## %1 kempolmain.m

```
    function kempo1main

      2.
3.
      %用于随机生成粒子的初始坐标和相位角
4.
      rng('default');
5.
      rng(1);
      global flag_exit
6.
7.
      flag_exit=0
8.
9.
      10.
      prm = Parameters
11.
12.
      13.
      [prm,ren] = renorm(prm);
14.
      15.
      %初始化画图设置, 粒子坐标和速度等
16.
17.
     [hdiag,output] = diagnostics init(prm);
      particle = Particle(prm);
18.
19.
      field = Field(prm);
20.
21.
     %初次更新粒子位置和求电荷量、电场分布
     position(particle,prm); %首次更新半个时间步的粒子位置
22.
23.
      if prm.iex
                        %静电开关: iex=1 为电磁, iex=2 为静电
24.
        charge(particle, field, prm); %求网格点电荷密度
                                %通过泊松方程求电场分布
25.
        poisson(field, prm);
26.
      end
27.
      28.
29.
      jtime=0;
30.
      jdiag=1; %诊断计数
31.
32.
      %-- Diagnostics at initial time --
33.
      hdiag=diagnostics(hdiag,particle,field,output,prm,jtime,jdiag,ren);
      if prm.nplot == 0 %nplot: number of output
34.
35.
        return
36.
      end
37.
38.
39.
40.
41.
42.
```

```
43.
        % Time advance loop
44.
       for jtime = 1:prm.ntime %? 时间间隔 dt 和总时间步数的选择
45.
           if prm.iex==2 %iex=2 静电; iex=1 电磁
46.
47.
               rvelocity(particle, field, prm);
48.
               position(particle, prm);
               position(particle, prm); %? 两次位置变化?? 每次更新半个时间步位置
49.
               charge(particle, field, prm);
50.
               poisson(field, prm);
51.
52.
           else
53.
54.
55.
               bfield(field,prm);
               rvelocity(particle, field, prm); %Boris 方法
56.
57.
               position(particle, prm);
               current(particle, field, jtime, prm);
58.
               bfield(field, prm);
59.
               efield(field, prm);
60.
61.
               position(particle, prm);
62.
           end
63.
64.
          %-- 时变诊断 diagnostics --
65.
          if mod(jtime,prm.ifdiag)==0
             jdiag = jdiag+1;
66.
             hdiag = diagnostics(hdiag, particle, field,output, prm, jtime, jdi
67.
   ag,ren);
68.
          end
          if flag_exit
69.
70.
             break;
71.
          end
```

