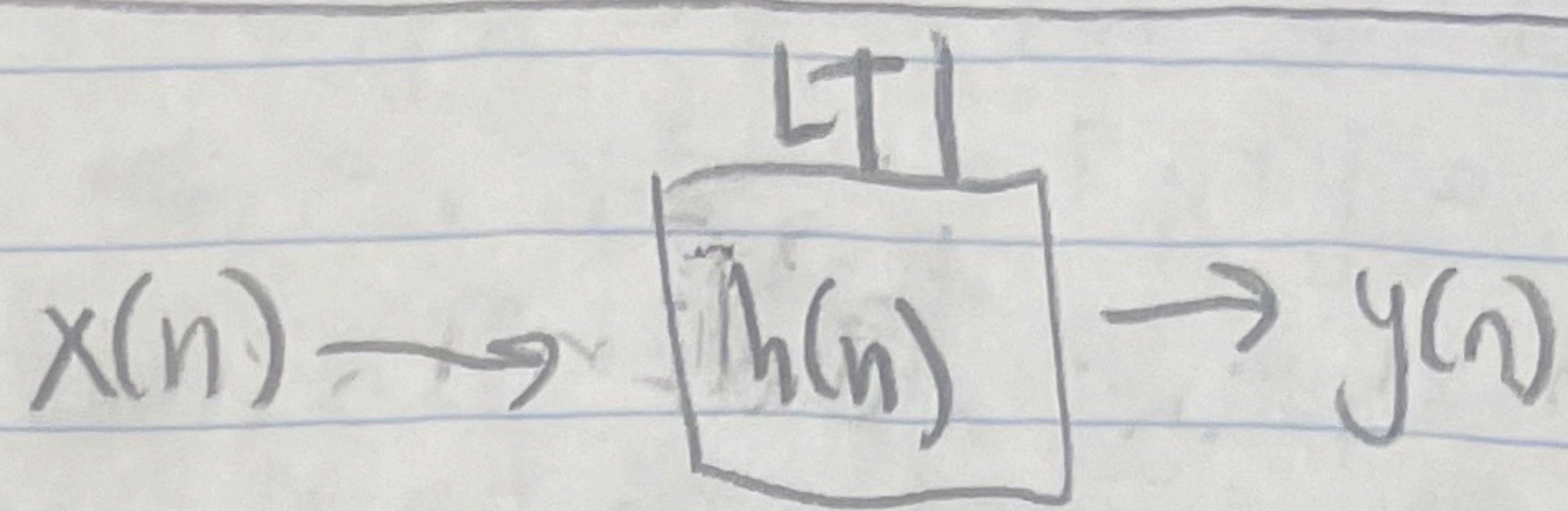


Transistor is Nonlinear
Most practical systems are nonlinear when range is large

5.15



$$y(n) = \sum_{k=-\infty}^{\infty} h[k] x[n-k]$$

a. $h[n] = \delta[n-3]$ $y[n] = 5u[n-2] - u[n-6]$

$$x[n] = 5u[n+1] - u[n-3]$$

b. $\begin{cases} h[n] = u[n-2] \\ x[n] = x[n] - x[n-1] \end{cases}$

$$\sum_{k=0}^{\infty} h[k] x[-k] = 0$$

$$n=1 \quad " \quad h[k] x[1-k] = 0$$

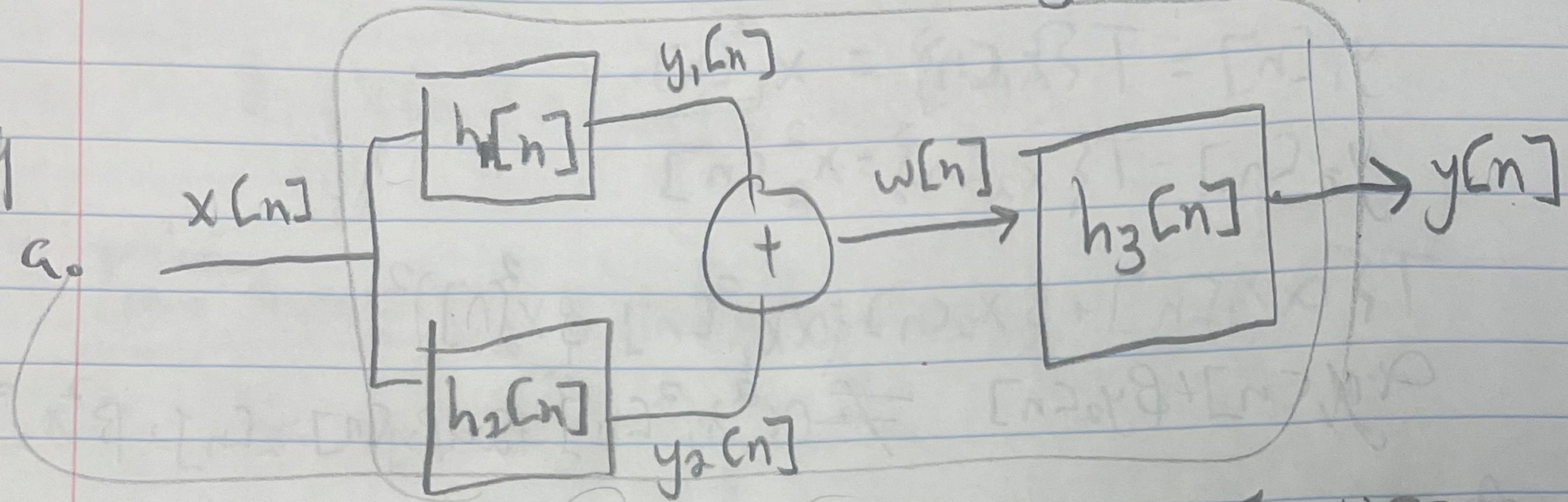
$$n=2 \quad " \quad = 1$$

$$y[n] = x[n-1]$$

Tabular Method of Convolution

