

## Homework7

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### Table of Contents

**No table of contents entries found.**

#Question 4

# a a. Fit regression model (8.58) using the number of cases shipped (X d and the binary variable(X3) as predictors.

load data

```
rdata<-read.table("../homework7/hello.txt",header = F)
colnames(rdata)<-c("Y", "X1", "X2", "X3")
```

```
tail(rdata,3)
```

```
##      Y      X1    X2 X3
## 50 4499 290455 7.99  0
## 51 4186 411750 7.83  0
## 52 4342 292087 7.77  0
```

Fit a regression model

```
rdata.reg=lm(Y~X1+I(X1^2)+X3+X1:X3,data = rdata)
rdata.reg
```

```
##
## Call:
## lm(formula = Y ~ X1 + I(X1^2) + X3 + X1:X3, data = rdata)
##
## Coefficients:
## (Intercept)          X1      I(X1^2)          X3      X1:X3
##  3.925e+03    1.570e-03   -1.154e-09    6.505e+02   -8.870e-05
```

```
summary(rdata.reg)
```

```
##
## Call:
## lm(formula = Y ~ X1 + I(X1^2) + X3 + X1:X3, data = rdata)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -288.253 -102.112  -7.251   72.363  294.646
##
## Coefficients:
```

```
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  3.925e+03  6.262e+02   6.268 1.06e-07 ***
## X1          1.570e-03  3.755e-03   0.418  0.6778
## I(X1^2)     -1.154e-09  5.481e-09  -0.211  0.8341
## X3          6.505e+02  2.801e+02   2.322  0.0246 *
## X1:X3       -8.870e-05  8.760e-04  -0.101  0.9198
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 145.2 on 47 degrees of freedom
## Multiple R-squared:  0.6865, Adjusted R-squared:  0.6599
## F-statistic: 25.74 on 4 and 47 DF,  p-value: 2.476e-11
```

our regression model is  $\hat{y} = 3925 - 0.00152X_1 - 1.154e-09 I(X_1^2) + (650.2X_3) - (8.870e-05 X_1:X_3)$

#b Test whether or not the interaction terms and the quadratic term can be dropped from the model; use  $\alpha = .05$ . State the alternatives, decision rule, and conclusion. What is the P-value of the test?

Hypothesis  $H_0: B_2 = B_4 = 0$   $H_a$  : Atleast one inequality

The full Regression model  $Y_i = B_0 + B_1(X_1) - B_2(x^2_1) + B_3(X_3) - B_4(X_1X_3) + e$

The reduced model  $Y_i = B_0 + B_1(X_1) + B_3(X_3) + e$

```
rdata.reg<- lm(Y~X1+X3,data =rdata)
rdata.reg2<-lm(Y~X1+I(X1^2)+X3+X1:X3,data = rdata)
anova(rdata.reg,rdata.reg2)

## Analysis of Variance Table
##
## Model 1: Y ~ X1 + X3
## Model 2: Y ~ X1 + I(X1^2) + X3 + X1:X3
##   Res.Df    RSS Df Sum of Sq    F Pr(>F)
## 1      49 992204
## 2      47 991173  2    1031.2 0.0244 0.9759
```

use formula based calculation

$SSE(F) = SSE(X_1, I(X_1^2), X_3, X_1:X_3) = 991173$   $SSE(R) = SSE(X_1, X_2) = 992204$  The F - partial  
 $= (SSE(R) - SSE(F) / (dfe(R) - dfe(F))) / (SSE(F) / dfe(F)) = ((1031.2) / (49 - 47)) / (991173 / 47)$   
 $= (1031.2) / (2) / (991173 / 7) = 0.0244901$  p-value calculation

```
p_value<-1-pf(0.0244901,2,47)
p_value

## [1] 0.9758198
```

p-value =  $P(F(df_1 = dfe(R) - dfe(F), df_2 = dfe(F))) > F_{partial}$   
 $= P(F(df_1 = 1, df_2 = 57) > 0.02444901) = 0.9758598.$

Decision rule Reject  $H_0$  if p-value is  $< \alpha$

Statistical conclusion since p-value (0.9758598) is greater than  $\alpha(0.025)$ , we do not reject  $H_0$ . Therefore, we do not have significance evidence to support that  $x_1^2, X_1X_3$  needed in the model so  $x_1^2, X_1X_3$  can be dropped from the model when  $X_1$  and  $X_2$  are in the model.

#C Why would we wish to include number of cases ( $X_1$ ) in the regression when our interest is in estimating the effects of holiday on labor hours? This is because at this point we do not have evidence that the number of cases is insignificant in this model such that it can be removed and not affecting the model. Hence to ensure better results we include the number of cases.