

SELECTION SORT

$$S(n) = \begin{cases} d, & n = \{0, 1\} \\ S(n-1) + cn, & n > 1 \end{cases}$$

$$i=1 \quad S(n) = S(n-1) + cn$$

$$i=2 \quad S(n) = (S(n-2) + c(n-1)) + cn$$

$$S(n) = S(n-2) + 2cn - c$$

$$i=3 \quad S(n) = (S(n-3) + c(n-2)) + 2cn - c$$

$$S(n) = S(n-3) + 3cn - (1+2)c$$

$$i=k \quad S(n) = S(n-k) + kcn - c \sum_{i=1}^{k-1} i$$

$$n=k \quad S(n) = S(0) + cn^2 - c \frac{(n-1)n}{2}$$

$$S(n) = d + cn^2 - \frac{cn^2}{2} - \frac{cn}{2}$$

$$S(n) = d + \frac{cn^2}{2} - \frac{cn}{2} \in O(n^2)$$