

Reference Points with FLBRP, Summer School in Quantative Fisheries Stock Assessment, Capo Granitola

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July 13th, 2017

```
# load the library
library(FLBRP)

## Loading required package: FLCore
## Loading required package: MASS
## Loading required package: lattice
## FLCore (Version 2.6.3, packaged: 2017-07-05 12:26:15 UTC)
## Loading required package: FLaash
## Loading required package: ggplotFL
## Loading required package: ggplot2
##
## Attaching package: 'ggplot2'
## The following object is masked from 'package:FLCore':
##
##      %+%
##
## Warning: replacing previous import 'ggplot2::%+%' by 'FLCore::%+%' when
## loading 'ggplotFL'
# Load the example FLStock object from FLCore
# we are going to use one of the stock objects from the HKE_09_10_11 stock assessment
load("HKEFbar0_3.RData")
hke<-HKE.new_xsa

# Create the corresponding FLBRP object
hkebrp <- FLBRP(hke)

summary(hkebrp)

## An object of class "FLBRP"
##
## Name:
## Description:
## Quant: age
## Dims: age      year      unit      season area      iter
## 7      101 1      1      1      1
##
## Range: min      max      pgroup      minfbar maxfbar
## 0      6      6      0      3
##
## fbar      : [ 1 101 1 1 1 1 ], units = f
## fbar.obs   : [ 1 9 1 1 1 1 ], units = f
```

```
## landings.obs : [ 1 9 1 1 1 1 ], units = t
## discards.obs : [ 1 9 1 1 1 1 ], units = NA
## rec.obs      : [ 1 9 1 1 1 1 ], units = NA
## ssb.obs      : [ 1 9 1 1 1 1 ], units = kg
## stock.obs    : [ 1 9 1 1 1 1 ], units = kg
## profit.obs   : [ 1 9 1 1 1 1 ], units = NA
## landings.sel : [ 7 1 1 1 1 1 ], units = f
## discards.sel : [ 7 1 1 1 1 1 ], units = f
## bycatch.harv : [ 7 1 1 1 1 1 ], units = f
## stock.wt     : [ 7 1 1 1 1 1 ], units = kg
## landings.wt  : [ 7 1 1 1 1 1 ], units = NA
## discards.wt  : [ 7 1 1 1 1 1 ], units = NA
## bycatch.wt   : [ 7 1 1 1 1 1 ], units = NA
## m            : [ 7 1 1 1 1 1 ], units = NA
## mat          : [ 7 1 1 1 1 1 ], units = NA
## harvest.spwn : [ 7 1 1 1 1 1 ], units = NA
## m.spwn       : [ 7 1 1 1 1 1 ], units = NA
## availability : [ 7 1 1 1 1 1 ], units = NA
## price        : [ 7 1 1 1 1 1 ], units = NA
## vcost        : [ 1 1 1 1 1 1 ], units = NA
## fcost        : [ 1 1 1 1 1 1 ], units = NA
```

The FLBRP class has information on:

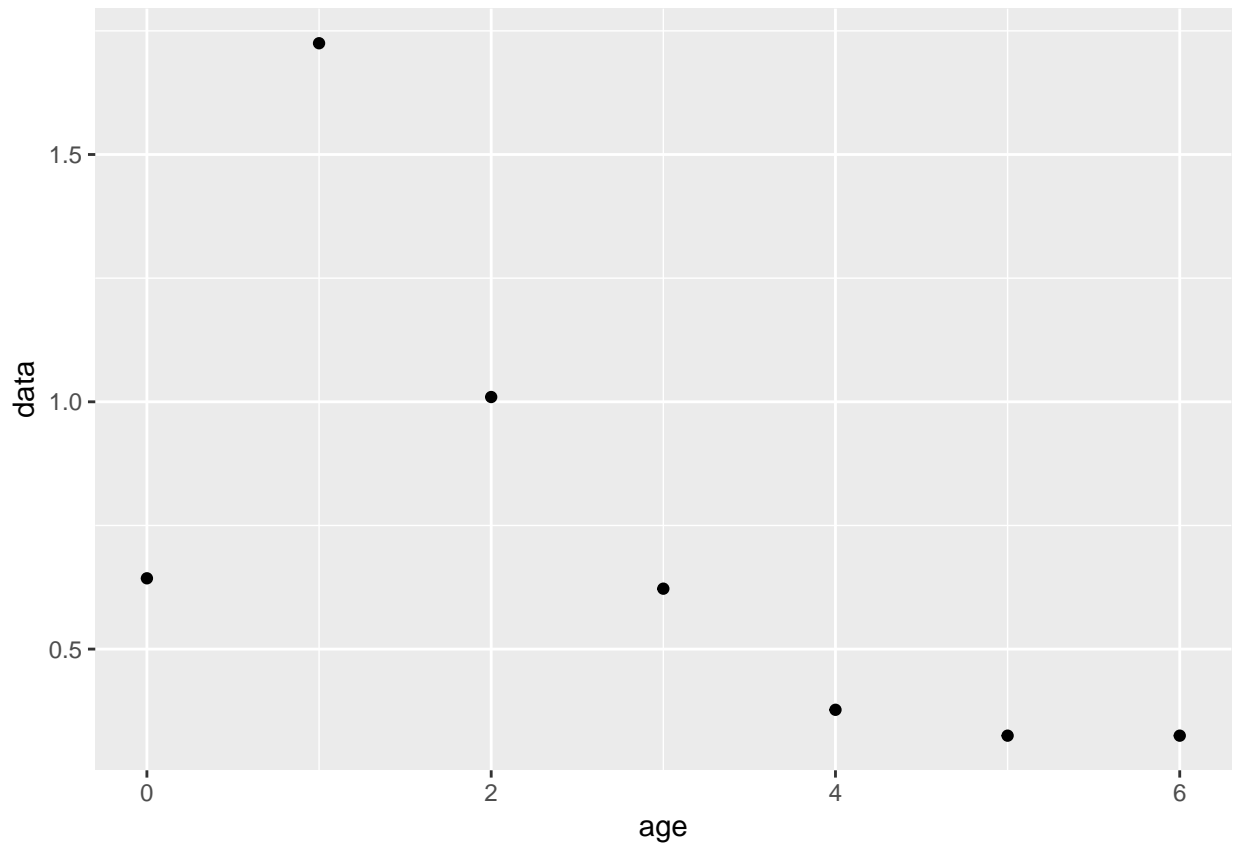
selection Patterns

```
catch.sel(hkebrp)
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##   year
## age 1
##   0 0.64312
##   1 1.72500
##   2 1.00969
##   3 0.62219
##   4 0.37727
##   5 0.32497
##   6 0.32497
##
## units: f
```

discards.sel(hkebrp)

```
ggplot(catch.sel(hkebrp), aes( age, data))+geom_point()
```



```
# ggplot(discards.sel(hkebrp), aes( age, data))+geom_point()
```

```
# mass-at-age
stock.wt(hkebrp)
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##   year
## age 1
##   0 0.010913
##   1 0.147273
##   2 0.504652
##   3 1.145925
##   4 1.871101
##   5 2.691069
##   6 4.024266
##
## units:  kg
```

```
catch.wt(hkebrp)
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##   year
```

```

## age 1
##   0 0.010913
##   1 0.147273
##   2 0.504652
##   3 1.145925
##   4 1.871101
##   5 2.691069
##   6 4.024266
##
## units:  NA

# discards.wt(hkebrp)

# biological parameters
m(hkebrp)

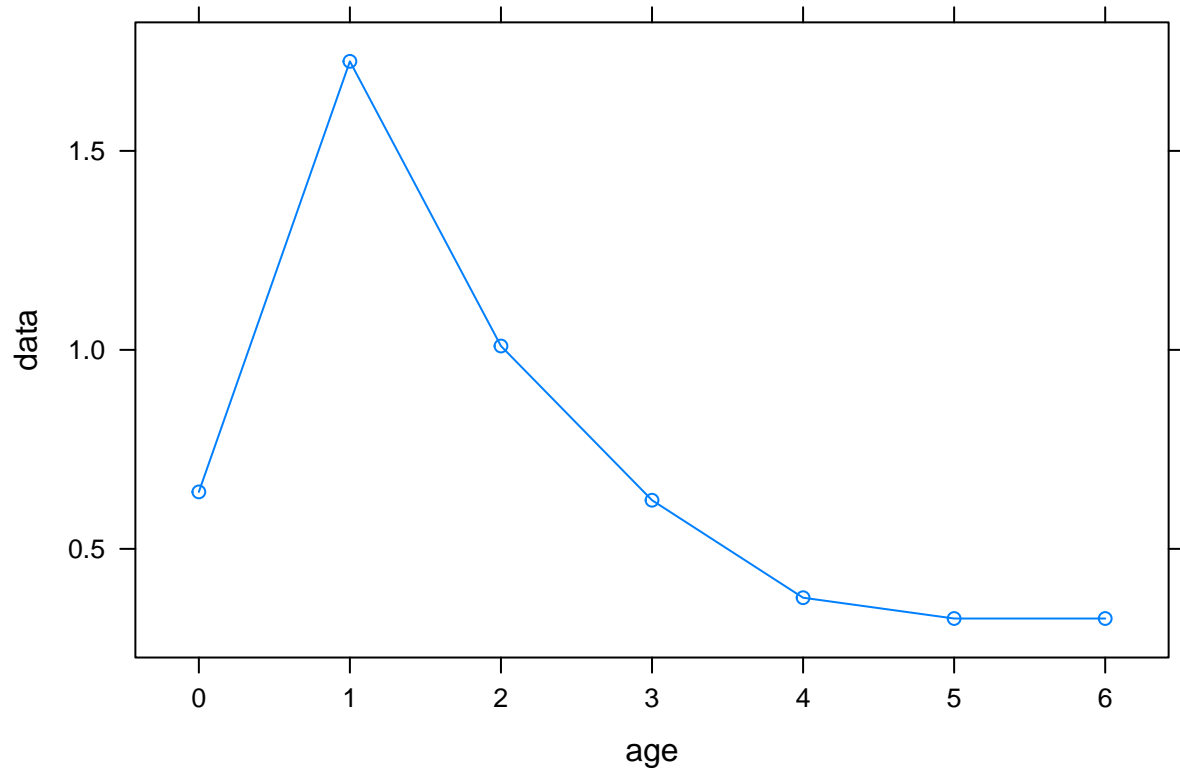
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##   year
## age 1
##   0 1.18108
##   1 0.57816
##   2 0.42077
##   3 0.36116
##   4 0.32880
##   5 0.31803
##   6 0.29796
##
## units:  NA

mat(hkebrp)

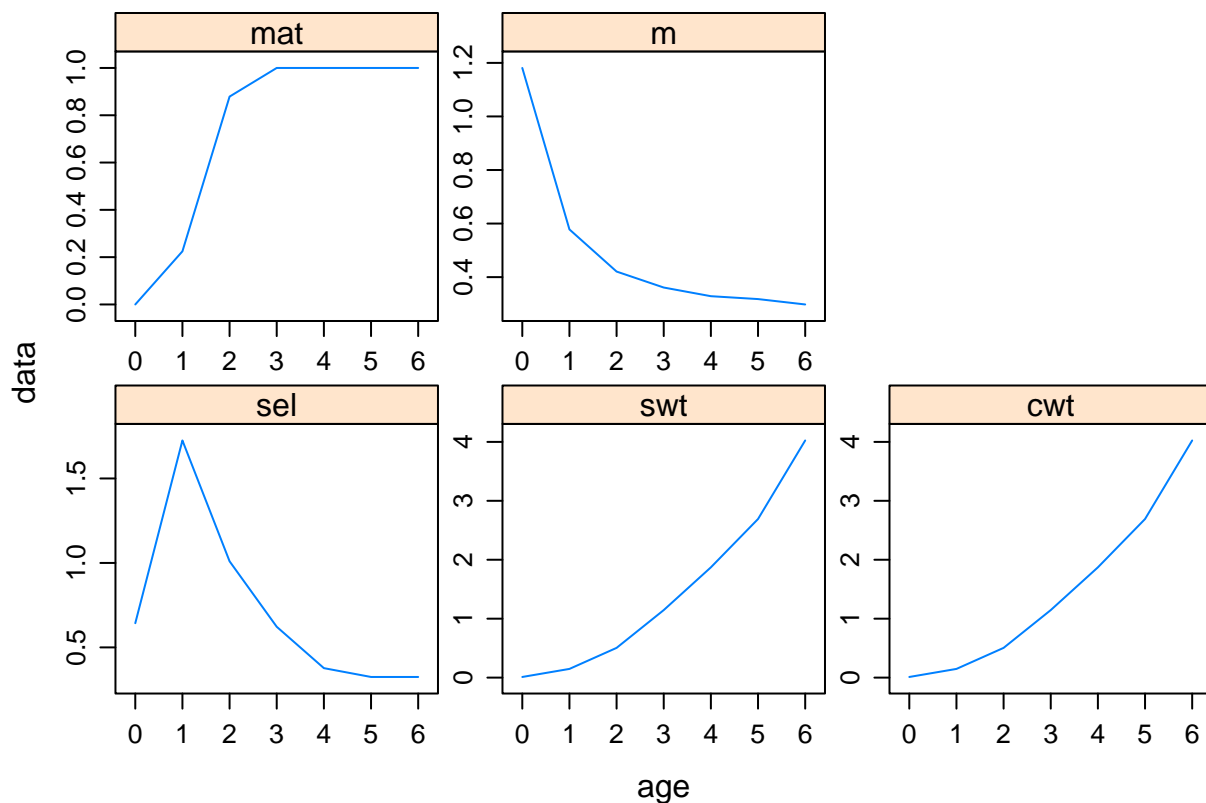
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##   year
## age 1
##   0 0.00000
##   1 0.22468
##   2 0.87888
##   3 1.00000
##   4 1.00000
##   5 1.00000
##   6 1.00000
##
## units:  NA

# selectivity
xyplot(data~age,data=catch.sel(hkebrp),type=c('l', 'p'))

