

⑤

□ Variance-Covariance Matrix

▷ Residuals, $\text{var}(e) = \begin{bmatrix} \text{var}(e_1) & \text{cov}(e_1, e_2) & \dots \\ \text{cov}(e_2, e_1) & \text{var}(e_2) & \dots \\ & & \ddots \\ & & & \text{var}(e_n) \end{bmatrix}$

$\text{var}(e_1) = \text{var}(e_2) = \dots = \text{var}(e_n) = \sigma_e^2$ "Residual variance component"

$\text{cov}(e_1, e_2) = \dots = 0$

$\Rightarrow \text{var}(e) = I \times \sigma_e^2 = R$
 \downarrow
 Identity matrix

estimated from data
 extracted σ_e as standard error in output from lm()

▷ Breeding values u :

$\text{var}(u) = \begin{bmatrix} \text{var}(u_1) & \text{cov}(u_1, u_2) & \dots \\ \text{cov}(u_2, u_1) & \text{var}(u_2) & \dots \\ & & \ddots \\ & & & \text{var}(u_p) \end{bmatrix}$

$\text{var}(u) = U = A \times \sigma_u^2$
 \downarrow relationship matrix
 $\underbrace{\sigma_u^2}_{\text{additive genetic variance}}$

• $\text{var}(y) = V = ZUZ^T + R$