#### %2 Parameter.m

```
1. %*******读取输入参数********
2. classdef Parameters < handle
3.
4.
        properties
           %网格距和时间步长,需满足库朗条件\Delta x > c\Delta t 且小于徳拜长度 \Delta x \leq 3\lambda_e
5.
6.
           dx double {mustBePositive}
7.
            dt double {mustBePositive}
8.
           %网格点数
           nx double {mustBePositive}
9.
10.
           %时间步数
11.
           ntime double {mustBeInteger,mustBePositive}
12.
           % number of outputs
13.
           nplot double {mustBeInteger, mustBePositive}
           %光速,程序输入的光速为20??
14.
           cv double {mustBePositive}
15.
           %粒子的回旋频率
16.
17.
           wc double {mustBeReal}
           %外部电流的振幅 jz
18.
           ajamp double {mustBeNonnegative}
19.
           %电场振幅
20.
21.
           eamp double {mustBePositive}
22.
           %maximum range for plotting the electric field
23.
           emax double {mustBeReal}
24.
           %磁场的振幅
25.
           bamp double {mustBePositive}
           %maximum range for plotting the magnetic field
26.
27.
           bmax double {mustBeReal}
           % control parameter for electrostatic option
28.
           iex double {mustBeMember(iex,[0,1,2])}
29.
           % maximum range for plotting velocity
30.
31.
           vmax double {mustBeReal}
32.
           %number of bins for deriving the particle distribution function
33.
           nv double {mustBeInteger}
           % 外部电流的频率 jz
34.
           wj double {mustBeNonnegative}
35.
```

```
36.
            % 粒子种类的数量
37.
            ns double {mustBeInteger, mustBePositive}
            % number of particles for species
38.
39.
            np double {mustBeInteger, mustBePositive}
40.
            % plasma frequency of species
41.
            wp double {mustBePositive}
            % charge-to-mass ratio of species
42.
43.
            qm double {mustBeReal}
            % parallel thermal velocity of species
44.
            vpa double {mustBePositive}
45.
46.
            % perpendicular thermal velocity of species
            vpe double {mustBePositive}
47.
48.
            % drift velocity of species
49.
            vd double {mustBeNonnegative}
50.
            %漂移速度和水平方向的夹角,满足以下关系(Ø=pch*pi/180)
51.
            %v_{d\perp} = v_d \sin \phi
52.
            %v_{d||} = v_d \cos \phi
53.
            pch double {mustBeGreaterThanOrEqual(pch,0), mustBeLessThanOrEqual(p
   ch,180)}
54.
            %颜色开关
55.
            icolor
56.
            %画图开关
57.
            iparam
            %诊断方式
58.
59.
            diagtype
            angle double {mustBeGreaterThanOrEqual(angle,0), mustBeLessThanOrEq
60.
   ual(angle,90)}
       end
61.
62.
63.
      % Actually I am not sure if this should be calculated only once. It
64.
      % might be better.
      % For example, in the initialization part, slx has been used several
65.
      % times inside the nested loop. q is used in function charge.
66.
67.
      properties (Dependent)
68.
         slx
69.
         npt
70.
         nxp1
71.
         nxp2
72.
         Х1
73.
         X2
74.
         Х3
75.
         cs
76.
         tcs
77.
```

```
78.
          mass
79.
          rho0
80.
          bx0
81.
          by0
82.
          ifdiag
83.
       end
84.
85.
       methods
          function obj = Parameters(fname)
86.
87.
             % read input parameters and set values
88.
89.
             if nargin==0
90.
                fname = 'input_tmp.dat'; % default input filename
91.
             end
92.
93.
             try
94.
                fid = fopen(fname);
95.
                C = textscan(fid,'%s%s','delimiter','=;','commentstyle','matlab'
   );
96.
                [StrName,StrValue] = C{:};
97.
                fclose(fid);
98.
             catch
99.
                errordlg(sprintf('Can''t open input file: %s',fname),'Error')
100.
              end
101.
102.
              for l=1:length(StrName)
103.
                 value = eval(char(StrValue(1)));
104.
                 prmname = strtrim(StrName{1});
105.
                 switch prmname
                     case 'dx'
106.
107.
                        obj.dx = value;
                     case 'dt'
108.
109.
                        obj.dt = value;
110.
                     case 'nx'
111.
                        obj.nx = value;
112.
                     case 'ntime'
113.
                        obj.ntime = value;
114.
                     case 'nplot'
115.
                        obj.nplot = value;
                     case 'cv'
116.
                        obj.cv = value;
117.
                     case 'wc'
118.
119.
                        obj.wc = value;
                     case 'ajamp'
120.
```

```
121.
                       obj.ajamp = value;
122.
                    case 'eamp'
123.
                       obj.eamp = value;
124.
                    case 'emax'
125.
                       obj.emax = value;
126.
                    case 'bamp'
127.
                       obj.bamp = value;
                    case 'bmax'
128.
129.
                       obj.bmax = value;
                    case 'iex'
130.
131. %
                        obj.iex = value;
132.
                         obj.iex = 2;
133.
                    case 'vmax'
134.
                       obj.vmax = value;
                    case 'nv'
135.
                       obj.nv = value;
136.
                    case 'wj'
137.
138.
                       obj.wj = value;
139.
                    case 'ns'
140.
                       obj.ns = value;
                    case 'np'
141.
142.
                       obj.np = value;
                    case 'wp'
143.
144.
                       obj.wp = value;
145.
                    case 'qm'
146.
                       obj.qm = value;
147.
                    case 'vpa'
148.
                       obj.vpa = value;
149.
                    case 'vpe'
150.
                       obj.vpe = value;
                    case 'vd'
151.
                       obj.vd = value;
152.
                    case 'pch'
153.
154.
                       obj.pch = value;
155.
                    case 'icolor'
156.
                       obj.icolor = value;
                    case 'iparam'
157.
158.
                       obj.iparam = value;
159.
                    case 'diagtype'
                         obj.diagtype = value;
160. %
                       obj.diagtype = [1, 4, 5, 10, 11.000000,15, 25.000000, 3
161.
 0.000000];
162.
                    case 'angle'
163.
                       obj.angle = value;
```

```
164.
                    otherwise
165.
                       error('Plese check input parameter %s.',prmname)
166.
                 end
167.
              end
168.
           end
169.
           % Get the dependent vars
170.
171.
172.
           %网格点数
           function value = get.slx(obj)
173.
174.
               value = obj.nx;
175.
           end
176.
           %总的网格点数
177.
178.
           function value = get.npt(obj)
               %总的粒子数量
179.
180.
               value = sum(obj.np(1:obj.ns));
181.
           end
182.
183.
           %网格点数+1
           function value = get.nxp1(obj)
184.
185.
186.
               value = obj.nx+1;
187.
           end
188.
           %网格点数+2
189.
           function value = get.nxp2(obj)
190.
              value = obj.nx+2;
191.
192.
           end
193.
           %1:128
194.
           function value = get.X1(obj)
195.
196.
              value = 1:obj.nx;
197.
           end
198.
199.
           %2:129
200.
           function value = get.X2(obj)
201.
              value = 2:(obj.nx+1);
202.
           end
203.
204.
           %3:130
           function value = get.X3(obj)
205.
206.
              value = 3:(obj.nx+2);
207.
           end
```

```
208.
209.
           %光速平方
           function value = get.cs(obj)
210.
211.
              value = obj.cv^2;
212.
           end
213.
           %光速平方的 2 倍
214.
           function value = get.tcs(obj)
215.
216.
              value = 2*obj.cs;
217.
           end
218.
219.
           %电荷量
220.
           function value = get.q(obj)
221.
              value = obj.nx ./ obj.np(1:obj.ns) .* (obj.wp(1:obj.ns).^2) ./ ...
222.
                 obj.qm(1:obj.ns);
223.
           end
224.
225.
           % This is a case where you have inter-dependency.
226.
           function value = get.mass(obj)
              value = obj.q ./ obj.qm(1:obj.ns);
227.
228.
           end
229.
230.
           %电荷密度
           function value = get.rho0(obj)
231.
232.
              value = -sum(obj.q(1:obj.ns) .* obj.np(1:obj.ns)) / obj.nx *...
233.
                 ones(obj.nxp2,1);
           end
234.
235.
236.
           function value = get.bx0(obj)
237.
              theta = pi/180*obj.angle;
              value = obj.wc/obj.qm(1)*cos(theta);
238.
239.
           end
240.
           function value = get.by0(obj)
241.
242.
              theta = pi/180*obj.angle;
              value = obj.wc/obj.qm(1)*sin(theta);
243.
244.
           end
245.
           %每次画的步长数
246.
247.
           function value = get.ifdiag(obj)
248.
              value = ceil(obj.ntime/obj.nplot);
249.
           end
250.
        end
```

