

# Computer Vision

## 1. Camera

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# Outline

- ▶ Pinhole cameras
- ▶ Cameras with lenses
- ▶ Human eyes

## **Textbook:**

- David A. Forsyth and Jean Ponce, Computer Vision: A Modern Approach, Prentice Hall, New Jersey, (1<sup>st</sup> Ed. 2003, 2<sup>nd</sup> Ed. 2012) .

## **Some contents are from the reference lecture notes:**

- Prof. D.A. Forsyth, Computer Vision, UIUC.
- Prof. T. Darrell, Computer Vision and Applications, MIT.
- Prof. J. Rehg, Computer Vision, Georgia Inst. of Tech.
- Prof. D. Lowe, Computer Vision, UBC, CA.

# Which one is more realistic?

► How about these pictures?

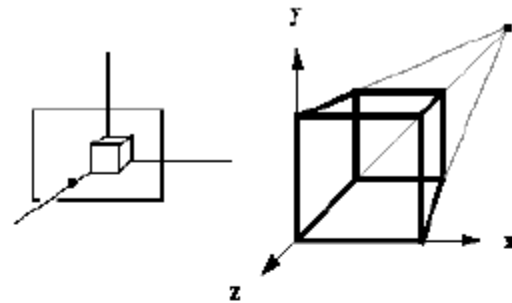
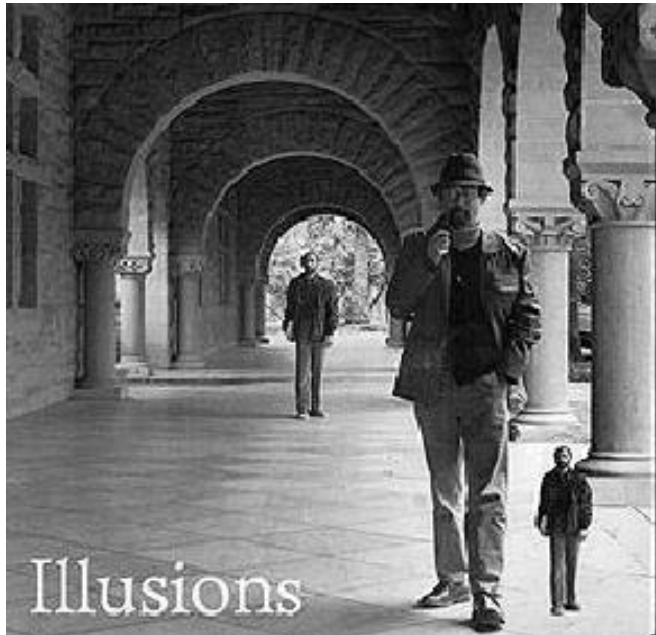


Picasso, The Dream, 1932  
(Cubism)

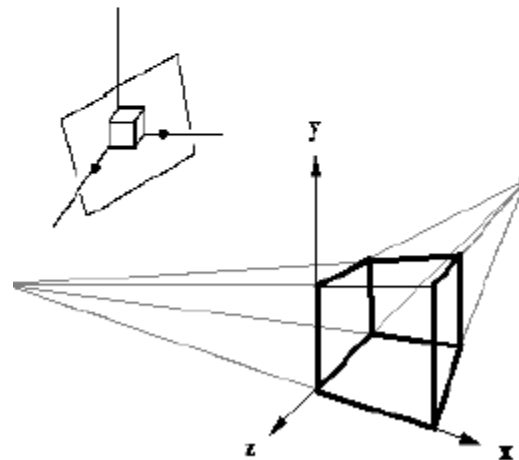


Raphael, The School of Athens, around 1509-1511  
(the Renaissance)

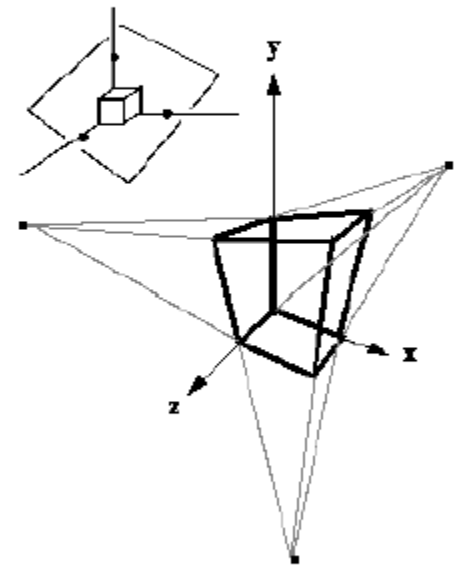
# Vanishing points



*One Point Perspective*  
(z-axis vanishing point)



*Two Point Perspective*  
z, and x-axis vanishing points



*Three Point Perspective*  
(z, x, and y-axis  
vanishing points)

