

# Community Structure in Networks

Social Networks Analysis and Graph Algorithms

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# Sources

- A. L. Barabási (2016). Network Science – Chapter 09
- D. Easley and J. Kleinberg (2010). Networks, Crowds, and Markets – Chapter 03
- F. Menczer, S. Fortunato, C. A. Davis (2020). A First Course in Network Science – Chapter 06
- URLs cited in the footer of slides

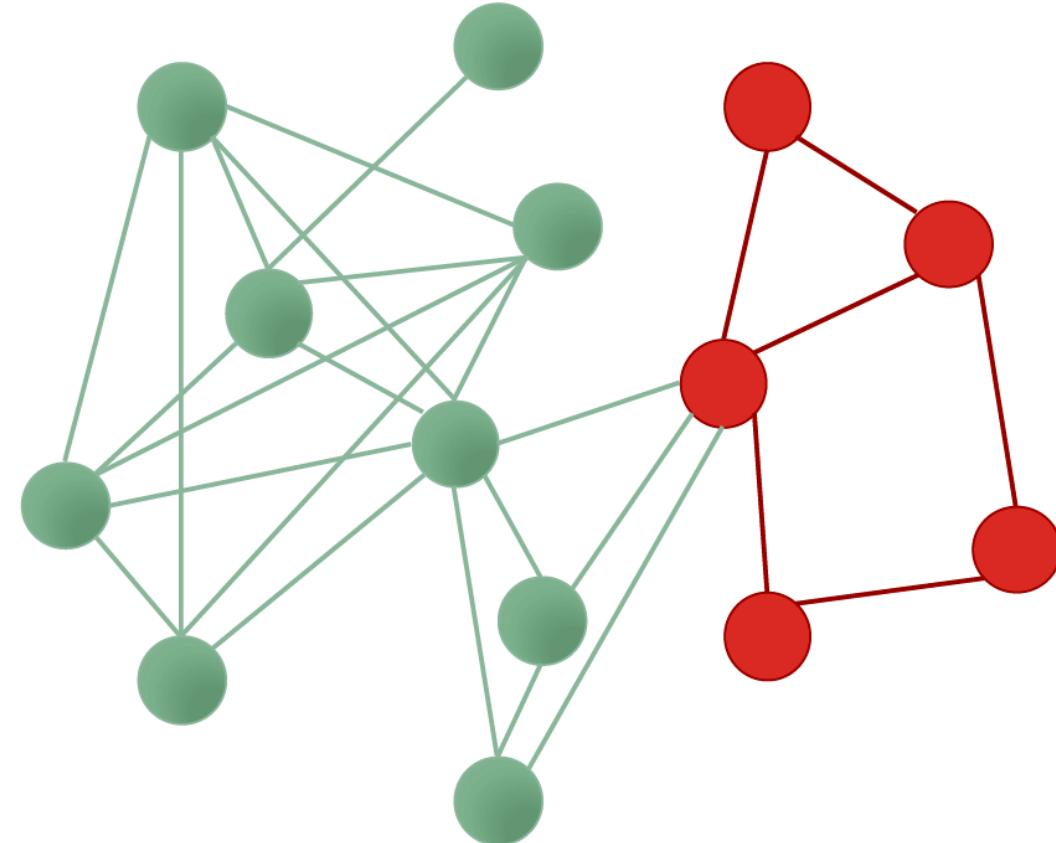
# Typical community structures

- One dense sub-graph
  - embedded somewhere within a larger graph
- Two groups (polarization)
  - plus perhaps some ambiguous nodes
- Multiple communities

# One dense sub-graph

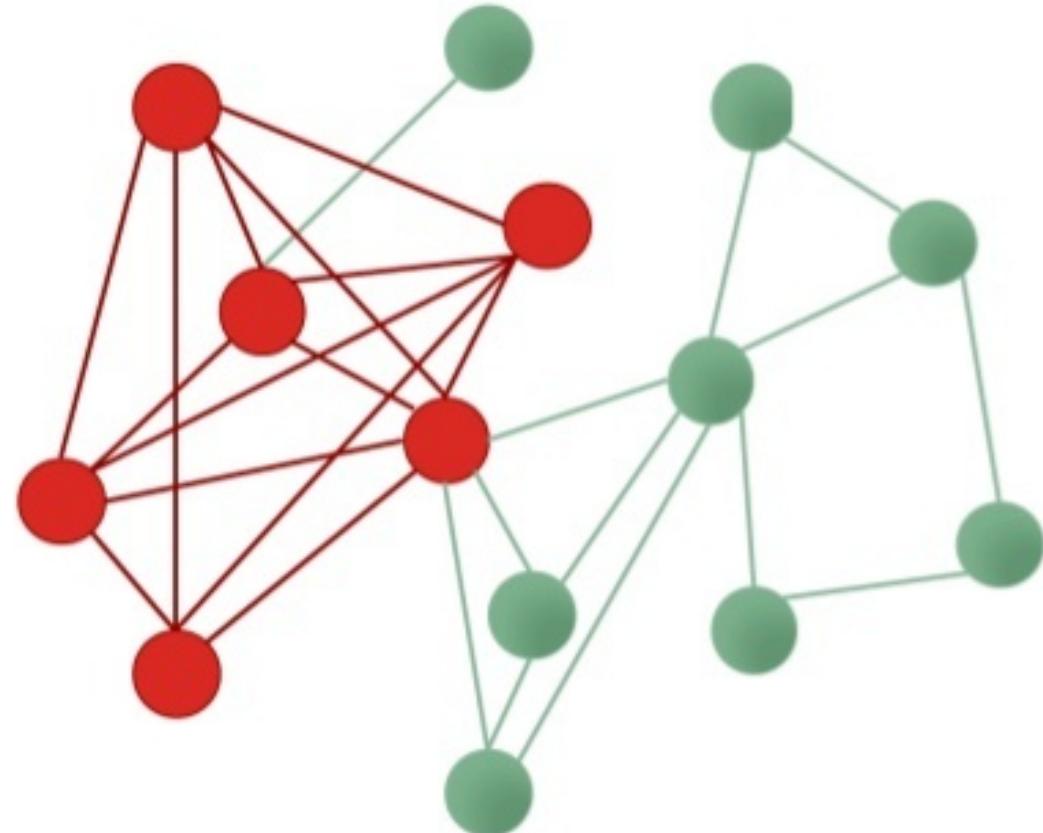
# What is a sub-graph?