#### %3 renorm.m

```
1. %*********归一化系数********
2. %ren.*=实际/模拟(归一化指的是网格距归一,其他参数并不归一而是等比例变化)
3. function [prm,ren]=renorm(prm)
     ren.x=prm.dx
                          %网格距系数,将网格距归一化为1
4.
5.
     ren.t=prm.dt/2
                          %时间步长系数,将时间步统一化为2
6.
     ren.v=ren.x/ren.t
                          %速度系数
7.
     ren.e=ren.x/(ren.t^2)
                          %电场系数
8.
     ren.b=1.0/ren.t
                          %磁场系数
9.
     ren.j=ren.x/(ren.t^3)
                          %电流密度系数
10.
     ren.r=1.0/(ren.t^2)
                          %电荷密度系数
     ren.s=(ren.x^2)/(ren.t^4)%能量密度系数
11.
12.
13.
     prm.cv=prm.cv/ren.v
                          %等比列变化后的光速
14.
                          %等比列变化后的回旋频率
     prm.wc=prm.wc*ren.t
15.
                   .*ren.t %等比列变化后的等离子体频率
16.
      prm.wp=prm.wp
     prm.vpa=prm.vpa ./ren.v %等比列变化后的平行速度
17.
18.
     prm.vpe=prm.vpe ./ren.v %等比列变化后的垂直速度
19.
                   ./ren.v %等比列变化后的漂移速度
     prm.vd=prm.vd
20.
21.
     prm.vmax=prm.vmax ./ren.v%等比列变化后的速度上限
22.
     prm.wj=prm.wj*ren.t %等比列变化后的外部电流的频率 jz
23.
24.
     prm.ajamp=prm.ajamp/ren.j%等比列变化后的外部电流的振幅 ajamp
25.
26. end
```

