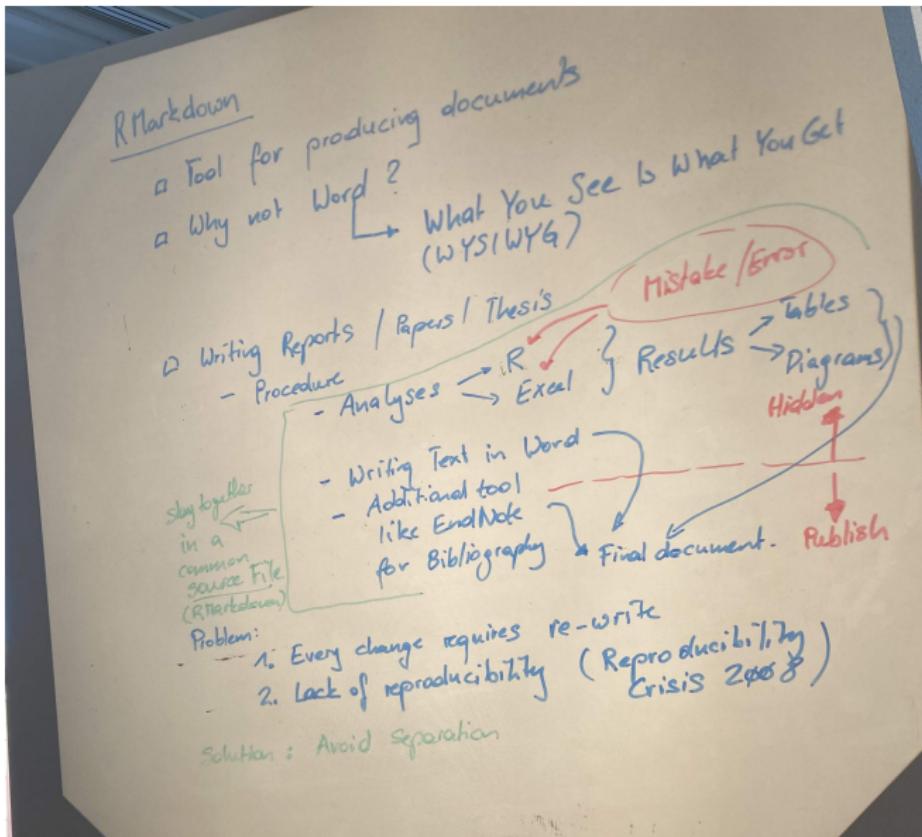


# OHP Page 1



# OHP Page 2

RMarkdown as an example of a unified source file

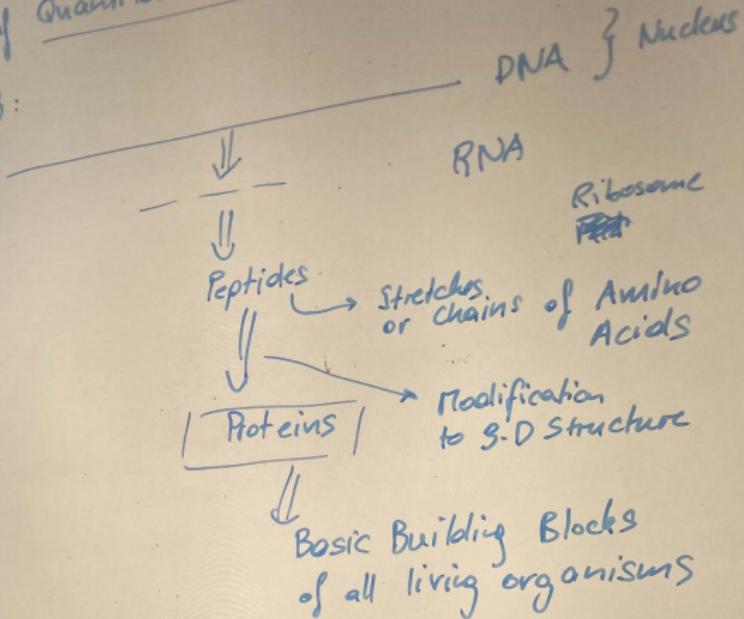
- Not WYSIWYG (other examples: HTML websites)
- Source file with special characters that are defining the structure of the document
- Information of the document is separated from its appearance.