Subset of nodes,  
and edges  
among those  
nodes



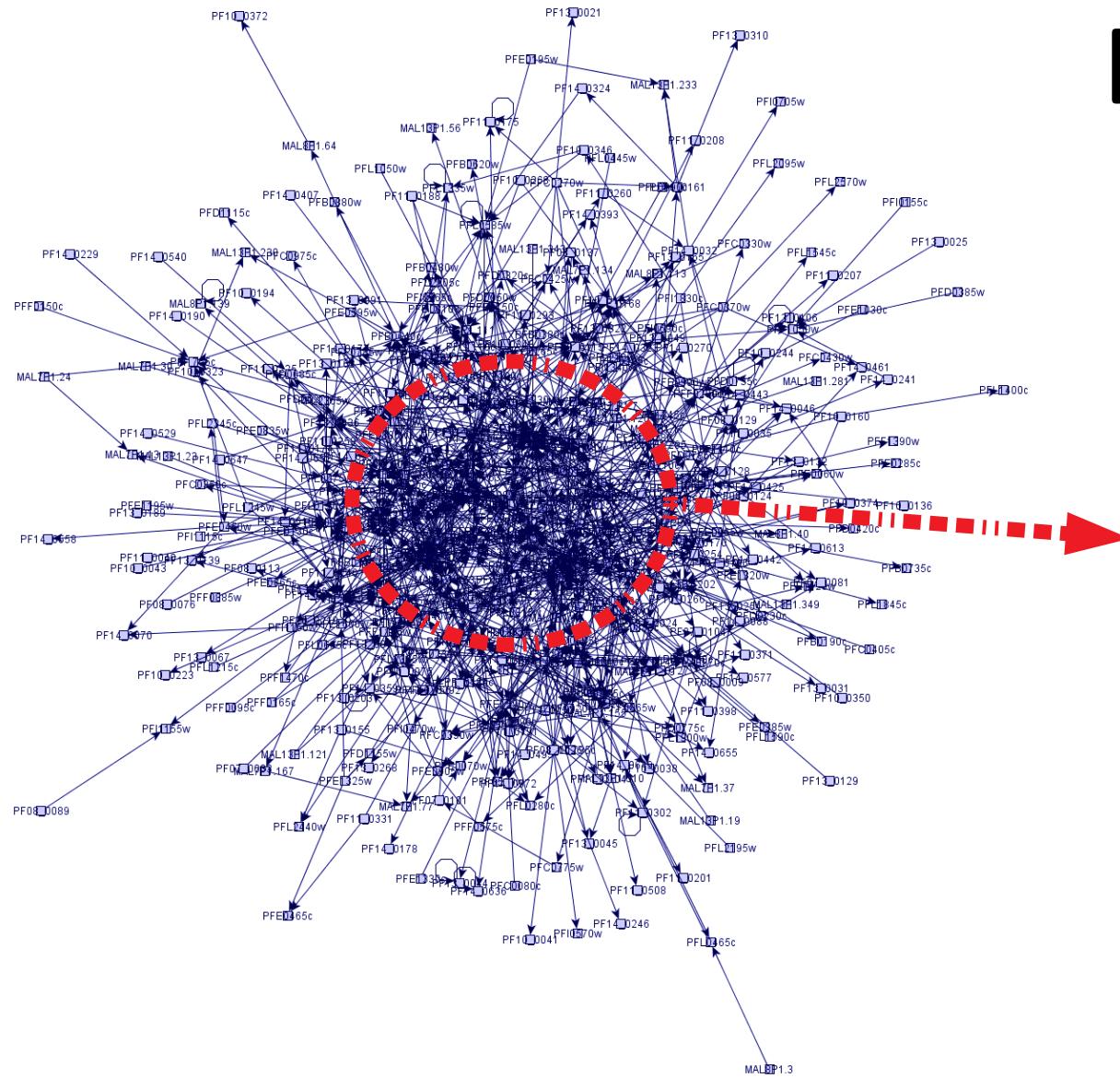
# Densest sub-graph

Sub-graph  
having the  
maximum  
density



Many graphs look  
like “hairballs”

Sometimes, at the center these graphs may have an interesting dense sub-graph



# Asthma-related genes



[https://www.youtube.com/watch?v=VU\\_7FHAKMgA](https://www.youtube.com/watch?v=VU_7FHAKMgA)