#### %4 Particle.m

```
    classdef Particle < handle</li>

2.
3.
        properties
                          %粒子坐标
4.
             x double
5.
             vx double
6.
             vy double
             vz double
7.
8.
        end
9.
10.
        methods
11.
             function obj=Particle(prm)
```

```
12.
             %粒子初始化
13.
             obj.x =zeros(prm.npt,1);
14.
             obj.vx=zeros(prm.npt,1);
             obj.vy=zeros(prm.npt,1);
15.
16.
             obj.vz=zeros(prm.npt,1);
17.
             n2=0;
18.
19.
             for k=1:prm.ns
20.
                 n1=n2;
                 n2=n2+prm.np(k);
21.
22.
23.
                 phi = pi/180.0*prm.pch(k); %漂移速度与水平方向的夹角
24.
                 vdpa = prm.vd(k)*cos(phi); %漂移速度的平行分量
                 vdpe = prm.vd(k)*sin(phi); %漂移速度的垂直分量
25.
26.
27.
                 xx = 0;
28.
                 nphase = 1;
29.
                 phase = 0;
30.
31.
                 %对每一个粒子进行操作
32.
                 for i=(n1+1):n2
33.
                     if mod(i,nphase) == 0
34.
                        phase = 2*pi*rand;
                                                    %随机粒子的相位
                                                    %等间距分配每一个粒子坐标
35.
                       xx = xx + prm.nx/prm.np(k);
36.
                     else
37.
                        phase = phase + 2*pi/nphase; %随机粒子相位角
38.
                     end
39.
40.
                     obj.x(i) = xx;
                                                    %初始化粒子坐标
41.
                     if obj.x(i) < 0.0
42.
                       obj.x(i) = obj.x(i) + prm.slx;%slx 网格点数=nx
43.
                     end
44.
                     if obj.x(i) >= prm.slx
45.
                       obj.x(i) = obj.x(i) - prm.slx;%保证粒子坐标在网格内
                     end
46.
47.
                                                           %平行热速度+平行漂
48.
                     uxi = prm.vpa(k)*randn + vdpa;
   移速度
49.
                     uyi = prm.vpe(k)*randn + vdpe*cos(phase);%垂直热速度的 y 分
   量+平行漂移速度的 y 分量
50.
                     uz = prm.vpe(k)*randn + vdpe*sin(phase);%垂直热速度的 z 分
   量+平行漂移速度的 z 分量
51.
52.
                     % rotation to the direction of the magnetic field
```

```
53.
                      % angle 为静磁场 B0 与波矢 k 的夹角, 其中 B0 在 x-y 平面内
54.
                      costh = cos(pi/180*prm.angle); %costh=1
55.
                      sinth = sin(pi/180*prm.angle); %sinth=0
                      ux = costh*uxi - sinth*uyi;
                                                  %当 angle=0 时,
56.
                      uy = sinth*uxi + costh*uyi; %静磁场对速度没偏转
57.
58.
                      %? 抑制初始场的波动(Birdsall and Langdon[1985])
59.
60.
                     g = prm.cv /sqrt(prm.cs + ux*ux + uy*uy + uz*uz);
61.
                      obj.vx(i) = ux*g;
62.
                      obj.vy(i) = uy*g;
63.
                      obj.vz(i) = uz*g;
64.
                  end
65.
              end
66.
           end
       end
67.
68. end
```

#### %5 position.m

```
1. function particle = position(particle,prm)
2. % Update the position in one step
3.
4. slx = prm.slx
5. p = particle
6.
7. %更新半个时间步的位置,\Delta t时间内需调用 2 次(注: 一个时间步为 2)
x^{t+\Delta t/2} = x^t + v_x^{t+\Delta t/2} \frac{\Delta t}{2}
8. % x^{t+\Delta t/2} = x^t + v_x^{t+\Delta t/2} \frac{\Delta t}{2}
10. p.x = p.x + p.vx
11.
12. % 周期性边界条件:保证粒子在网格内 Periodic BC
13. p.x = p.x + slx.*(p.x<0.0) - slx.*(p.x>=slx)
14. end
```

