

Decomposition of  $\sigma_y^2$  for repeated observations:

$$\text{var}(y_{ij}) = \underbrace{\text{var}(u_i) + \text{var}(p_{e_i})}_{\text{constant across all observations for animal } i} + \text{var}(t_{e_{ij}})$$

□ Repeatability  $t$ : Tells us the ratio of variance components that are permanent compared to the total variance of all observations

$$t = \frac{\text{var}(u_i) + \text{var}(p_{e_i})}{\text{var}(y_{ij})} \Rightarrow \underline{\text{var}(u_i) + \text{var}(p_{e_i}) = t \cdot \sigma_y^2}$$

$$1-t = \frac{\text{var}(y_{ij})}{\text{var}(y_{ij})} - \frac{\text{var}(u_i) + \text{var}(p_{e_i})}{\text{var}(y_{ij})}$$

$$= \frac{\text{var}(y_{ij}) - \text{var}(u_i) - \text{var}(p_{e_i})}{\text{var}(y_{ij})} = \frac{\text{var}(t_{e_{ij}})}{\text{var}(y_{ij})}$$

$$\Downarrow$$
$$\underline{\text{var}(t_{e_{ij}}) = (1-t)\sigma_y^2}$$