

(5)

Least Squares
Before

$$e_i = y_i - E(y_i) \\ = y_i - b_0 - b_1 x_{1i} - b_2 x_{2i}$$

- New vector $e = y - X \cdot b$ from $y = Xb + e$
subtract Xb on both sides

$$SSQR = \sum_{i=1}^N e_i^2 = e_1^2 + e_2^2 + \dots + e_N^2$$

$$\text{New SSQR} = e^T \cdot e$$

For a column vector $e = \begin{bmatrix} e_1 \\ e_2 \\ \vdots \\ e_N \end{bmatrix}$ its transpose e^T

is defined as the row vector $e^T = [e_1 \ e_2 \ e_3 \ \dots \ e_N]$

By definition of dot-product:

$$[e^T \cdot e] = [e_1 \ e_2 \ \dots \ e_N] \cdot \begin{bmatrix} e_1 \\ e_2 \\ \vdots \\ e_N \end{bmatrix} = e_1^2 + e_2^2 + \dots + e_N^2$$

cross product of e , in R: $\text{crossprod}()$