## %6 charge.m

```
    function charge(particle,field,prm)
    % Calculate the charge on the grid from particles
    p = particle; % reference to the particle obj
    Field.rho = zeros(prm.nxp2,1);
```

```
7. field.rho = prm.rho0; % w_{pi} = \sqrt{\frac{n_i q_i^2}{m_i}} -> \rho_i = \frac{w_{pi}^2}{q_i/m_i}
8.
9. n2 = 0;
10. for k=1:prm.ns
      n1 = n2;
11.
       n2 = n1 + prm.np(k);
12.
13.
      for m = (n1+1):n2
14.
          i = floor(p.x(m) + 2.0);
                                                  %每个粒子所在的网格点坐标
                                                  %每个粒子坐标的下一个网格点坐标
15.
          i1 = i + 1;
16.
          s2 = (p.x(m) + 2.0 - i)*prm.q(k);
                                                  %分到右侧网格点的电荷密度
17.
          s1 = prm.q(k) - s2;
                                                  %分配到左侧网格点的电荷量
               Territory of Grid i |Territory of Grid i+1|
                                    \Delta x
                                   \frac{\Delta x}{2}
                     X_i
                                    X_{i+1}
                                  a
                                       b = X_{i+1} - x_p
18.
          field.rho(i ) = field.rho(i ) + s1; %累加分配到左侧网格的电荷量
19.
          field.rho(i1) = field.rho(i1) + s2; %累加分配到右侧网格的电荷量
20.
          %? 这里分配的电荷密度是否归一化 % w_{pi}=\sqrt{\frac{n_iq_i^2}{m_i}} -> q_i^2=\frac{w_{pi}^2m_i}{n_i}
21.
22.
23. end
24. end
25.
26. %电荷密度边界条件
27. field.rho(2) = field.rho(2) + field.rho(prm.nxp2) - prm.rho0(2);%?
28. field.rho(1) = field.rho(prm.nxp1);
29. field.rho(prm.nxp2) = field.rho(2);
30.
31.
32. end
```

# %7 poisson.m

function poisson(field, prm)
 % Calculate Ex from Poisson equation
 f = field; % reference to the Field obj

```
%泊松方程 \frac{\partial E_x}{\partial x} = \rho
         %差分形式 E_{x,i+1/2} - E_{x,i-1/2} = \rho_i
         %这里定义真空介电常数等于1
         %\varepsilon_0\mu_0 = \frac{1}{c^2}, \ \varepsilon_0 = 1, \mu_0 = \frac{1}{c^2}
         f.ex(prm.X2) = f.ex(prm.X2-1) + f.rho(prm.X2);
10.
11.
        ex0 = sum(f.ex(prm.X2))/prm.nx
                                                    %所有网格点的平均电场强度
12.
         f.ex(prm.X2) = f.ex(prm.X2) - ex0; %? ? ?
13.
         f.ex(1) = f.ex(prm.nxp1);
                                                     %对称边界条件 nxp1=nx+1
14.
15.
         f.ex(prm.nxp2) = f.ex(2);
                                                   %对称边界条件 nxp2=nx+2
16. end
```

## %8 rvelocity.m

```
    function rvelocity(particle, field, prm)
```

- 2. % Update velocity in one step
- 4. % References to class obj
- 5. p = particle;
- 6. f = field;
- 7.
- 8. nxp1 = prm.nxp1; nxp2 = prm.nxp2; ns = prm.ns; np = prm.np;
- 9. qm = prm.qm;
- 10. bx0 = prm.bx0; %bx0=prm.wc/prm.qm(1)\*cos(theta);
- 11. cs = prm.cs;
- 12. X1 = prm.X1; X2 = prm.X2; X3 = prm.X3; %X2=2:(prm.nx+1);X3=3:(prm.nx+2)
- 14. %\*\*\*\*\*\*通过 Boris 方法更新粒子速度\*\*\*\*\*\*
- 15. %牛顿第二定律  $\frac{d oldsymbol{v}}{dt} = \frac{q_s}{m_s} (oldsymbol{E} + oldsymbol{v} imes oldsymbol{B})$

16.%差分形式 
$$\frac{\boldsymbol{v}^{t+\Delta t/2} - \boldsymbol{v}^{t-\Delta t/2}}{\Delta t} = \frac{q_s}{m_s} (\boldsymbol{E}^t + \frac{\boldsymbol{v}^{t+\Delta t/2} + \boldsymbol{v}^{t-\Delta/2}}{2} \times \boldsymbol{B}^t)$$

$$oldsymbol{v}^- = oldsymbol{v}^{t-\Delta t/2} + rac{q_s}{m_s} oldsymbol{E}^t rac{\Delta t}{2}$$