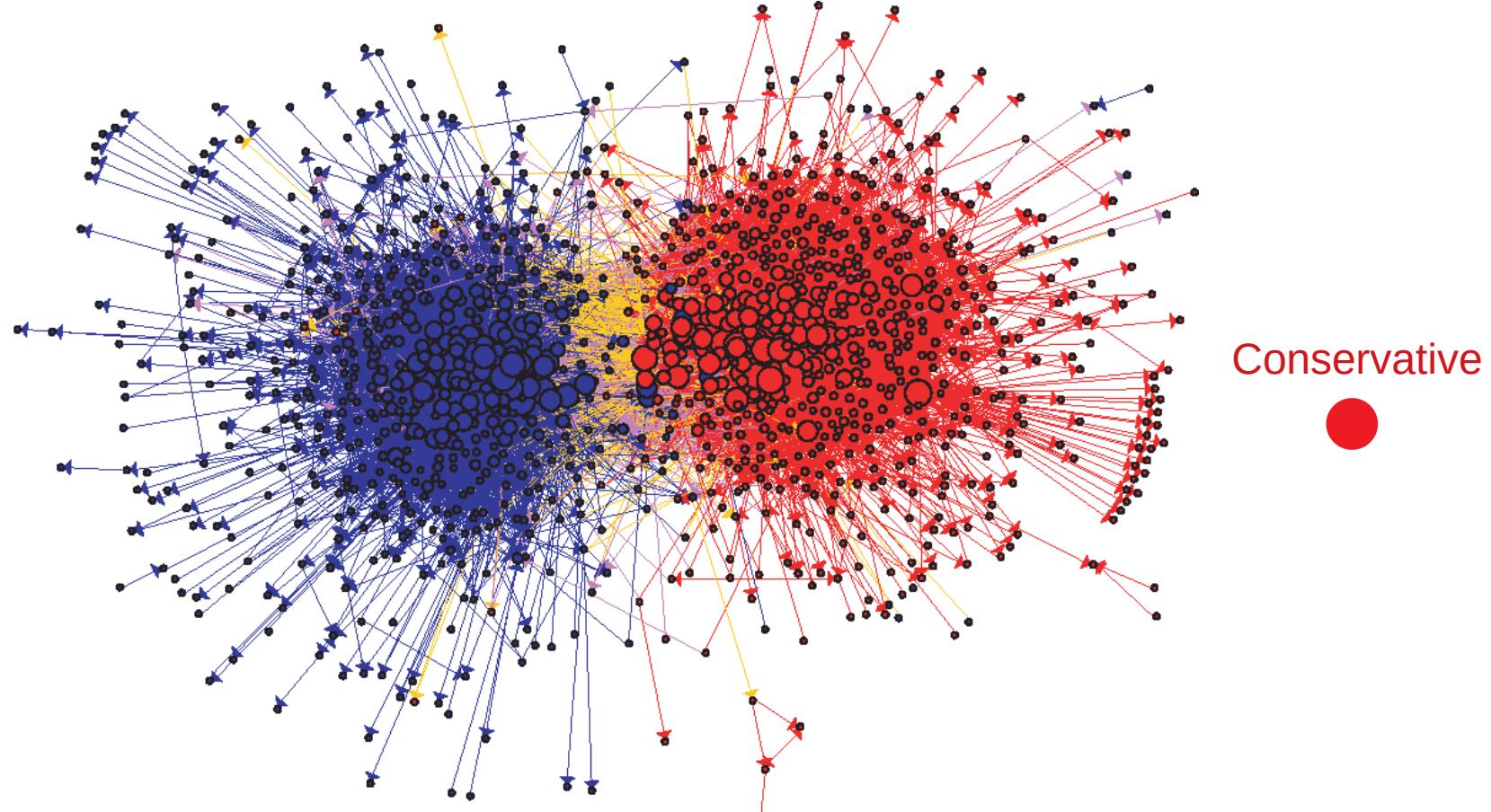
# Two groups (polarization)