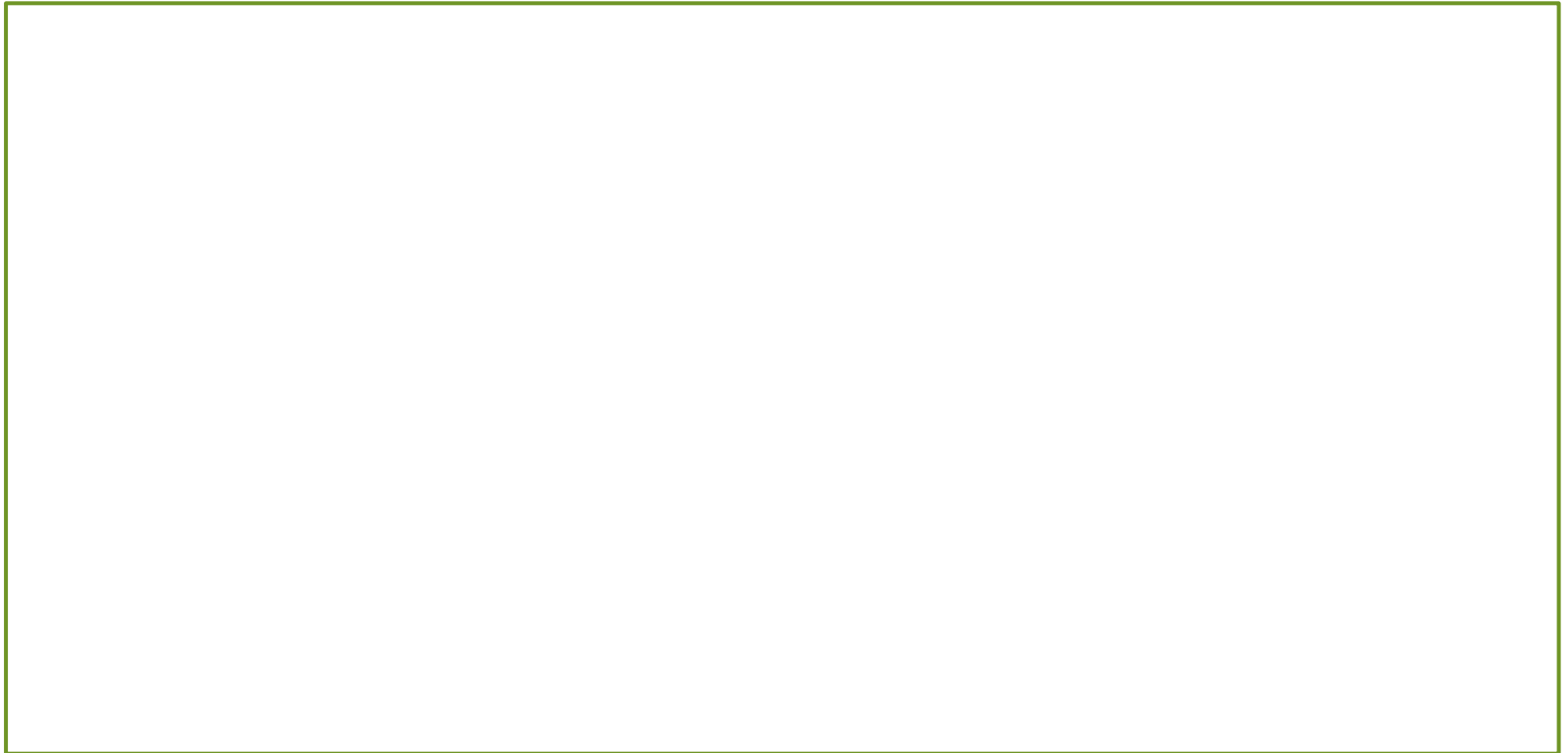
# Drawing with vanishing points



Examples of two vanishing points: <http://www.alifetimeofcolor.com/main.taf?p=2,1,1,15>

# Camera obscura

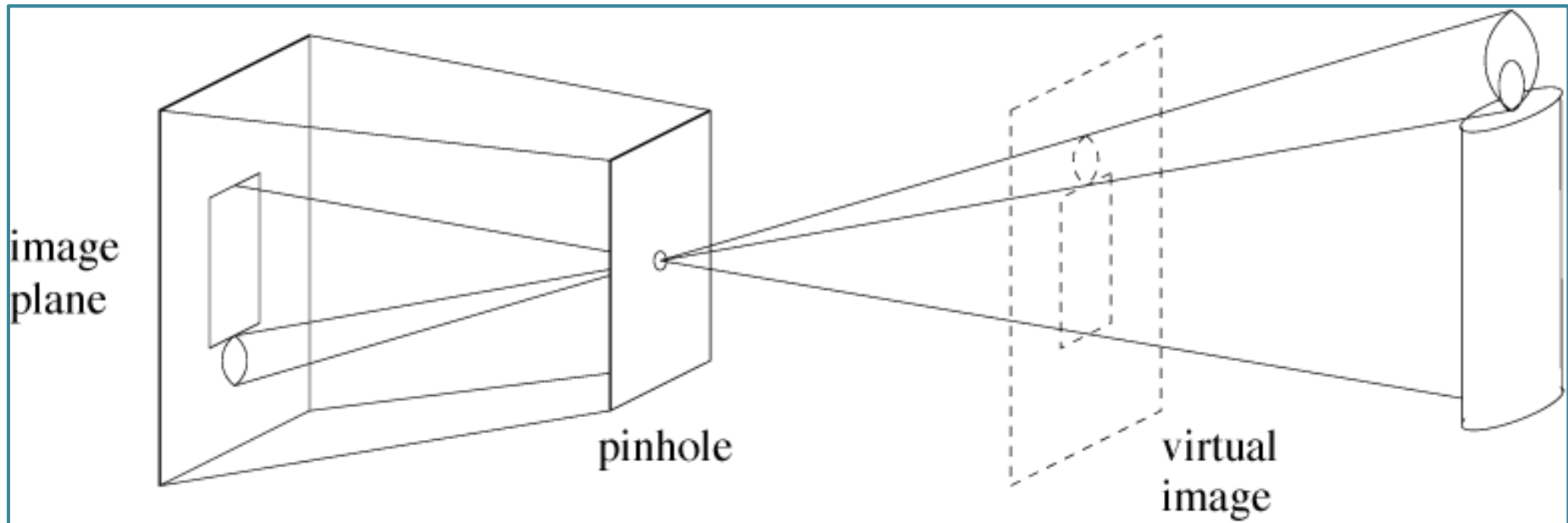
- ▶ Camera Obscura, Reinerus Gemma-Frisius, 1544
  - ▶ (L. dark chamber), an aid to painting, consists of a darkened box and a small aperture where light passes.



[http://www.acmi.net.au/AIC/CAMERA\\_OBSCURA.html](http://www.acmi.net.au/AIC/CAMERA_OBSCURA.html)

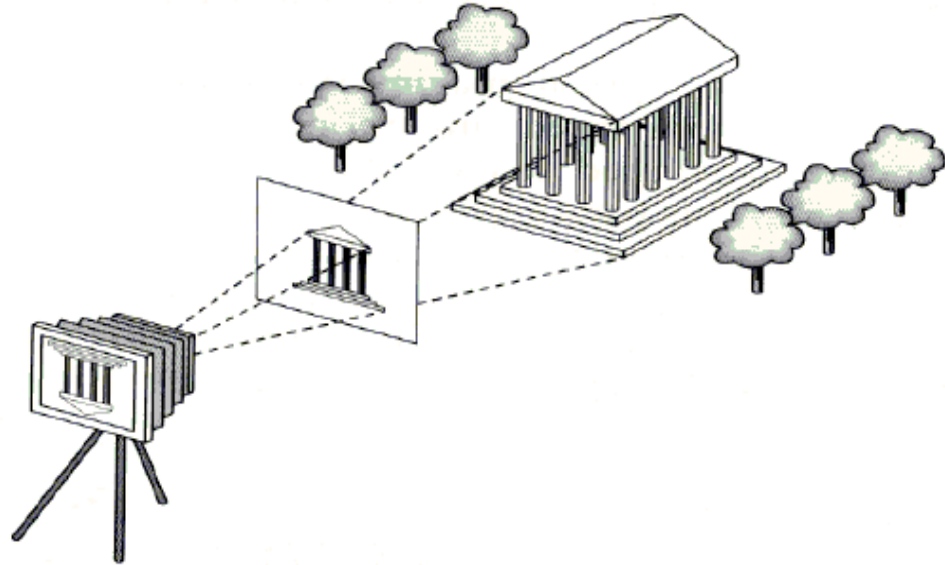
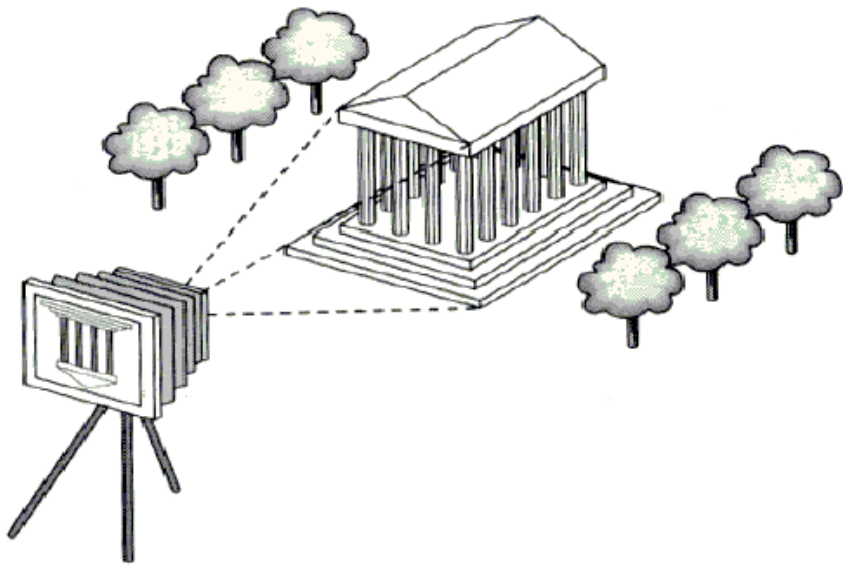
# Pinhole model

