

(6)

$$SSQR = e^T \cdot e = (y - Xb)^T (y - Xb)$$

with $e = y - Xb$

$$= y^T y - y^T X b - b^T X^T y + \underbrace{b^T X^T X}_{\uparrow} \underbrace{b}_{\uparrow}$$

Least-Squares means, find values of vector b such that $SSQR$ is minimal

This is done by taking the "gradient" of $SSQR$ with respect to the vector b :

$$\nabla SSQR = \begin{bmatrix} \frac{\partial SSQR}{\partial b_0} \\ \frac{\partial SSQR}{\partial b_1} \\ \vdots \\ \frac{\partial SSQR}{\partial b_k} \end{bmatrix}$$

$$\begin{aligned} \frac{\partial SSQR}{\partial b} &= 0 - y^T X - y^T X + 2 b^T X^T X \\ &= -2y^T X + 2b^T X^T X \end{aligned}$$

Find $\hat{b} \rightarrow 0 = -2y^T X + 2\hat{b}^T X^T X$