

$$4.13 \text{ a. } x[n] = \frac{1}{\pi} \cos(1.8\pi + 2.03) \quad \text{Convert to primary along}$$

$$= \frac{1}{\pi} \cos(0.2\pi - 2.03) \\ = \frac{1}{\pi} \cos(0.3600\pi) - 2.03$$

Reconstruction Sampling Frequency

Frequency that will be heard is 3200 Hz

$$b. x(t) \cos(\omega t + \frac{\pi}{3})$$
 ~~$\cos(3600t + 3600\pi + \frac{\pi}{3}) = \cos(t + \frac{\pi}{3}) \rightarrow$~~ Sampling must be at least $\frac{1}{3}$ Hz
$$x[t] = \cos(\omega t + \frac{1800\pi + \pi}{2}) + \frac{\pi}{3} \rightarrow \cos(\frac{3600\pi + \pi}{2} + \frac{\pi}{3}) \rightarrow \cos(\frac{3600\pi + \pi}{2} + \frac{\pi}{3})$$

$$\cos(\omega t + \frac{\pi}{3}) \rightarrow \cos(-\frac{\pi}{2} + \frac{\pi}{3}) \rightarrow \cos(\frac{\pi}{2} - \frac{\pi}{3})$$

Convert to primary alias $\rightarrow \cos(\frac{\pi}{2} - \frac{\pi}{3}) = \cos(\frac{\pi}{6})$

To achieve a frequency of 2400 Hz $f_s = \frac{2400}{14800} = 0.1600$

c) Duration = $\frac{64 \times 8000}{4000} = 12.8$

Frequency = $\frac{1}{\text{Duration}} = \frac{1}{12.8} = 0.08$

4.15 $x[n] = 7 \cos(0.7\pi n + 0.2\pi)$: $n \in \mathbb{Z}$

then $x(t)$ is periodic w/ $T_0 = \frac{1}{f_0}$
 $f_0 = \text{fundamental freq}$

g) Find $x_1(t) \wedge x_2(t)$ such that $x[n] = x_1(nT_s) = x_2(nT_s)$ if $T_s = 125 \mu s$

Replace n w/ f_s

$$x(t) = 7 \cos(0.7\pi(8000t) + 0.2\pi)$$

$$= 7 \cos(5600\pi t + 0.2\pi) \rightarrow f = 1400$$

Sub 2π to 0, use even parity

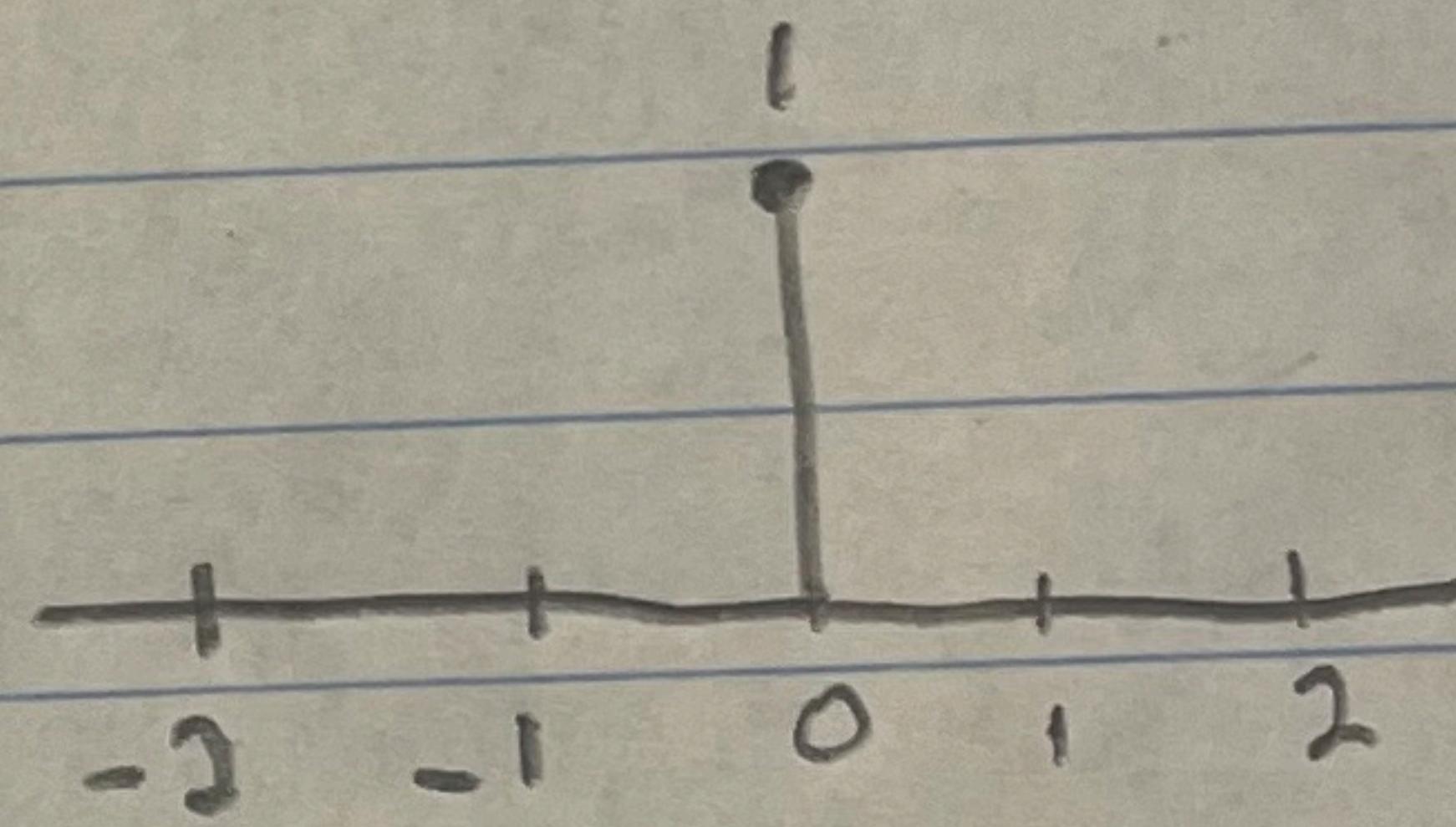
$$x(t) = 7 \cos(-1.3\pi(8000t) - 0.2\pi) \rightarrow f = 5200$$

