Programming with Big Data in R

Drew Schmidt and George Ostrouchov

useR! 2014





The **pbd**R Core Team

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Support

This work used resources of National Institute for Computational Sciences at the University of Tennessee, Knoxville, which is supported by the Office of Cyberinfrastructure of the U.S. National Science Foundation under Award No.

ARRA-NSF-OCI-0906324 for NICS-RDAV center. This work also used resources of the Oak Ridge Leadership Computing Facility at the Oak Ridge National Laboratory, which is supported by the Office of Science of the U.S. Department of Energy under Contract No. DE-AC05-00OR22725.

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About This Presentation

Downloads

This presentation is available at: http://r-pbd.org/tutorial



About This Presentation

Installation Instructions

Installation instructions for setting up a $\mbox{\bf pbd}\mbox{\bf R}$ environment are available:

This includes instructions for installing R, MPI, and pbdR.



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- Introduction
- Profiling and Benchmarking
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- MPI Profiling
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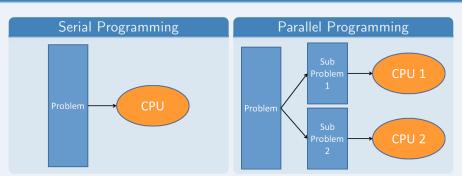
- Introduction
 - A Concise Introduction to Parallelism
 - A Quick Overview of Parallel Hardware
 - A Quick Overview of Parallel Software
 - Summary



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Parallelism





Difficulty in Parallelism

- Implicit parallelism: Parallel details hidden from user
- Explicit parallelism: Some assembly required...
- Embarrassingly Parallel: Also called loosely coupled. Obvious how to make parallel; lots of independence in computations.
- Tightly Coupled: Opposite of embarrassingly parallel; lots of dependence in computations.



Speedup

- Wallclock Time: Time of the clock on the wall from start to finish
- Speedup: unitless measure of improvement; more is better.

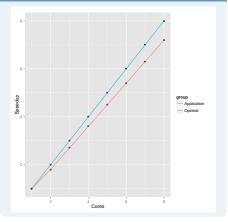
$$S_{n_1,n_2} = \frac{\text{Run time for } n_1 \text{ cores}}{\text{Run time for } n_2 \text{ cores}}$$

- n_1 is often taken to be 1
- In this case, comparing parallel algorithm to serial algorithm

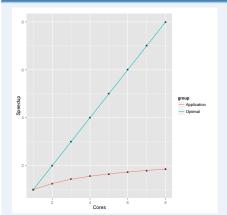




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Bad Speedup





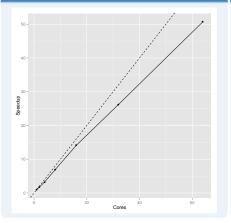
Scalability and Benchmarking

- Strong: Fixed total problem size.
 Less work per core as more cores are added.
- Weak: Fixed local (per core) problem size. Same work per core as more cores are added.

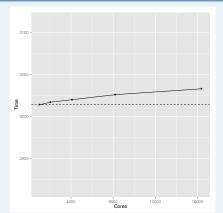


Good Strong Scaling

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Good Weak Scaling





Shared and Distributed Memory Machines

Shared Memory

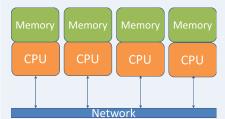
http://r-pbd.org/tutorial

Direct access to read/change memory (one node)



Distributed

No direct access to read/change memory (many nodes); requires communication



Programming with Big Data in R



Shared and Distributed Memory Machines

Shared Memory Machines

Thousands of cores



Nautilus, University of Tennessee 1024 cores 4 TR RAM

Distributed Memory Machines

Hundreds of thousands of cores



Kraken, University of Tennessee 112.896 cores 147 TR RAM



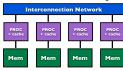
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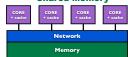


Three Basic Flavors of Hardware

Distributed Memory



Shared Memory



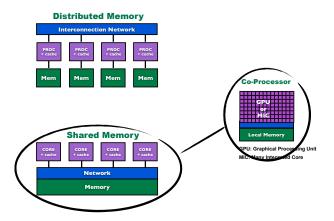
Co-Processor



GPU: Graphical Processing Unit MIC: Many Integrated Core

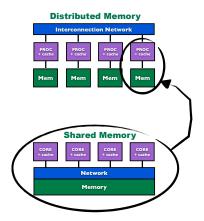


Your Laptop or Desktop





A Server or Cluster



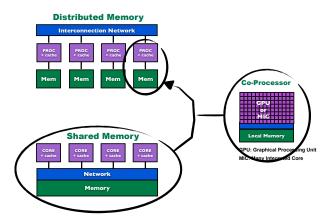
Co-Processor



GPU: Graphical Processing Unit MIC: Many Integrated Core

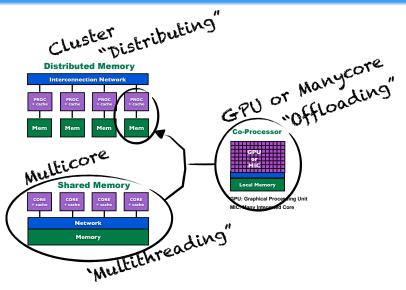


Server to Supercomputer





Knowing the Right Words

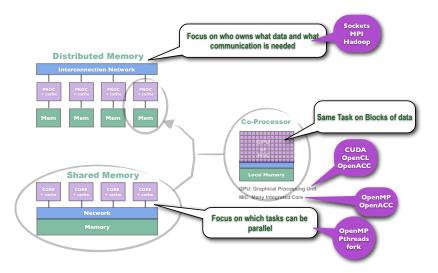




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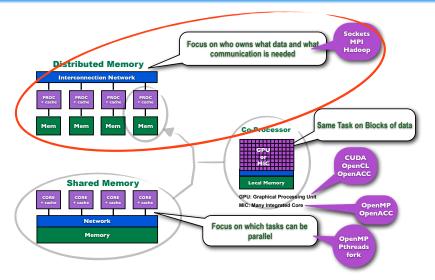


"Native" Programming Models and Tools





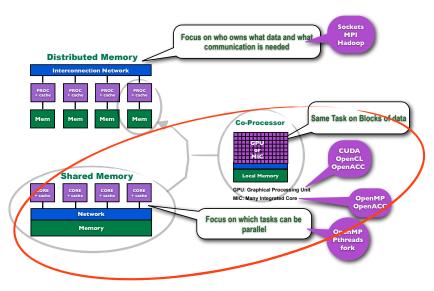
30+ Years of Parallel Computing Research





Programming with Big Data in R

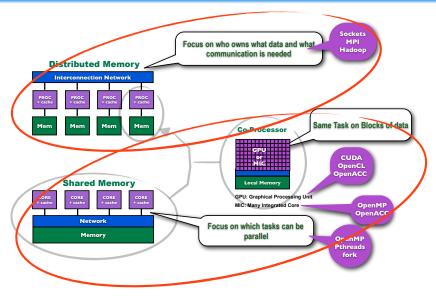
Last 10 years of Advances





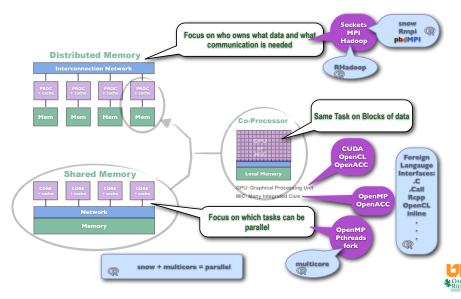
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Putting It All Together Challenge





R Interfaces to Native Tools



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Summary

- Three flavors of hardware
 - Distributed is stable
 - Multicore and co-processor are evolving
 - Two memory models
 - Distributed works in multicore
- Parallelism hierarchy
- Medium to big machines have all three



Contents

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 - Why Profile?
 - Profiling R Code
 - Advanced R Profiling
 - Summary



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Performance and Accuracy



Sometimes $\pi = 3.14$ is (a) infinitely faster than the "correct" answer and (b) the difference between the "correct" and the "wrong" answer is meaningless. . . . The thing is, some specious value of "correctness" is often irrelevant because it doesn't matter. While performance almost always matters. And I absolutely detest the fact that people so often dismiss performance concerns so readily.