c. $y[n] = x[n] - x[n-1]$ $n=2$ $y[2] = x[2] - x[1] = 0$
 \vdots
 $n=2$ $y[2] = x[2] - x[1] = 1$

5.9



$$h_1[n] = \delta[n] + 2\delta[n-1] + 3\delta[n-2] + 4\delta[n-3]$$

$$h_2[n] = \delta[n] + \delta[n-1] + \delta[n-2] + \delta[n-3]$$

$$h_3[n] = \delta[n] - 8\delta[n-1]$$

b. $y_1[n] = h_1[n] * x[n]$

$$y_2[n] = h_2[n] * x[n]$$

$$w[n] = y_1[n] + y_2[n]$$

$$y[n] = h_3[n] * w[n]$$

$$= h_3[n] * (y_1[n] + y_2[n])$$

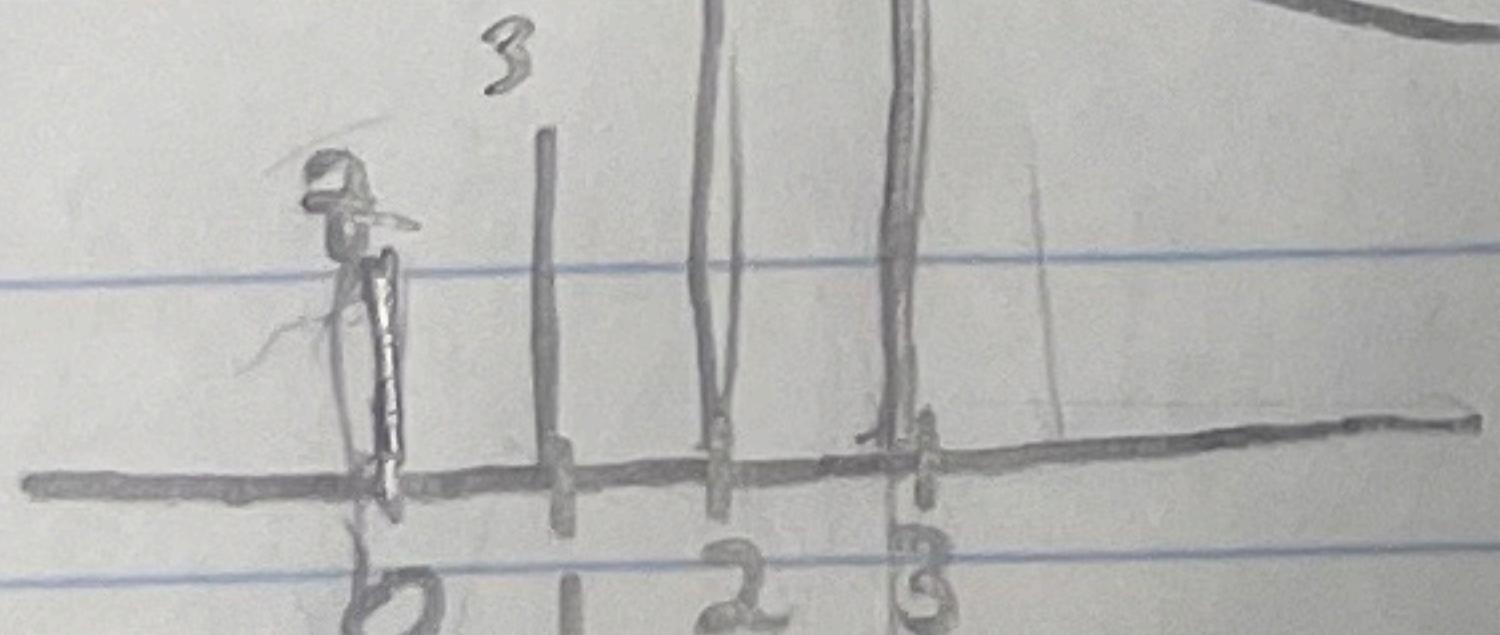
$$= h_3[n] * (h_1[n] * x[n] + h_2[n] * x[n])$$