b) $x[n] = 7 \cos(0.7\pi n + 0.2\pi)$

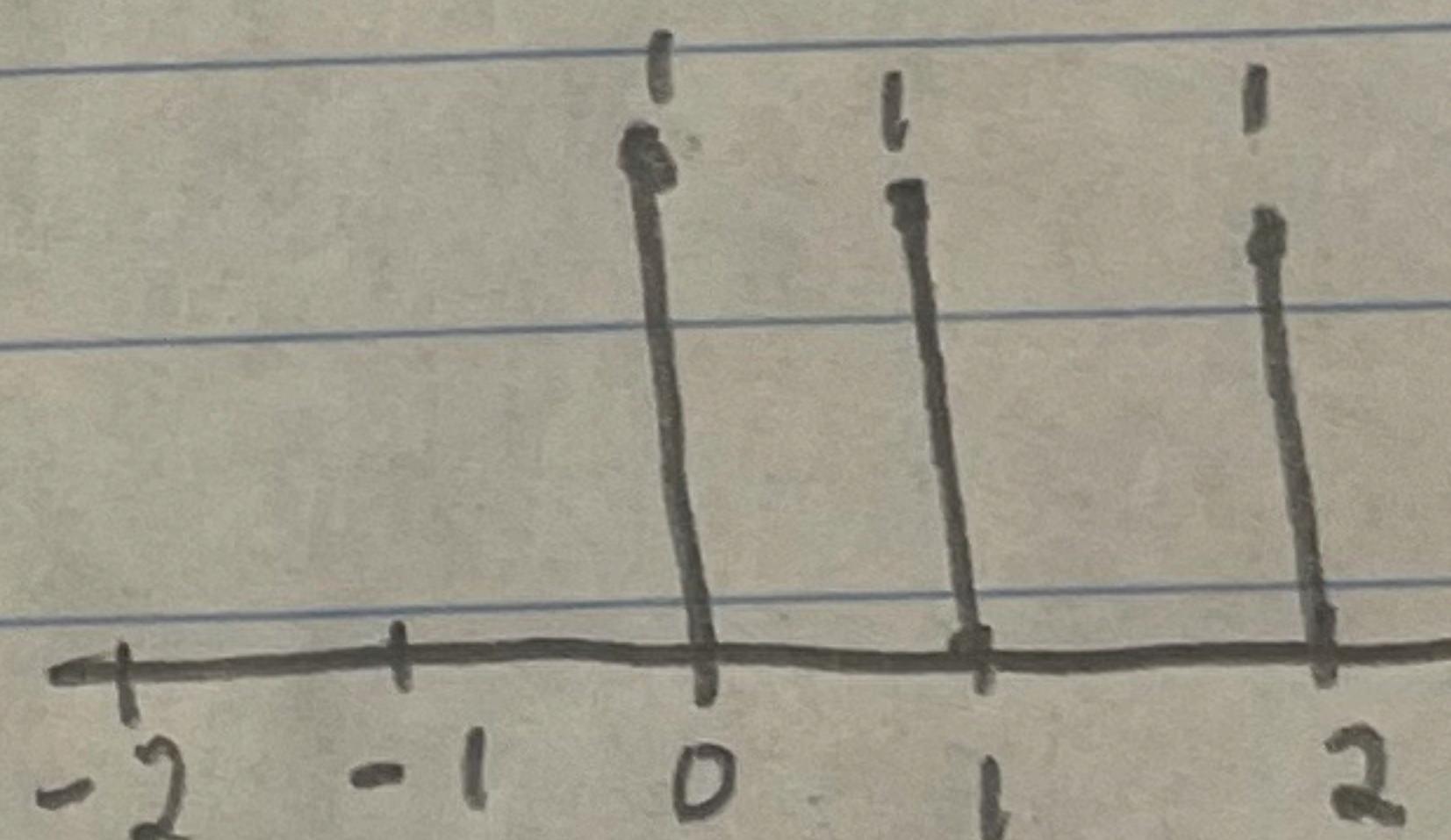
$$x(t) = 7 \cos(0.7\pi(5000t) + 0.2\pi)$$