- Linus Torvalds, August 8, 2008



Why Profile?

- Because performance matters.
- Bad practices scale up!
- Your bottlenecks may surprise you.
- Because R is dumb.
- R users claim to be data people...so act like it!



Compilers often correct bad behavior...

A Really Dumb Loop

```
int main() {
    int x, i;
    for (i=0; i<10; i++)
        x = 1;
    return 0;
}</pre>
```

clang -O3 example.c

clang example.c

```
main:
        .cfi_startproc
# BB#0:
                 $0, -4(\% rsp)
        movl
        movl
                 $0, -12(\% rsp)
.LBB0_1:
        cmpl
                 $10, -12(%rsp)
                 .LBB0_4
        jge
# BB#2:
                 $1, -8(%rsp)
        movl
# BB#3:
                 -12(%rsp), %eax
        movl
                 $1, %eax
        addl
                 %eax, -12(%rsp)
        movl
                 .LBBO 1
        jmp
.LBB0_4:
                 $0. %eax
        movl
        ret.
```

R will not!

Dumb Loop

```
for (i in 1:n){
    tA <- t(A)
    Y <- tA %*% Q
    Q <- qr.Q(qr(Y))
    Y <- A %*% Q
    Q <- qr.Q(qr(Y))
}</pre>
```

Better Loop

```
tA <- t(A)

for (i in 1:n){
    Y <- tA %*% Q
    Q <- qr.Q(qr(Y))
    Y <- A %*% Q
    Q <- qr.Q(qr(Y))
}
```



Example from a Real R Package

Exerpt from Original function

```
while(i <= N) {
  for(j in 1:i) {
    d.k <- as.matrix(x)[l==j,l==j]
    ...</pre>
```

Exerpt from Modified function

By changing just 1 line of code, performance of the main method improved by **over 350%!**



Some Thoughts

- R is slow.
- Bad programmers are slower.
- R isn't very clever (compared to a compiler).
- The Bytecode compiler helps, but not nearly as much as a compiler.



- Profiling and Benchmarking
 - Why Profile?
 - Profiling R Code
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Timings

Getting simple timings as a basic measure of performance is easy, and valuable.

- system.time() timing blocks of code.
- Rprof() timing execution of R functions.
- Rprofmem() reporting memory allocation in R .
- tracemem() detect when a copy of an R object is created.
- The **rbenchmark** package Benchmark comparisons.



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http://r-pbd.org/tutorial



Other Profiling Tools

- perf (Linux)
- PAPI
- MPI profiling: fpmpi, mpiP, TAU



Profiling MPI Codes with pbdPROF

1. Rebuild pbdR packages

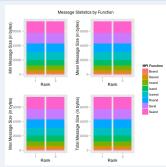
```
R CMD INSTALL pbdMPI_0.2-1.tar.gz \
--configure-args= \
"--enable-pbdPROF"
```

2. Run code

```
mpirun -np 64 Rscript my_script.R
```

3. Analyze results

```
library(pbdPROF)
prof <- read.prof( "output.mpiP")
plot(prof, plot.type="messages2")</pre>
```







Profiling with pbdPAPI

- Performance Application Programming Interface
- High and low level interfaces
- Linux only :(



Function	Description of Measurement
system.flips()	Time, floating point instructions, and Mflips
<pre>system.flops()</pre>	Time, floating point operations, and Mflops
<pre>system.cache()</pre>	Cache misses, hits, accesses, and reads
<pre>system.epc()</pre>	Events per cycle
<pre>system.idle()</pre>	Idle cycles
<pre>system.cpuormem()</pre>	CPU or RAM bound*
<pre>system.utilization()</pre>	CPU utilization*



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Summary

http://r-pbd.org/tutorial

- Profile, profile, profile.
- Use system.time() to get a general sense of a method.
- Use rbenchmark's benchmark() to compare 2 methods.
- Use Rprof() for more detailed profiling.
- Other tools exist for more hardcore applications (pbdPAPI and pbdPROF).



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- The pbdR Project
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Programming with Big Data in R (pbdR)

Striving for Productivity, Portability, Performance

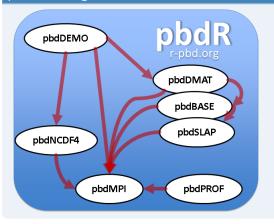


- Free^a R packages.
- Bridging high-performance compiled code with high-productivity of R
- Scalable, big data analytics.
- Offers implicit and explicit parallelism.
- Methods have syntax identical to R.



^aMPL, BSD, and GPL licensed

pbdR Packages



pbdR					
R	ScaLAPACK		NetCDF4	3	
LAPACK		PBLAS	HDF5	ηρiP	
BLAS		BLACS			
			MPI		



pbdR Motivation

Why HPC libraries (MPI, ScaLAPACK, PETSc, ...)?

- The HPC community has been at this for decades.
- They're tested. They work. They're fast.
- You're not going to beat Jack Dongarra at dense linear algebra.



Simple Interface for MPI Operations with **pbdMPI**

Rmpi

```
# int
mpi.allreduce(x, type=1)
# double
mpi.allreduce(x, type=2)
```

pbdMPI

```
allreduce(x)
```

Types in R

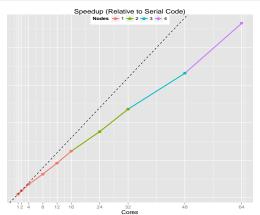
http://r-pbd.org/tutorial

```
> is.integer(1)
[1] FALSE
> is.integer(2)
[1] FALSE
> is.integer(1:2)
[1] TRUE
```



Distributed Matrices and Statistics with **pbdDMAT**

Matrix Exponentiation

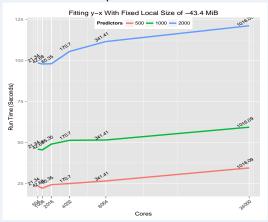


```
1 library(pbdDMAT)
2 
3 dx <- ddmatrix("rnorm", 5000, 5000)
4 expm(dx)</pre>
```



Distributed Matrices and Statistics with pbdDMAT

Least Squares Benchmark



```
x <- ddmatrix("rnorm", nrow=m, ncol=n)
y <- ddmatrix("rnorm", nrow=m, ncol=1)
mdl <- lm.fit(x=x, y=y)</pre>
```