# US Political Blogs (2004)

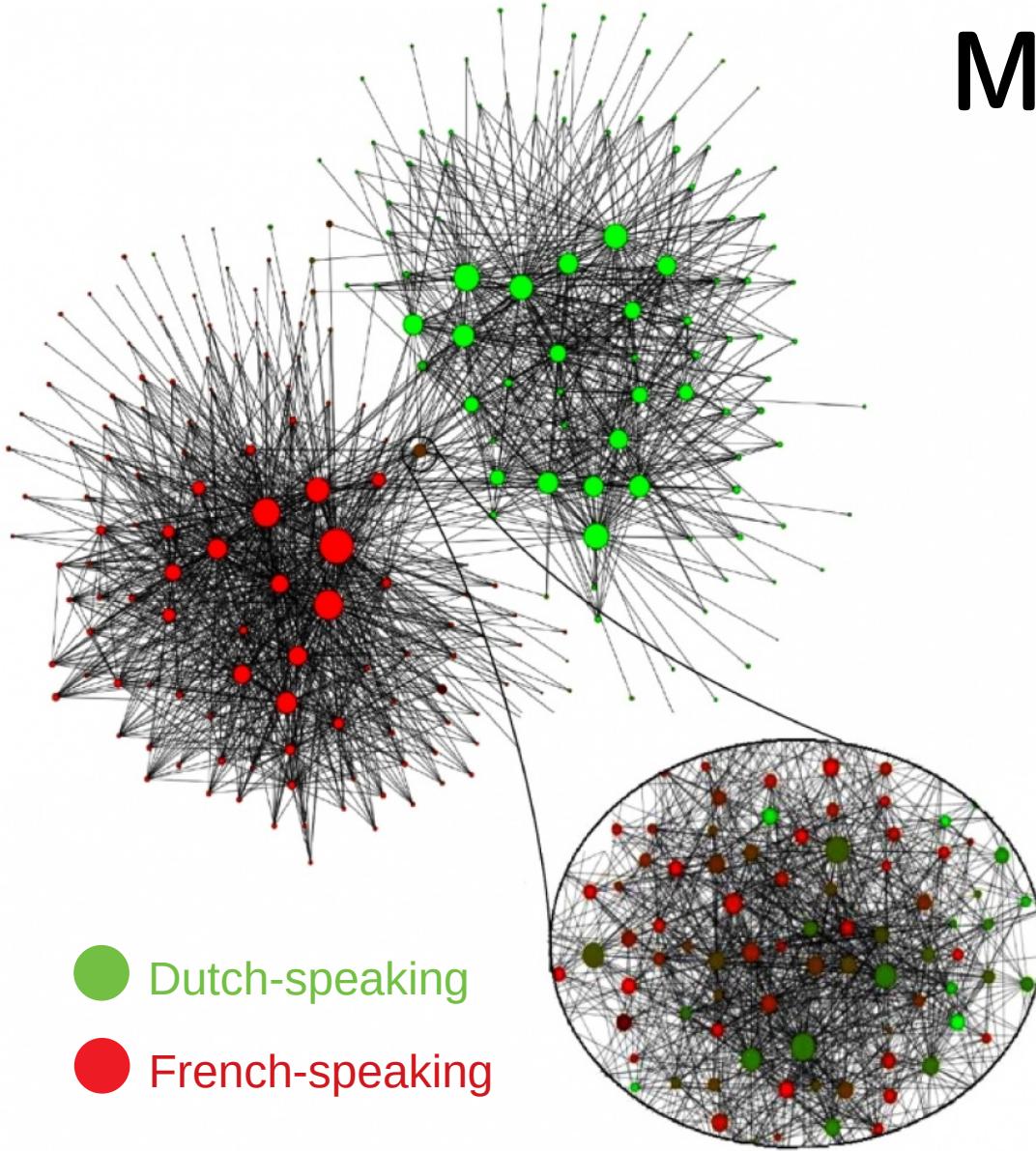
Liberal



Conservative



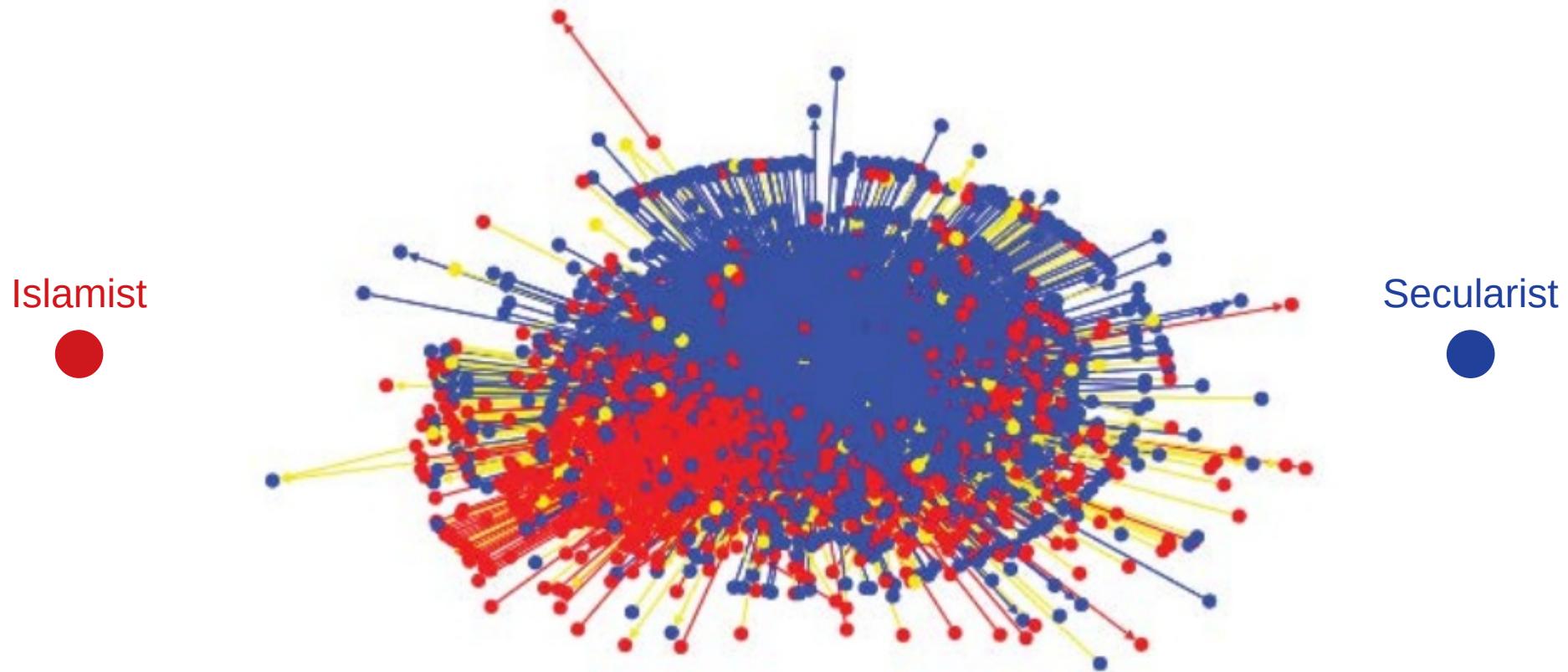
# Mobile phone users in Belgium (2008)



Each node is a community of 100 mobile users or more that tend to call each other

V. D. Blondel, J.-L. Guillaume, R. Lambiotte, and E. Lefebvre. Fast unfolding of communities in large networks. *J. Stat. Mech.*, 2008.