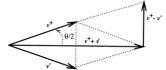
17. %定义

$$oldsymbol{v}^+ = oldsymbol{v}^{t+\Delta t/2} - rac{q_s}{m_s} oldsymbol{E}^t rac{\Delta t}{2}$$

19. %将
$$v^+$$
和 $v^-$ 代入差分形式得  $\dfrac{m{v}^+-m{v}^-}{\Delta t}=\dfrac{1}{2}\dfrac{q_s}{m_s}(m{v}^++m{v}^-) imesm{B}^t$ 

$$({m v}^+)^2 = ({m v}^-)^2$$

20. %两边同乘以 $(v^+ - v^-)$ 得  $(oldsymbol{v}^+)^2 = (oldsymbol{v}^-)^2$ 



21. %Boris 方法矢量关系图

$$\theta = -2tan^{-1}(\frac{\Delta t}{2}\frac{q_s}{m_s}B^t)$$

22. %由矢量可以求得夹角 $\theta$ ,即

$$\mathbf{v}^{-} = \mathbf{v}^{t-\Delta t/2} + (q/m)_{s} \mathbf{E}^{t} \frac{\Delta t}{2}$$

$$\mathbf{v}^{o} = \mathbf{v}^{-} + \mathbf{v}^{-} \times (q/m)_{s} \mathbf{B}^{t} \frac{\Delta t}{2}$$

$$\mathbf{v}^{+} = \mathbf{v}^{-} + \frac{2}{1 + ((q/m)_{s} B^{t} \Delta t/2)^{2}} \mathbf{v}^{o} \times \mathbf{B}^{t} \frac{\Delta t}{2}$$

$$\mathbf{v}^{t+\Delta t/2} = \mathbf{v}^{+} + (q/m)_{s} \mathbf{E}^{t} \frac{\Delta t}{2}$$

```
23. work1 = zeros(nxp2,1);
24. work2 = zeros(nxp2,1);
25. work1(X2) = 0.5*(f.ex(X1) + f.ex(X2));
26. work1(nxp2)= work1(2);
27. work2(X2) = 0.5*(f.by(X3) + f.by(X2));
28. work2(1) = work2(nxp1);
29.
30. %----
31. n2 = 0;
32. for k=1:ns
      n1 = n2;
33.
      n2 = n2 + np(k);
35.
36.
      for m=(n1+1):n2
         i = floor(p.x(m) + 2.0);
37.
         sf2 = (p.x(m) + 2.0 - i)*qm(k);
38.
39.
         sf1 = qm(k) - sf2;
40.
         ih = floor(p.x(m) + 1.5);
41.
42.
         sh2 = (p.x(m) + 1.5 - ih)*qm(k);
         sh1 = qm(k) - sh2;
43.
44.
         i1 = i + 1;
45.
         ih1 = ih + 1;
46.
47.
         ex1 = sf1*work1(i) + sf2*work1(i1);
48.
         ey1 = sf1*f.ey(i) + sf2*f.ey(i1);
49.
         ez1 = sh1*f.ez(ih) + sh2*f.ez(ih1);
50.
```

```
51.
52.
         bx1 = bx0*prm.qm(k);
         by1 = sh1*work2(ih) + sh2*work2(ih1);
53.
         bz1 = sh1*f.bz(ih) + sh2*f.bz(ih1);
54.
55.
56.
         g = prm.cv / sqrt(cs - p.vx(m)^2 - p.vy(m)^2 - p.vz(m)^2);
57.
58.
         ux = p.vx(m)*g + ex1;%?
59.
         uy = p.vy(m)*g + ey1;
60.
         uz = p.vz(m)*g + ez1;
61.
62.
          g = prm.cv/sqrt(cs + ux*ux + uy*uy + uz*uz);
63.
         bx1 = bx1*g;
64.
65.
         by1 = by1*g;
66.
         bz1 = bz1*g;
67.
68.
         boris = 2.0/(1+ bx1*bx1 + by1*by1 + bz1*bz1);
69.
70.
         uxt = ux + uy*bz1 - uz*by1;
         uyt = uy + uz*bx1 - ux*bz1;
71.
72.
         uzt = uz + ux*by1 - uy*bx1;
73.
74.
         ux = ux + boris*(uyt*bz1 - uzt*by1) + ex1;
         uy = uy + boris*(uzt*bx1 - uxt*bz1) + ey1;
75.
76.
         uz = uz + boris*(uxt*by1 - uyt*bx1) + ez1;
77.
78.
         g = prm.cv / sqrt(cs + ux*ux + uy*uy + uz*uz);
79.
80.
         % this is causing speed issue. Why?
81.
         p.vx(m) = ux*g;
82.
         p.vy(m) = uy*g;
83.
         p.vz(m) = uz*g;
84.
      end
85. end
86.
87. end
```