Getting Started with HPC for R Users: pbdDEMO



Programming with Big Data in R

Speaking Serial R with a Parallel Accent

Package Examples and Demonstrations

pbdR Core Team

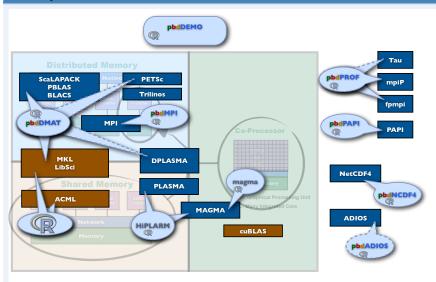
- 140 page, textbook-style vignette.
- Over 30 demos, utilizing all* packages.
- Not just a hello world!
- Demos include:
 - PCA
 - Regression
 - Parallel data input
 - Model-based clustering
 - Simple Monte Carlo simulation
 - Bayesian MCMC



- The pbdR Project
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R and pbdR Interfaces to HPC Libraries





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pbdR Paradigms

pbdR programs are R programs!

Differences:

- Batch execution (non-interactive).
- Parallel code utilizes Single Program/Multiple Data (SPMD) style
- Emphasizes data parallelism.



Batch Execution

• Running a serial R program in batch:

```
1 Rscript my_script.r
```

or

```
1 R CMD BATCH my_script.r
```

• Running a parallel (with MPI) R program in batch:

```
mpirun -np 2 Rscript my_par_script.r
```



Single Program/Multiple Data (SPMD)

- SPMD is a programming paradigm.
- Not to be confused with SIMD.

Paradigms

Programming modelsOOP, Functional, SPMD, ...

SIMD

Hardware instructions MMX, SSE, ...



Single Program/Multiple Data (SPMD)

SPMD is arguably the simplest extension of serial programming.

- Only one program is written, executed in batch on all processors.
- Different processors are autonomous; there is no manager.
- Dominant programming model for large machines for 30 years.



Summary

- **pbd**R connects R to scalable HPC libraries.
- The pbdDEMO package offers numerous examples and explanations for getting started with distributed R programming.
- pbdR programs are R programs.



Contents

- Introduction to pbdMPI
 - Managing a Communicator
 - Reduce, Gather, Broadcast, and Barrier
 - Other pbdMPI Tools
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Message Passing Interface (MPI)

- MPI: Standard for managing communications (data and instructions) between different nodes/computers.
- Implementations: OpenMPI, MPICH2, Cray MPT, ...
- Enables parallelism (via communication) on distributed machines.
- Communicator: manages communications between processors.



MPI Operations (1 of 2)

- Managing a Communicator: Create and destroy communicators.
 init() initialize communicator
 finalize() shut down communicator(s)
- Rank query: determine the processor's position in the communicator.
 comm.rank() "who am I?"
 comm.size() "how many of us are there?"
- Printing: Printing output from various ranks.
 comm.print(x)
 comm.cat(x)

WARNING: only use these functions on *results*, never on yet-to-be-computed things.



Quick Example 1

Rank Query: 1_rank.r

```
library(pbdMPI, quietly = TRUE)
init()

my.rank <- comm.rank()
comm.print(my.rank, all.rank=TRUE)

finalize()</pre>
```

Execute this script via:

```
1 mpirun -np 2 Rscript 1_rank.r 1 COMM.RANK = 0 2 [1] 0 3 COMM.RANK = 1 4 [1] 1
```



Sample Output:

Quick Example 2

Hello World: 2 hello.r

```
library(pbdMPI, quietly=TRUE)
  init()
3
  comm.print("Hello, world")
5
  comm.print("Hello again", all.rank=TRUE, quietly=TRUE)
7
 finalize()
```

Execute this script via:

Sample Output:

```
COMM.RANK = O
mpirun -np 2 Rscript 2_hello.r
                                          [1] "Hello, world"
                                          [1] "Hello again"
                                          [1] "Hello again"
```



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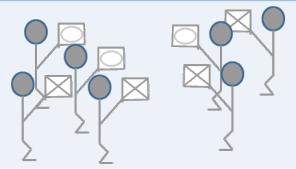
MPI Operations

- Reduce
- Gather
- Broadcast
- Barrier



Programming with Big Data in R

Reductions — Combine results into single result



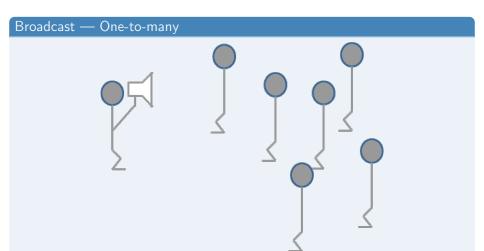


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Gather — Many-to-one



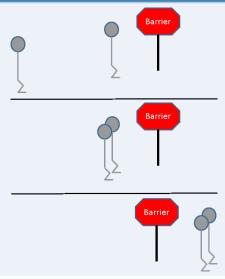
Programming with Big Data in R





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Barrier — Synchronization





MPI Operations (2 of 2)

 Reduction: each processor has a number x; add all of them up, find the largest/smallest,

```
reduce(x, op='sum') — reduce to one
allreduce(x, op='sum') — reduce to all
```

 Gather: each processor has a number; create a new object on some processor containing all of those numbers.

```
gather(x) — gather to one
allgather(x) — gather to all
```

 Broadcast: one processor has a number x that every other processor should also have.
 bcast(x)

 Barrier: "computation wall"; no processor can proceed until all processors can proceed.
 barrier()



Quick Example 3

Reduce and Gather: 3_gt.r

```
library(pbdMPI, quietly=TRUE)
  init()
3
  comm.set.seed(diff=TRUE)
  n <- sample(1:10, size=1)
7
  gt <- gather(n)
  comm.print(unlist(gt))
10
  sm <- allreduce(n, op='sum')</pre>
  comm.print(sm, all.rank=T)
13
  finalize()
```

Execute this script via:

```
mpirun -np 2 Rscript 3_gt.r
```

Sample Output:

```
COMM.RANK = O
[1] 2 8
COMM.RANK = O
[1] 10
COMM.RANK = 1
[1] 10
```



Quick Example 4

Broadcast: 4 bcast r

```
library(pbdMPI, quietly=T)
  init()
3
  if (comm.rank()==0){
    x <- matrix(1:4, nrow=2)</pre>
  } else {
    x <- NULL
8
  y <- bcast(x, rank.source=0)
11
  comm.print(y, rank=1)
13
  finalize()
```

Execute this script via:

Sample Output:

```
mpirun -np 2 Rscript 4_bcast.r
                                           COMM.RANK = 1
                                                 [,1] [,2]
                                           [1,]
                                           [2,]
                                                    2
                                                         4
```



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Random Seeds

pbdMPI offers a simple interface for managing random seeds:

- comm.set.seed(seed=1234, diff=FALSE) All processors use the same seed.
- comm.set.seed(seed=1234, diff=FALSE) All processors use the same seed.