Read Format:

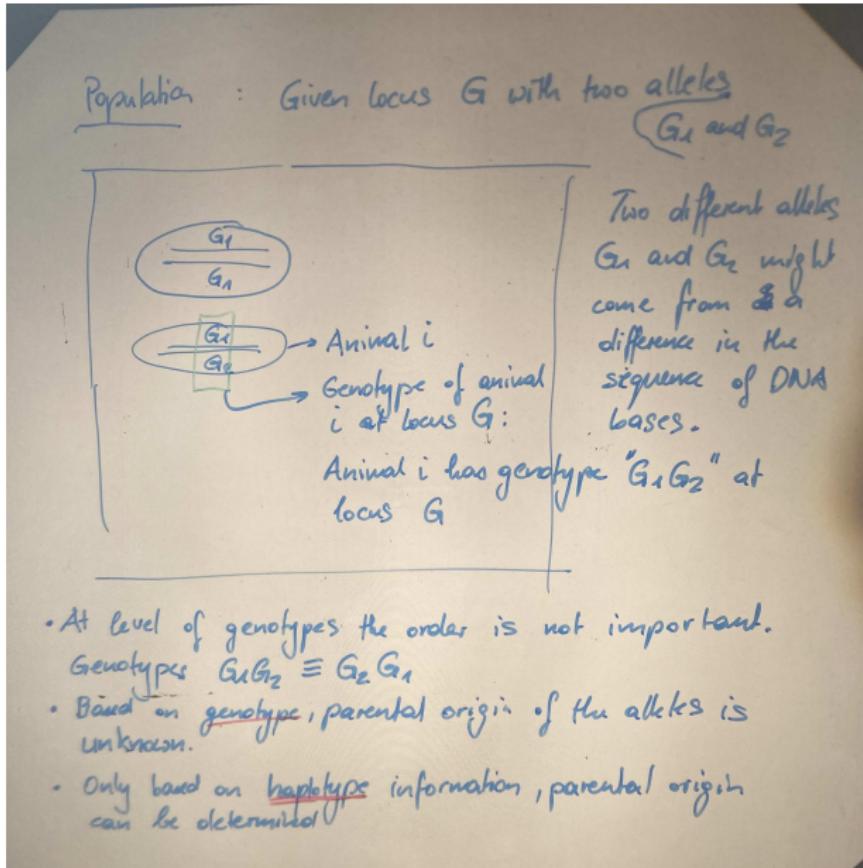
- URLs
- `#text**` → bold
- `# text#` ⇒ italics
- ````{r name}` ⇒ R-code chunk start
- ````` ⇒ R-code chunk end

## Basics of Quantitative Genetics

- CDMB:



# OHP Page 4



## Frequencies of Genotypes

$$\begin{aligned}
 f(G_1G_1) &= \frac{\# G_1G_1}{N} = \frac{4}{10} = 0.4 \\
 f(G_1G_2) &= \frac{\# G_1G_2}{N} = \frac{3}{10} = 0.3 \\
 f(G_2G_2) &= \frac{\# G_2G_2}{N} = \frac{3}{10} = 0.3
 \end{aligned}
 \left. \begin{array}{l} \text{Sum:} \\ f(G_1G_1) + f(G_1G_2) \\ + f(G_2G_2) = 1 \end{array} \right\}$$

↓  
 Number of      total number of animals  
 in the population

- Alleles:

$$\begin{aligned}
 f(G_1) &= \frac{\# G_1}{2N} = \frac{11}{20} = 0.55 \\
 f(G_2) &= \frac{\# G_2}{2N} = \frac{9}{20} = 0.45
 \end{aligned}
 \left. \begin{array}{l} f(G_1) + f(G_2) = 1 \end{array} \right\}$$

- Allele frequencies from Genotype frequencies

$$f(G_1) = \frac{\# G_1}{2N} = \frac{2N \cdot f(G_1G_1) + f(G_1G_2) \cdot N}{2N} = \frac{f(G_1G_1) + \frac{1}{2} f(G_1G_2)}{f(G_1G_1) + f(G_1G_2)}$$

$$\# G_1 = 2 \cdot \underbrace{\# G_1G_1}_{\hookrightarrow N \cdot f(G_1G_1)} + 1 \cdot \underbrace{\# G_1G_2}_{f(G_1G_2) \cdot N} f(G_1G_2) \cdot N$$