#### %9 bfield.m

```
    function [field] = bfield(field,prm)
    % Update magnetic field in one step
    X2 = prm.X2; %2:129
    f = field; % reference to Field obj
```

```
5.
                % \frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}, 标量形式如下: \nabla \times \mathbf{E} = \left(\frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z}\right)\mathbf{i} + \left(\frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x}\right)\mathbf{j} + \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y}\right)\mathbf{k}
                \frac{\partial B_y}{\partial t} = \frac{\partial E_z}{\partial x}
                \frac{\partial B_z}{\partial t} = -\frac{\partial E_y}{\partial x}
9.
                 f.by(X2) = f.by(X2) + f.ez(X2) - f.ez(X2-1);
                 f.bz(X2) = f.bz(X2) - f.ey(X2+1) + f.ey(X2); %?
10.
11.
12.
                 f.by(prm.nxp2)= f.by(2);%对称边界条件
                 f.bz(prm.nxp2) = f.bz(2);
13.
14.
                 f.by(1) = f.by(prm.nxp1);
                 f.bz(1) = f.bz(prm.nxp1);
15.
16. end
```

## %10 current.m

```
    function current(particle, field, jtime, prm)

2. % Calculate the current in one step
3.
4. nx = prm.nx; nxp1 = prm.nxp1; nxp2 = prm.nxp2;
5. X2 = prm.X2;
6. np = prm.np; ns = prm.ns;
7. q = prm.q;
8.
9. % references to class obj
10. f = field;
11. p = particle;
12.
13. f.ajx = zeros(nxp2,1);
14. f.ajy = zeros(nxp2,1);
15. f.ajz = zeros(nxp2,1);
16.
17. %----
18. n2 = 0;
19. for k=1:ns
20. n1 = n2;
21. n2 = n2 + np(k);
22. qh = q(k)*0.5;
23.
24.
     for m=(n1+1):n2
25.
        ih = floor(p.x(m) + 1.5);
        s2 = (p.x(m) + 1.5 - ih)*q(k);
26.
```

```
27.
           s1 = q(k) - s2;
28.
           ih1= ih+1;
           %jy和 jz 按线性比重分配到相邻网格点
29.
           f.ajy(ih) = f.ajy(ih) + p.vy(m)*s1;
30.
31.
           f.ajy(ih1) = f.ajy(ih1) + p.vy(m)*s2;
32.
           f.ajz(ih) = f.ajz(ih) + p.vz(m)*s1;
           f.ajz(ih1) = f.ajz(ih1) + p.vz(m)*s2;
33.
34.
35.
           %--Jx 采用电荷守恒方法-
             \frac{\partial \rho}{\partial t} + \nabla \cdot \boldsymbol{J} = 0
          \% \frac{\dot{\partial t}}{\partial t}
36.
            \rho_i^{t+\Delta t} - \rho_i^t = -(J_{i+1/2}^{t+\Delta t/2} - J_{i-1/2}^{t+\Delta t/2}) \frac{\Delta t}{\Delta x}
37.
38.
           if prm.iex
39.
              qhs = qh * sign(p.vx(m));
40.
              avx = abs(p.vx(m));
41.
42.
              x1 = p.x(m) + 2.0 - avx;
              x2 = p.x(m) + 2.0 + avx;
43.
44.
              i1 = floor(x1);
              i2 = floor(x2);
45.
46.
47.
              % This is causing me speed issue
48.
              f.ajx(i1) = f.ajx(i1) + (i2 - x1)*qhs;
49.
              f.ajx(i2) = f.ajx(i2) + (x2 - i2)*qhs;
           end
50.
51.
       end
52. end
53.
54. %-- boundary --
55. f.ajx(nxp1) = f.ajx(1) + f.ajx(nxp1);
56. f.ajx(2) = f.ajx(2) + f.ajx(nxp2);
57.
58. f.ajy(nxp1) = f.ajy(1) + f.ajy(nxp1);
59. f.ajy(2) = f.ajy(2) + f.ajy(nxp2);
60. f.ajy(1)
               = f.ajy(nxp1);
61.
62. f.ajz(nxp1) = f.ajz(1) + f.ajz(nxp1);
63. f.ajz(2) = f.ajz(2) + f.ajz(nxp2);
64.
65. %--
66. f.ajy(X2) = 0.5*(f.ajy(X2) + f.ajy(X2-1));
67.
68. %-- external current source ----
```

```
69. if prm.ajamp
      f.ajz(nx/2+1) = f.ajz(nx/2+1) + prm.ajamp*sin(prm.wj*jtime);
71. else
72.
      %--cancellation of uniform Jx,Jy,Jz components---
73. ajxu = sum(f.ajx(X2))/nx;
74.
      ajyu = sum(f.ajy(X2))/nx;
75. ajzu = sum(f.ajz(X2))/nx;
76.
     f.ajx(X2) = f.ajx(X2) - ajxu;
77. f.ajy(X2) = f.ajy(X2) - ajyu;
      f.ajz(X2) = f.ajz(X2) - ajzu;
78.
79. end
80.
81. end
```

