

$$SSQR = \sum_{i=1}^N [y_i - b_0 - b_1 x_i]^2$$

(7)

$$\begin{aligned} \frac{\partial SSQR}{\partial b_1} &= -2 \sum_{i=1}^N x_i [y_i - b_0 - b_1 x_i] \\ &= -2 \left[\sum_{i=1}^N x_i y_i - b_0 \sum_{i=1}^N x_i - b_1 \sum_{i=1}^N x_i^2 \right] \end{aligned}$$

$$\begin{aligned} x_0 &= \sum_{i=1}^N x_i ; \quad \bar{x}_0 = \frac{x_0}{N} ; \quad y_0 = \sum_{i=1}^N y_i ; \quad \bar{y}_0 = \frac{y_0}{N} \\ (x^2)_0 &= \sum_{i=1}^N x_i^2 ; \quad (xy)_0 = \sum_{i=1}^N x_i y_i \end{aligned}$$

$$\textcircled{1} \quad \frac{\partial SSQR}{\partial b_0} = [y_0 - N b_0 - b_1 x_0] \cdot (-2)$$

$$\textcircled{2} \quad \frac{\partial SSQR}{\partial b_1} = -2 [(xy)_0 - b_0 x_0 - b_1 (x^2)_0]$$

final values
b₀ and
b₁ such
that

from ①: $y_0 - N \hat{b}_0 - \hat{b}_1 x_0 = 0 \Leftrightarrow N \hat{b}_0 + \hat{b}_1 x_0 = y_0$

from ②: $(xy)_0 - \hat{b}_0 x_0 - \hat{b}_1 (x^2)_0 = 0 \Leftrightarrow \hat{b}_0 x_0 + \hat{b}_1 (x^2)_0 = (xy)_0$