```



```
# and other quantities by age
xyplot(data~age|qname, data=FLQuants(sel=catch.sel(hkebrp),
                                       swt=stock.wt(hkebrp),
                                       cwt =catch.wt(hkebrp), mat= mat(hkebrp), m = m(hkebrp)),
       type="l",scale="free")
```



```
# we have not provided a SR relationship yet
# so analyses will be per-recruit
```

```
# All *.obs slots hold the observations from FLStock
fbar.obs(hkebrp)
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##      year
## age  2006      2007      2008      2009      2010      2011      2012      2013
##   all 1.32180 1.16916 1.10318 1.04618 1.05383 1.24175 0.99996 0.91843
##      year
## age  2014
##   all 1.16887
##
## units:  f
```

```
# Once an FLBRP object has been created then equilibrium
# quantities can be estimated
```

```
# we estimate equilibrium quantities
hkebrp <- brp(hkebrp)
```

```
# and a set of equilibrium quantities for a range of F values
```

```
# fishing mortality
fbar(hkebrp)
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##      year
## age  1   2   3   4   5   6   7   8   9  10  11  12  13
## all 0.00 0.04 0.08 0.12 0.16 0.20 0.24 0.28 0.32 0.36 0.40 0.44 0.48
##      year
## age 14  15  16  17  18  19  20  21  22  23  24  25  26
## all 0.52 0.56 0.60 0.64 0.68 0.72 0.76 0.80 0.84 0.88 0.92 0.96 1.00
##      year
## age 27  28  29  30  31  32  33  34  35  36  37  38  39
## all 1.04 1.08 1.12 1.16 1.20 1.24 1.28 1.32 1.36 1.40 1.44 1.48 1.52
##      year
## age 40  41  42  43  44  45  46  47  48  49  50  51  52
## all 1.56 1.60 1.64 1.68 1.72 1.76 1.80 1.84 1.88 1.92 1.96 2.00 2.04
##      year
## age 53  54  55  56  57  58  59  60  61  62  63  64  65
## all 2.08 2.12 2.16 2.20 2.24 2.28 2.32 2.36 2.40 2.44 2.48 2.52 2.56
##      year
## age 66  67  68  69  70  71  72  73  74  75  76  77  78
## all 2.60 2.64 2.68 2.72 2.76 2.80 2.84 2.88 2.92 2.96 3.00 3.04 3.08
##      year
## age 79  80  81  82  83  84  85  86  87  88  89  90  91
## all 3.12 3.16 3.20 3.24 3.28 3.32 3.36 3.40 3.44 3.48 3.52 3.56 3.60
##      year
## age 92  93  94  95  96  97  98  99  100 101
## all 3.64 3.68 3.72 3.76 3.80 3.84 3.88 3.92 3.96 4.00
##
## units:  f
```

```
harvest(hkebrp)
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##      year
## age 1           2           3           4           5           6           7
## 0 0.000000 0.025725 0.051450 0.077175 0.102900 0.128625 0.154350
## 1 0.000000 0.069000 0.138000 0.207000 0.276000 0.345000 0.413999
## 2 0.000000 0.040388 0.080775 0.121163 0.161550 0.201938 0.242325
## 3 0.000000 0.024888 0.049775 0.074663 0.099550 0.124438 0.149326
## 4 0.000000 0.015091 0.030181 0.045272 0.060363 0.075453 0.090544
## 5 0.000000 0.012999 0.025998 0.038997 0.051996 0.064995 0.077994
## 6 0.000000 0.012999 0.025998 0.038997 0.051996 0.064995 0.077994
##      year
## age 8           9           10          11          12          13          14
## 0 0.180074 0.205799 0.231524 0.257249 0.282974 0.308699 0.334424
## 1 0.482999 0.551999 0.620999 0.689999 0.758999 0.827999 0.896999
## 2 0.282713 0.323100 0.363488 0.403875 0.444263 0.484651 0.525038
## 3 0.174213 0.199101 0.223989 0.248876 0.273764 0.298651 0.323539
## 4 0.105635 0.120725 0.135816 0.150907 0.165997 0.181088 0.196178
```

```

## 5 0.090993 0.103992 0.116990 0.129989 0.142988 0.155987 0.168986
## 6 0.090993 0.103992 0.116990 0.129989 0.142988 0.155987 0.168986
## year
## age 15 16 17 18 19 20 21
## 0 0.360149 0.385874 0.411599 0.437324 0.463049 0.488774 0.514498
## 1 0.965999 1.034999 1.103999 1.172999 1.241998 1.310998 1.379998
## 2 0.565426 0.605813 0.646201 0.686588 0.726976 0.767363 0.807751
## 3 0.348427 0.373314 0.398202 0.423089 0.447977 0.472865 0.497752
## 4 0.211269 0.226360 0.241450 0.256541 0.271632 0.286722 0.301813
## 5 0.181985 0.194984 0.207983 0.220982 0.233981 0.246980 0.259979
## 6 0.181985 0.194984 0.207983 0.220982 0.233981 0.246980 0.259979
## year
## age 22 23 24 25 26 27 28
## 0 0.540223 0.565948 0.591673 0.617398 0.643123 0.668848 0.694573
## 1 1.448998 1.517998 1.586998 1.655998 1.724998 1.793998 1.862998
## 2 0.848138 0.888526 0.928914 0.969301 1.009689 1.050076 1.090464
## 3 0.522640 0.547528 0.572415 0.597303 0.622190 0.647078 0.671966
## 4 0.316904 0.331994 0.347085 0.362176 0.377266 0.392357 0.407448
## 5 0.272978 0.285977 0.298976 0.311975 0.324974 0.337972 0.350971
## 6 0.272978 0.285977 0.298976 0.311975 0.324974 0.337972 0.350971
## year
## age 29 30 31 32 33 34 35
## 0 0.720298 0.746023 0.771748 0.797473 0.823198 0.848923 0.874647
## 1 1.931998 2.000997 2.069997 2.138997 2.207997 2.276997 2.345997
## 2 1.130851 1.171239 1.211626 1.252014 1.292401 1.332789 1.373177
## 3 0.696853 0.721741 0.746629 0.771516 0.796404 0.821291 0.846179
## 4 0.422538 0.437629 0.452720 0.467810 0.482901 0.497992 0.513082
## 5 0.363970 0.376969 0.389968 0.402967 0.415966 0.428965 0.441964
## 6 0.363970 0.376969 0.389968 0.402967 0.415966 0.428965 0.441964
## year
## age 36 37 38 39 40 41 42
## 0 0.900372 0.926097 0.951822 0.977547 1.003272 1.028997 1.054722
## 1 2.414997 2.483997 2.552997 2.621997 2.690997 2.759997 2.828996
## 2 1.413564 1.453952 1.494339 1.534727 1.575114 1.615502 1.655889
## 3 0.871067 0.895954 0.920842 0.945729 0.970617 0.995505 1.020392
## 4 0.528173 0.543264 0.558354 0.573445 0.588535 0.603626 0.618717
## 5 0.454963 0.467962 0.480961 0.493960 0.506959 0.519958 0.532957
## 6 0.454963 0.467962 0.480961 0.493960 0.506959 0.519958 0.532957
## year
## age 43 44 45 46 47 48 49
## 0 1.080447 1.106172 1.131897 1.157622 1.183347 1.209071 1.234796
## 1 2.897996 2.966996 3.035996 3.104996 3.173996 3.242996 3.311996
## 2 1.696277 1.736664 1.777052 1.817440 1.857827 1.898215 1.938602
## 3 1.045280 1.070168 1.095055 1.119943 1.144830 1.169718 1.194606
## 4 0.633807 0.648898 0.663989 0.679079 0.694170 0.709261 0.724351
## 5 0.545956 0.558955 0.571953 0.584952 0.597951 0.610950 0.623949
## 6 0.545956 0.558955 0.571953 0.584952 0.597951 0.610950 0.623949
## year
## age 50 51 52 53 54 55 56
## 0 1.260521 1.286246 1.311971 1.337696 1.363421 1.389146 1.414871
## 1 3.380996 3.449996 3.518996 3.587995 3.656995 3.725995 3.794995
## 2 1.978990 2.019377 2.059765 2.100152 2.140540 2.180927 2.221315
## 3 1.219493 1.244381 1.269268 1.294156 1.319044 1.343931 1.368819
## 4 0.739442 0.754533 0.769623 0.784714 0.799805 0.814895 0.829986