# Egyptian Twitter Users (2013)



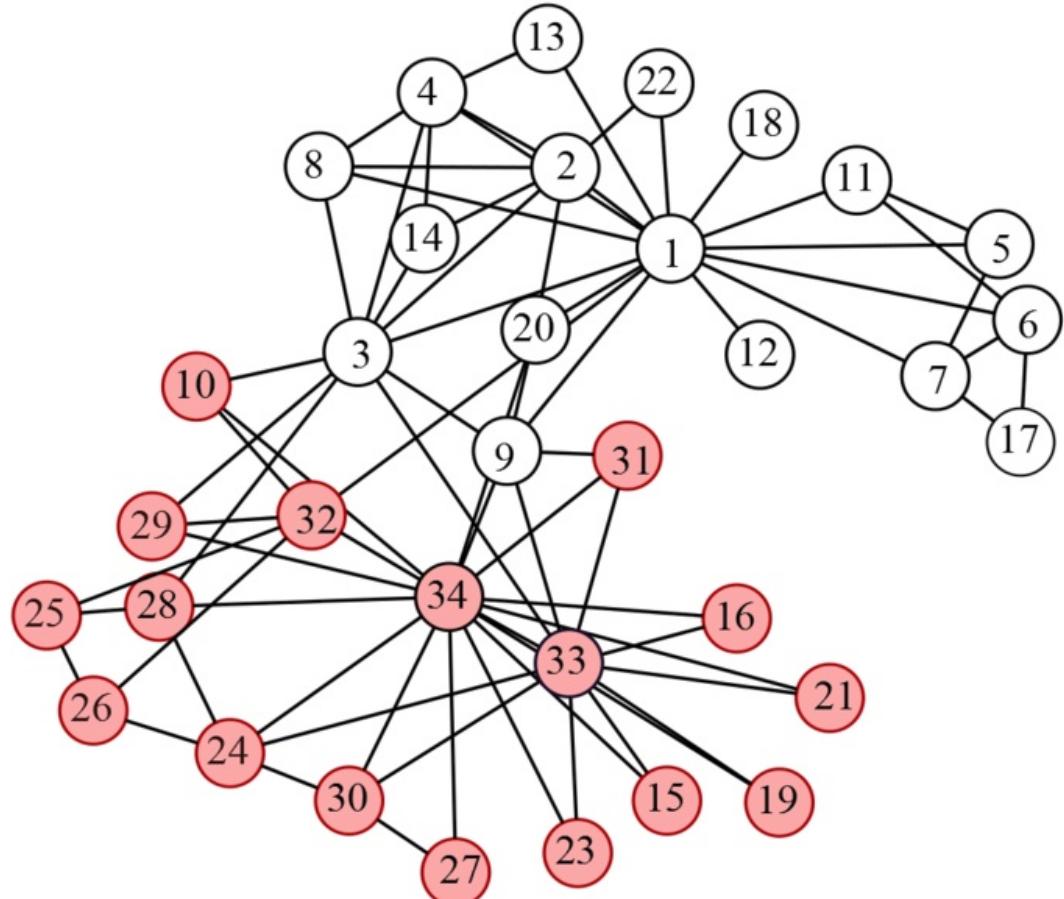
# Political Books



Source:  
Valdis Kreb  
& The Economist

# Wayne Zachary's PhD Thesis (1972)

- Studied 34 members of a karate club
- Found 78 links between members who regularly interacted outside the club
- The club splitted in two during the study
- 1=sensei, 34=president



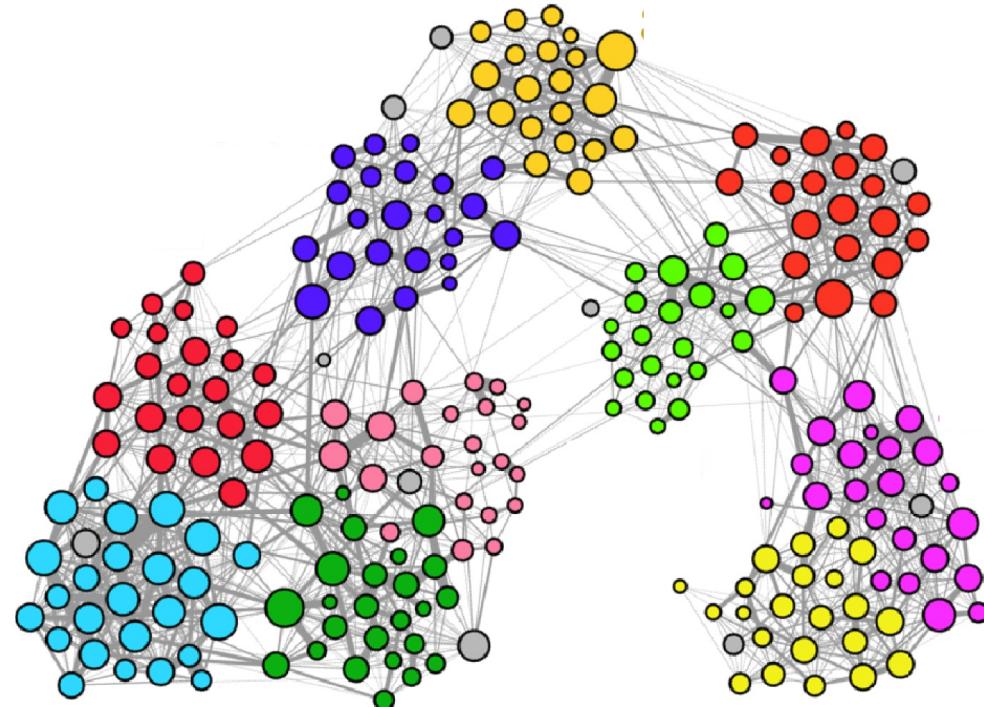
# Multiple communities

# Primary school contacts

Links connect students who spent more than two minutes facing each other at less than 1.0m-1.5m during one day.

Students wore RF-ID badges hanging on their chest.

