

Decomposition of $\text{var}(u_i)$

$$\begin{aligned}\text{var}(u_i) &= \text{var}\left(\frac{1}{2}u_s + \frac{1}{2}u_d + m_i\right) \\&= \text{var}\left(\frac{1}{2}u_s\right) + \text{var}\left(\frac{1}{2}u_d\right) + \text{var}(m_i) \\&\quad + 2\text{cov}\left(\frac{1}{2}u_s, \frac{1}{2}u_d\right) \\&\quad + 2\text{cov}\left(\frac{1}{2}u_s, m_i\right) \\&\quad + 2\text{cov}\left(\frac{1}{2}u_d, m_i\right) \quad \left. \vphantom{\begin{aligned} &+ 2\text{cov}\left(\frac{1}{2}u_s, m_i\right) \\ &+ 2\text{cov}\left(\frac{1}{2}u_d, m_i\right) \end{aligned}} \right\} = 0 \\&= \frac{1}{4}\text{var}(u_s) + \frac{1}{4}\text{var}(u_d) + \text{var}(m_i) \\&\quad + \frac{1}{2}\text{cov}(u_s, u_d)\end{aligned}$$