

(3)

□ BLUP of  $u$

$\text{var}(u - \hat{u})$  is called Prediction Error Variance (PEV)

□  $u$  is random  $\Rightarrow \text{var}(u) = G$

□ Compute  $\text{var}(u - \hat{u}) = \text{var}(u) + \text{var}(\hat{u}) - 2\text{cov}(u, \hat{u})$

□ Based on properties of BLUP

$\text{var}(\hat{u}) = \text{cov}(u, \hat{u})$  insert in PEV

where  $\hat{u} = G \cdot Z \cdot V^{-1} (y - X\beta)$

$$\begin{aligned}\Rightarrow \text{PEV} &= \text{var}(u - \hat{u}) = \text{var}(u) + \text{var}(\hat{u}) - 2\text{cov}(u, \hat{u}) \\ &= \text{var}(u) - \text{var}(\hat{u})\end{aligned}$$

□ PEV is related to reliability ( $B\%$  - Bestimmtheitsmass)

$$B = r_{u, \hat{u}}^2 \quad \text{with} \quad B\% = 100 \cdot B$$