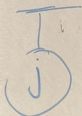
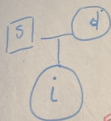
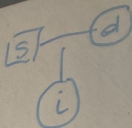


General:

$$G = \text{var}(u) = A \cdot \sigma_u^2$$

↓
 A Numerator Relationship Matrix
 (Additiv genetische Verwandtschaftsmatrix)



Element in row i and column j of matrix A

$$\text{cov}(u_i, u_j) = (A)_{ij} \cdot \sigma_u^2 = \left[\frac{1}{2}(A_{ij}) + \frac{1}{2}(A_{ji}) \right] \cdot \sigma_u^2$$

$$\text{cov}(u_1, u_3) = \text{cov}\left(u_1, \frac{1}{2}u_1 + \frac{1}{2}u_2 + u_3\right)$$

$$= \text{cov}\left(u_1, \frac{1}{2}u_1\right) + \text{cov}\left(u_1, \frac{1}{2}u_2\right) + \text{cov}(u_1, u_3)$$

$$= \frac{1}{2} \text{cov}(u_1, u_1) + \frac{1}{2} \underbrace{\text{cov}(u_1, u_2)}_0 + \text{cov}(u_1, u_3)$$

$$= \frac{1}{2} \text{var}(u_1) + \frac{1}{2} \cdot 0 + 0$$

$$= \frac{1}{2} (1 + F_1) \cdot \sigma_u^2 ; F_1 \text{ corresponds to } \frac{1}{2}$$