

Regression Coefficient  $b_r$

$$b_r = \frac{\text{Cov}(u, \tilde{y})}{\text{var}(\tilde{y})}$$

□ For  $\text{var}(\tilde{y})$ , we have an additional variance component:

$\text{var}(y)$  using for  $y = \mu + u + e \rightarrow \begin{matrix} \text{temp env}(te) \\ \text{permanent} \\ \text{environment}(pe) \end{matrix}$

$$\begin{aligned} \text{var}(y) &= \text{var}(\mu + u + e) \\ &= \text{var}(\mu + u + pe + te) \\ &= \underbrace{\text{var}(\mu)}_{=0} + \text{var}(u) + \text{var}(pe) + \text{var}(te) \\ &= \text{var}(u) + \text{var}(pe) + \text{var}(te) \end{aligned}$$

□ Define Repeatability  $t$

$$t = \frac{\text{var}(u) + \text{var}(pe)}{\text{var}(y)} = \frac{\sigma_u^2 + \sigma_{pe}^2}{\sigma_y^2}$$