## Livestock Breeding and Genomics - Solution 6

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## Problem 1: Parent Offspring Breeding Values

As shown in the course notes, the breeding value  $u_i$  of animal i can be decomposed into the average of the parent breeding values plus a mendelian sampling term  $(m_i)$ . This means

$$u_i = \frac{1}{2}u_s + \frac{1}{2}u_d + m_i$$

where animal i has parents s and d. The mendelian sampling term  $m_i$  is the deviation of the single breeding value  $u_i$  from the parent average breeding value. Because  $m_i$  is modelled as a deviation, it follows that for a large number (N) of offspring from parents s and d, the average over all mendelian sampling terms must be 0.

## Your Task

Show that the average mendelian sampling term over a large number of offspring is 0 using a single locus model for the following cases.

Case 1: Homozygous and Heterozygous Parents Parent s with genotype  $G_1G_1$  and parent d with genotype  $G_1G_2$ 

Case 2: Homozygous and Heterozygous Parents Parent s with genotype  $G_2G_2$  and parent d with genotype  $G_1G_2$ 

Case 3: Heterozygous Parents Both parents s and d have genotype  $G_1G_2$ 

## Solution