

PRODUCTION RULE

Jug 1: 13 liters, Jug 2: 11 liters

1. Fill the 13-liter jug

$$(x,y) \rightarrow (13,y)$$

Condition: $x < 13$

(Fill jug 1 to its full capacity.)

2. Fill the 11-liter jug

$$(x,y) \rightarrow (x,11)$$

Condition: $y < 11$

(Fill jug 2 to its full capacity.)

3. Empty the 13-liter jug onto the ground

$$(x,y) \rightarrow (0,y)$$

Condition: $x > 0$

(Empty jug 1 completely.)

4. Empty the 11-liter jug onto the ground

$$(x,y) \rightarrow (x,0)$$

Condition: $y > 0$

(Empty jug 2 completely.)

5. Pour water from the 11-liter jug into the 13-liter jug

$$(x,y) \rightarrow (x+y,0)$$

Condition: $0 < x+y \leq 13$ and $y > 0$

(Pour water from jug 2 into jug 1 until jug 1 is full or jug 2 is empty.)

6. Pour water from the 13-liter jug into the 11-liter jug

$$(x,y) \rightarrow (0,x+y)$$

Condition: $0 < x+y \leq 11$ and $x > 0$

(Pour water from jug 1 into jug 2 until jug 2 is full or jug 1 is empty.)

7. Pour water from the 11-liter jug into the 13-liter jug until the 13-liter jug is full

$$(x,y) \rightarrow (13,y-(13-x))$$

Condition: $x+y \geq 13$ and $y > 0$

(Transfer water from jug 2 to jug 1 until jug 1 is full.)

8. **Pour water from the 13-liter jug into the 11-liter jug until the 11-liter jug is full**

$$(x,y) \rightarrow (x-(11-y), 11)$$

Condition: $x+y \geq 11$ and $x > 0$

(Transfer water from jug 1 to jug 2 until jug 2 is full.)

Goal:

The goal is to have **8 liters in the 13-liter jug**, i.e., the state $(8,y)$.