- ▶ Pinhole camera – a box with a small hole in it.
- ▶ Image is upside down.
- ▶ (We usually use a virtual plane on the opposite side of the image plane)



# Perspective projection

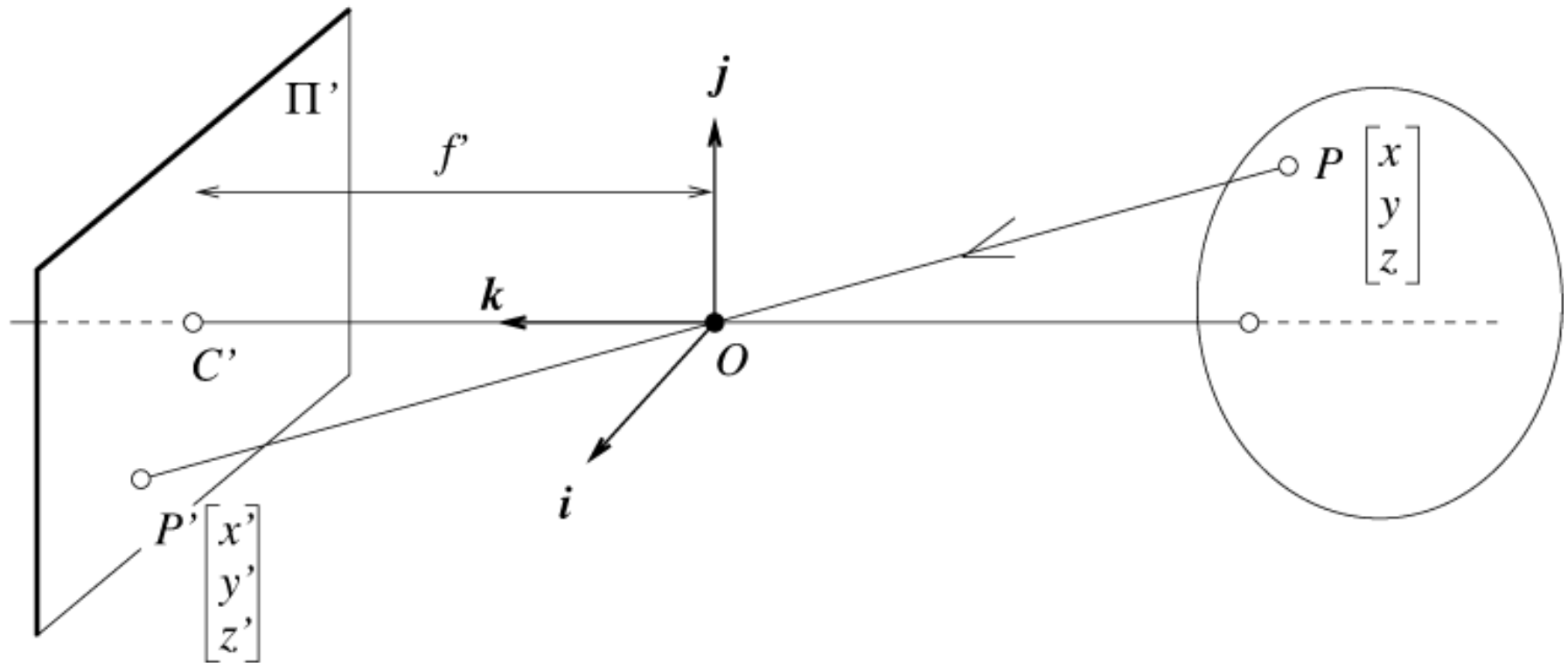
- ▶ Taking photographing as an example.
- ▶ A camera records the lights on projective paths.





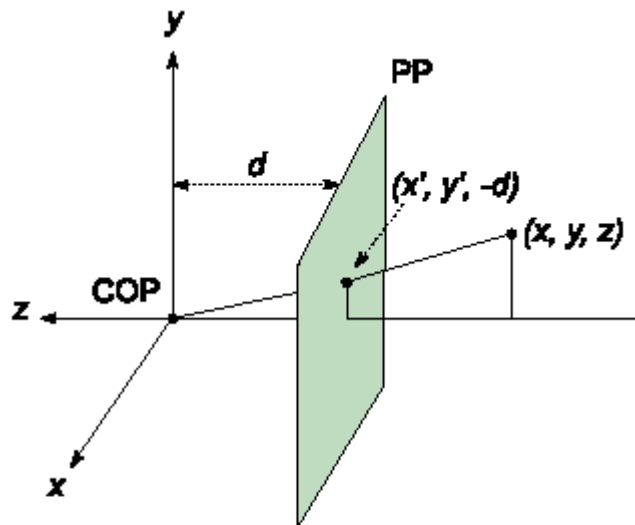
# Perspective projection with the pinhole model