Other Helper Tools

pbdMPI Also contains useful tools for Manager/Worker and task parallelism codes:

- Task Subsetting: Distributing a list of jobs/tasks get.jid(n)
- *ply: Functions in the *ply family.
 pbdApply(X, MARGIN, FUN, ...) analogue of apply()
 pbdLapply(X, FUN, ...) analogue of lapply()
 pbdSapply(X, FUN, ...) analogue of sapply()



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Summary

http://r-pbd.org/tutorial

Start by loading the package:

```
1 library(pbdMPI, quiet = TRUE)
```

• Always initialize before starting and finalize when finished:

```
init()
2
3
4
  finalize()
```

Programming with Big Data in R



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Distributing Data

Problem: How to distribute the data

$$x = \begin{bmatrix} x_{1,1} & x_{1,2} & x_{1,3} \\ x_{2,1} & x_{2,2} & x_{2,3} \\ x_{3,1} & x_{3,2} & x_{3,3} \\ x_{4,1} & x_{4,2} & x_{4,3} \\ x_{5,1} & x_{5,2} & x_{5,3} \\ x_{6,1} & x_{6,2} & x_{6,3} \\ x_{7,1} & x_{7,2} & x_{7,3} \\ x_{8,1} & x_{8,2} & x_{8,3} \\ x_{9,1} & x_{9,2} & x_{9,3} \\ x_{10,1} & x_{10,2} & x_{10,3} \end{bmatrix}_{10 \times 3}$$





Distributing a Matrix Across 4 Processors: Block Distribution

	_		_	
x =	<i>x</i> _{1,1}	<i>x</i> _{1,2}	<i>x</i> _{1,3}	
	<i>x</i> _{2,1}	<i>x</i> _{2,2}	<i>x</i> _{2,3}	
	<i>x</i> _{3,1}	<i>x</i> _{3,2}	<i>x</i> _{3,3}	
	<i>x</i> _{4,1}	<i>X</i> _{4,2}	X _{4,3}	
	<i>X</i> 5,1	<i>X</i> 5,2	<i>X</i> 5,3	
	<i>x</i> _{6,1}	<i>X</i> _{6,2}	<i>x</i> _{6,3}	
	x _{7,1}	<i>X</i> 7,2	<i>X</i> 7,3	
	<i>X</i> 8,1	<i>X</i> 8,2	<i>X</i> 8,3	
	<i>x</i> _{9,1}	<i>X</i> _{9,2}	<i>X</i> 9,3	
	x _{10,1}	<i>x</i> _{10,2}	<i>x</i> _{10,3}] _{10×3}

Data

Processors



Distributing a Matrix Across 4 Processors: Local Load Balance

$x = \begin{bmatrix} x_{1,1} & x_{1,2} & x_{1,3} \\ x_{2,1} & x_{2,2} & x_{2,3} \\ x_{3,1} & x_{3,2} & x_{3,3} \\ \hline x_{4,1} & x_{4,2} & x_{4,3} \\ x_{5,1} & x_{5,2} & x_{5,3} \\ x_{6,1} & x_{6,2} & x_{6,3} \\ \hline x_{7,1} & x_{7,2} & x_{7,3} \\ \hline x_{8,1} & x_{8,2} & x_{8,3} \\ \hline x_{9,1} & x_{9,2} & x_{9,3} \\ x_{10,1} & x_{10,2} & x_{10,3} \end{bmatrix}_{10 \times 3}$

Data

Processors

1 2 3



The GBD Data Structure

Throughout the examples, we will make use of the Generalized Block Distribution, or GBD distributed matrix structure.

- GBD is distributed. No processor owns all the data.
- ② GBD is non-overlapping. Rows uniquely assigned to processors.
- GBD is row-contiguous. If a processor owns one element of a row, it owns the entire row.
- GBD is globally row-major, locally column-major.
- GBD is often locally balanced, where each processor owns (almost) the same amount of data. But this is not required.

_		
<i>x</i> _{1,1}	$x_{1,2}$	<i>x</i> _{1,3}
$x_{2,1}$	$x_{2,2}$	$x_{2,3}$
X3,1	X3,2	X3,3
<i>X</i> 4,1	X4,2	X4,3
<i>X</i> 5,1	<i>X</i> 5,2	X5,3
<i>x</i> _{6,1}	<i>x</i> _{6,2}	<i>x</i> _{6,3}
<i>x</i> _{7,1}	<i>x</i> _{7,2}	<i>X</i> 7,3
<i>X</i> 8,1	<i>X</i> 8,2	X8,3
X9,1	X9,2	X9,3
X _{10,1}	X _{10,2}	<i>X</i> _{10,3}

- The last row of the local storage of a processor is adjacent (by global row) to the first row of the local storage of next processor (by communicator number) that owns data.
- GBD is (relatively) easy to understand, but can lead to bottlenecks if you have many more columns than rows



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Understanding GBD: Global Matrix

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{9 \times 9}$$

Processors = 0 1 2 3 4 5



Understanding GBD: Load Balanced GBD

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ \hline X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}_{9}$$

Processors = 0 1 2 3 4



Understanding GBD: Local View

$$\begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \end{bmatrix}_{2\times 9}$$

$$\begin{bmatrix} x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \end{bmatrix}_{2\times 9}$$

$$\begin{bmatrix} x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \end{bmatrix}_{2\times 9}$$

$$\begin{bmatrix} x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \end{bmatrix}_{1\times 9}$$

$$\begin{bmatrix} x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \end{bmatrix}_{1\times 9}$$

$$\begin{bmatrix} x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{1\times 9}$$

Processors = 0 1 2 3 4 5



Understanding GBD: Non-Balanced GBD

$$X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ \hline x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ \hline x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ \hline x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{\mathbf{9} \times \mathbf{9}}$$

Processors = 0 1 2 3 4 5



Understanding GBD: Local View

```
X19
                 X<sub>13</sub>
                         X<sub>14</sub>
                                  X<sub>15</sub>
                                          X16
                                                   X<sub>17</sub>

    X21
    X22
    X23
    X24

    X31
    X32
    X33
    X34

                                                   X27
                                  X25
                                          X26
                                                           X28
                                                                    X29
                                  X35 X36
                                                   X37
                                                           X38
                                                                    X39
        X42
                 X43
                         X44
                                  X45
                                          X46
                                                   X47
                                                           X48
                                                                    X49
                                  X55
                                         X56
                                                   X57
                                                            X58
                          X64
                                  X65
                                           X66
                                                    X67
                                                            X68
                                                                    X69
                  X73 X74 X75
                                           X76
                                                    X77
                                  X<sub>85</sub>
                                           X86
                                  X95
                                           X96
                                                    X97
                                                            X98
```

Processors = 0



- 5 The Generalized Block Distribution
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Summary

- Need to distribute your data? Try splitting by row.
- May not work well if your data is square (or longer than tall).



