

$$b = \frac{\text{Cov}(u_i, \bar{y}_i)}{\text{Var}(\bar{y}_i)} = \frac{\frac{1}{2} \cdot \text{Var}(u_i)}{\left[t + (1-t)/n \right] \cdot \text{Var}(y)}$$

$$= \frac{\frac{1}{2} h^2 \cdot \text{Var}(y)}{\left[\frac{h^2}{4} + (1 - \frac{h^2}{4})/n \right] \cdot \text{Var}(y)}$$

$$= \frac{\frac{1}{2} h^2}{\frac{h^2}{4} + (1 - \frac{h^2}{4})/n}$$

$$= \frac{\frac{1}{2} n h^2}{\frac{nh^2}{4} + (1 - \frac{h^2}{4})} = \frac{2nh^2}{nh^2 + (4 - h^2)}$$

$$= \frac{2n}{n + (4 - h^2)/h^2} = \underline{\underline{\frac{2n}{n+k}}}$$

$$k = \frac{4 - h^2}{h^2}$$

$$\hat{u}_i = \frac{2n}{n+k} (\bar{y}_i - \mu)$$