

# Logistic Regression





### Concept of Regression technique for classification

- Decision boundary
- Parameter randomization and optimization
- Learning rate
- Adjustment based on error
- Example using scikit-learn

# Today's Outline



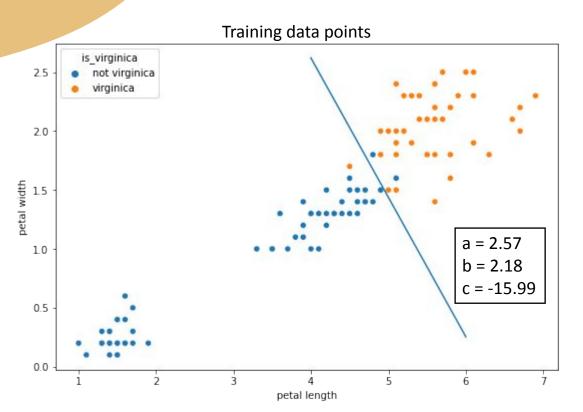


### **Logistic Regression**

- A technique for classification
- Create a linear decision boundary
  - Points on or above this boundary are predicted as one class
  - Points below this boundary predicted as the other class
- Use optimization technique to find best boundary



### Line and weight vector



- A line can be described using an equation y = ax+c where
  - x and y are two variables
  - c is an intercept of the line
  - a is the slope of the line
- Rearrange the equation to be

$$a*x + b*y + c*1 = 0$$

 a, b, c is called the weight (or coefficient) vector





2.5

2.0

petal width

1.0

0.5

0.0

is virginica

virginica

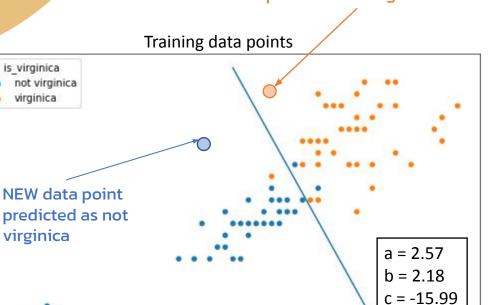
2

3

petal length

not virginica virginica

#### **NEW data point** predicted as virginica



### **Decision boundary**

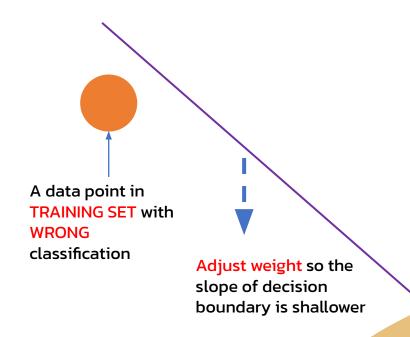
- Suppose that we have a new data point x2, y2
  - If a\*x2 + b\*y2 + c\*1 > 0, then the data point is above the line, and we can predict that it is of one class
  - If the data point is below the line, we can predict that it is of the other class
- So this line is a linear decision boundary





### How to find a "good" weight vector?

- Randomize initial values of weight factor
- Loop a lot of times (ex. 1000 times) or until almost no change
  - Calculate the accuracy (or other measure) of classification on the training set data points one-by-one
  - 2) Adjust the weight to improve the accuracy



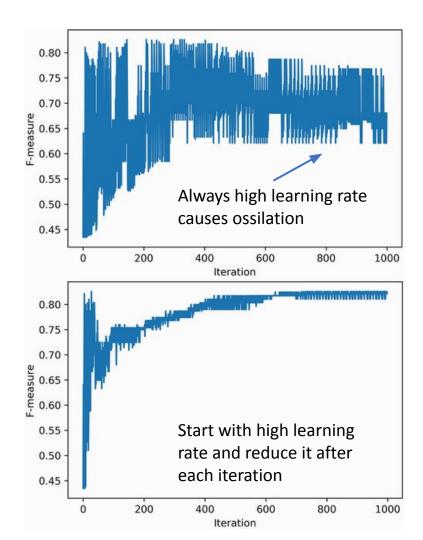




# How much weight to adjust?

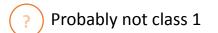
- Learning rate: the rate of weight adjustment as a fraction of unit e.g., 0.1 or 0.01
- High rate: fast adjustment, but may overshoot
- Low rate: smaller adjustment, take longer time to reach good solution
- One technique: start with high rate then lower the rate after each loop

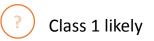


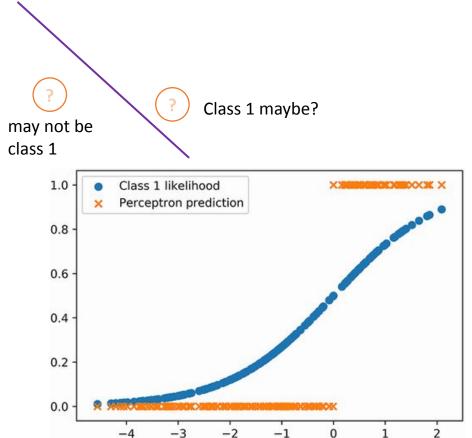


### Model confidence

- So far: simple perceptron (0-1 decision)
- Problem: no context about confidence of model prediction
  - Model should be less confidence if data point lies close to the decision boundary
- How can we calculate confidence?







Directed distance





## **Logistic function**

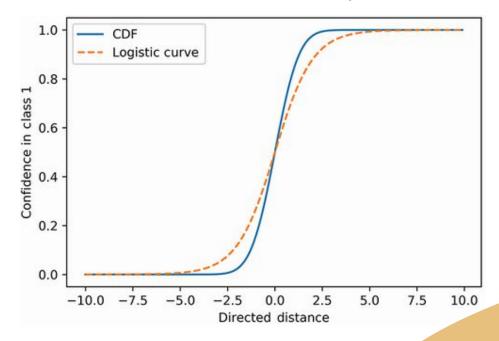
#### Characteristic of needed function

- Zero distance from the decision line equation results in 50% confidence with no adjustment
- Large distance from the decision line equation gives large, stable positive/negative confidence adjustment
- Confidence adjusted linearly between the two extremes

#### Possible 2 functions

- CDF (cumulative density function)
- Logistic function
- distance is standardized

confidence(distance) = 
$$\frac{1}{1 + e^{-\text{distance}}}$$





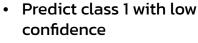


### Using confidence to adjust weight

- Model confidence can be used to adjust weight vector
- If the model is confidence but wrong, we can strongly adjust the weight
- Weight adjustment is now a function of learning rate, iteration, confidence of prediction, and actual value
- More consistent model



- Predict class 1 with high confidence
- Data point is actually class 0
- large weight adjustment



- Data point is actually class O
- small weight adjustment





#### **Benefits and Limitations**

- Works well where difference between classes follow mostly linear boundary
- Easy to use and give respectable performance, often used as baseline model
- Works with numeric data only
  - Must convert categorical values using one-hot encoding
- Don't forget to standardize or normalize numeric data



### **Sklearn**

from sklearn.



### **Scikit-learn implementation**

### **DEMO**





#### Reference

• Leonard Apeltsin, "Data Science Bookcamp", Manning Publications, November 2021.