Contents

- 6 Basic Statistics Examples
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 - pbdMPI Example: Sample Covariance
 - pbdMPI Example: Linear Regression
 - Summary



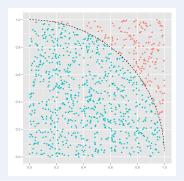
- 6 Basic Statistics Examples
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Example 1: Monte Carlo Simulation

Sample N uniform observations (x_i, y_i) in the unit square $[0, 1] \times [0, 1]$. Then

$$\pi \approx 4 \left(\frac{\# \ \textit{Inside Circle}}{\# \ \textit{Total}} \right) = 4 \left(\frac{\# \ \textit{Blue}}{\# \ \textit{Blue} + \# \ \textit{Red}} \right)$$





Example 1: Monte Carlo Simulation GBD Algorithm

- ① Let n be big-ish; we'll take n = 50,000.
- Generate an $n \times 2$ matrix x of standard uniform observations.
- Count the number of rows satisfying $x^2 + y^2 \le 1$
- Ask everyone else what their answer is; sum it all up.
- Take this new answer, multiply by 4 and divide by n
- If my rank is 0, print the result.



Example 1: Monte Carlo Simulation Code

Serial Code

```
N <- 50000
 X <- matrix(runif(N * 2), ncol=2)</pre>
3 r \le sum(rowSums(X^2) \le 1)
4 PI <- 4*r/N
5 print (PI)
```

Parallel Code

```
library(pbdMPI, quiet = TRUE)
  init()
  comm.set.seed(seed=1234567, diff=TRUE)
  N.gbd <- 50000 / comm.size()
  X.gbd <- matrix(runif(N.gbd * 2), ncol = 2)</pre>
  r.gbd <- sum(rowSums(X.gbd^2) <= 1)</pre>
8 r <- allreduce(r.gbd)</pre>
9 PI <- 4*r/(N.gbd * comm.size())
10 comm.print(PI)
11
12 finalize()
```

Note

For the remainder, we will exclude loading, init, and finalize calls.



- **Basic Statistics Examples**
 - pbdMPI Example: Monte Carlo Simulation
 - pbdMPI Example: Sample Covariance
 - pbdMPI Example: Linear Regression

http://r-pbd.org/tutorial



Basic Statistics Examples

Example 2: Sample Covariance

http://r-pbd.org/tutorial

$$cov(x_{n \times p}) = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \mu_x) (x_i - \mu_x)^T$$

Programming with Big Data in R



Example 2: Sample Covariance GBD Algorithm

- Determine the total number of rows N.
- Compute the vector of column means of the full matrix.
- Subtract each column's mean from that column's entries in each local matrix.
- Compute the crossproduct locally and reduce.
- Divide by N-1.



Example 2: Sample Covariance Code

Serial Code

```
N \leftarrow nrow(X)
mu <- colSums(X) / N
X <- sweep(X, STATS=mu, MARGIN=2)
Cov.X <- crossprod(X) / (N-1)
print(Cov.X)
```

Parallel Code

```
N <- allreduce(nrow(X.gbd), op="sum")</pre>
 mu <- allreduce(colSums(X.gbd) / N, op="sum")</pre>
3
 X.gbd <- sweep(X.gbd, STATS=mu, MARGIN=2)
 Cov.X <- allreduce(crossprod(X.gbd), op="sum") / (N-1)
6
  comm.print(Cov.X)
```



- 6 Basic Statistics Examples
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Example 3: Linear Regression

Find β such that

$$\mathbf{y} = \mathbf{X}\boldsymbol{eta} + \boldsymbol{\epsilon}$$

When X is full rank,

$$\hat{\boldsymbol{\beta}} = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{y}$$



Example 3: Linear Regression GBD Algorithm

- Locally, compute $tx = x^T$
- Locally, compute A = tx * x. Query every other processor for this result and sum up all the results.
- **Solution** Locally, compute B = tx * y. Query every other processor for this result and sum up all the results.
- Locally, compute $A^{-1} * B$



Example 3: Linear Regression Code

Serial Code

```
1 tX <- t(X)
2 A <- tX %*% X
3 B <- tX %*% y
4 ols <- solve(A) %*% B
```

Parallel Code

```
tX.gbd <- t(X.gbd)
A <- allreduce(tX.gbd %*% X.gbd, op = "sum")
B <- allreduce(tX.gbd %*% y.gbd, op = "sum")
ols <- solve(A) %*% B
```



- **Basic Statistics Examples**
 - pbdMPI Example: Monte Carlo Simulation
 - pbdMPI Example: Sample Covariance
 - pbdMPI Example: Linear Regression
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Summary

- SPMD programming is (often) a natural extension of serial programming.
- More **pbdMPI** examples in **pbdDEMO**.



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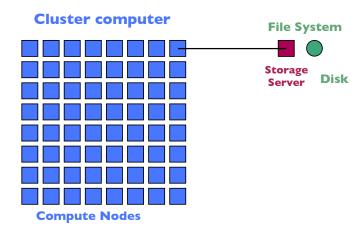
- Data Input
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- Data Input
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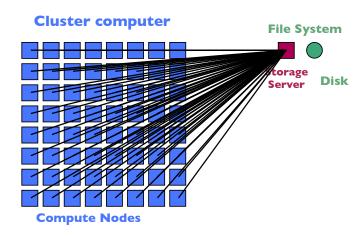
One Node to One Storage Server





Programming with Big Data in R

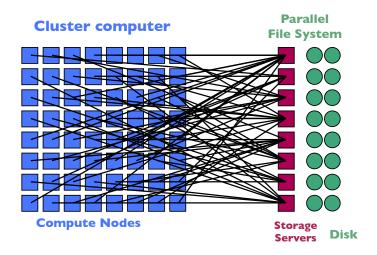
Many Nodes to One Storage Server





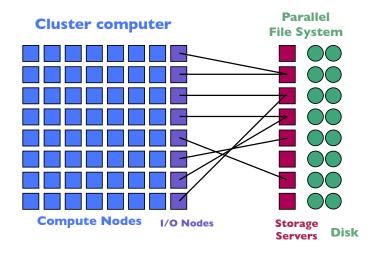
http://r-pbd.org/tutorial

Many Nodes to Few Storage Servers



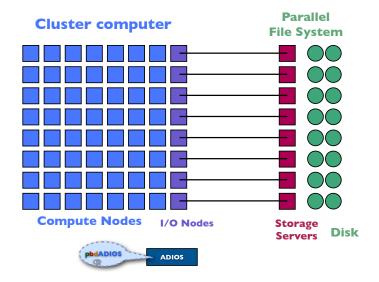


Few Nodes to Few Storage Servers - Default





Few Nodes to Few Storage Servers - Coordinated





- 🕡 Data Input
 - Cluster Computer and File System
 - Serial Data Input
 - Parallel Data Input
 - Summary



Separate manual: http://r-project.org/

- scan()
- read.table()
- read.csv()
- socket



CSV Data: Read Serial then Distribute

Listing:

```
library(pbdDMAT)
  if(comm.rank() == 0) { # only read on process 0
    x <- read.csv("myfile.csv")</pre>
  } else {
    x <- NULL
6
  dx <- as.ddmatrix(x)</pre>
```



- 🕡 Data Input
 - Cluster Computer and File System
 - Serial Data Input
 - Parallel Data Input
 - Summary



New Issues

- How to read in parallel?
- CSV, SQL, NetCDF4, HDF, ADIOS, custom binary
- How to partition data across nodes?
- How to structure for scalable libraries?
- Read directly into form needed or restructure?
- A lot of work needed here!