►  $x' = f'(x/z) ; y' = f'(y/z)$

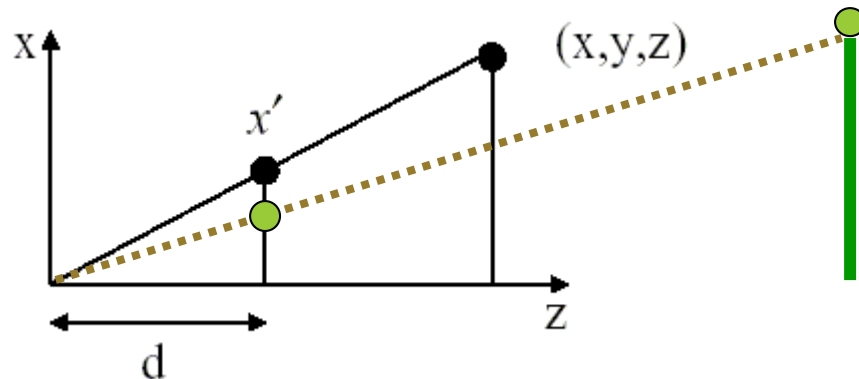


# Perspective projection (cont.)

## ► Projection

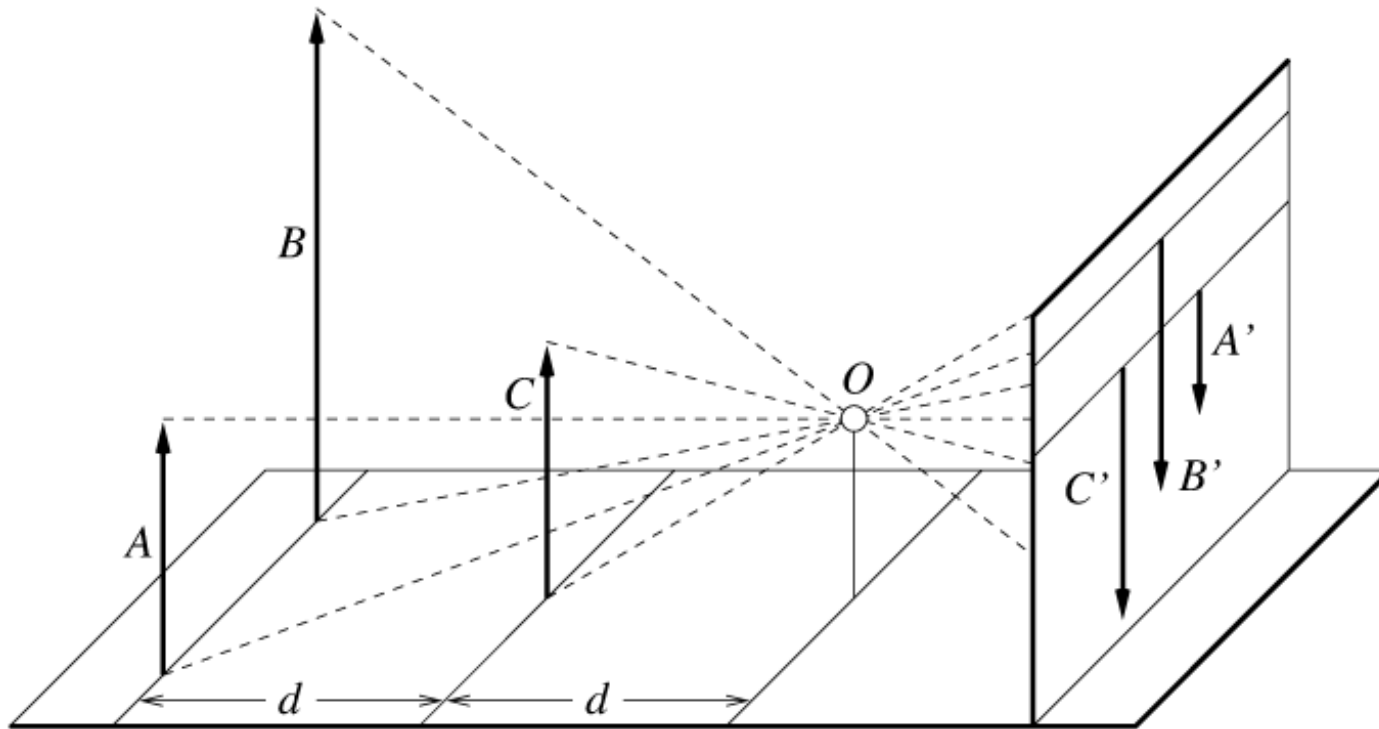


Using similar triangles gives:



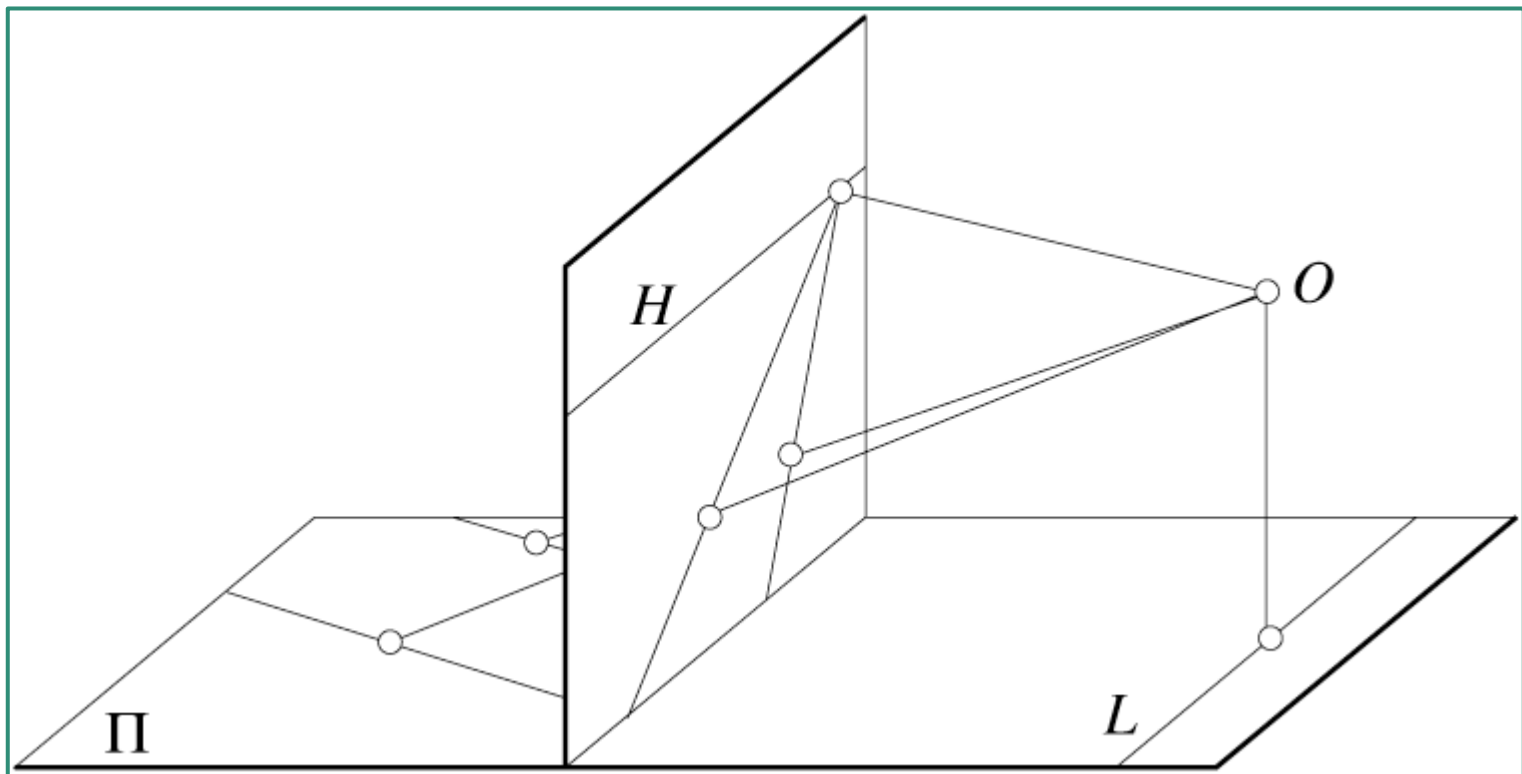
[http://commons.wikimedia.org/wiki/File:Taiwan\\_HighSpeedRail\\_Train\\_Business\\_Class\\_Car.JPG](http://commons.wikimedia.org/wiki/File:Taiwan_HighSpeedRail_Train_Business_Class_Car.JPG)

