

# INDUCTION

## BASE CASE

- SET  $n$  to lowest possible value

$$\sum_{k=0}^n 2^k = 2^{n+1} - 1$$
$$2^0 = 2^{0+1} - 1$$

- SOLVE AND PROVE TRUE

$$1 = 2 - 1$$

$$1 = 1$$

#t

## INDUCTIVE HYPOTHESIS

- RESTATE PROBLEM WITH  $n+1$

$$\sum_{k=0}^{n+1} 2^k = 2^{(n+1)+1} - 1$$

- EXPAND SUM

$$\sum_{k=0}^n 2^k + 2^{(n+1)} = 2^{(n+2)} - 1$$

- REPLACE BASE CASE

$$2^{(n+1)} - 1 + 2^{(n+1)} = 2^{(n+2)} - 1$$

- SOLVE AND PROVE TRUE

$$2^{n+2} - 1 = 2^{n+2} - 1$$

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