Genetic Evaluation

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Consequences of Definition of Breeding Value

- ▶ Based on the average of a large number of offspring, because
 - offspring inherit a random sample of parental alleles
 - average over a large number of offspring reduces sampling effect
- ► The breeding value is defined as a deviation from the population mean
 - population mean depends on allele frequencies which are specific for each population
 - hence breeding values can only be compared within one population.
- Because the breeding value is defined as a deviation its expected value of the breeding value is 0

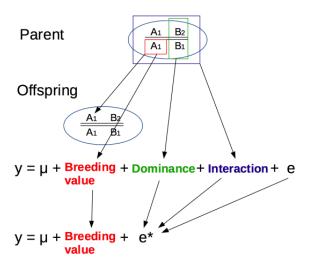
The Basic Model

$$y_{ij} = \mu_i + g_i + e_{ij}$$

where

 y_{ij} j^{th} record of animal i μ_i identifiable fixed environmental effect g_i sum of all additive (a), dominance (d) and epistatic effects of the genotype of animal i e_{ii} random environmental effects of animal i

Re-arranging Terms



New Model

$$y_{ij} = \mu_i + a_i + e_{ij}^*$$

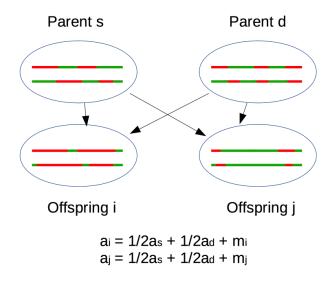
where

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\mu_i identifiable fixed environmental effect
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e^*_{ii} dominance, epistatic and random environmental effects of
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Infinitesimal Model

- Central Limit Theorem for a_i and e_{ij} lead to multivariate normal distributions with
 - E(a) = 0 and E(e) = 0 and
 - Known variances and co-variances
 - ▶ No co-variances between a_i and e_{ij}
- \blacktriangleright μ is assumed to be constant for a given evaluation
- Phenotypic observation y_{ij} is the sum of two normally distributed random variables, therefore
 - \triangleright y_{ij} also follows a multivariate normal distribution
 - \triangleright $E(y) = \mu$

Decomposition of Breeding Value



Basic Principle of Predicting Breeding Values

Breeding values are predicted according to the following two steps.

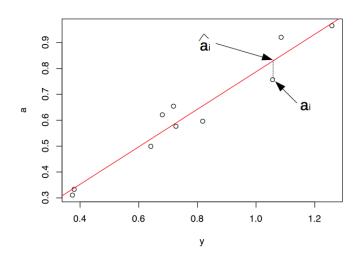
- 1. Observations corrected for the appropriate mean performance values of animals under the same conditions
 - \triangleright conditions are described by the effects captured in μ_i .
- 2. The corrected observations are weighted by a certain factor
 - ▶ factor reflects the amount of information available for prediction

Animal's Own Performance - Single Record

- one phenotypic observation per animal
- \triangleright search for prediction \hat{a}_i of the breeding value a_i of animal i
- \triangleright assume a_i and y_i known for a certain population

 \rightarrow plot

Plot a against y



Regression

- red line denotes regression line from a_i onto y_i
- ▶ because phenotypes have genetic basis \rightarrow connection between a_i and y_i
- measure for connection: regression coefficient b

$$b = \frac{cov(a, y)}{var(y)}$$

$$= \frac{cov(a, \mu + a + e)}{var(y)}$$

$$= \frac{cov(a, a)}{var(y)}$$

$$= \frac{var(a)}{var(y)} = h^2$$

where h^2 is called **heritability**

Prediction

- ▶ Given a new y_i , what would be the predicted a_i ?
- ▶ Use regression line and compute $\hat{a_i}$

$$\hat{a}_i = b * (y_i - \mu)$$
$$= h^2 * (y_i - \mu)$$

Accuracy

Measured as correlation between true breeding value a and selection criterion y

$$r_{a,y} = \frac{cov(a, y)}{\sigma_a \sigma_y}$$
$$= \frac{\sigma_a^2}{\sigma_a \sigma_y}$$
$$= \frac{\sigma_a}{\sigma_y}$$
$$= h$$

Response To Selection

$$R = i * r_{a,y}^2 * \sigma_y = i * h^2 * \sigma_y$$