q &= 1.6 \times 10^{-19} \text{ C} \\ \epsilon_0 &= 8.85 \times 10^{-14} \text{ Fm}^{-1}, \epsilon_{r_{Si}} = 11.8 \\ h &= 6.626 \times 10^{-34} \text{ m}^2\text{kg/s} \\ \hbar &= \frac{h}{2\pi} = 1.055 \times 10^{-31} \text{ Js/rad} \\ m^* &= 9.11 \times 10^{-31} \text{ kg} \\ kT|_{T=300K} &\approx 0.026 \text{ eV} \\ n_i(Si)|_{300K} &= 1.5 \times 10^{10} \text{ cm}^{-3} \\ v_{th} &= \text{Thermal Velocity} \approx 10^7 \text{ cm/sec} \\ \vec{\varepsilon}_c &= \text{critical field} = 10^4 \text{ V/cm}\end{aligned}$$



**Figure 3–23**

Variation of mobility with total doping impurity concentration ( $N_a + N_d$ ) for Ge, Si, and GaAs at 300 K.

**Figure 3–17**  
Intrinsic carrier concentration for Ge, Si, and GaAs as a function of inverse temperature. The room temperature values are marked for reference.

