

Matrix L:

$$u = L \cdot m$$

$$(L)_{ij} = \frac{1}{2}(L)_{sj} + \frac{1}{2}(L)_{dj}$$

Decomposition for $\text{var}(u)$:

□ Because $u = L \cdot m$

$$\begin{aligned}\text{var}(u) &= \text{var}(L \cdot m) \\ &= L \cdot \text{var}(m) \cdot L^T\end{aligned}$$

□ The vector m contains random mendelian sampling terms (m_i) for animal i :

Full sibs i and j with parents s and d

$$\left. \begin{aligned}u_i &= \frac{1}{2}u_s + \frac{1}{2}u_d + m_i \\ u_j &= \frac{1}{2}u_s + \frac{1}{2}u_d + m_j\end{aligned} \right\} \begin{array}{l} \text{in general } u_i \neq u_j \\ \text{because } i \text{ and } j \\ \text{did not receive the same} \\ \text{sample of random alleles} \end{array}$$

But m_i and m_j are independent

$$\Rightarrow \text{cov}(m_i, m_j) = 0$$