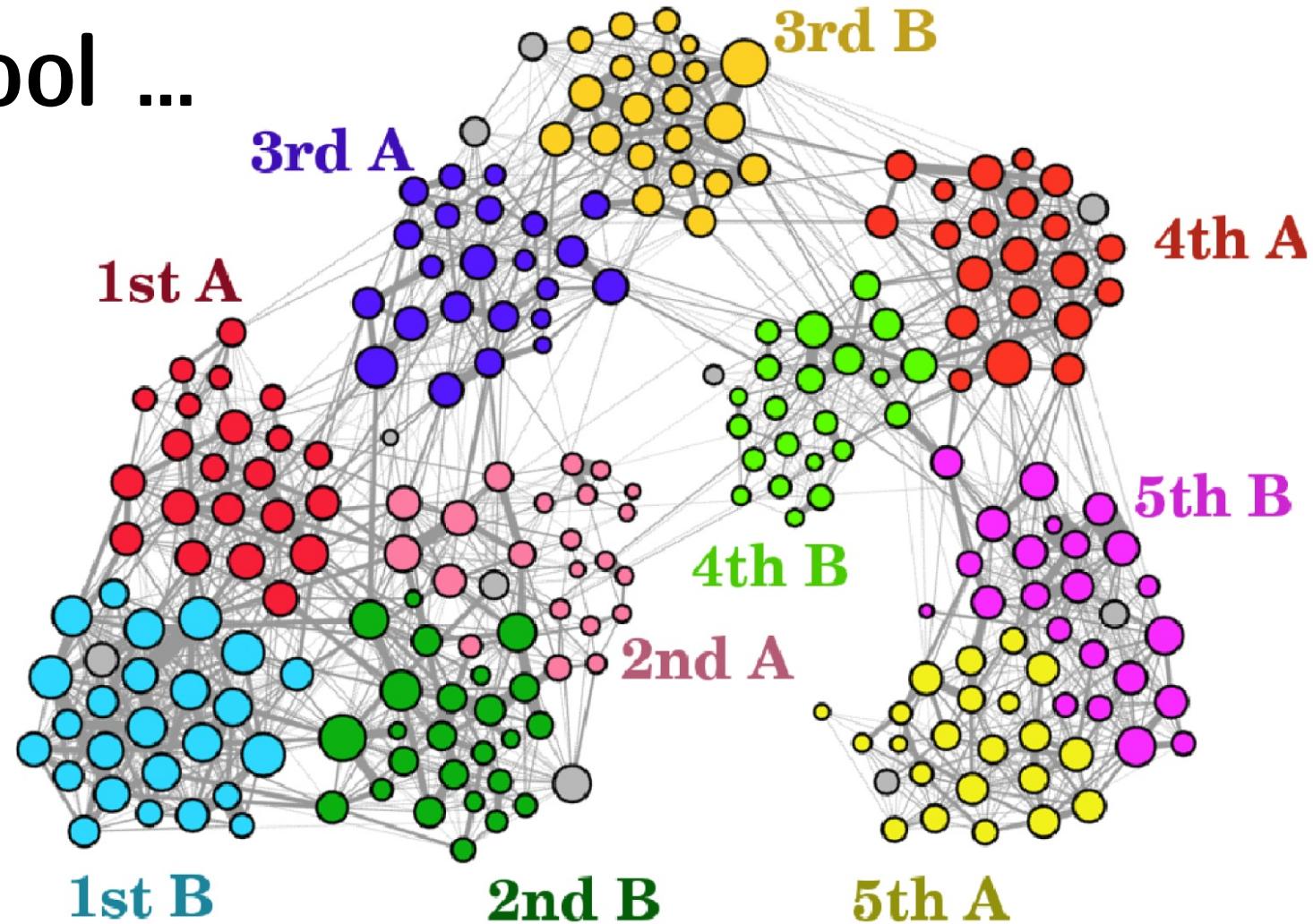
What do you think the colors represent in this visualization?



# Primary school ...

Colors represent classes. Teachers are shown in gray color.

Node sizes are number of connections.



Stehlé, J., et al. (2011).

High-resolution measurements of face-to-face contact patterns in a primary school.

PloS one, 6(8), e23176.