## %11 efield.m

```
    function [field] = efield(field,prm)

2. % Update the electric field in one step
3.
4.
5. nxp1 = prm.nxp1; nxp2 = prm.nxp2;
6. tcs = prm.tcs;
                                              %2*obj.cs;
7. X1 = prm.X1; X2 = prm.X2; X3 = prm.X3;
9. f = field; % reference to class obj
10.
         \label{eq:epsilon} \% \; \frac{\partial E}{\partial t} = c^2 \nabla \times B - J \qquad \% \varepsilon_0 \mu_0 = \frac{1}{c^2}, \; \varepsilon_0 = \mathbf{1} \text{,} \mu_0 = \frac{1}{c^2}
11.
12. %\frac{\partial E_x}{\partial t} = -J_x,标量形式如下
13.  \% \frac{\partial E_x}{\partial t} = -J_x 
15. \% \frac{\partial E_z}{\partial t} = c^2 \frac{\partial B_y}{\partial x} - J_z
16.
17. if prm.iex == 0 %iex==0:没有电场
18.
         f.ex(:) = 0;
19. else
20. f.ex(X2) = f.ex(X2) - 2*f.ajx(X2);
21.
         f.ex(1) = f.ex(nxp1);
22. f.ex(nxp2) = f.ex(2);
23. end
24.
```

```
25. f.ey(X2) = f.ey(X2) - tcs*(f.bz(X2) - f.bz(X1)) - 2*f.ajy(X2);

26. f.ez(X2) = f.ez(X2) + tcs*(f.by(X3) - f.by(X2)) - 2*f.ajz(X2);

27.

28. f.ey(1) = f.ey(nxp1);

29. f.ez(1) = f.ez(nxp1);

30. f.ey(nxp2) = f.ey(2);

31. f.ez(nxp2) = f.ez(2);

32.

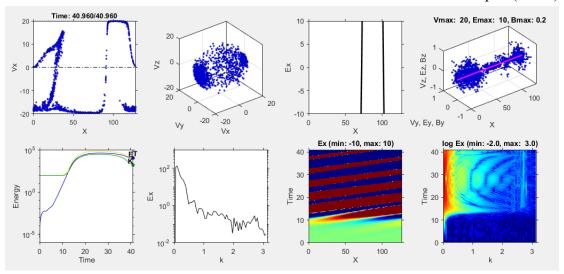
33. end
```

## %12 Inputs and Outputs

## %12.1 Inputs

```
1. dx = 1.000000;
2. dt = 0.040000;
3. nx = 128.000000;
4. ntime = 1024.000000;
5. cv = 20.000000;
6. wc = 0.000000;
7. angle = 0.000000;
8.
9. ns = 1.000000;
10. np = [2048.000000, ];
11. wp = [1.000000, ];
12. qm = [-1.000000, ];
13. vpa = [0.500000, ];
14. vpe = [10.000000, ];
15. vd = [0.000000, ];
16. pch = [0.000000, ];
17.
18. iex = 2;
19.
20. ajamp = 0.000000;
21. wj = 0.000000;
22.
23. nplot = 256.000000;
24. \text{ nv} = 100.000000;
25. icolor = 1.000000;
26. iparam = 1.000000;
27. \text{ vmax} = 20.000000;
28. \text{ emax} = 10.000000;
29. bmax = 0.200000;
30. diagtype = [11.000000, 23.000000, 18.000000, 4.000000, ];
```

%12.2 Outputs(iex=2)



# %12.3 Outputs(iex=1)