```



```

## 5 0.636948 0.649947 0.662946 0.675945 0.688944 0.701943 0.714942
## 6 0.636948 0.649947 0.662946 0.675945 0.688944 0.701943 0.714942
## year
## age 57      58      59      60      61      62      63
## 0 1.440596 1.466321 1.492046 1.517771 1.543495 1.569220 1.594945
## 1 3.863995 3.932995 4.001995 4.070995 4.139995 4.208995 4.277995
## 2 2.261703 2.302090 2.342478 2.382865 2.423253 2.463640 2.504028
## 3 1.393707 1.418594 1.443482 1.468369 1.493257 1.518145 1.543032
## 4 0.845077 0.860167 0.875258 0.890349 0.905439 0.920530 0.935621
## 5 0.727941 0.740940 0.753939 0.766938 0.779937 0.792935 0.805934
## 6 0.727941 0.740940 0.753939 0.766938 0.779937 0.792935 0.805934
## year
## age 64      65      66      67      68      69      70
## 0 1.620670 1.646395 1.672120 1.697845 1.723570 1.749295 1.775020
## 1 4.346994 4.415994 4.484994 4.553994 4.622994 4.691994 4.760994
## 2 2.544415 2.584803 2.625190 2.665578 2.705966 2.746353 2.786741
## 3 1.567920 1.592808 1.617695 1.642583 1.667470 1.692358 1.717246
## 4 0.950711 0.965802 0.980892 0.995983 1.011074 1.026164 1.041255
## 5 0.818933 0.831932 0.844931 0.857930 0.870929 0.883928 0.896927
## 6 0.818933 0.831932 0.844931 0.857930 0.870929 0.883928 0.896927
## year
## age 71      72      73      74      75      76      77
## 0 1.800745 1.826470 1.852195 1.877920 1.903644 1.929369 1.955094
## 1 4.829994 4.898994 4.967994 5.036994 5.105994 5.174993 5.243993
## 2 2.827128 2.867516 2.907903 2.948291 2.988678 3.029066 3.069453
## 3 1.742133 1.767021 1.791908 1.816796 1.841684 1.866571 1.891459
## 4 1.056346 1.071436 1.086527 1.101618 1.116708 1.131799 1.146890
## 5 0.909926 0.922925 0.935924 0.948923 0.961922 0.974921 0.987920
## 6 0.909926 0.922925 0.935924 0.948923 0.961922 0.974921 0.987920
## year
## age 78      79      80      81      82      83      84
## 0 1.980819 2.006544 2.032269 2.057994 2.083719 2.109444 2.135169
## 1 5.312993 5.381993 5.450993 5.519993 5.588993 5.657993 5.726993
## 2 3.109841 3.150229 3.190616 3.231004 3.271391 3.311779 3.352166
## 3 1.916347 1.941234 1.966122 1.991009 2.015897 2.040785 2.065672
## 4 1.161980 1.177071 1.192162 1.207252 1.222343 1.237434 1.252524
## 5 1.000919 1.013917 1.026916 1.039915 1.052914 1.065913 1.078912
## 6 1.000919 1.013917 1.026916 1.039915 1.052914 1.065913 1.078912
## year
## age 85      86      87      88      89      90      91
## 0 2.160894 2.186619 2.212344 2.238068 2.263793 2.289518 2.315243
## 1 5.795993 5.864993 5.933992 6.002992 6.071992 6.140992 6.209992
## 2 3.392554 3.432941 3.473329 3.513716 3.554104 3.594492 3.634879
## 3 2.090560 2.115447 2.140335 2.165223 2.190110 2.214998 2.239886
## 4 1.267615 1.282706 1.297796 1.312887 1.327978 1.343068 1.358159
## 5 1.091911 1.104910 1.117909 1.130908 1.143907 1.156906 1.169905
## 6 1.091911 1.104910 1.117909 1.130908 1.143907 1.156906 1.169905
## year
## age 92      93      94      95      96      97      98
## 0 2.340968 2.366693 2.392418 2.418143 2.443868 2.469593 2.495318
## 1 6.278992 6.347992 6.416992 6.485992 6.554992 6.623992 6.692992
## 2 3.675267 3.715654 3.756042 3.796429 3.836817 3.877204 3.917592
## 3 2.264773 2.289661 2.314548 2.339436 2.364324 2.389211 2.414099
## 4 1.373249 1.388340 1.403431 1.418521 1.433612 1.448703 1.463793