CSV Data

Serial Code

```
1 x <- read.csv("x.csv")
2 3 x
```

Parallel Code



Binary Data: Vector

```
## set up start and length for reading a vector of n doubles
size <- 8 # bytes

my_ids <- get.jid(n, method="block")

my_start <- (my_ids[1] - 1)*size
my_length <- length(my_ids)

con <- file("binary.vector.file", "rb")
seekval <- seek(con, where=my_start, rw="read")
x <- readBin(con, what="double", n=my_length, size=size)</pre>
```



Binary Data: Matrix

```
## read an nrow by ncol matrix of doubles split by columns
  size <- 8 # bytes
3
  my_ids <- get.jid(ncol, method="block")</pre>
5 | my_ncol <- length(my_ids)</pre>
6 my_start <- (my_ids[1] - 1)*nrow*size
  my_length <- my_ncol*nrow</pre>
8
9 con <- file("binary.matrix.file", "rb")
10 seekval <- seek(con, where=my_start, rw="read")
11 x <- readBin(con, what="double", n=my_length, size=size)
12
13 ## glue together as a column-block ddmatrix
14 gdim <- c(nrow, ncol)
15 | ldim <- c(nrow, my_ncol)
16 bldim <- c(nrow, allreduce(my_ncol, op="max"))
17 X <- new("ddmatrix", Data=matrix(x, nrow, my_ncol),</pre>
            dim=gdim, ldim=ldim, bldim=bldim, ICTXT=1)
18
19
20 ## redistribute for ScaLAPACK's block-cyclic
21 X <- redistribute(X, bldim=c(2, 2), ICTXT=0)
22 Xprc <- prcomp(X)
```

NetCDF4 Data

```
### parallel read after determining start and length
nc <- nc_open_par(file_name)

nc_var_par_access(nc, "variable_name")
new.X <- ncvar_get(nc, "variable_name", start, length)
nc_close(nc)

finalize()</pre>
```



- Data Input
 - Cluster Computer and File System
 - Serial Data Input
 - Parallel Data Input
 - Summary



- Mostly "do it yourself"
- Parallel file system for big data
 - Binary files for true parallel reads
 - Know number of readers vs number of storage servers
- Redistribution help from ddmatrix functions
- More help under development



Contents

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 - Introduction to Distributed Matrices
 - pbdDMAT
 - Summary

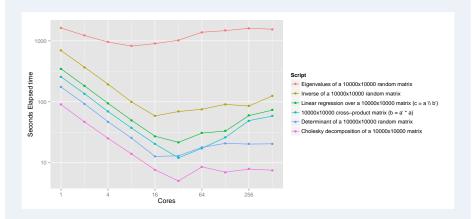


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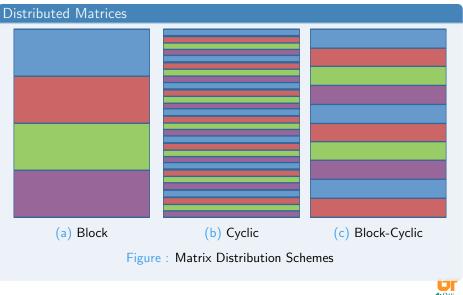
Distributed Matrices

You can only get so far with one node...



The solution is to distribute the data.





Distributed Matrices (b) 2d Cyclic (c) 2d Block-Cyclic (a) 2d Block

Figure: Matrix Distribution Schemes Onto a 2-Dimensional Grid



Processor Grid Shapes

$$\begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix}^{7} \qquad \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix} \qquad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix} \qquad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix} \qquad \begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}$$

$$(a) \ 1 \times 6 \qquad (b) \ 2 \times 3 \qquad (c) \ 3 \times 2 \qquad (d) \ 6 \times 1$$

Table: Processor Grid Shapes with 6 Processors



http://r-pbd.org/tutorial

The ddmatrix Class

For **d**istributed **d**ense **matrix** objects, we use the special S4 class ddmatrix.

$$\mathtt{ddmatrix} = \begin{cases} \textbf{Data} & \mathsf{The\ local\ submatrix\ (an\ R\ matrix)} \\ \textbf{dim} & \mathsf{Dimension\ of\ the\ global\ matrix} \\ \textbf{Idim} & \mathsf{Dimension\ of\ the\ local\ submatrix} \\ \textbf{bldim} & \mathsf{Dimension\ of\ the\ blocks} \\ \textbf{ICTXT} & \mathsf{MPI\ Grid\ Context} \end{cases}$$



Understanding ddmatrix: Global Matrix

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}_{0.06}$$



ddmatrix: 1-dimensional Row Block

$$X = \begin{bmatrix} X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} & X_{18} & X_{19} \\ X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} & X_{28} & X_{29} \\ X_{31} & X_{32} & X_{33} & X_{34} & X_{35} & X_{36} & X_{37} & X_{38} & X_{39} \\ X_{41} & X_{42} & X_{43} & X_{44} & X_{45} & X_{46} & X_{47} & X_{48} & X_{49} \\ X_{51} & X_{52} & X_{53} & X_{54} & X_{55} & X_{56} & X_{57} & X_{58} & X_{59} \\ X_{61} & X_{62} & X_{63} & X_{64} & X_{65} & X_{66} & X_{67} & X_{68} & X_{69} \\ X_{71} & X_{72} & X_{73} & X_{74} & X_{75} & X_{76} & X_{77} & X_{78} & X_{79} \\ X_{81} & X_{82} & X_{83} & X_{84} & X_{85} & X_{86} & X_{87} & X_{88} & X_{89} \\ X_{91} & X_{92} & X_{93} & X_{94} & X_{95} & X_{96} & X_{97} & X_{98} & X_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \end{vmatrix} = \begin{vmatrix} (0,0) \\ (1,0) \\ (2,0) \\ (3,0) \end{vmatrix}$$



ddmatrix: 2-dimensional Row Block

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ \hline x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{\mathbf{9} \times \mathbf{9}}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



ddmatrix: 1-dimensional Row Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 \\ 1 \\ 2 \\ 3 \end{vmatrix} = \begin{vmatrix} (0,0) \\ (1,0) \\ (2,0) \\ (3,0) \end{vmatrix}$$



ddmatrix: 2-dimensional Row Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

 9×9

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



ddmatrix: 2-dimensional Block-Cyclic

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) \\ (1,0) & (1,1) \end{vmatrix}$$



- Introduction to pbdDMAT and the ddmatrix Structure
 - Introduction to Distributed Matrices
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The ddmatrix Data Structure

The more complicated the processor grid, the more complicated the distribution.



ddmatrix: 2-dimensional Block-Cyclic with 6 Processors

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} & x_{16} & x_{17} & x_{18} & x_{19} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} & x_{26} & x_{27} & x_{28} & x_{29} \\ x_{31} & x_{32} & x_{33} & x_{34} & x_{35} & x_{36} & x_{37} & x_{38} & x_{39} \\ x_{41} & x_{42} & x_{43} & x_{44} & x_{45} & x_{46} & x_{47} & x_{48} & x_{49} \\ x_{51} & x_{52} & x_{53} & x_{54} & x_{55} & x_{56} & x_{57} & x_{58} & x_{59} \\ x_{61} & x_{62} & x_{63} & x_{64} & x_{65} & x_{66} & x_{67} & x_{68} & x_{69} \\ x_{71} & x_{72} & x_{73} & x_{74} & x_{75} & x_{76} & x_{77} & x_{78} & x_{79} \\ x_{81} & x_{82} & x_{83} & x_{84} & x_{85} & x_{86} & x_{87} & x_{88} & x_{89} \\ \hline x_{91} & x_{92} & x_{93} & x_{94} & x_{95} & x_{96} & x_{97} & x_{98} & x_{99} \end{bmatrix}_{9}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \end{vmatrix}$$



