

$$\begin{aligned}\text{var}(u) &= \text{var}(L \cdot m) \\ &= L \cdot \text{var}(m) \cdot L^T\end{aligned}$$

with $\text{var}(m)$ being a diagonal matrix D with diagonal elements

$$\sigma_u^2 \cdot (D)_{ii} = \text{var}(m_i) = \begin{cases} \left(\frac{1}{2} - \frac{1}{4}(F_3, F_4)\right) \sigma_u^2 & (1) \\ \left(\frac{3}{4} - \frac{1}{4}F_3\right) \sigma_u^2 & (2) \\ \sigma_u^2 & (3) \end{cases}$$

where (1) : both parents known

(2) : only one parent is known

(3) : no parents known

$$\Rightarrow \text{var}(u) = L \cdot D \sigma_u^2 L^T \quad \text{where } \sigma_u^2 D = \text{var}(m)$$

$$= \underbrace{L \cdot D \cdot L^T}_{A} \cdot \sigma_u^2$$

$$= A \cdot \sigma_u^2$$