```

```

## 5 1.182904 1.195903 1.208902 1.221901 1.234900 1.247898 1.260897
## 6 1.182904 1.195903 1.208902 1.221901 1.234900 1.247898 1.260897
## year
## age 99      100      101
## 0 2.521043 2.546768 2.572492
## 1 6.761991 6.830991 6.899991
## 2 3.957979 3.998367 4.038755
## 3 2.438986 2.463874 2.488762
## 4 1.478884 1.493975 1.509065
## 5 1.273896 1.286895 1.299894
## 6 1.273896 1.286895 1.299894
##
## units: f
# abundance-at-age
stock.n(hkebrp)

## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
## year
## age 1      2      3      4      5      6
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 3.0695e-01 2.9915e-01 2.9155e-01 2.8415e-01 2.7693e-01 2.6990e-01
## 2 1.7217e-01 1.5661e-01 1.4246e-01 1.2958e-01 1.1787e-01 1.0722e-01
## 3 1.1304e-01 9.8754e-02 8.6273e-02 7.5370e-02 6.5844e-02 5.7523e-02
## 4 7.8774e-02 6.7127e-02 5.7202e-02 4.8744e-02 4.1537e-02 3.5395e-02
## 5 5.6701e-02 4.7593e-02 3.9949e-02 3.3532e-02 2.8146e-02 2.3626e-02
## 6 1.6010e-01 1.2789e-01 1.0234e-01 8.2026e-02 6.5840e-02 5.2920e-02
## year
## age 7      8      9      10     11     12
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 2.6304e-01 2.5636e-01 2.4985e-01 2.4351e-01 2.3732e-01 2.3130e-01
## 2 9.7530e-02 8.8716e-02 8.0698e-02 7.3405e-02 6.6771e-02 6.0736e-02
## 3 5.0253e-02 4.3902e-02 3.8353e-02 3.3506e-02 2.9272e-02 2.5572e-02
## 4 3.0162e-02 2.5702e-02 2.1902e-02 1.8664e-02 1.5904e-02 1.3553e-02
## 5 1.9831e-02 1.6646e-02 1.3972e-02 1.1728e-02 9.8442e-03 8.2630e-03
## 6 4.2589e-02 3.4316e-02 2.7680e-02 2.2351e-02 1.8065e-02 1.4614e-02
## year
## age 13     14     15     16     17     18
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 2.2542e-01 2.1970e-01 2.1412e-01 2.0868e-01 2.0338e-01 1.9821e-01
## 2 5.5247e-02 5.0254e-02 4.5712e-02 4.1581e-02 3.7823e-02 3.4405e-02
## 3 2.2340e-02 1.9517e-02 1.7050e-02 1.4895e-02 1.3013e-02 1.1368e-02
## 4 1.1549e-02 9.8413e-03 8.3862e-03 7.1462e-03 6.0896e-03 5.1892e-03
## 5 6.9358e-03 5.8218e-03 4.8867e-03 4.1018e-03 3.4430e-03 2.8900e-03
## 6 1.1833e-02 9.5882e-03 7.7755e-03 6.3100e-03 5.1242e-03 4.1640e-03
## year
## age 19     20     21     22     23     24
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 1.9318e-01 1.8827e-01 1.8349e-01 1.7883e-01 1.7429e-01 1.6986e-01
## 2 3.1295e-02 2.8467e-02 2.5894e-02 2.3554e-02 2.1425e-02 1.9489e-02
## 3 9.9316e-03 8.6764e-03 7.5799e-03 6.6219e-03 5.7850e-03 5.0539e-03
## 4 4.4220e-03 3.7681e-03 3.2110e-03 2.7362e-03 2.3317e-03 1.9869e-03
## 5 2.4258e-03 2.0362e-03 1.7091e-03 1.4346e-03 1.2042e-03 1.0108e-03

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## 6 3.3857e-03 2.7546e-03 2.2423e-03 1.8263e-03 1.4882e-03 1.2132e-03
## year
## age 25 26 27 28 29 30
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 1.6555e-01 1.6135e-01 1.5725e-01 1.5325e-01 1.4936e-01 1.4557e-01
## 2 1.7727e-02 1.6125e-02 1.4668e-02 1.3342e-02 1.2136e-02 1.1040e-02
## 3 4.4152e-03 3.8572e-03 3.3697e-03 2.9438e-03 2.5718e-03 2.2467e-03
## 4 1.6931e-03 1.4428e-03 1.2295e-03 1.0477e-03 8.9278e-04 7.6078e-04
## 5 8.4841e-04 7.1214e-04 5.9776e-04 5.0175e-04 4.2116e-04 3.5351e-04
## 6 9.8958e-04 8.0749e-04 6.5919e-04 5.3834e-04 4.3982e-04 3.5946e-04
## year
## age 31 32 33 34 35 36
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 1.4187e-01 1.3827e-01 1.3476e-01 1.3133e-01 1.2800e-01 1.2475e-01
## 2 1.0042e-02 9.1343e-03 8.3088e-03 7.5579e-03 6.8748e-03 6.2535e-03
## 3 1.9628e-03 1.7147e-03 1.4980e-03 1.3087e-03 1.1433e-03 9.9881e-04
## 4 6.4829e-04 5.5244e-04 4.7076e-04 4.0115e-04 3.4184e-04 2.9130e-04
## 5 2.9673e-04 2.4907e-04 2.0906e-04 1.7548e-04 1.4730e-04 1.2364e-04
## 6 2.9389e-04 2.4036e-04 1.9665e-04 1.6094e-04 1.3175e-04 1.0789e-04
## year
## age 37 38 39 40 41 42
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 1.2158e-01 1.1849e-01 1.1548e-01 1.1255e-01 1.0969e-01 1.0691e-01
## 2 5.6883e-03 5.1742e-03 4.7066e-03 4.2812e-03 3.8943e-03 3.5424e-03
## 3 8.7258e-04 7.6230e-04 6.6596e-04 5.8179e-04 5.0827e-04 4.4403e-04
## 4 2.4823e-04 2.1152e-04 1.8025e-04 1.5360e-04 1.3089e-04 1.1153e-04
## 5 1.0378e-04 8.7111e-05 7.3119e-05 6.1375e-05 5.1517e-05 4.3242e-05
## 6 8.8375e-05 7.2410e-05 5.9345e-05 4.8649e-05 3.9891e-05 3.2718e-05
## year
## age 43 44 45 46 47 48
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 1.0419e-01 1.0154e-01 9.8966e-02 9.6452e-02 9.4003e-02 9.1615e-02
## 2 3.2222e-03 2.9310e-03 2.6661e-03 2.4251e-03 2.2060e-03 2.0066e-03
## 3 3.8791e-04 3.3889e-04 2.9606e-04 2.5864e-04 2.2595e-04 1.9740e-04
## 4 9.5044e-05 8.0991e-05 6.9016e-05 5.8812e-05 5.0116e-05 4.2706e-05
## 5 3.6297e-05 3.0467e-05 2.5573e-05 2.1466e-05 1.8018e-05 1.5124e-05
## 6 2.6840e-05 2.2024e-05 1.8075e-05 1.4838e-05 1.2183e-05 1.0005e-05
## year
## age 49 50 51 52 53 54
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 8.9289e-02 8.7021e-02 8.4811e-02 8.2657e-02 8.0558e-02 7.8512e-02
## 2 1.8253e-03 1.6603e-03 1.5102e-03 1.3737e-03 1.2496e-03 1.1367e-03
## 3 1.7245e-04 1.5065e-04 1.3161e-04 1.1498e-04 1.0045e-04 8.7754e-05
## 4 3.6392e-05 3.1011e-05 2.6426e-05 2.2519e-05 1.9189e-05 1.6352e-05
## 5 1.2695e-05 1.0656e-05 8.9442e-06 7.5076e-06 6.3017e-06 5.2896e-06
## 6 8.2178e-06 6.7512e-06 5.5473e-06 4.5589e-06 3.7473e-06 3.0806e-06
## year
## age 55 56 57 58 59 60
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 7.6518e-02 7.4575e-02 7.2681e-02 7.0835e-02 6.9036e-02 6.7283e-02
## 2 1.0339e-03 9.4049e-04 8.5549e-04 7.7817e-04 7.0784e-04 6.4387e-04
## 3 7.6664e-05 6.6975e-05 5.8510e-05 5.1116e-05 4.4656e-05 3.9012e-05
## 4 1.3934e-05 1.1874e-05 1.0118e-05 8.6222e-06 7.3473e-06 6.2610e-06
## 5 4.4400e-06 3.7268e-06 3.1282e-06 2.6258e-06 2.2040e-06 1.8500e-06

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## 6 2.5330e-06 2.0830e-06 1.7133e-06 1.4093e-06 1.1595e-06 9.5407e-07
## year
## age 61 62 63 64 65 66
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 6.5574e-02 6.3908e-02 6.2285e-02 6.0703e-02 5.9162e-02 5.7659e-02
## 2 5.8568e-04 5.3275e-04 4.8460e-04 4.4080e-04 4.0097e-04 3.6473e-04
## 3 3.4082e-05 2.9774e-05 2.6011e-05 2.2724e-05 1.9852e-05 1.7343e-05
## 4 5.3353e-06 4.5464e-06 3.8742e-06 3.3014e-06 2.8132e-06 2.3973e-06
## 5 1.5529e-06 1.3034e-06 1.0941e-06 9.1835e-07 7.7085e-07 6.4704e-07
## 6 7.8515e-07 6.4622e-07 5.3195e-07 4.3793e-07 3.6058e-07 2.9693e-07
## year
## age 67 68 69 70 71 72
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 5.6195e-02 5.4768e-02 5.3377e-02 5.2021e-02 5.0700e-02 4.9412e-02
## 2 3.3176e-04 3.0178e-04 2.7451e-04 2.4970e-04 2.2713e-04 2.0660e-04
## 3 1.5151e-05 1.3236e-05 1.1564e-05 1.0102e-05 8.8254e-06 7.7100e-06
## 4 2.0428e-06 1.7408e-06 1.4834e-06 1.2641e-06 1.0772e-06 9.1790e-07
## 5 5.4311e-07 4.5588e-07 3.8265e-07 3.2119e-07 2.6960e-07 2.2630e-07
## 6 2.4454e-07 2.0141e-07 1.6591e-07 1.3668e-07 1.1262e-07 9.2797e-08
## year
## age 73 74 75 76 77 78
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 4.8157e-02 4.6934e-02 4.5742e-02 4.4581e-02 4.3449e-02 4.2345e-02
## 2 1.8793e-04 1.7095e-04 1.5550e-04 1.4144e-04 1.2866e-04 1.1703e-04
## 3 6.7356e-06 5.8843e-06 5.1407e-06 4.4910e-06 3.9234e-06 3.4275e-06
## 4 7.8219e-07 6.6654e-07 5.6798e-07 4.8400e-07 4.1244e-07 3.5146e-07
## 5 1.8995e-07 1.5944e-07 1.3383e-07 1.1234e-07 9.4293e-08 7.9148e-08
## 6 7.6473e-08 6.3027e-08 5.1950e-08 4.2823e-08 3.5304e-08 2.9107e-08
## year
## age 79 80 81 82 83 84
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 4.1270e-02 4.0222e-02 3.9200e-02 3.8204e-02 3.7234e-02 3.6289e-02
## 2 1.0646e-04 9.6834e-05 8.8083e-05 8.0122e-05 7.2881e-05 6.6294e-05
## 3 2.9944e-06 2.6159e-06 2.2853e-06 1.9965e-06 1.7442e-06 1.5237e-06
## 4 2.9949e-07 2.5521e-07 2.1748e-07 1.8532e-07 1.5792e-07 1.3457e-07
## 5 6.6435e-08 5.5764e-08 4.6807e-08 3.9289e-08 3.2979e-08 2.7682e-08
## 6 2.4000e-08 1.9791e-08 1.6321e-08 1.3461e-08 1.1103e-08 9.1584e-09
## year
## age 85 86 87 88 89 90
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 3.5367e-02 3.4469e-02 3.3593e-02 3.2740e-02 3.1909e-02 3.1098e-02
## 2 6.0303e-05 5.4853e-05 4.9895e-05 4.5386e-05 4.1284e-05 3.7553e-05
## 3 1.3312e-06 1.1629e-06 1.0160e-06 8.8756e-07 7.7539e-07 6.7739e-07
## 4 1.1467e-07 9.7719e-08 8.3270e-08 7.0958e-08 6.0467e-08 5.1526e-08
## 5 2.3235e-08 1.9503e-08 1.6371e-08 1.3741e-08 1.1534e-08 9.6816e-09
## 6 7.5552e-09 6.2331e-09 5.1427e-09 4.2434e-09 3.5015e-09 2.8896e-09
## year
## age 91 92 93 94 95 96
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 3.0308e-02 2.9539e-02 2.8789e-02 2.8057e-02 2.7345e-02 2.6650e-02
## 2 3.4159e-05 3.1072e-05 2.8264e-05 2.5709e-05 2.3386e-05 2.1272e-05
## 3 5.9178e-07 5.1699e-07 4.5165e-07 3.9457e-07 3.4471e-07 3.0114e-07
## 4 4.3908e-08 3.7416e-08 3.1884e-08 2.7169e-08 2.3152e-08 1.9729e-08
## 5 8.1265e-09 6.8213e-09 5.7256e-09 4.8060e-09 4.0341e-09 3.3861e-09

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## 6 2.3848e-09 1.9683e-09 1.6246e-09 1.3411e-09 1.1070e-09 9.1393e-10
## year
## age 97 98 99 100 101
## 0 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00 1.0000e+00
## 1 2.5974e-02 2.5314e-02 2.4671e-02 2.4044e-02 2.3434e-02
## 2 1.9350e-05 1.7601e-05 1.6010e-05 1.4563e-05 1.3247e-05
## 3 2.6308e-07 2.2983e-07 2.0079e-07 1.7541e-07 1.5324e-07
## 4 1.6812e-08 1.4326e-08 1.2208e-08 1.0403e-08 8.8648e-09
## 5 2.8422e-09 2.3857e-09 2.0025e-09 1.6809e-09 1.4109e-09
## 6 7.5454e-10 6.2299e-10 5.1440e-10 4.2476e-10 3.5077e-10
##
## units: NA
# catch-at-age
catch.n(hkebrp)

## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
## year
## age 1 2 3 4 5 6
## 0 0.0000e+00 1.4940e-02 2.9573e-02 4.3906e-02 5.7947e-02 7.1702e-02
## 1 0.0000e+00 1.5197e-02 2.8729e-02 4.0749e-02 5.1396e-02 6.0795e-02
## 2 0.0000e+00 5.0674e-03 9.0491e-03 1.2121e-02 1.4434e-02 1.6116e-02
## 3 0.0000e+00 2.0389e-03 3.5213e-03 4.5614e-03 5.2524e-03 5.6703e-03
## 4 0.0000e+00 8.5717e-04 1.4505e-03 1.8410e-03 2.0770e-03 2.1968e-03
## 5 0.0000e+00 5.2669e-04 8.7878e-04 1.0997e-03 1.2233e-03 1.2757e-03
## 6 0.0000e+00 1.4288e-03 2.2727e-03 2.7156e-03 2.8885e-03 2.8844e-03
## year
## age 7 8 9 10 11 12
## 0 8.5177e-02 9.8379e-02 1.1131e-01 1.2399e-01 1.3641e-01 1.4858e-01
## 1 6.9064e-02 7.6307e-02 8.2620e-02 8.8090e-02 9.2797e-02 9.6813e-02
## 2 1.7277e-02 1.8010e-02 1.8392e-02 1.8492e-02 1.8365e-02 1.8059e-02
## 3 5.8769e-03 5.9222e-03 5.8463e-03 5.6815e-03 5.4535e-03 5.1825e-03
## 4 2.2307e-03 2.2022e-03 2.1297e-03 2.0275e-03 1.9064e-03 1.7746e-03
## 5 1.2771e-03 1.2431e-03 1.1853e-03 1.1126e-03 1.0314e-03 9.4660e-04
## 6 2.7687e-03 2.5869e-03 2.3703e-03 2.1402e-03 1.9104e-03 1.6898e-03
## year
## age 13 14 15 16 17 18
## 0 1.6050e-01 1.7219e-01 1.8364e-01 1.9487e-01 2.0587e-01 2.1666e-01
## 1 1.0021e-01 1.0303e-01 1.0535e-01 1.0721e-01 1.0865e-01 1.0973e-01
## 2 1.7614e-02 1.7063e-02 1.6433e-02 1.5748e-02 1.5026e-02 1.4283e-02
## 3 4.8846e-03 4.5720e-03 4.2543e-03 3.9387e-03 3.6305e-03 3.3335e-03
## 4 1.6383e-03 1.5020e-03 1.3690e-03 1.2413e-03 1.1206e-03 1.0077e-03
## 5 8.6161e-04 7.7882e-04 6.9982e-04 6.2564e-04 5.5684e-04 4.9368e-04
## 6 1.4836e-03 1.2946e-03 1.1238e-03 9.7135e-04 8.3640e-04 7.1786e-04
## year
## age 19 20 21 22 23 24
## 0 2.2723e-01 2.3760e-01 2.4776e-01 2.5772e-01 2.6749e-01 2.7707e-01
## 1 1.1046e-01 1.1090e-01 1.1107e-01 1.1099e-01 1.1070e-01 1.1022e-01
## 2 1.3532e-02 1.2782e-02 1.2042e-02 1.1317e-02 1.0614e-02 9.9348e-03
## 3 3.0504e-03 2.7828e-03 2.5318e-03 2.2978e-03 2.0808e-03 1.8805e-03
## 4 9.0306e-04 8.0680e-04 7.1881e-04 6.3883e-04 5.6647e-04 5.0128e-04
## 5 4.3618e-04 3.8419e-04 3.3746e-04 2.9568e-04 2.5849e-04 2.2551e-04
## 6 6.1437e-04 5.2450e-04 4.4678e-04 3.7983e-04 3.2236e-04 2.7314e-04

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##      year
## age 25      26      27      28      29      30
##  0 2.8646e-01 2.9567e-01 3.0470e-01 3.1356e-01 3.2225e-01 3.3077e-01
##  1 1.0957e-01 1.0877e-01 1.0783e-01 1.0678e-01 1.0562e-01 1.0437e-01
##  2 9.2827e-03 8.6595e-03 8.0661e-03 7.5033e-03 6.9709e-03 6.4689e-03
##  3 1.6963e-03 1.5276e-03 1.3736e-03 1.2333e-03 1.1059e-03 9.9038e-04
##  4 4.4277e-04 3.9041e-04 3.4369e-04 3.0213e-04 2.6523e-04 2.3255e-04
##  5 1.9637e-04 1.7070e-04 1.4815e-04 1.2840e-04 1.1112e-04 9.6050e-05
##  6 2.3112e-04 1.9531e-04 1.6485e-04 1.3900e-04 1.1709e-04 9.8540e-05
##      year
## age 31      32      33      34      35      36
##  0 3.3913e-01 3.4733e-01 3.5537e-01 3.6326e-01 3.7101e-01 3.7861e-01
##  1 1.0305e-01 1.0166e-01 1.0021e-01 9.8712e-02 9.7176e-02 9.5606e-02
##  2 5.9966e-03 5.5533e-03 5.1380e-03 4.7497e-03 4.3872e-03 4.0493e-03
##  3 8.8595e-04 7.9169e-04 7.0676e-04 6.3035e-04 5.6172e-04 5.0015e-04
##  4 2.0365e-04 1.7815e-04 1.5569e-04 1.3592e-04 1.1856e-04 1.0333e-04
##  5 8.2925e-05 7.1514e-05 6.1611e-05 5.3028e-05 4.5599e-05 3.9178e-05
##  6 8.2864e-05 6.9629e-05 5.8467e-05 4.9063e-05 4.1147e-05 3.4488e-05
##      year
## age 37      38      39      40      41      42
##  0 3.8606e-01 3.9338e-01 4.0056e-01 4.0760e-01 4.1452e-01 4.2131e-01
##  1 9.4010e-02 9.2394e-02 9.0763e-02 8.9121e-02 8.7474e-02 8.5824e-02
##  2 3.7349e-03 3.4426e-03 3.1712e-03 2.9195e-03 2.6864e-03 2.4706e-03
##  3 4.4498e-04 3.9561e-04 3.5148e-04 3.1207e-04 2.7692e-04 2.4557e-04
##  4 8.9984e-05 7.8303e-05 6.8089e-05 5.9168e-05 5.1382e-05 4.4594e-05
##  5 3.3633e-05 2.8852e-05 2.4733e-05 2.1187e-05 1.8138e-05 1.5518e-05
##  6 2.8893e-05 2.4193e-05 2.0249e-05 1.6940e-05 1.4167e-05 1.1843e-05
##      year
## age 43      44      45      46      47      48
##  0 4.2797e-01 4.3451e-01 4.4094e-01 4.4724e-01 4.5343e-01 4.5951e-01
##  1 8.4175e-02 8.2531e-02 8.0895e-02 7.9267e-02 7.7652e-02 7.6051e-02
##  2 2.2710e-03 2.0866e-03 1.9163e-03 1.7592e-03 1.6144e-03 1.4809e-03
##  3 2.1766e-04 1.9282e-04 1.7073e-04 1.5110e-04 1.3367e-04 1.1820e-04
##  4 3.8681e-05 3.3533e-05 2.9055e-05 2.5163e-05 2.1781e-05 1.8846e-05
##  5 1.3269e-05 1.1340e-05 9.6857e-06 8.2688e-06 7.0558e-06 6.0180e-06
##  6 9.8970e-06 8.2679e-06 6.9049e-06 5.7649e-06 4.8117e-06 4.0151e-06
##      year
## age 49      50      51      52      53      54
##  0 4.6548e-01 4.7134e-01 4.7710e-01 4.8275e-01 4.8831e-01 4.9376e-01
##  1 7.4464e-02 7.2895e-02 7.1345e-02 6.9813e-02 6.8302e-02 6.6812e-02
##  2 1.3580e-03 1.2449e-03 1.1409e-03 1.0452e-03 9.5734e-04 8.7659e-04
##  3 1.0447e-04 9.2307e-05 8.1527e-05 7.1981e-05 6.3531e-05 5.6055e-05
##  4 1.6299e-05 1.4090e-05 1.2176e-05 1.0518e-05 9.0819e-06 7.8395e-06
##  5 5.1306e-06 4.3722e-06 3.7244e-06 3.1713e-06 2.6994e-06 2.2969e-06
##  6 3.3496e-06 2.7937e-06 2.3295e-06 1.9421e-06 1.6187e-06 1.3490e-06
##      year
## age 55      56      57      58      59      60
##  0 4.9912e-01 5.0438e-01 5.0956e-01 5.1464e-01 5.1963e-01 5.2454e-01
##  1 6.5345e-02 6.3899e-02 6.2477e-02 6.1078e-02 5.9703e-02 5.8352e-02
##  2 8.0245e-04 7.3440e-04 6.7197e-04 6.1470e-04 5.6220e-04 5.1408e-04
##  3 4.9443e-05 4.3598e-05 3.8433e-05 3.3870e-05 2.9842e-05 2.6286e-05
##  4 6.7647e-06 5.8354e-06 5.0321e-06 4.3382e-06 3.7388e-06 3.2214e-06
##  5 1.9537e-06 1.6613e-06 1.4122e-06 1.2000e-06 1.0195e-06 8.6583e-07
##  6 1.1240e-06 9.3633e-07 7.7988e-07 6.4947e-07 5.4079e-07 4.5023e-07

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##      year
## age 61      62      63      64      65      66
##  0 5.2936e-01 5.3410e-01 5.3876e-01 5.4333e-01 5.4783e-01 5.5226e-01
##  1 5.7024e-02 5.5722e-02 5.4443e-02 5.3188e-02 5.1958e-02 5.0752e-02
##  2 4.6999e-04 4.2960e-04 3.9262e-04 3.5875e-04 3.2776e-04 2.9940e-04
##  3 2.3148e-05 2.0380e-05 1.7938e-05 1.5786e-05 1.3889e-05 1.2218e-05
##  4 2.7748e-06 2.3895e-06 2.0572e-06 1.7706e-06 1.5237e-06 1.3109e-06
##  5 7.3514e-07 6.2402e-07 5.2955e-07 4.4928e-07 3.8108e-07 3.2316e-07
##  6 3.7478e-07 3.1193e-07 2.5959e-07 2.1601e-07 1.7972e-07 1.4951e-07
##      year
## age 67      68      69      70      71      72
##  0 5.5661e-01 5.6088e-01 5.6509e-01 5.6922e-01 5.7329e-01 5.7729e-01
##  1 4.9570e-02 4.8412e-02 4.7277e-02 4.6165e-02 4.5077e-02 4.4012e-02
##  2 2.7345e-04 2.4971e-04 2.2801e-04 2.0817e-04 1.9002e-04 1.7344e-04
##  3 1.0746e-05 9.4490e-06 8.3073e-06 7.3023e-06 6.4177e-06 5.6395e-06
##  4 1.1275e-06 9.6960e-07 8.3364e-07 7.1660e-07 6.1587e-07 5.2920e-07
##  5 2.7398e-07 2.3224e-07 1.9681e-07 1.6676e-07 1.4126e-07 1.1965e-07
##  6 1.2437e-07 1.0344e-07 8.6029e-08 7.1540e-08 5.9485e-08 4.9458e-08
##      year
## age 73      74      75      76      77      78
##  0 5.8122e-01 5.8509e-01 5.8889e-01 5.9263e-01 5.9631e-01 5.9994e-01
##  1 4.2969e-02 4.1949e-02 4.0950e-02 3.9973e-02 3.9018e-02 3.8084e-02
##  2 1.5829e-04 1.4445e-04 1.3180e-04 1.2025e-04 1.0970e-04 1.0007e-04
##  3 4.9548e-06 4.3526e-06 3.8230e-06 3.3574e-06 2.9480e-06 2.5883e-06
##  4 4.5465e-07 3.9053e-07 3.3540e-07 2.8800e-07 2.4726e-07 2.1225e-07
##  5 1.0132e-07 8.5780e-08 7.2613e-08 6.1457e-08 5.2006e-08 4.4001e-08
##  6 4.1117e-08 3.4180e-08 2.8412e-08 2.3615e-08 1.9626e-08 1.6310e-08
##      year
## age 79      80      81      82      83      84
##  0 6.0350e-01 6.0701e-01 6.1046e-01 6.1385e-01 6.1720e-01 6.2049e-01
##  1 3.7170e-02 3.6277e-02 3.5404e-02 3.4550e-02 3.3716e-02 3.2901e-02
##  2 9.1271e-05 8.3241e-05 7.5912e-05 6.9222e-05 6.3118e-05 5.7547e-05
##  3 2.2721e-06 1.9944e-06 1.7503e-06 1.5360e-06 1.3477e-06 1.1824e-06
##  4 1.8217e-07 1.5633e-07 1.3414e-07 1.1508e-07 9.8713e-08 8.4664e-08
##  5 3.7223e-08 3.1484e-08 2.6626e-08 2.2515e-08 1.9035e-08 1.6091e-08
##  6 1.3553e-08 1.1262e-08 9.3573e-09 7.7743e-09 6.4587e-09 5.3654e-09
##      year
## age 85      86      87      88      89      90
##  0 6.2372e-01 6.2691e-01 6.3005e-01 6.3314e-01 6.3618e-01 6.3917e-01
##  1 3.2104e-02 3.1326e-02 3.0565e-02 2.9823e-02 2.9097e-02 2.8388e-02
##  2 5.2465e-05 4.7828e-05 4.3598e-05 3.9740e-05 3.6221e-05 3.3011e-05
##  3 1.0373e-06 9.0988e-07 7.9803e-07 6.9986e-07 6.1372e-07 5.3812e-07
##  4 7.2606e-08 6.2257e-08 5.3377e-08 4.5758e-08 3.9222e-08 3.3615e-08
##  5 1.3601e-08 1.1495e-08 9.7131e-09 8.2067e-09 6.9332e-09 5.8566e-09
##  6 4.4569e-09 3.7021e-09 3.0749e-09 2.5539e-09 2.1210e-09 1.7614e-09
##      year
## age 91      92      93      94      95      96
##  0 6.4212e-01 6.4503e-01 6.4789e-01 6.5070e-01 6.5348e-01 6.5621e-01
##  1 2.7696e-02 2.7020e-02 2.6360e-02 2.5715e-02 2.5085e-02 2.4471e-02
##  2 3.0085e-05 2.7416e-05 2.4983e-05 2.2765e-05 2.0742e-05 1.8899e-05
##  3 4.7180e-07 4.1362e-07 3.6258e-07 3.1781e-07 2.7855e-07 2.4412e-07
##  4 2.8807e-08 2.4684e-08 2.1149e-08 1.8119e-08 1.5521e-08 1.3294e-08
##  5 4.9466e-09 4.1775e-09 3.5276e-09 2.9786e-09 2.5147e-09 2.1228e-09
##  6 1.4627e-09 1.2147e-09 1.0086e-09 8.3746e-10 6.9533e-10 5.7730e-10

