

First idea to compute  $A^{-1}$ :

- Compute  $A$
- then invert  $A$  to get to  $A^{-1}$  (in R: ~~inv~~ solve())
- Small data sets  $\Rightarrow$  OK

$\Rightarrow$  Not possible for large data sets

Simple structure of  $A^{-1}$  was discovered by Henderson who developed simple rules of computing  $A^{-1}$  directly, that means without first computing  $A$ .

The rules of computing  $A^{-1}$  are based on properties of  $A$  and  $A^{-1}$ .

- From Linear Algebra it is known that symmetric matrices can be decomposed into a product of three factors:

$$A = L \cdot D \cdot L^T$$

where  $L$  is lower triangular matrix  $\Rightarrow$

$$L = \begin{bmatrix} 1 & & \\ & \ddots & \\ & & 1 \end{bmatrix}$$

and  $D$  is a diagonal