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## Hardy-Weinberg Equilibrium

- Given allele frequencies  $f(G_1) = p$
  - $f(G_2) = q$
- $$\left. \begin{array}{l} f(G_1) = p \\ f(G_2) = q \end{array} \right\} p+q=1$$

- Resulting genotype frequencies under random mating and no selection (idealized population). Genotypes are the result of randomly combining gametes (eggs and sperm)

		egg	
		$G_1$	$G_2$
Sperm	$G_1$	$f(G_1G_1) = p \cdot p = p^2$	$f(G_1G_2) = p \cdot q$
	$G_2$	$f(G_2G_1) = q \cdot p = q^2$	$f(G_2G_2) = q \cdot q = q^2$

Genotype frequencies:

$$\begin{aligned}f(G_1G_1) &= p^2 \\f(G_1G_2) &= 2pq \\f(G_2G_2) &= q^2\end{aligned}$$

$$f(G_1G_1) + f(G_1G_2) + f(G_2G_2) = 1$$
$$\frac{p^2}{2} + \frac{2pq}{2} + \frac{q^2}{2} = \frac{(p+q)^2}{2} = 1$$

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- Genotype frequencies and allele frequencies remain constant over time

Population :  $f(G_1G_1) = p^2, f(G_1G_2) = 2pq, f(G_2G_2) = q^2$

↓

Random Matings

parents

$f(G_1) = p$	$f(G_2) = q$
$f(G_1G_1) = p^2$	$f(G_2G_2) = q^2$
$f(G_1G_2) = 2pq$	$f(G_2G_1) = pq$

1<sup>st</sup> generation

$f(G_1) = \frac{f(G_1G_1) + \frac{1}{2}f(G_1G_2)}{=}$

$$= p^2 + \frac{1}{2} \cdot 2 \cdot p \cdot q = p^2 + p \cdot q$$
$$= p(p+q) = p$$
$$= 1$$

$f(G_2) = \frac{f(G_2G_2) + \frac{1}{2}f(G_2G_1)}{=}$

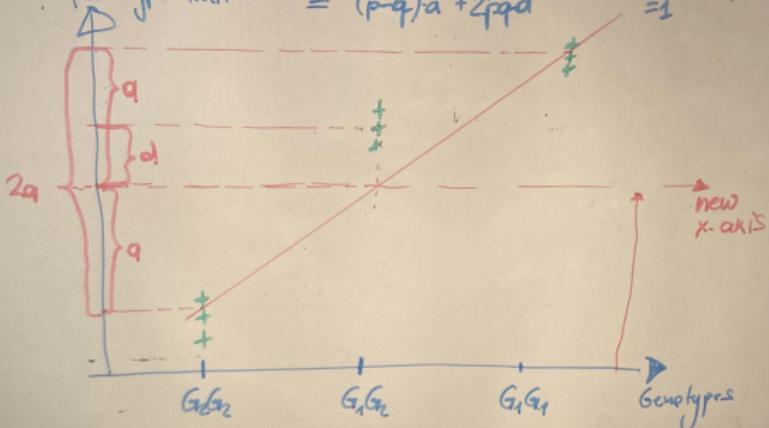
$$= q^2 + p \cdot q = q(q+p) = q$$

## Genotypic Values

- Expected value for the random variable  $V$  is the population mean:

$$\begin{aligned}
 \mu &= V_{11} \cdot f(G_1 G_1) + V_{12} \cdot f(G_1 G_2) + V_{22} \cdot f(G_2 G_2) \\
 &= a \cdot p^2 + d \cdot 2pq + 0(-a) \cdot q^2 \\
 &= a(p^2) + 2pqd = a(p-q)(pq) + 2pqd \\
 &= (p-q)a + 2pqd = 1
 \end{aligned}$$

Measurements from  
phenotypic trait



Genotypic Value for  $G_1 G_1$  is called  $V_{11} = a$

$G_1 G_2$  is called  $V_{12} = d$

$G_2 G_1$  is called  $V_{22} = -a$