

□ Var of a vector corresponds to a variance-covariance matrix.

Example: vector $y^* = \begin{bmatrix} y_1^* \\ y_2^* \\ \vdots \\ y_k^* \end{bmatrix}$

$$P = \text{var}(y^*) = \begin{bmatrix} \text{var}(y_1^*) & \text{cov}(y_1^*, y_2^*) & \dots & \text{cov}(y_1^*, y_k^*) \\ \text{cov}(y_2^*, y_1^*) & \text{var}(y_2^*) & \dots & \text{cov}(y_2^*, y_k^*) \\ \vdots & \vdots & \ddots & \vdots \\ \text{cov}(y_k^*, y_1^*) & \text{cov}(y_k^*, y_2^*) & \dots & \text{var}(y_k^*) \end{bmatrix}$$

~ symmetric matrix
 - it has k rows and k columns

$$G = \text{cov}(u, (y^*)^T) = \begin{bmatrix} \text{cov}(u, y_1^*) \\ \text{cov}(u, y_2^*) \\ \vdots \\ \text{cov}(u, y_k^*) \end{bmatrix}$$

$$R = b_u^2 + b^T P b + 2 b^T G$$

□ Minimization: $\underbrace{\frac{\partial R}{\partial b}}_{\text{Gradient}} = 0 = \begin{bmatrix} \frac{\partial R}{\partial b_1} \\ \frac{\partial R}{\partial b_2} \\ \vdots \end{bmatrix}$