

Meaning of $\text{var}(x)$, if x is a scalar random variable

For a vector u of random variables:

$\text{var}(u)$ is a $q \times q$ variance-covariance matrix

$$G = \text{var}(u) = \begin{bmatrix} \text{var}(u_1) & \text{cov}(u_1, u_2) & \text{cov}(u_1, u_3) & \dots & \text{cov}(u_1, u_q) \\ \text{cov}(u_2, u_1) & \text{var}(u_2) & \text{cov}(u_2, u_3) & \dots & \text{cov}(u_2, u_q) \\ \vdots & \vdots & \vdots & \ddots & \vdots \end{bmatrix}$$

What are the single components of matrix G :

$$(G)_{11} = \text{var}(u_1) = 1 \cdot \sigma_u^2 \quad (\text{because animal 1 has unknown parents and is not inbred})$$

$$(G)_{12} = \text{cov}(u_1, u_2) = 0$$

genetic additive variance

Animal 2 has unknown parents, hence animals 1 and 2 are assumed to be unrelated

$$(G)_{13} = \text{cov}(u_1, u_3) = \text{cov}(u_1, \underbrace{\frac{1}{2}(u_1 + u_2) + m_3}_{\text{decomposition } u_3 \text{ into breed}})$$

decomposition
 u_3 into breed