$$= 7 \cos(3500\pi t + 0.2\pi)$$

$\delta[n]$: unit impulse = $\begin{cases} 1 & \text{when } n=0 \\ 0 & \text{when } n \neq 0 \end{cases}$



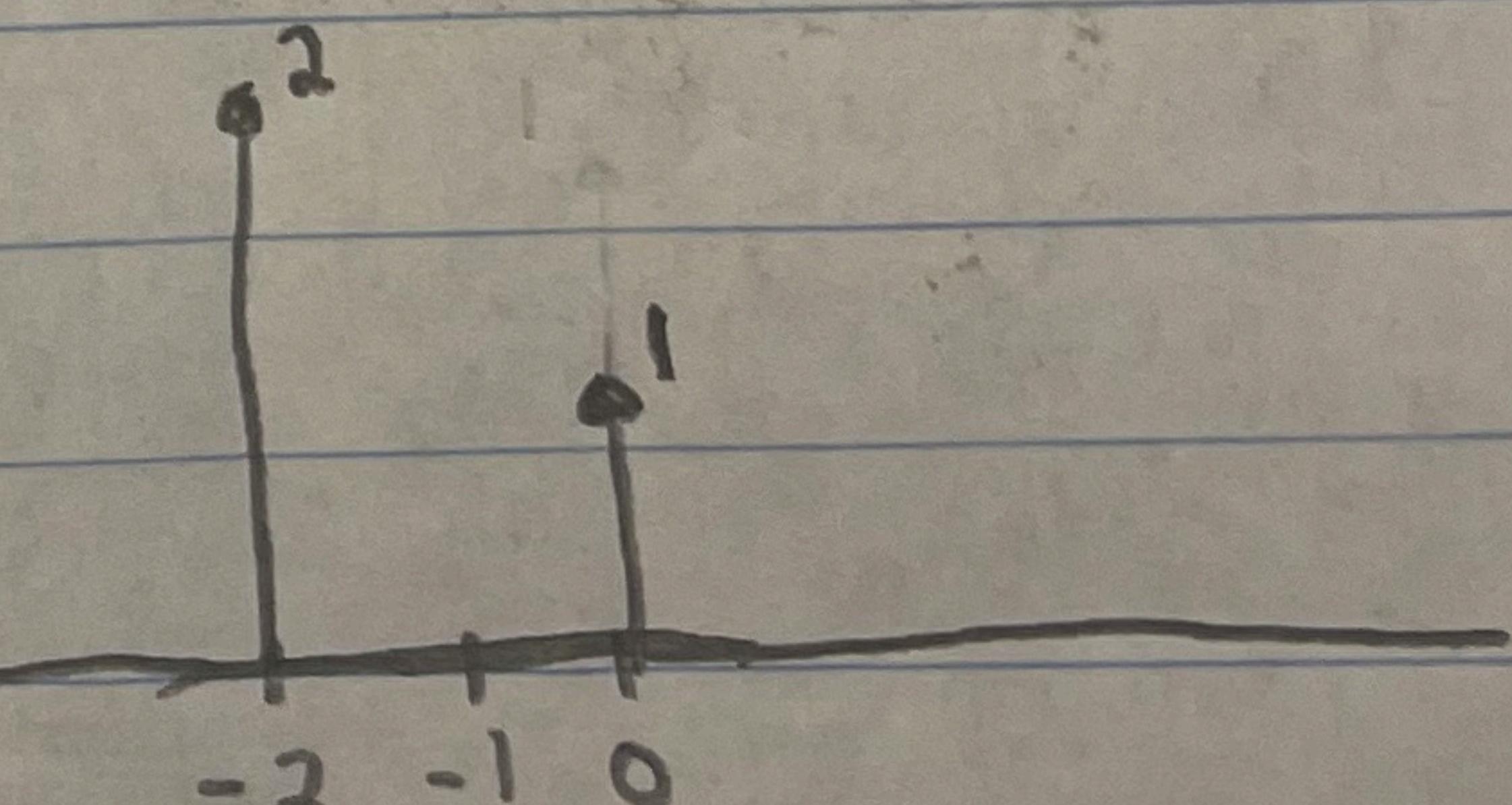
$u[n]$: unit step = $\begin{cases} 1 & \text{when } n \geq 0 \\ 0 & \text{when } n < 0 \end{cases}$