# Distant objects are smaller



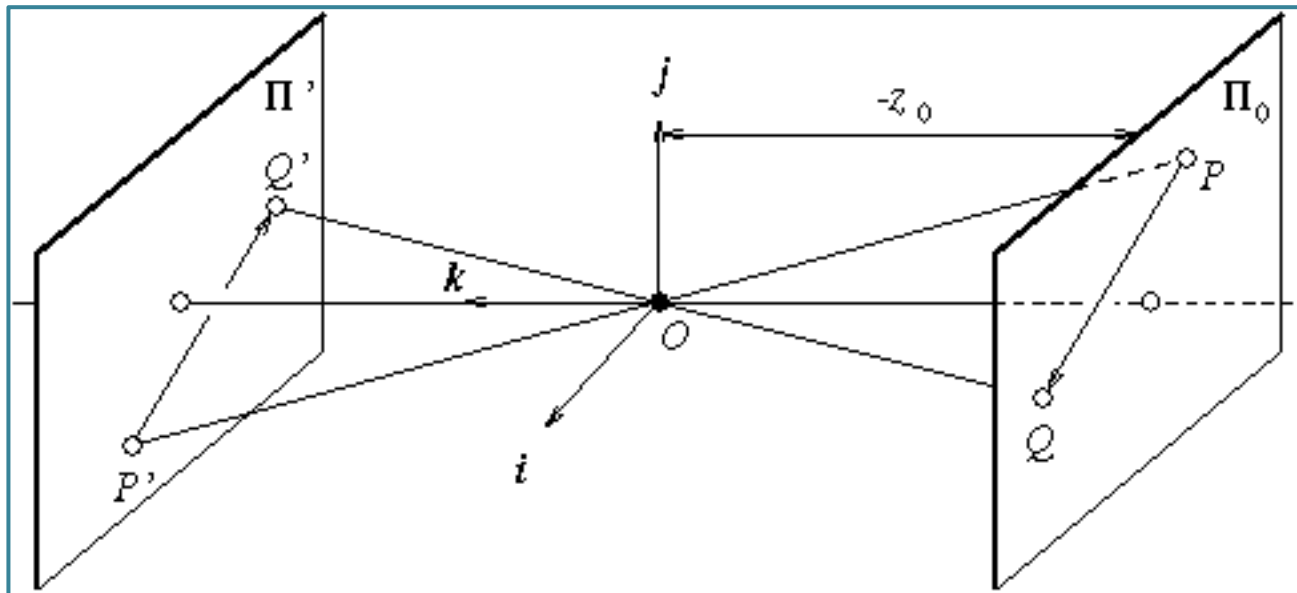
# Vanishing point

- ▶ Each set of parallel lines meets at a different point.
- ▶ Sets of parallel lines on the same plane lead to collinear vanishing points, called the horizon for that plane.



# Weak-perspective

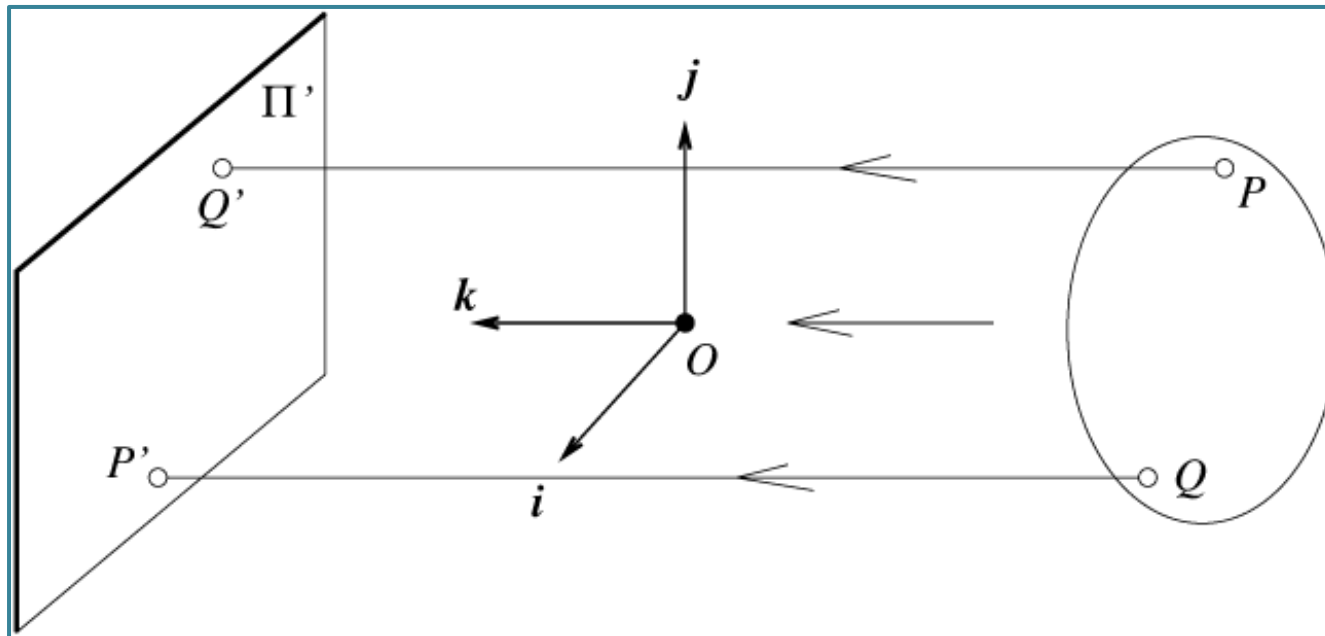
- ▶ When the scene depth is small relative to the average distance from the camera.
- ▶ All line segments in the plane  $\Pi_0$  are projected with the same magnification.
  - ▶ Simple but incorrect.