# Science

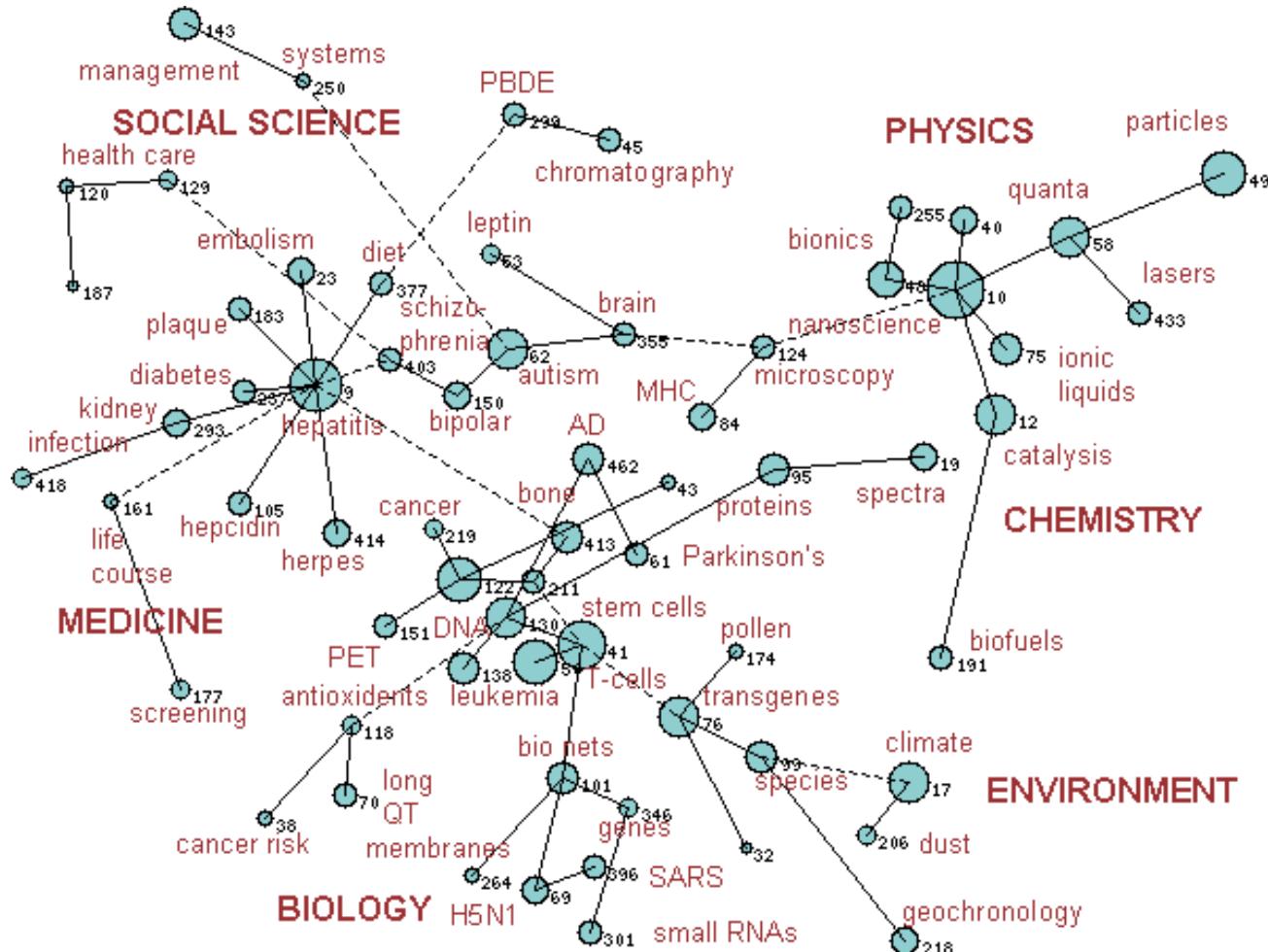
Two topics  $T_1$ ,  $T_2$ , are

connected if there is at least

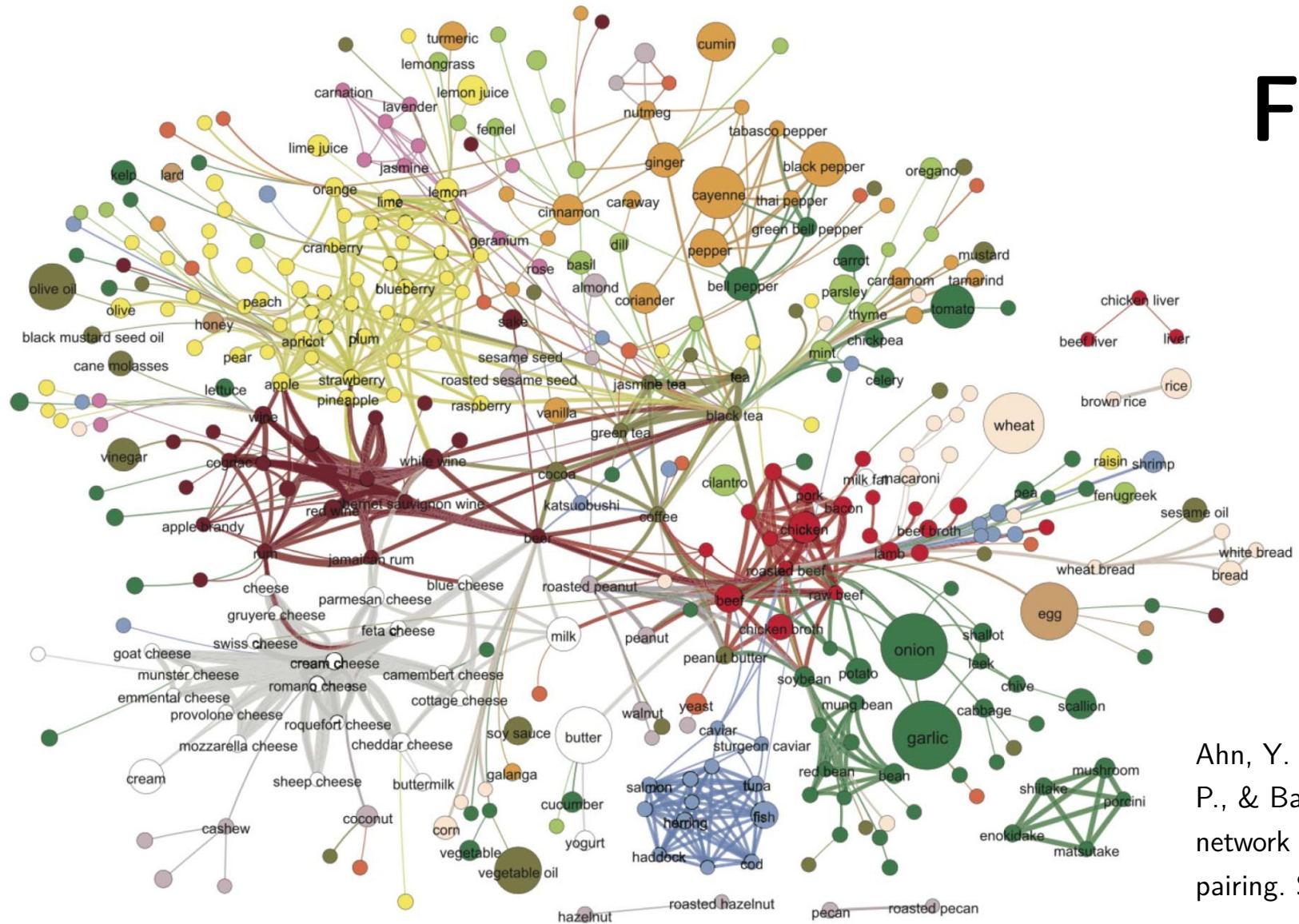
one paper that cites:

a paper  $u$  in  $T_1$  and

a paper  $v$  in  $T_2$ .