```

```

##      year
## age 97      98      99      100      101
##   0 6.5890e-01 6.6156e-01 6.6417e-01 6.6675e-01 6.6928e-01
##   1 2.3871e-02 2.3285e-02 2.2713e-02 2.2155e-02 2.1610e-02
##   2 1.7218e-05 1.5686e-05 1.4290e-05 1.3018e-05 1.1858e-05
##   3 2.1393e-07 1.8746e-07 1.6426e-07 1.4391e-07 1.2608e-07
##   4 1.1386e-08 9.7504e-09 8.3492e-09 7.1488e-09 6.1204e-09
##   5 1.7919e-09 1.5123e-09 1.2763e-09 1.0770e-09 9.0877e-10
##   6 4.7929e-10 3.9790e-10 3.3032e-10 2.7421e-10 2.2762e-10
##
## units:  NA

# plus some age-aggregated values
yield.hat(hkebrp)

## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##      year
## age  1      2      3      4      5      6      7
## all 0.000000 0.016066 0.027381 0.035157 0.040307 0.043518 0.045307
##      year
## age  8      9     10     11     12     13     14
## all 0.046063 0.046077 0.045569 0.044703 0.043600 0.042350 0.041019
##      year
## age 15     16     17     18     19     20     21
## all 0.039655 0.038292 0.036953 0.035655 0.034408 0.033219 0.032090
##      year
## age 22     23     24     25     26     27     28
## all 0.031023 0.030016 0.029069 0.028178 0.027341 0.026555 0.025817
##      year
## age 29     30     31     32     33     34     35
## all 0.025123 0.024471 0.023856 0.023278 0.022732 0.022216 0.021728
##      year
## age 36     37     38     39     40     41     42
## all 0.021266 0.020828 0.020412 0.020017 0.019640 0.019281 0.018939
##      year
## age 43     44     45     46     47     48     49
## all 0.018611 0.018297 0.017997 0.017708 0.017432 0.017165 0.016909
##      year
## age 50     51     52     53     54     55     56
## all 0.016663 0.016425 0.016196 0.015975 0.015761 0.015555 0.015355
##      year
## age 57     58     59     60     61     62     63
## all 0.015162 0.014975 0.014793 0.014618 0.014448 0.014283 0.014123
##      year
## age 64     65     66     67     68     69     70
## all 0.013967 0.013817 0.013670 0.013528 0.013391 0.013257 0.013127
##      year
## age 71     72     73     74     75     76     77
## all 0.013000 0.012877 0.012758 0.012642 0.012529 0.012420 0.012314
##      year
## age 78     79     80     81     82     83     84
## all 0.012210 0.012110 0.012012 0.011917 0.011825 0.011735 0.011648
##      year

