

Ex 9: Pr 1:

$$\Delta F = \frac{1}{(2N)} = 1/(2N)$$

$$\text{var}(m) = D \cdot \sigma_u^2 = ?$$

diagonal

$$u_i = 1/2 u_s + 1/2 u_d + m_i$$

$$\begin{aligned} \text{var}(u_i) &= \text{var}\left(\frac{1}{2} u_s + \frac{1}{2} u_d + m_i\right) \\ (1+F_i) \sigma_u^2 &= \frac{1}{4} \text{var}(u_s) + \frac{1}{4} \text{var}(u_d) + \text{var}(m_i) \\ &\quad + 2 \cdot \text{cov}\left(\frac{1}{2} u_s, \frac{1}{2} u_d\right) \\ &= \frac{1}{4} \text{var}(u_s) + \frac{1}{4} \text{var}(u_d) + \text{var}(m_i) \\ &\quad + \frac{1}{2} \text{cov}(u_s, u_d) \end{aligned}$$

$$\begin{aligned} (1+F_i) \sigma_u^2 &= \frac{1}{4} (1+F_s) \sigma_u^2 + \frac{1}{4} (1+F_d) \sigma_u^2 + \text{var}(m_i) \\ &\quad + \frac{1}{2} A_{sd} \sigma_u^2 \\ &= \frac{1}{4} \sigma_u^2 (1+F_s) + \frac{1}{4} \sigma_u^2 (1+F_d) + \underbrace{\text{var}(m_i)}_{(D)_{ii} \sigma_u^2} \\ &\quad + \frac{1}{2} \cdot 2 F_L \sigma_u^2 \end{aligned}$$

$$\text{var}(m_i) = (1+F_i) \sigma_u^2 - F_L \sigma_u^2 - \frac{1}{4} \sigma_u^2 (1+F_s)$$