

| Distribution | PDF | Support | Mean | Variance | MGF |
|--|---|---|-------------------------------|--|---|
| Discrete Distributions | | | | | |
| Bernoulli | $p^x(1-p)^{1-x}$ | $x \in \{0, 1\}$ | p | $p(1-p)$ | $(1-p) + pe^t$ |
| Binomial | $\binom{n}{x}p^x(1-p)^{n-x}$ | $0 \leq x \leq n$ | np | $np(1-p)$ | $[(1-p) + pe^t]^n$ |
| Geometric (Failures, "before") | $p(1-p)^x$ | $x \geq 0$ | $\frac{1}{p}$ | $\frac{1-p}{p^2}$ | $\frac{p}{(1-(1-p)e^t)}, t < -\ln(1-p)$ |
| Geometric (Trails, "until") | $p(1-p)^{x-1}$ | $x \geq 1$ | $\frac{1}{p}$ | $\frac{1-p}{p^2}$ | $\frac{pe^t}{(1-(1-p)e^t)}, t < -\ln(1-p)$ |
| Negative Binomial (Failures, "before") | $\binom{x+r-1}{r-1}p^r(1-p)^x$ | $x \geq 0$ | $\frac{r(1-p)}{p}$ | $\frac{r(1-p)}{p^2}$ | $[\frac{p}{(1-(1-p)e^t)}]^r, t < -\ln(1-p)$ |
| Negative Binomial (Trails, "until") | $\binom{x-1}{r-1}p^r(1-p)^{x-r}$ | $x \geq r$ | $\frac{r}{p}$ | $\frac{r(1-p)}{p^2}$ | $[\frac{pe^t}{(1-(1-p)e^t)}]^r, t < -\ln(1-p)$ |
| Hypergeometric | $\frac{\binom{k}{x}\binom{N-k}{n-x}}{\binom{N}{n}}$ | $\max(0, n-N+k) \leq x \leq \min(n, k)$ | $\frac{nk}{N}$ | $\frac{nk(N-k)(N-n)}{N^2(N-1)}$ | |
| Poisson | $\frac{\lambda^x e^{-\lambda}}{x!}$ | $x \geq 0$ | λ | λ | $e^{\lambda(e^t-1)}$ |
| Uniform Discrete | $\frac{1}{n}$ | $a \leq x \leq b$ | $\frac{a+b}{2}$ | $\frac{n^2-1}{12}$ | $\frac{e^{at}-e^{(b+1)t}}{n(1-e^t)}$ |
| Continuous Distributions | | | | | |
| Normal | $\frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}(\frac{x-\mu}{\sigma})^2}$ | $-\infty \leq x \leq \infty$ | μ | σ^2 | $e^{\mu t + \frac{\sigma^2 t^2}{2}}$ |
| Exponential (Gamma with $\alpha = 1$) | $\lambda e^{-\lambda x}$ | $x \geq 0$ | $\frac{1}{\lambda}$ | $\frac{1}{\lambda^2}$ | $\frac{1}{1-\frac{t}{\lambda}}, t < \lambda$ |
| Gamma | $\frac{1}{\Gamma(\alpha)\beta^\alpha}x^{\alpha-1}e^{-\lambda x}$ | $x \geq 0$ | $\alpha\beta$ | $\alpha\beta^2$ | $[\frac{1}{1-\frac{t}{\lambda}}]^\alpha, t < \lambda$ |
| Uniform Continuous | $\frac{1}{b-a}$ | $a \leq x \leq b$ | $\frac{a+b}{2}$ | $\frac{(b-a)^2}{12}$ | $\frac{e^{tb}-e^{ta}}{t(b-a)}$ |
| Beta | $\frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)}x^{\alpha-1}(1-x)^{\beta-1}$ | $x \in \{0, 1\}$ | $\frac{\alpha}{\alpha+\beta}$ | $\frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta+1)}$ | |
| Chi-square (Gamma, $\alpha = \frac{1}{2}, \beta = 2$) | $\frac{1}{\Gamma(\frac{v}{2})2^{\frac{v}{2}}}x^{\frac{v}{2}-1}e^{-\frac{x}{2}}$ | $x \geq 0$ | v | $2v$ | $(1-2t)^{-\frac{v}{2}}, t < \frac{1}{2}$ |