```



```
## age 85      86      87      88      89      90      91
## all 0.011563 0.011481 0.011401 0.011323 0.011247 0.011174 0.011102
##      year
## age 92      93      94      95      96      97      98
## all 0.011033 0.010966 0.010900 0.010837 0.010775 0.010715 0.010657
##      year
## age 99      100      101
## all 0.010601 0.010546 0.010493
##
## units: NA
```

```
# mean recruitment
rec.hat(hkebrp)
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##      year
## age 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26
##    0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
##      year
## age 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49
##    0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
##      year
## age 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72
##    0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
##      year
## age 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95
##    0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
##      year
## age 96 97 98 99 100 101
##    0 1 1 1 1 1
##
## units: NA
```

```
# and we get a table of reference points
refpts(hkebrp)
```

```
## An object of class "FLPar"
##      quantity
## refpt harvest yield rec ssb biomass revenue
## virgin 0.0000e+00 0.0000e+00 1.0000e+00 1.1603e+00 1.2168e+00 NA
## msy 3.0035e-01 4.6147e-02 1.0000e+00 3.0193e-01 3.4690e-01 NA
## crash 1.2052e+01 9.4880e-03 1.0000e+00 4.3705e-06 1.0933e-02 NA
## f0.1 2.1604e-01 4.4382e-02 1.0000e+00 4.3362e-01 4.8134e-01 NA
## fmax 3.0035e-01 4.6147e-02 1.0000e+00 3.0193e-01 3.4690e-01 NA
## spr.30 2.6686e-01 4.5909e-02 1.0000e+00 3.4810e-01 3.9413e-01 NA
## mey NA NA NA NA NA NA
##      quantity
## refpt cost profit
## virgin NA NA
## msy NA NA
## crash NA NA
## f0.1 NA NA
## fmax NA NA
## spr.30 NA NA
```

```
##   mey           NA           NA
## units:  NA
```

```
plot(refpts(hkebrp))
```

cost	cost	cost	cost	cost	cost	cost
virgin	msy	crash	f0.1	fmax	spr.30	mey

revenue	revenue	revenue	revenue	revenue	revenue	revenue
virgin	msy	crash	f0.1	fmax	spr.30	mey

biomass	biomass	biomass	biomass	biomass	biomass	biomass
virgin	msy	crash	f0.1	fmax	spr.30	mey

0.8 1.2 1.6 0.0 0.4 0.8 0.4 0.0 0.4 0.2 0.6 0.0 0.4 0.8 0.0 0.4 0.8

ssb	ssb	ssb	ssb	ssb	ssb	ssb
virgin	msy	crash	f0.1	fmax	spr.30	mey

0.8 1.2 1.6 0.0 0.4 -0.4 0.0 0.4 0.0 0.4 0.8 0.0 0.4 0.0 0.4 0.8

rec	rec	rec	rec	rec	rec	rec
virgin	msy	crash	f0.1	fmax	spr.30	mey

0.6 1.0 1.4 0.6 1.0 1.4 0.6 1.0 1.4 0.6 1.0 1.4 0.6 1.0 1.4

yield	yield	yield	yield	yield	yield	yield
virgin	msy	crash	f0.1	fmax	spr.30	mey

-0.4 0.0 0.4 0.4 0.0 0.4 -0.4 0.0 0.4 0.4 0.0 0.4 0.4 0.0 0.4

```
# In this case, Fmsy is the same as Fmax, since the assumed stock recruitment
# relationship is mean recruitment
```

```
refpts(hkebrp)[c('msy', ('fmax')), ]
```

```
## An object of class "FLPar"
##      quantity
## refpt harvest yield  rec    ssb    biomass revenue  cost
##   msy  0.300346 0.046147 1.000000 0.301927 0.346900      NA      NA
##   fmax 0.300346 0.046147 1.000000 0.301927 0.346900      NA      NA
##      quantity
## refpt profit
##   msy      NA
##   fmax      NA
## units:  NA
```