$$= [h_3[n] * (h_1[n] + h_2[n])] * x[n]$$

$$= [h_3[n] * (2\delta[n] + 3\delta[n-1] + 4\delta[n-2] + 5\delta[n-3])] * x[n]$$

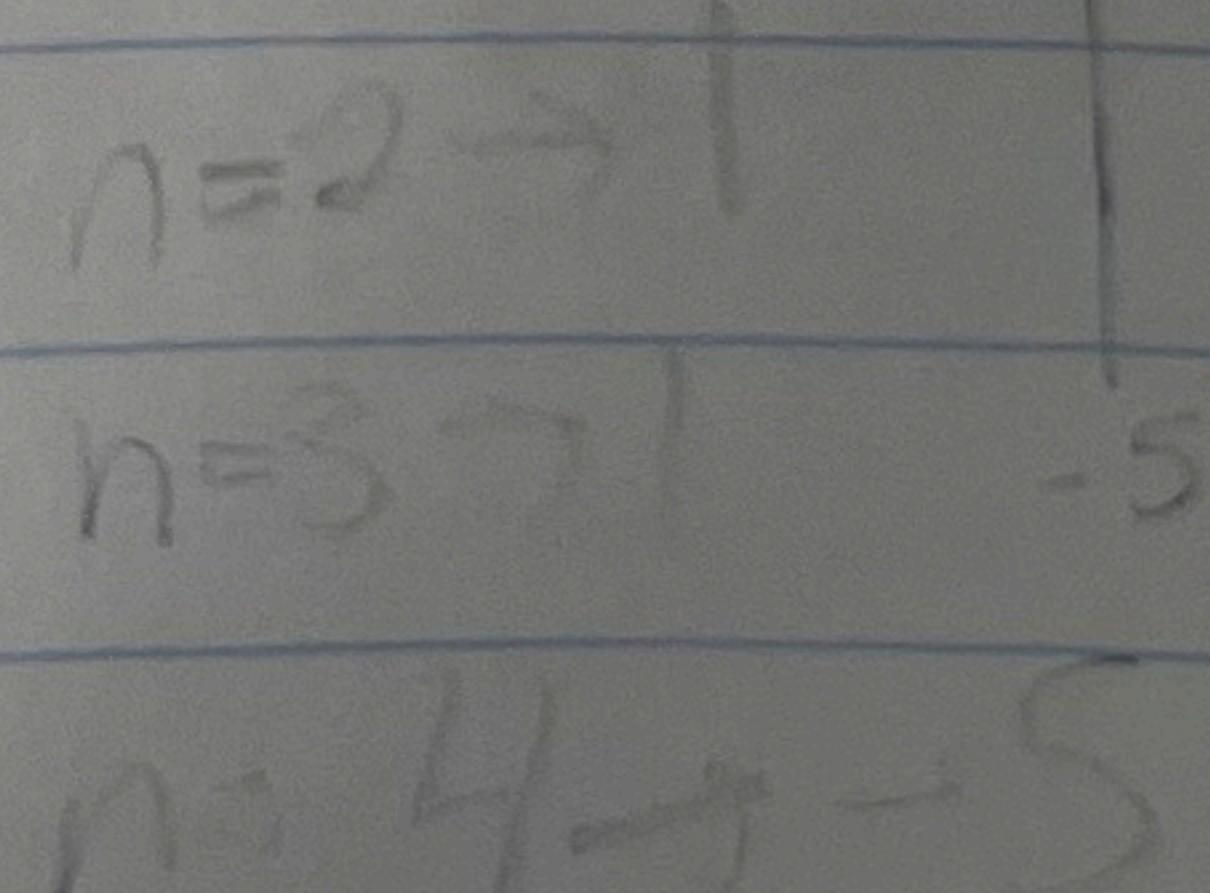
$$= \underbrace{\delta[n] - 8\delta[n-1]}_{\text{impulse response}} * \underbrace{[2\delta[n] + 3\delta[n-1] + 4\delta[n-2] + 5\delta[n-3]]}_{\text{filter coefficients}} * x[n]$$

$h[n]$



$$(2\delta[n] + 3\delta[n-1] + 4\delta[n-2] + 5\delta[n-3] - 8\delta[n-4]) * x[n]$$

$x[n]$



$x[-n]$