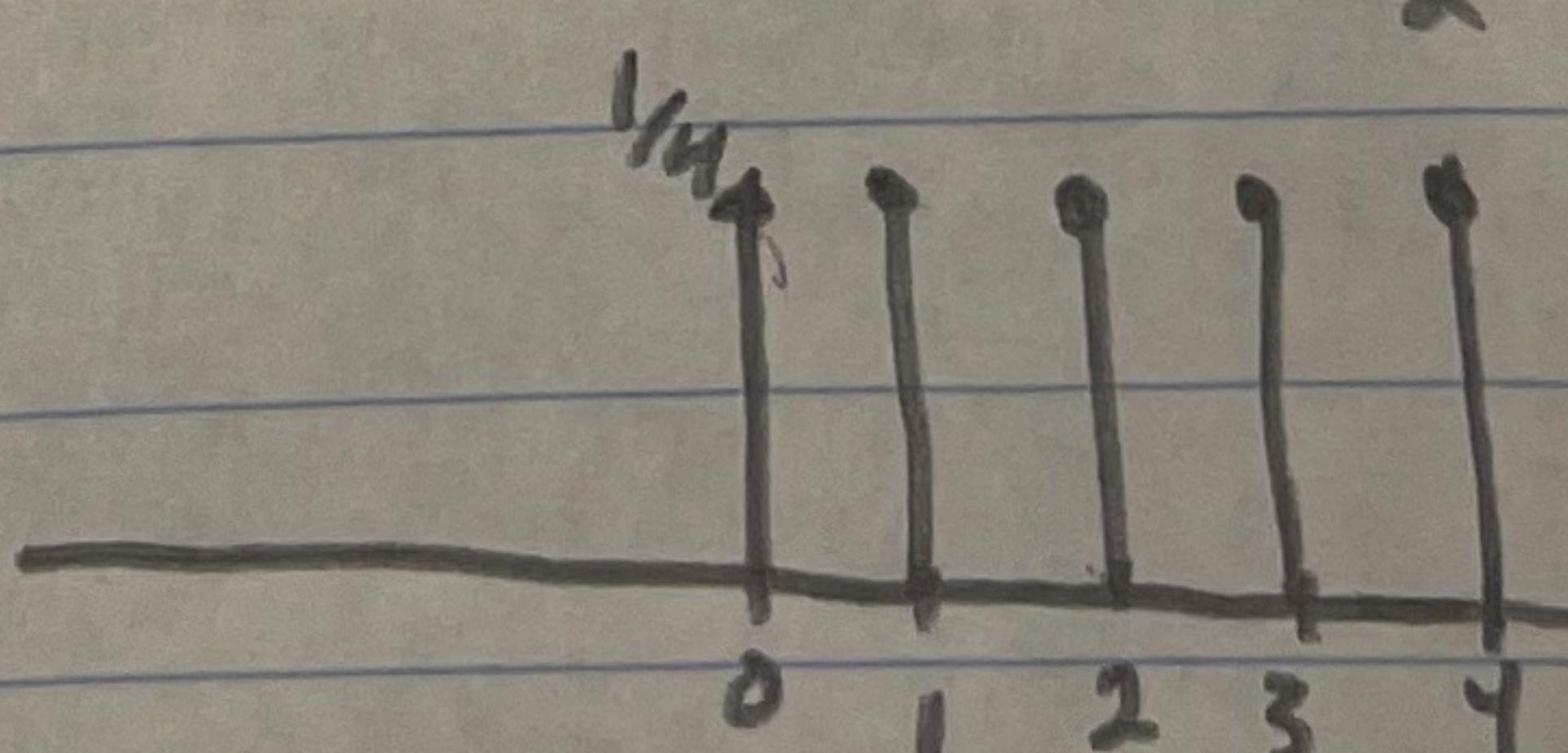
h denotes ~~impulse~~ impulse response

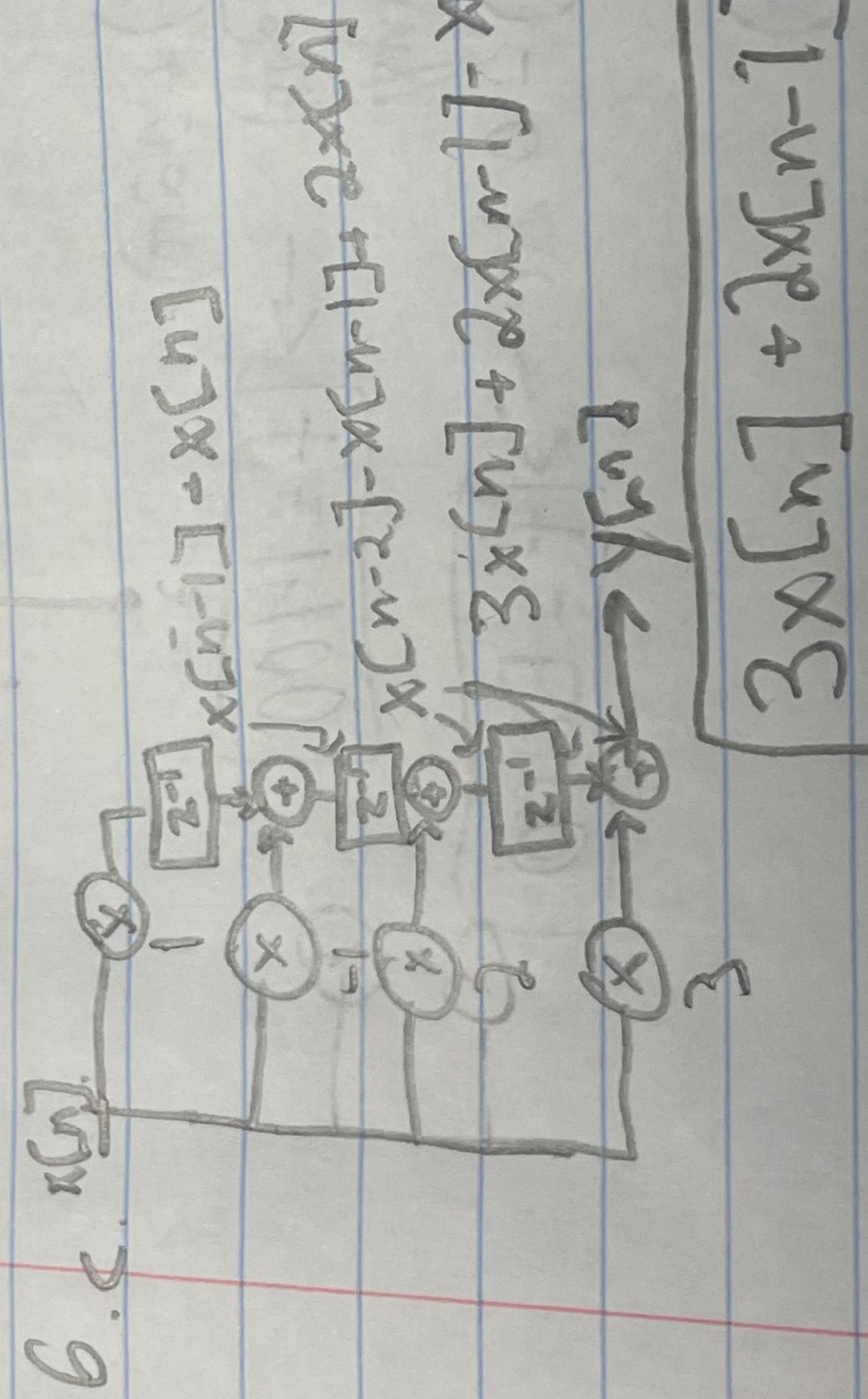
