## Mixed Linear Effects Models

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## Repeated Measurements

► Same characteristics (Body Weight, BC, ...) measured multiple times for the same animal

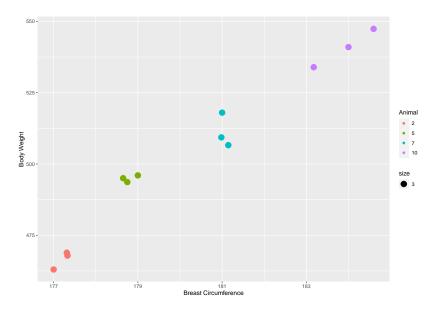
Animal	Breast Circumference	Body Weight
2	177.0000	463.0000
2	177.3129	468.8940
2	177.3292	467.8753
5	179.0000	496.0000
5	178.6501	495.0033
5	178.7485	493.6563
7	181.0000	518.0000
7	180.9819	509.3221

Column Animal no longer just a counter, it becomes a model factor

## **Properties**

- What is the benefit of repeated measurements?
- ▶ Equivalent to more animals in the dataset?
- ► Assumption: repeated observations of the same animal are more "similar"
- ► No longer independence of observations

# Data Scatterplot



## Statistical Analysis

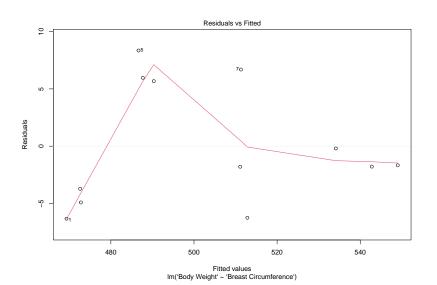
- ► Technically, same regression analysis is possible
- But assumption of independence is violoted
- Consequence of independence

$$var(\mathbf{e}) = \mathbf{I} * \sigma_e^2$$

\* Check residuals plot

# Diagnostics Plot

plot(lm\_rep\_obs)



### **ANOVA**

data = tbl\_rep\_obs\_breed)

aov\_bw\_breed <- aov(`Body Weight` ~ Breed,</pre>

### ANOVA I: Breed and Animal

```
## Df Sum Sq Mean Sq F value Pr(>F)

## Breed 2 7356 3678 160.06 3.53e-07 ***

## Animal 1 1302 1302 56.64 6.76e-05 ***

## Residuals 8 184 23

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.05
```

### **ANOVA II**

```
aov_bw_no_breed_rep <- aov(`Body Weight` ~ Error(Animal),</pre>
                           data = tbl_rep_obs_no_breed)
summary(aov_bw_no_breed_rep)
##
## Error: Animal
##
             Df Sum Sq Mean Sq F value Pr(>F)
## Residuals 3 8658
                          2886
##
## Error: Within
             Df Sum Sq Mean Sq F value Pr(>F)
##
## Residuals 8 183.8 22.98
```

### **ANOVA III**

```
aov bw breed rep <- aov(`Body Weight` ~ Breed +
                           Error(Animal).
                         data = tbl rep obs breed)
summary(aov bw breed rep)
##
## Error: Animal
##
            Df Sum Sq Mean Sq F value Pr(>F)
## Breed 2 7356 3678 2.826 0.388
## Residuals 1 1302 1302
##
## Error: Within
            Df Sum Sq Mean Sq F value Pr(>F)
##
## Residuals 8 183.8 22.98
```

#### Ime4

```
lme_bw_no_breed_rep <- lme4::lmer(`Body Weight` ~ (1|Anima)</pre>
                                 data = tbl_rep_obs_no_bre
summary(lme_bw_no_breed_rep)
## Linear mixed model fit by REML ['lmerMod']
## Formula: 'Body Weight' ~ (1 | Animal)
##
     Data: tbl rep obs no breed
##
## REML criterion at convergence: 82.7
##
## Scaled residuals:
## Min 1Q Median 3Q
                                           Max
## -1.36360 -0.50301 0.06086 0.26850 1.43838
##
## Random effects:
```

## Groups Name Variance Std.Dev. ## Animal (Intercept) 954.34 30.892 ## Residual 22.98 4.794

## With Breed

Animal	Body Weight	Breed
2	463.0000	Angus
2	468.8940	Angus
2	467.8753	Angus
5	496.0000	Simmental
5	495.0033	Simmental
5	493.6563	Simmental
7	518.0000	Limousin
7	509.3221	Limousin
7	506.5958	Limousin
10	541.0000	Limousin
10	547.3609	Limousin
10	533.9288	Limousin

### **ANOVA**

```
aov bw breed rep <- aov(`Body Weight` ~ Breed +
                        Error(Animal).
                         data = tbl rep obs breed)
summary(aov bw breed rep)
##
## Error: Animal
##
            Df Sum Sq Mean Sq F value Pr(>F)
## Breed 2 7356 3678 2.826 0.388
## Residuals 1 1302 1302
##
## Error: Within
            Df Sum Sq Mean Sq F value Pr(>F)
##
## Residuals 8 183.8 22.98
```

#### Ime4

##

```
lme_bw_breed_rep <- lme4::lmer(`Body Weight` ~ Breed +</pre>
                                 (1|Animal),
                                 data = tbl_rep_obs_breed)
summary(lme_bw_breed_rep)
## Linear mixed model fit by REML ['lmerMod']
## Formula: 'Body Weight' ~ Breed + (1 | Animal)
     Data: tbl rep obs breed
##
##
## REML criterion at convergence: 61.8
##
## Scaled residuals:
      Min 1Q Median
                               3Q
                                      Max
##
```

## Random effects:
## Groups Name Variance Std.Dev.
## Animal (Intercept) 426.21 20.645

## -1.3714 -0.5383 0.0640 0.3213 1.4305