# Orthographic projection

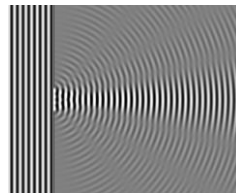
►  $x' = x$

►  $y' = y$

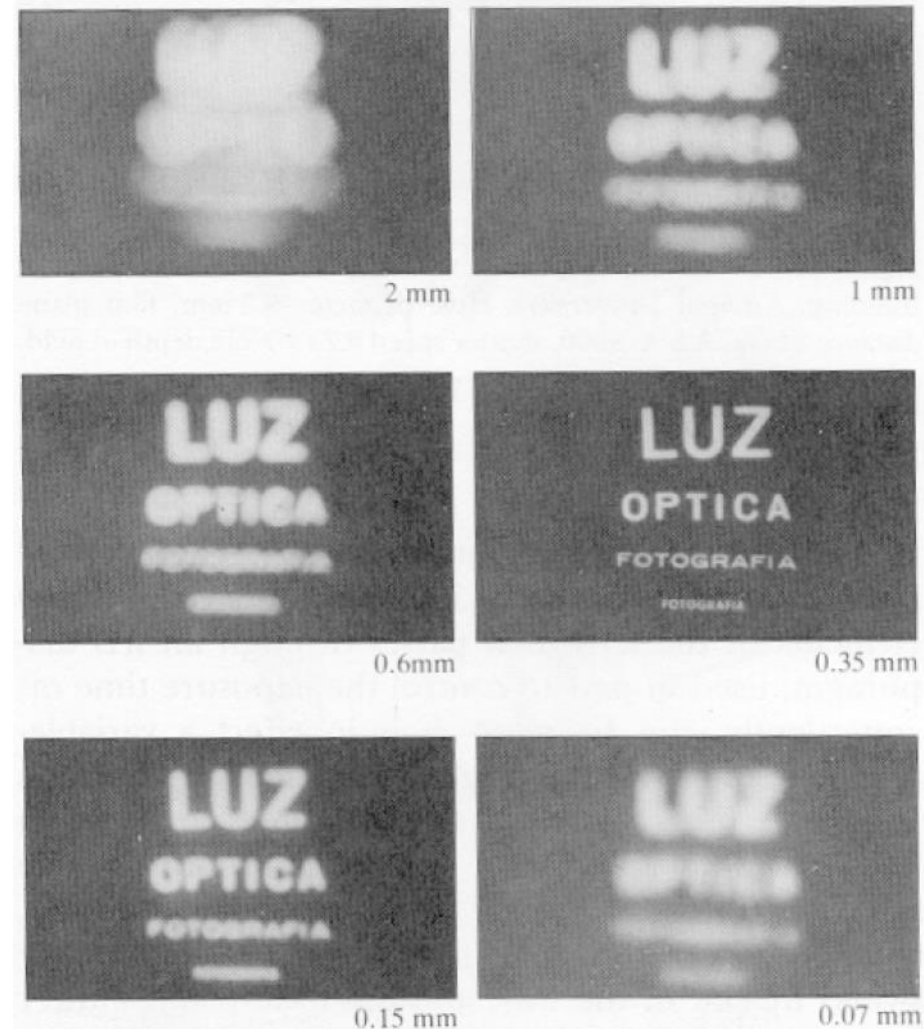


# The problem

- ▶ Pinhole too big:
  - ▶ brighter, but blurred.
- ▶ Pinhole right size:
  - ▶ sharp, but dark.
- ▶ Pinhole too small:
  - ▶ blurred due to diffraction.



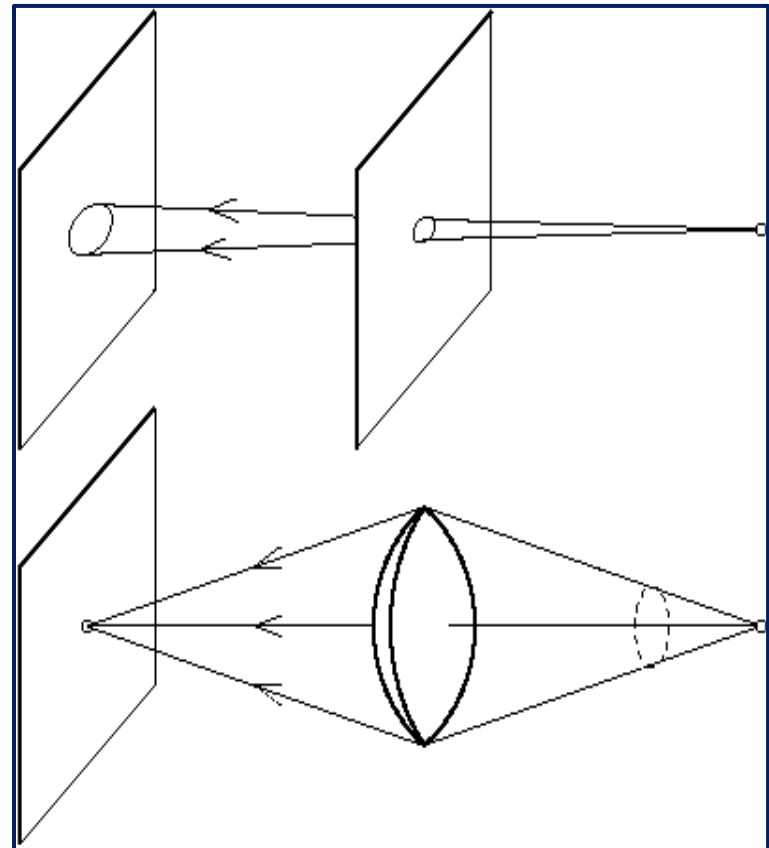
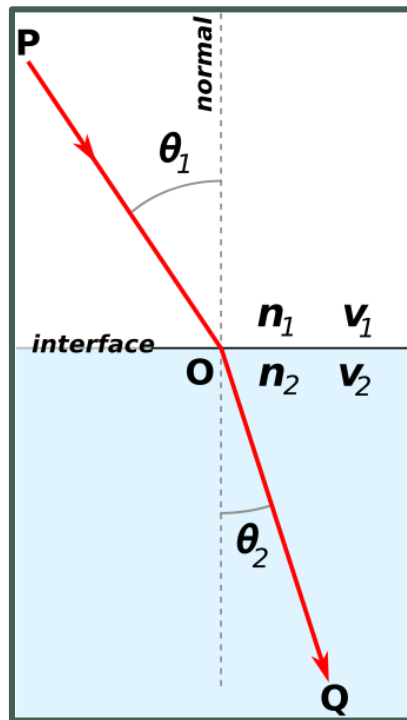
<http://en.wikipedia.org/wiki/Diffraction>



# Cameras with lenses

► According to Snell's law:

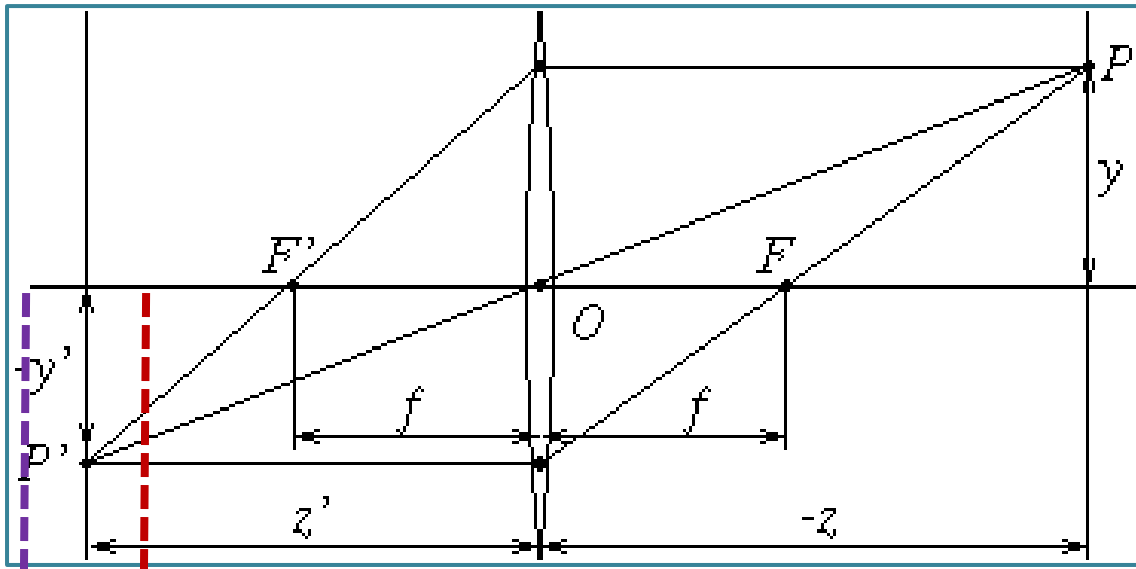
►  $n_1 \sin \theta_1 = n_2 \sin \theta_2$





# Thin lens

- ▶ A lens follows the pinhole model for objects that are in focus.
- ▶ All rays through  $P$  also pass through  $P'$ , but only for points at  $-z$ : “depth of field”.
- ▶ The image becomes blurred if  $P$  is at a “wrong” distance.