Understanding ddmatrix: Local View

$$\begin{bmatrix} x_{11} & x_{12} & x_{17} & x_{18} \\ x_{21} & x_{22} & x_{27} & x_{28} \\ x_{51} & x_{52} & x_{57} & x_{58} \\ x_{61} & x_{62} & x_{67} & x_{68} \\ x_{91} & x_{92} & x_{97} & x_{98} \end{bmatrix}_{5\times 4} \begin{bmatrix} x_{13} & x_{14} & x_{19} \\ x_{23} & x_{24} & x_{29} \\ x_{53} & x_{54} & x_{59} \\ x_{63} & x_{64} & x_{69} \\ x_{93} & x_{94} & x_{99} \end{bmatrix}_{5\times 3} \begin{bmatrix} x_{15} & x_{16} \\ x_{25} & x_{26} \\ x_{55} & x_{56} \\ x_{65} & x_{66} \\ x_{95} & x_{96} \end{bmatrix}_{5\times 2}$$

$$\begin{bmatrix} x_{31} & x_{32} & x_{37} & x_{38} \\ x_{41} & x_{42} & x_{47} & x_{48} \\ x_{71} & x_{72} & x_{77} & x_{78} \\ x_{81} & x_{82} & x_{87} & x_{88} \end{bmatrix}_{4\times 4} \begin{bmatrix} x_{33} & x_{34} & x_{39} \\ x_{43} & x_{44} & x_{49} \\ x_{73} & x_{74} & x_{79} \\ x_{83} & x_{84} & x_{89} \end{bmatrix}_{4\times 3} \begin{bmatrix} x_{35} & x_{36} \\ x_{45} & x_{46} \\ x_{75} & x_{76} \\ x_{85} & x_{86} \end{bmatrix}_{4\times 2}$$

Processor grid =
$$\begin{vmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{vmatrix} = \begin{vmatrix} (0,0) & (0,1) & (0,2) \\ (1,0) & (1,1) & (1,2) \end{vmatrix}$$



The ddmatrix Data Structure

- ddmatrix is distributed. No one processor owns all of the matrix
- ddmatrix is non-overlapping. Any piece owned by one processor is owned by no other processors.
- ddmatrix can be row-contiguous or not, depending on the processor grid and blocking factor used.
- ddmatrix is locally column-major and globally, it depends...

_				
<i>x</i> ₁₁	<i>x</i> ₁₂	X ₁₃	X ₁₄	X ₁₅
X ₂₁	X22	X23	X24	X ₂₅
X31	X32	X33	X34	X35
X41	X42	X43	X44	X45
×51	<i>X</i> 52	X53	<i>X</i> 54	<i>X</i> 55
×61	<i>X</i> 62	<i>X</i> 63	<i>X</i> 64	<i>X</i> 65
×71	X ₇₂	X73	<i>X</i> 74	X ₇₅
<i>X</i> 81	X82	X83	X84	X85
X91	X92	X93	<i>X</i> 94	<i>X</i> 95

- GBD is a generalization of the one-dimensional block ddmatrix distribution.
 Otherwise there is no relation
- ddmatrix is confusing, but very robust.



Pros and Cons of This Data Structure

Pros

Robust for matrix computations.

Cons

Confusing layout.

This is why we hide most of the distributed details.

The details are there if you want them (you don't want them).



Methods for class ddmatrix

pbdDMAT has over 100 methods with identical syntax to R:

- `[`, rbind(), cbind(), ...
- lm.fit(), prcomp(), cov(), ...
- `%*%`, solve(), svd(), norm(), ...
- median(), mean(), rowSums(), ...

Serial Code

1 cov(x)

Parallel Code

1 cov(x)



Comparing pbdMPI and pbdDMAT

pbdMPI:

- MPI + sugar.
- GBD not the only structure pbdMPI can handle (just a useful convention).

pbdDMAT:

- Distributed matrices + statistics.
- The ddmatrix structure must be used for pbdDMAT.
- If the data is not 2d block-cyclic compatible, ddmatrix will *definitely* give the wrong answer.



- Introduction to pbdDMAT and the ddmatrix Structure
 - Introduction to Distributed Matrices
 - pbdDMAT
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Summary

Start by loading the package:

```
1 library(pbdDMAT, quiet = TRUE)
```

Always initialize before starting and finalize when finished:

```
1 init.grid()
2
3 # ...
4
5 finalize()
```



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- Examples Using pbdDMAT
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- Examples Using pbdDMAT
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Randomized SVD¹

Prototype for Randomized SVD

Given an $m \times n$ matrix A, a target number k of singular vectors, and an exponent q (say, q = 1 or q = 2), this procedure computes an approximate rank-2k factorization $U\Sigma V^*$, where U and V are orthonormal, and Σ is nonnegative and diagonal.

Stage A:

- Generate an n × 2k Gaussian test matrix Ω.
- 2 Form $Y = (AA^*)^q A\Omega$ by multiplying alternately with A and A^* .
- 3 Construct a matrix Q whose columns form an orthonormal basis for the range of Y.

Stage B:

- 4 Form $B = Q^*A$.
- Compute an SVD of the small matrix: $B = \widetilde{U}\Sigma V^*$.
- Set $U = Q\widetilde{U}$.

Note: The computation of Y in step 2 is vulnerable to round-off errors. When high accuracy is required, we must incorporate an orthonormalization step between each application of A and A^* ; see Algorithm 4.4.

ALGORITHM 4.4: RANDOMIZED SUBSPACE ITERATION

Given an $m \times n$ matrix A and integers ℓ and q, this algorithm computes an $m \times \ell$ orthonormal matrix Q whose range approximates the range of A.

- 1 Draw an $n \times \ell$ standard Gaussian matrix Ω .
- 2 Form $Y_0 = A\Omega$ and compute its QR factorization $Y_0 = Q_0R_0$.
- 3 for j = 1, 2, ..., q
 - Form $\widetilde{Y}_j = A^*Q_{j-1}$ and compute its QR factorization $\widetilde{Y}_j = \widetilde{Q}_j \widetilde{R}_j$. Form $Y_i = A\widetilde{Q}_j$ and compute its QR factorization $Y_j = Q_j R_j$.
- 6 end
- $7 \quad Q = Q_a$.

