

# Livestock Breeding and Genomics - Exercise 6

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## Problem 1: Parent Offspring Breeding Values

As shown in the course notes, the breeding value  $u_i$  of animal  $i$  can be decomposed into the average of the parent breeding values plus a mendelian sampling term ( $m_i$ ). This means

$$u_i = \frac{1}{2}u_s + \frac{1}{2}u_d + m_i$$

where animal  $i$  has parents  $s$  and  $d$ . The mendelian sampling term  $m_i$  is the deviation of the single breeding value  $u_i$  from the parent average breeding value. Because  $m_i$  is modelled as a deviation, it follows that for a large number ( $N$ ) of offspring from parents  $s$  and  $d$ , the average over all mendelian sampling terms must be 0.

### Your Task

Show that the average mendelian sampling term over a large number of offspring is 0 using a single locus model for the following cases.

**Case 1: Homozygous and Heterozygous Parents** Parent  $s$  with genotype  $G_1G_1$  and parent  $d$  with genotype  $G_1G_2$

**Case 2: Homozygous and Heterozygous Parents** Parent  $s$  with genotype  $G_2G_2$  and parent  $d$  with genotype  $G_1G_2$

**Case 3: Heterozygous Parents** Both parents  $s$  and  $d$  have genotype  $G_1G_2$