$$\frac{1}{z'} - \frac{1}{z} = \frac{1}{f}$$

$$z \rightarrow \infty \Rightarrow \frac{1}{z'} = \frac{1}{f}$$

# Appendix: depth of field

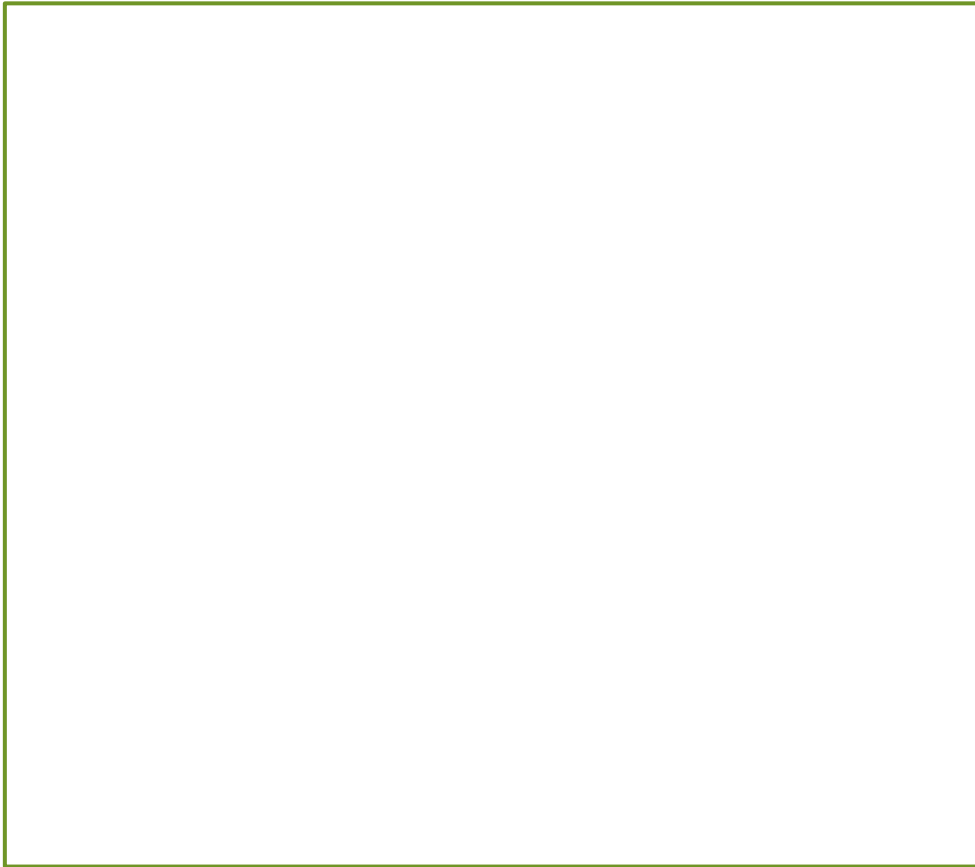
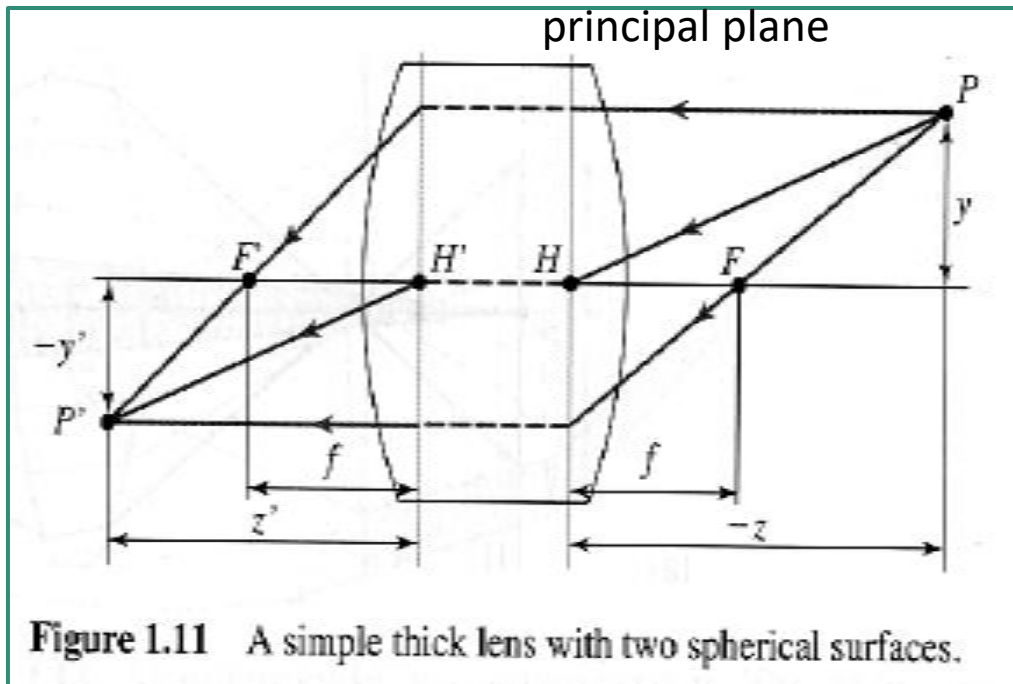


Fig. from: <https://www.vision-doctor.com/en/optical-basics/depth-of-field.html>

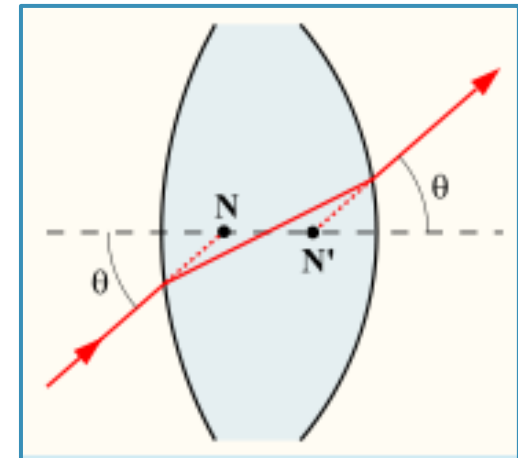


[https://en.wikipedia.org/wiki/Depth\\_of\\_field](https://en.wikipedia.org/wiki/Depth_of_field)