Serial R

```
randSVD \leftarrow function(A, k, \alpha=3)
 2
 3
         ## Stage A
         Omega <- matrix(rnorm(n*2*k),
                   nrow=n. ncol=2*k)
        Y <- A %*% Omega
        Q \leftarrow qr.Q(qr(Y))
         At < -t(A)
 9
         for(i in 1:q)
10
11
             Y <- At %*% Q
12
             Q \leftarrow ar.Q(ar(Y))
             Y <- A %*% Q
13
             Q \leftarrow ar.Q(ar(Y))
14
15
16
17
        ## Stage B
18
        B <- t(Q) %*% A
        U <- La.svd(B)$u
19
        U <- Q %*% U
20
21
        U[, 1:k]
22
```

¹Halko N, Martinsson P-G and Tropp J A 2011 Finding structure with randomness: probabilistic algorithms for constructing approximate matrix decompositions *SIAM Rev.* **53** 217–88



Randomized SVD

Serial R

```
randSVD \leftarrow function(A, k, q=3)
 2
         ## Stage A
 4
         Omega <- matrix(rnorm(n*2*k),
                nrow=n. ncol=2*k)
 5
6
7
8
         Y <- A %*% Omega
         Q \leftarrow qr.Q(qr(Y))
         At \leftarrow t(A)
 9
         for(i in 1:q)
10
              Y <- At %*% O
11
12
              Q \leftarrow qr.Q(qr(Y))
13
              Y <- A %*% Q
14
              Q \leftarrow qr.Q(qr(Y))
15
16
17
         ## Stage B
18
         B <- t(Q) %*% A
19
         U \leftarrow La.svd(B)u
20
         U <- Q %*% U
21
         U[, 1:k]
22
```

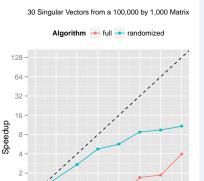
Parallel pbdR

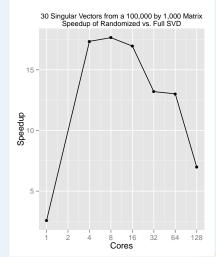
```
randSVD \leftarrow function(A, k, q=3)
 3
        ## Stage A
         Omega <- ddmatrix("rnorm",
                nrow=n. ncol=2*k)
         Y <- A %*% Omega
         Q \leftarrow qr.Q(qr(Y))
         At \leftarrow t(A)
 9
         for(i in 1:q)
10
11
              Y <- At %*% Q
12
              Q \leftarrow qr.Q(qr(Y))
13
              Y <- A %*% Q
14
              Q \leftarrow qr.Q(qr(Y))
15
16
17
         ## Stage B
         B <- t(Q) %*% A
18
         U <- La. svd (B)$u
19
20
         U <- Q %*% U
21
         U[, 1:k]
22
```



Randomized SVD

http://r-pbd.org/tutorial







64 128

16 32

Cores

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Summary

- pbdDMAT makes distributed (dense) linear algebra easier.
- Can enable rapid prototyping at large scale.



Contents

- MPI Profiling
 - Profiling with the pbdPROF Package
 - Installing pbdPROF
 - Example
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- MPI Profiling
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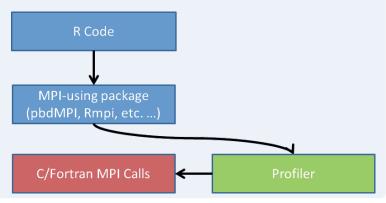
Introduction to **pbdPROF**

- Successful Google Summer of Code 2013 project.
- Available on the CRAN.
- Enables profiling of MPI-using R scripts.
- pbdR packages officially supported; can work with others...
- Also reads, parses, and plots profiler outputs.



How it works

MPI calls get hijacked by profiler and logged:





Introduction to pbdPROF

- Currently supports the profilers fpmpi and mpiP.
- fpmpi is distributed with pbdPROF and installs easily, but offers minimal profiling capabilities.
- mpiP is fully supported also, but you have to install and link it yourself.



http://r-pbd.org/tutorial

- MPI Profiling
 - Profiling with the pbdPROF Package
 - Installing pbdPROF
 - Example



Installing pbdPROF

- Build pbdPROF.
- 2 Rebuild **pbdMPI** (linking with **pbdPROF**).
- Run your analysis as usual.
- Interactively analyze profiler outputs with pbdPROF.

This is explained at length in the pbdPROF vignette.



Rebuild **pbdMPI**

```
R CMD INSTALL pbdMPI_0.2-2.tar.gz
--configure-args="--enable-pbdPROF"
```

- Any package which explicitly links with an MPI library must be rebuilt in this way (pbdMPI, Rmpi, ...).
- Other pbdR packages link with pbdMPI, and so do not need to be rebuilt.
- See **pbdPROF** vignette if something goes wrong.



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An Example from **pbdDMAT**

- Compute SVD in **pbdDMAT** package.
- Profile MPI calls with mpiP.



Example Script

http://r-pbd.org/tutorial

my_svd.r

```
library(pbdMPI, quietly=TRUE)
  library(pbdDMAT, quietly=TRUE)
  init.grid()
  n <- 1000
  x <- ddmatrix("rnorm", n, n)
  my.svd <- La.svd(x)</pre>
10
11
  finalize()
```



Programming with Big Data in R

Example Script

Run example with 4 ranks:

```
$ mpirun -np 4 Rscript my_svd.r
mpiP:
mpiP: mpiP: mpiP V3.3.0 (Build Sep 23 2013/14:00:47)
mpiP: Direct questions and errors to
        mpip-help@lists.sourceforge.net
mpiP:
Using 2x2 for the default grid size

mpiP:
mpiP: Storing mpiP output in [./R.4.5944.1.mpiP].
mpiP:
```



Read Profiler Data into R

Interactively (or in batch) Read in Profiler Data

```
library(pbdPROF)
prof.data <- read.prof("R.4.28812.1.mpiP")</pre>
```

Partial Output of Example Data

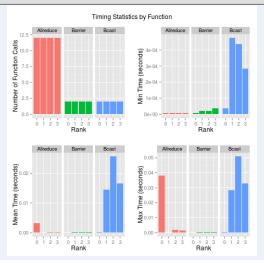
```
> prof.data
An mpip profiler object:
\lceil \lceil 1 \rceil \rceil
  Task AppTime MPITime MPI.
     0
          5.71 0.0387 0.68
1
          5.70 0.0297 0.52
     2 5.71 0.0540 0.95
3
     3 5.71 0.0355 0.62
4
         22.80 0.1580 0.69
[[2]]
     Lev File.Address Line_Parent_Funct MPI_Call
1
        0 1.397301e+14
                                 [unknown] Allreduce
2
        0.1.397301e+14
                                 [unknown]
                                                Boast
```



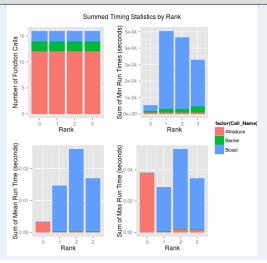
plot(prof.data)



















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Summary

http://r-pbd.org/tutorial

- **pbdPROF** offers tools for profiling R-using MPI codes.
- Easily builds fpmpi; also supports mpiP.



Contents

Wrapup



Summary

- Profile your code to understand your bottlenecks.
- pbdR makes distributed parallelism with R easier.
- Distributing data to multiple nodes
- For truly large data, I/O must be parallel as well.



The pbdR Project

- Our website: http://r-pbd.org/
- Email us at: RBigData@gmail.com
- Our google group: http://group.r-pbd.org/

Where to begin?

- The pbdDEMO package http://cran.r-project.org/web/packages/pbdDEMO/
- The **pbdDEMO** Vignette: http://goo.gl/HZkRt



Thanks for coming!

Questions?



http://r-pbd.org/

Come see our poster on Wednesday at 5:30!

