

Result:  $\bar{V}_G = \text{Var}(V) = \underbrace{2pq\alpha^2}_{\text{additive genetic variance}} + \underbrace{(2pqd)}_{\text{dominance variance}}$

$$= \bar{V}_A^2 + \bar{V}_D^2$$

with  $\bar{V}_A = 2pq\alpha^2$

$$\bar{V}_D = (2pqd)^2$$

Two Decompositions:

$$1. V_{ij} = \mu + BV_{ij} + D_{ij}$$

$$2. \bar{V}_G = \text{Var}(V) = \bar{V}_A^2 + \bar{V}_D^2$$

By computation rules with variances:

Taking the variance of  $V_{ij}$  in 1.

$$\begin{aligned} \text{Var}(V_{ij}) &= \text{Var}(\mu + BV_{ij} + D_{ij}) \\ &= \text{Var}(\mu) + \text{Var}(BV_{ij}) + \text{Var}(D_{ij}) \\ &\quad + 2\text{cov}(\mu, BV_{ij}) + 2\text{cov}(\mu, D_{ij}) \\ &\quad + 2\text{cov}(BV_{ij}, D_{ij}) \end{aligned} \left\{ \begin{array}{l} \text{variance of} \\ \text{a sum (a+b)} \\ \text{var(a+b)} \\ \text{var(a) +} \\ \text{var(b) +} \\ 2\text{cov(a,b)} \end{array} \right.$$