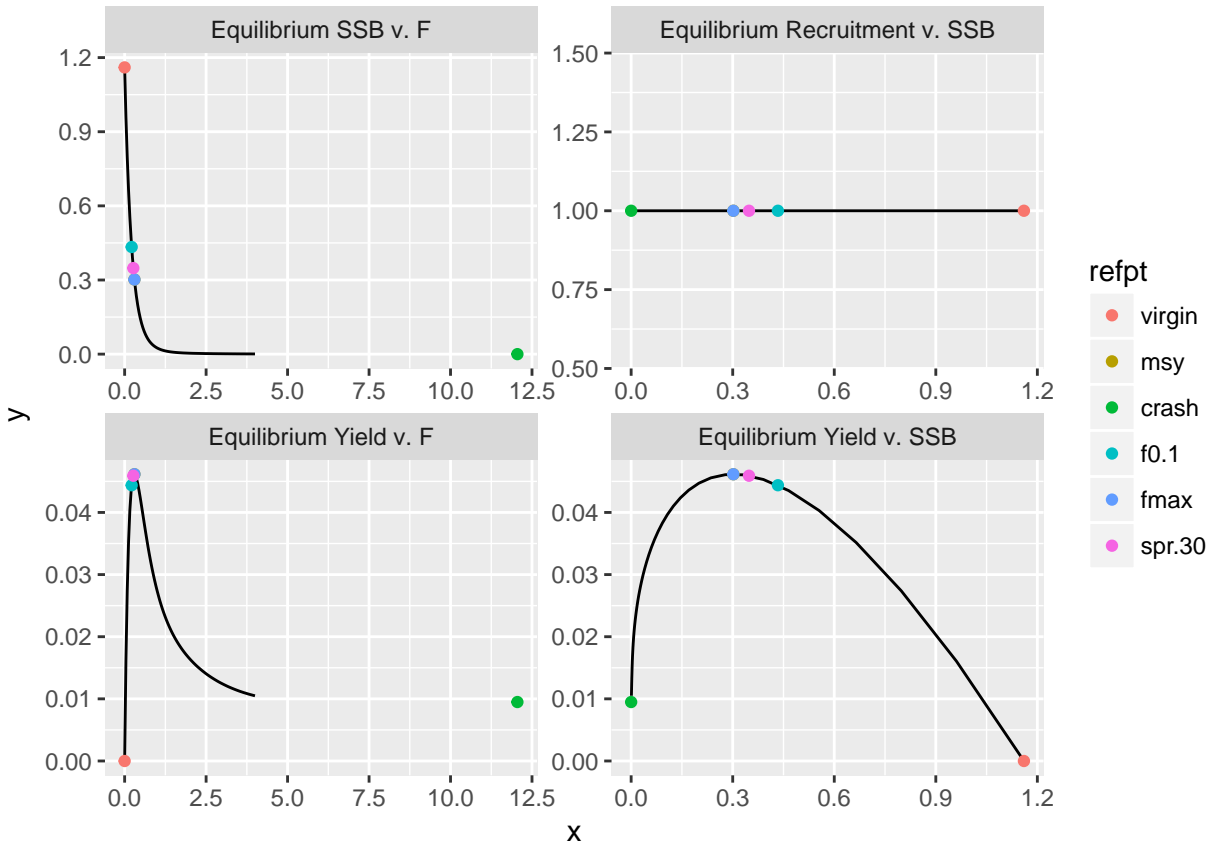
```
# Thus plotting the reference points and expected quantities
plot(hkebrp)
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
```

[illegible]

[illegible]



The derived reference points would be used to compare the fishing mortality (from Fbar) with the reference point of choice.

```
fbar(hke)[,"2014"]
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##      year
## age  2014
##   all 1.1689
##
## units:  f
```

```
refpts(hkebrp)['f0.1','harvest']
```

```
## An object of class "FLPar"
##      quantity
## refpt harvest
##   f0.1 0.21604
## units:  NA
```

F/F0.1 ?

```
fbar(hke)[,"2014"] / refpts(hkebrp)['f0.1','harvest']
```

```
## An object of class "FLQuant"
## , , unit = unique, season = all, area = unique
##
##      year
```

```
## age    2014
## all 5.4104
##
## units:  f
```

```
# SR
```

```
# Now we provide a stock-recruit relationship
```

```
model = "geomean"
srr <- fmle(as.FLSR(hke, model = model))
```

```
## Warning in optim(par = structure(160879.071868521, .Names = "a"), fn = function (par) : one-dimension
## use "Brent" or optimize() directly
```

```
## Nelder-Mead direct search function minimizer
## function value for initial parameters = -9.129982
## Scaled convergence tolerance is 1.36047e-07
## Stepsize computed as 16087.907187
## BUILD          2 -8.541476 -9.129982
## HI-REDUCTION   4 -8.968169 -9.129982
## HI-REDUCTION   6 -9.087978 -9.129982
## HI-REDUCTION   8 -9.119314 -9.129982
## HI-REDUCTION  10 -9.127296 -9.129982
## HI-REDUCTION  12 -9.129308 -9.129982
## HI-REDUCTION  14 -9.129813 -9.129982
## HI-REDUCTION  16 -9.129940 -9.129982
## HI-REDUCTION  18 -9.129971 -9.129982
## HI-REDUCTION  20 -9.129979 -9.129982
## HI-REDUCTION  22 -9.129981 -9.129982
## HI-REDUCTION  24 -9.129982 -9.129982
## Exiting from Nelder Mead minimizer
##      26 function evaluations used
```

```
#Reference points
```

```
hkebrpgm <- brp(FLBRP(hke, sr = srr))
ref_points<- refpts(hkebrpgm)
ref_points
```

```
## An object of class "FLPar"
```

```
##      quantity
## refpt  harvest  yield    rec      ssb      biomass  revenue
## virgin 0.0000e+00 0.0000e+00 1.6088e+05 1.8667e+05 1.9576e+05      NA
## msy    3.0035e-01 7.4241e+03 1.6088e+05 4.8574e+04 5.5809e+04      NA
## crash  3.0711e+01 1.6567e+03 1.6088e+05 4.3202e-06 1.7557e+03      NA
## f0.1    2.1604e-01 7.1401e+03 1.6088e+05 6.9760e+04 7.7437e+04      NA
## fmax    3.0035e-01 7.4241e+03 1.6088e+05 4.8574e+04 5.5809e+04      NA
## spr.30  2.6686e-01 7.3858e+03 1.6088e+05 5.6002e+04 6.3407e+04      NA
## mey      NA      NA      NA      NA      NA      NA
##      quantity
## refpt  cost      profit
## virgin      NA      NA
## msy      NA      NA
## crash      NA      NA
## f0.1      NA      NA
## fmax      NA      NA
```

```
## spr.30      NA      NA
## mey         NA      NA
## units:  NA
```

```
plot(refpts(hkebrpgm))
```

cost	cost	cost	cost	cost	cost	cost
virgin	msy	crash	f0.1	fmax	spr.30	mey

revenue	revenue	revenue	revenue	revenue	revenue	revenue
virgin	msy	crash	f0.1	fmax	spr.30	mey

biomass	biomass	biomass	biomass	biomass	biomass	biomass
virgin	msy	crash	f0.1	fmax	spr.30	mey

95761.4 195761.4 195761.4 195761.4 195761.4 195761.4 195761.4

ssb	ssb	ssb	ssb	ssb	ssb	ssb
virgin	msy	crash	f0.1	fmax	spr.30	mey

186674.2 48573.4 48573.4 0.0 0.0 0.0 0.0

rec	rec	rec	rec	rec	rec	rec
virgin	msy	crash	f0.1	fmax	spr.30	mey

30878.6 160878.6 160878.6 160878.6 160878.6 160878.6 160878.6

yield	yield	yield	yield	yield	yield	yield
virgin	msy	crash	f0.1	fmax	spr.30	mey

-0.4 0.0 0.4 423.8 7424.7 1656.2 1656.8 7139.8 7140.7 423.8 7424.7 385.4 7386.0

```
plot(hkebrpgm)
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
```

[illegible]


```
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

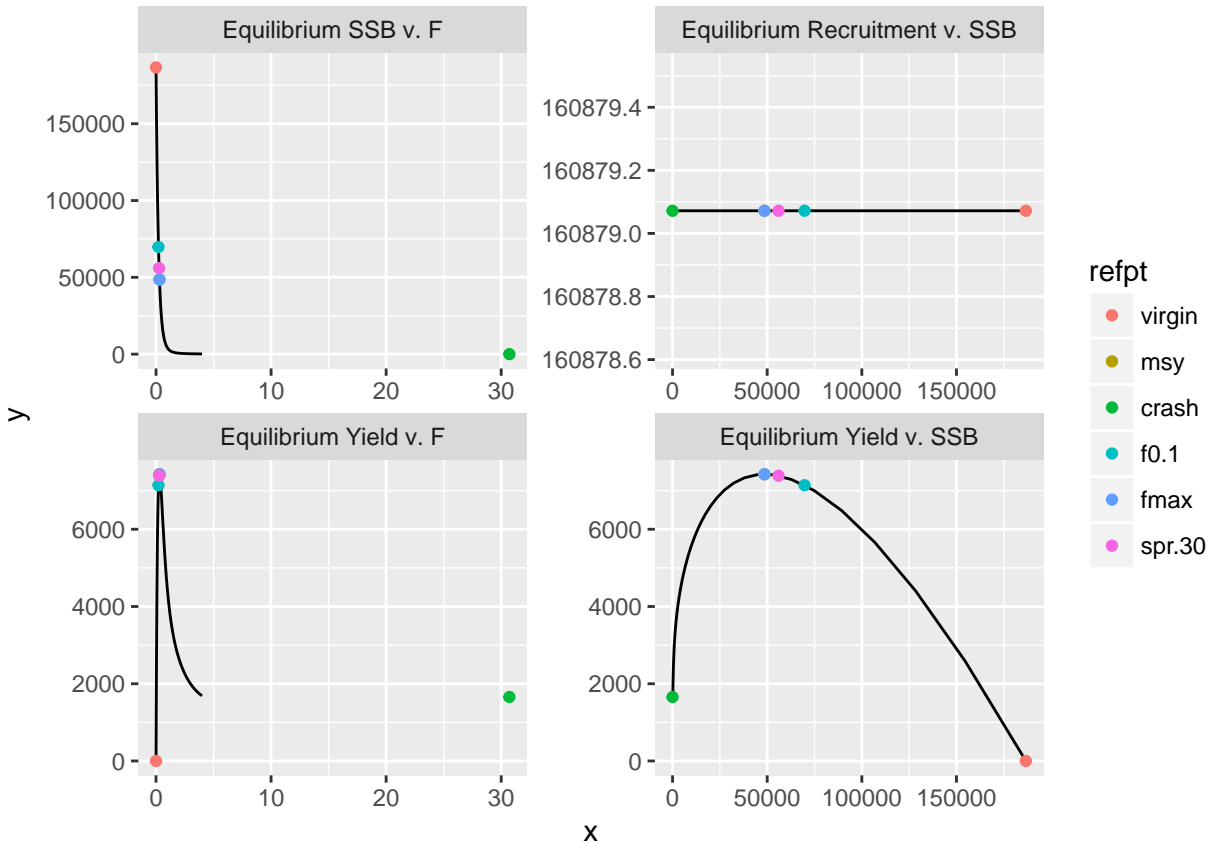
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore

## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```



