Midterm Study Guide

Professor Tanksley February 16, 2012

1 Arguments

For each of the following, put the argument in propositional form, then draw a truth table to prove whether it is valid or invalid.

Here's a sample truth table for you to work with:

| A | В | C | |
|---|---|---|--|
| T | T | T | |
| T | F | T | |
| F | T | T | |
| F | F | T | |
| T | T | F | |
| T | F | F | |
| F | T | F | |
| F | F | F | |

- 1.(a) Not both A and B.
 - ∴ Not A or not B.

2. You can go to graduate school only if you graduate from college. Therefore, if you didn't graduate from college, you didn't go to graduate school.

- 3.(a) The clock is not correct.
 - ... It is not the case that it is not the case that the clock is not correct.

- 4.(a) If we didn't eat out and go to the show, then we can go to the show or get ice cream.
 - ... If we didn't go to the show or get ice

cream, then we cannot eat out and go to the show.

- 2 Label the antecedent and consequent
 - 1. If it is cold, I will not be in class.

2. I'll vote for him only if he promises to lower taxes.

3. Only if you are 48 inches tall can you ride the ride.

3 Fill in the truth table

| | _1, | •—— | | |
|---|-----|-----|---|--------------------|
| ㅂ | ㅂ | Т | T | A |
| Ŧ | L | Ŧ | L | В |
| | | | | |
| | | | | A if and only if B |

| | | | -2 | • | | | | |
|---|---|---|----|---|---|--------|---|---------------------------------------|
| F | F | T | T | Ħ | Ħ | \Box | T | \triangleright |
| F | T | F | L | Ŧ | T | Ŧ | L | В |
| Ŧ | F | F | Ŧ | Τ | Τ | Τ | Τ | \bigcirc |
| | | | | | | | | If A and B, then not (C or not B BNB) |

Note that \leftrightarrow is 'if and only if'.

| | | | 3, | · | | | | |
|---|---|---|----------|---|----------|---|---|--|
| ㅂ | H | T | \vdash | H | H | Τ | Τ | \triangleright |
| Ŧ | T | F | Τ | H | T | H | T | В |
| Ħ | H | F | H | 丁 | \vdash | Τ | T | \bigcirc |
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| | | | | | | | | \widehat{A} |
| | | | | | | | | $A \leftrightarrow$ |
| | | | | | | | | , |
| | | | | | | | | \uparrow |
| | | | | | | | | $B) \leftrightarrow (B \leftrightarrow C)$ |
| | | | | | | | | → |
| | | | | | | | | \rightarrow |
| | | | | | | | | |