# Real lens



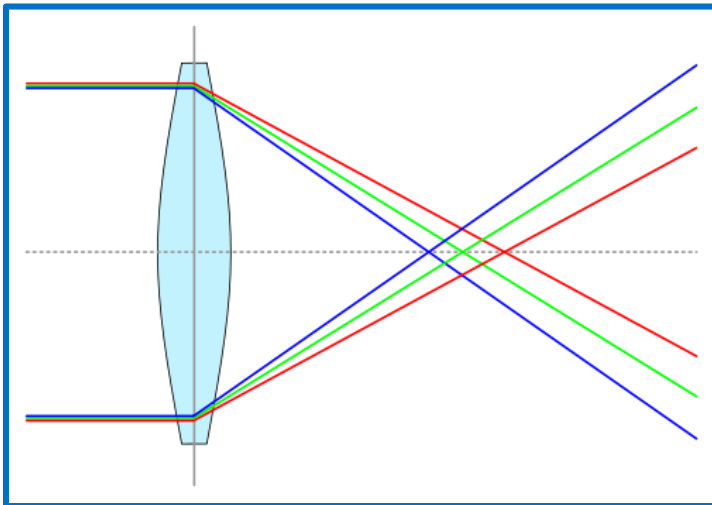
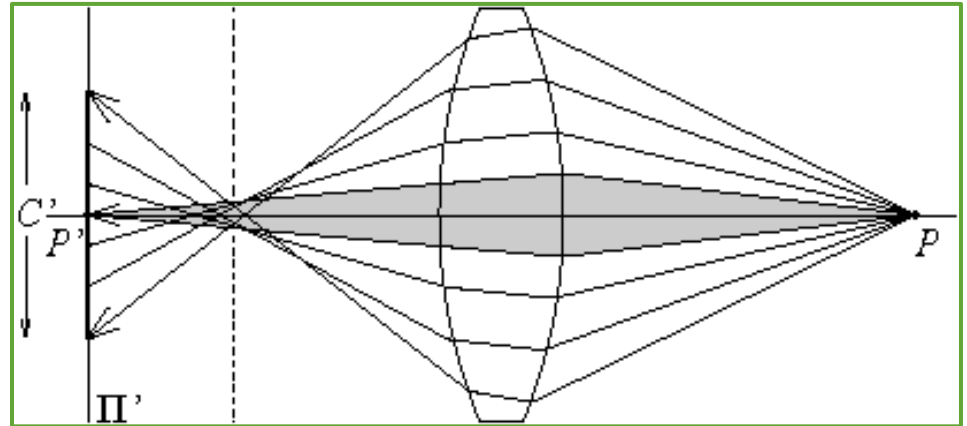
H: principal point



- Our equation based on small incident angle assumption; simple lenses suffer from a number of aberrations.

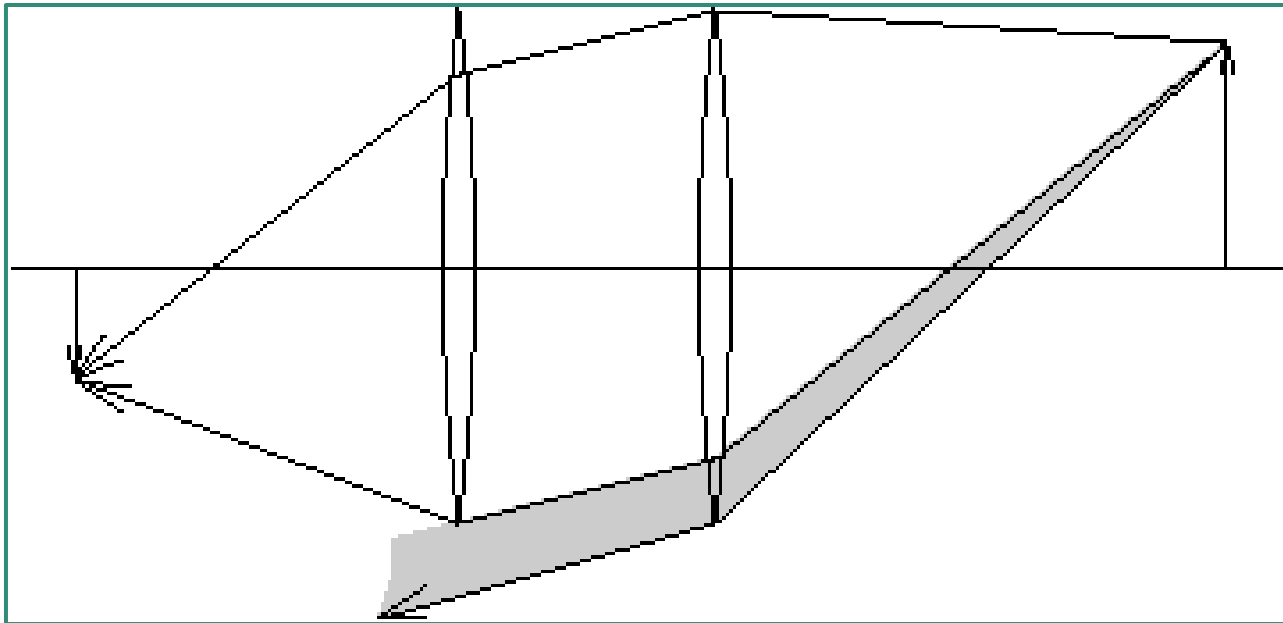
# Aberrations

- Spherical aberration
- Chromatic aberration



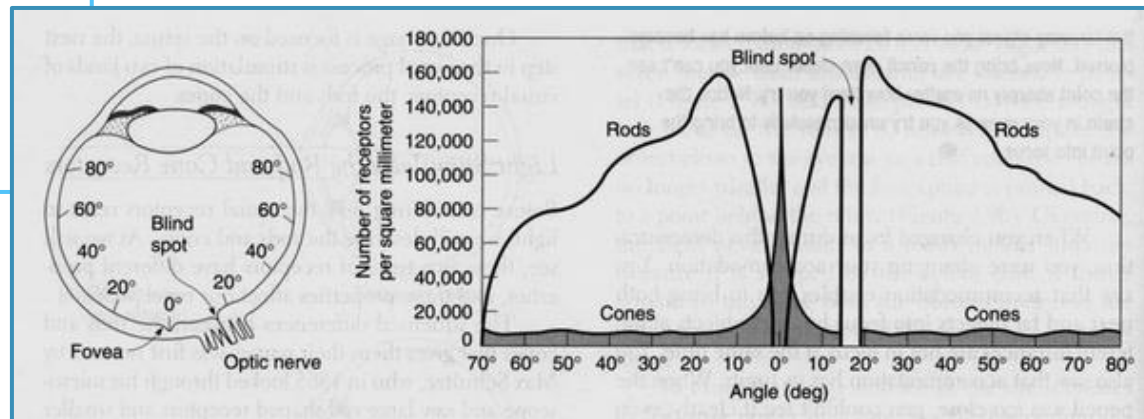
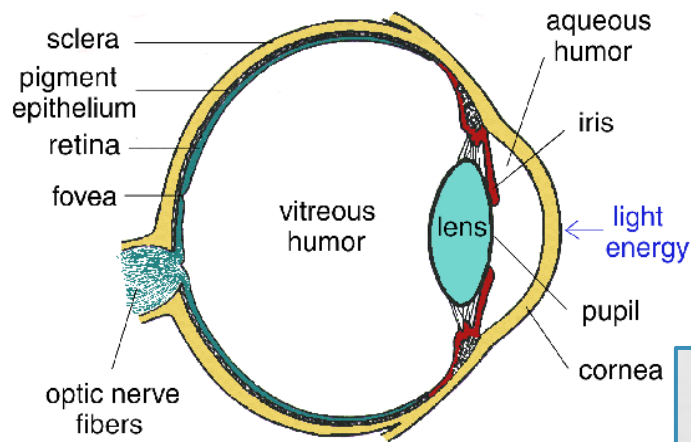
# Compound lenses

- ▶ Aberrations can be minimized by well-chosen lenses.
- ▶ Vignetting effect : the brightness to drop in the image periphery.



# Human eye and refraction

- ▶ Large part of refraction occurs at air-cornea interface
- ▶ It is fine tune through the crystalline lens.



# We still use the pinhole model ...

- ▶ The model does not include geometric distortions or blurring of unfocused objects caused by lenses.
- ▶ Several of such effects can be compensated by additional procedures.
- ▶ It is a good approximation of mapping a 3D scene to a 2D image.