```
rp_table = data.frame(ref_points@.Data)[,1:5]
temp <- rownames(rp_table)
rp_table = data.frame(rp_table, row.names = NULL)
rp_table <- cbind(temp, rp_table)
colnames(rp_table) = c("", "F", "Total Yield", "Recruitment", "SSB", "Biomass")

write.table(rp_table, file="Ref_points_HKE.csv", sep=";", row.names=FALSE, col.names=T)

#####

# we can add a SR fitted model

hkesr <- as.FLSR(hke, model=bevholt)
hkesr <- fmle(hkesr)

## Nelder-Mead direct search function minimizer
## function value for initial parameters = -2.355174
## Scaled convergence tolerance is 3.50948e-08
## Stepsize computed as 18687.676922
## BUILD          3 9.363309 -3.874934

## Warning in log(x@.Data, ...): NaNs produced
## HI-REDUCTION    5 6.700774 -3.874934

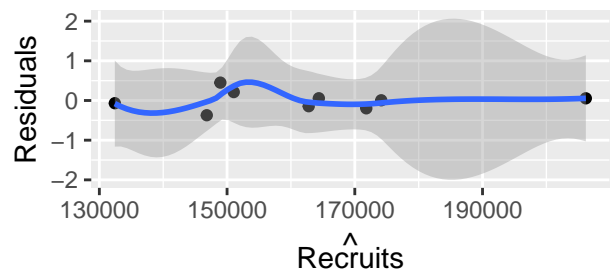
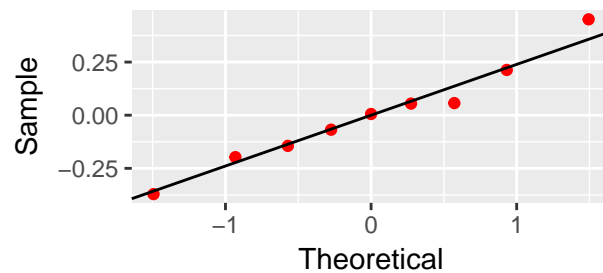
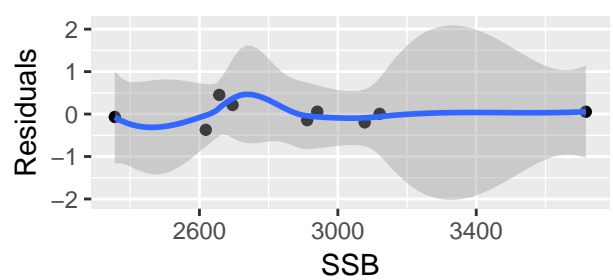
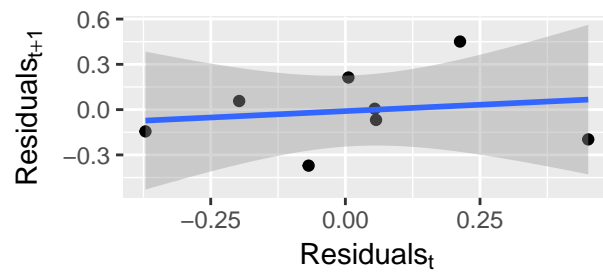
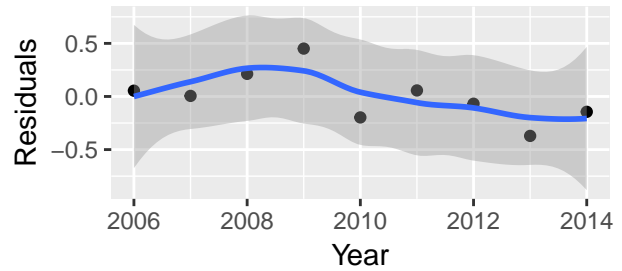
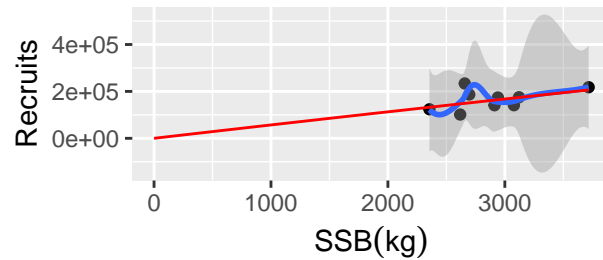
## Warning in log(x@.Data, ...): NaNs produced
## HI-REDUCTION    7 3.988498 -3.874934
```

```

## HI-REDUCTION      9  1.545284 -3.874934
## REFLECTION        11 -2.355174 -8.205219
## LO-REDUCTION      13 -3.874934 -9.524250
## HI-REDUCTION      15 -7.518147 -9.524250
## HI-REDUCTION      17 -8.205219 -9.524250
## HI-REDUCTION      19 -9.244832 -9.524250
## HI-REDUCTION      21 -9.292561 -9.524250
## LO-REDUCTION      23 -9.517158 -9.529330
## REFLECTION        25 -9.524250 -9.570396
## LO-REDUCTION      27 -9.529330 -9.570396
## REFLECTION        29 -9.562661 -9.577835
## HI-REDUCTION      31 -9.570396 -9.586610
## EXTENSION         33 -9.577835 -9.615444
## LO-REDUCTION      35 -9.586610 -9.615444
## EXTENSION         37 -9.596039 -9.640606
## EXTENSION         39 -9.615444 -9.688921
## EXTENSION         41 -9.640606 -9.744801
## EXTENSION         43 -9.688921 -9.842045
## EXTENSION         45 -9.744801 -9.926103
## EXTENSION         47 -9.842045 -10.049477
## EXTENSION         49 -9.926103 -10.109394
## EXTENSION         51 -10.049477 -10.189164
## EXTENSION         53 -10.109394 -10.199520
## EXTENSION         55 -10.189164 -10.229756
## LO-REDUCTION      57 -10.199520 -10.229756
## EXTENSION         59 -10.222950 -10.236260
## EXTENSION         61 -10.229756 -10.241241
## LO-REDUCTION      63 -10.236260 -10.241241
## REFLECTION        65 -10.240839 -10.241797
## HI-REDUCTION      67 -10.241241 -10.241797
## LO-REDUCTION      69 -10.241464 -10.241802
## LO-REDUCTION      71 -10.241748 -10.241802
## LO-REDUCTION      73 -10.241797 -10.241806
## HI-REDUCTION      75 -10.241802 -10.241820
## LO-REDUCTION      77 -10.241806 -10.241820
## LO-REDUCTION      79 -10.241817 -10.241820
## HI-REDUCTION      81 -10.241818 -10.241820
## HI-REDUCTION      83 -10.241819 -10.241820
## REFLECTION        85 -10.241820 -10.241820
## HI-REDUCTION      87 -10.241820 -10.241820
## HI-REDUCTION      89 -10.241820 -10.241820
## HI-REDUCTION      91 -10.241820 -10.241820
## Exiting from Nelder Mead minimizer
##      93 function evaluations used

```

```
plot(hkesr)
```



```
# and provide it when constructing FLBRP
hkebrp <- FLBRP(hke, sr=hkesr)
```

```
# let's have a look at the formula
model(hkebrp)
```

```
## rec ~ a * ssb/(b + ssb)
## <environment: 0x10538814>
```

```
# and parameters a and b
params(hkebrp)
```

```
## An object of class "FLPar"
## params
##      a      b
## 5677840 98637
## units: NA
```

```
# and we refit FLBRP
hkebrp <- brp(hkebrp)
```

```
# and see the difference in RPs
refpts(hkebrp)
```

```
## An object of class "FLPar"
##      quantity
## refpt  harvest  yield  rec      ssb      biomass  revenue
```

```
## virgin 0.0000e+00 0.0000e+00 5.5928e+06 6.4896e+06 6.8055e+06 NA
## msy 2.7544e-01 2.4776e+05 5.3839e+06 1.8067e+06 2.0530e+06 NA
## crash 1.1304e+00 3.7645e-06 1.5088e-04 2.6212e-06 6.9331e-06 NA
## f0.1 2.1604e-01 2.4190e+05 5.4504e+06 2.3634e+06 2.6235e+06 NA
## fmax 3.0035e-01 2.4694e+05 5.3511e+06 1.6157e+06 1.8563e+06 NA
## spr.30 2.6686e-01 2.4765e+05 5.3945e+06 1.8778e+06 2.1261e+06 NA
## mey NA NA NA NA NA NA
## quantity
## refpt cost profit
## virgin NA NA
## msy NA NA
## crash NA NA
## f0.1 NA NA
## fmax NA NA
## spr.30 NA NA
## mey NA NA
## units: NA
```

```
# and relationships
plot(hkebrp)
```

```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
## removed in later versions of FLCore
```

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```
## Warning in .local(x, i, j, ...): using a local copy of '[' which will be
```

[illegible]

removed in later versions of FLCore

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