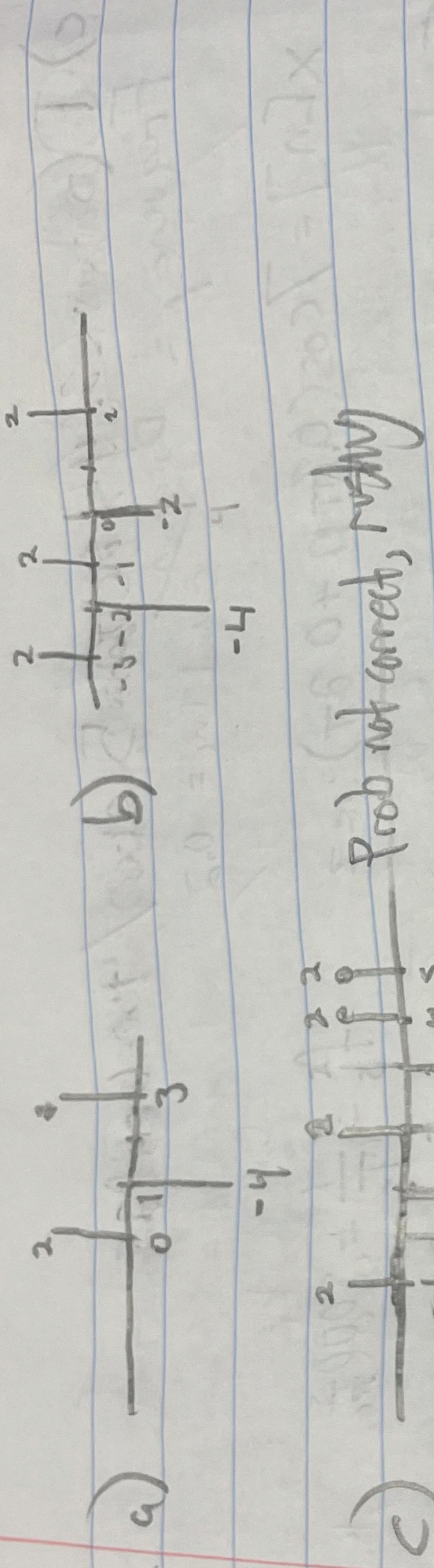
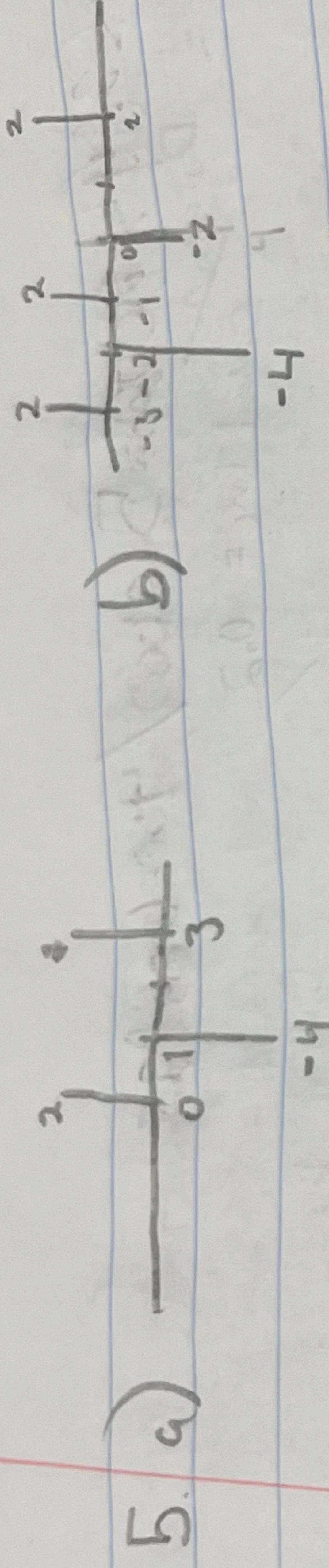
Dr Harleys Examples

2b) $h[n] = 2\delta[n+2] + \delta[n]$



c) $h[n] = \frac{1}{4} \sum_{m=0}^4 \delta[n-m]$





$$\boxed{3x[n] + 2x[n-1] - x[n-2] + x[n-3]}$$