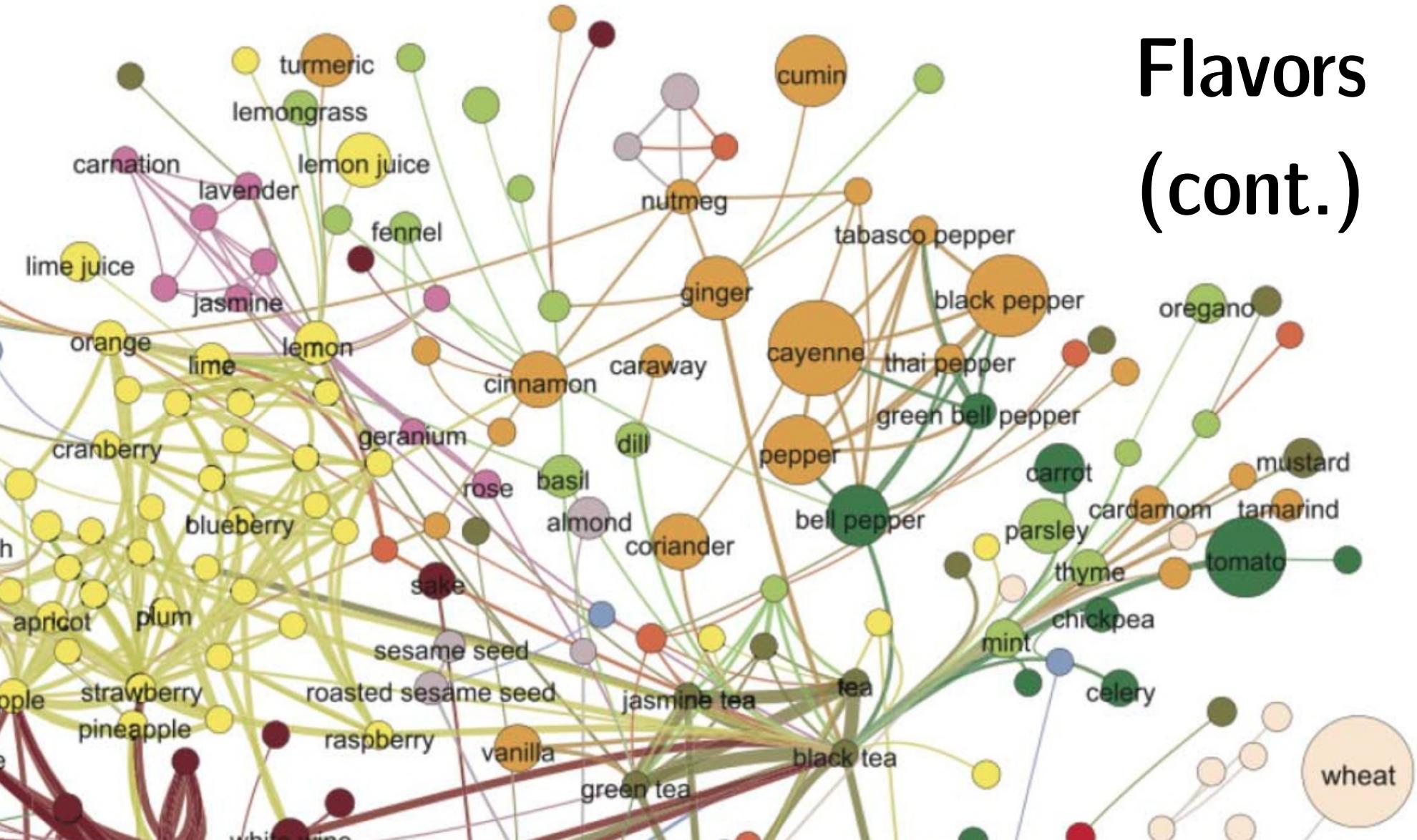


# Flavors

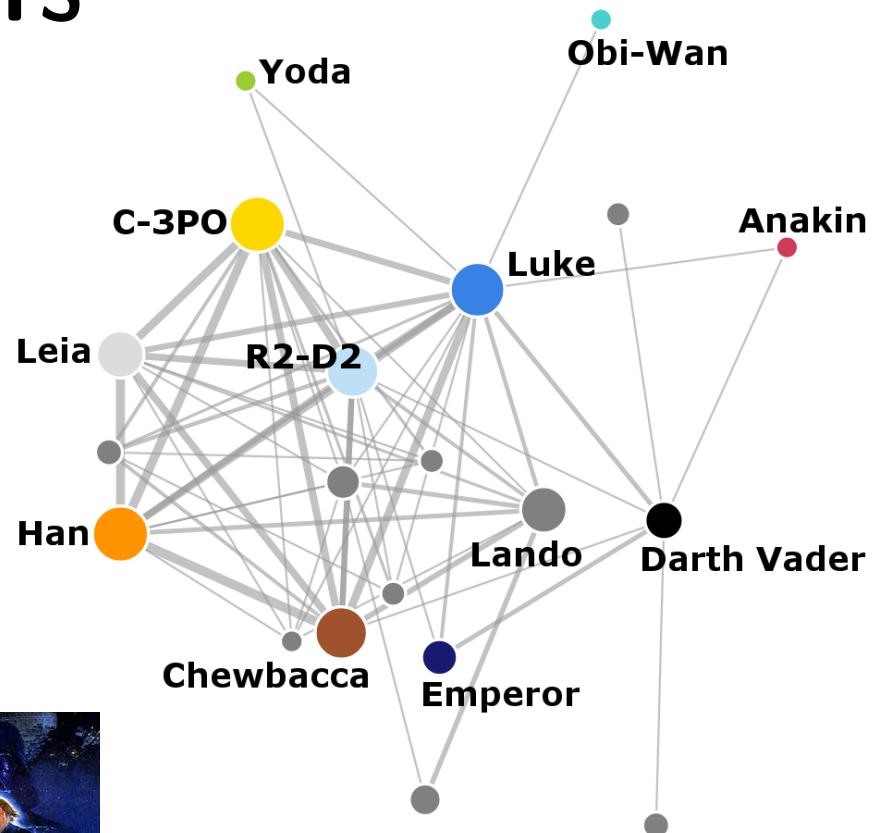
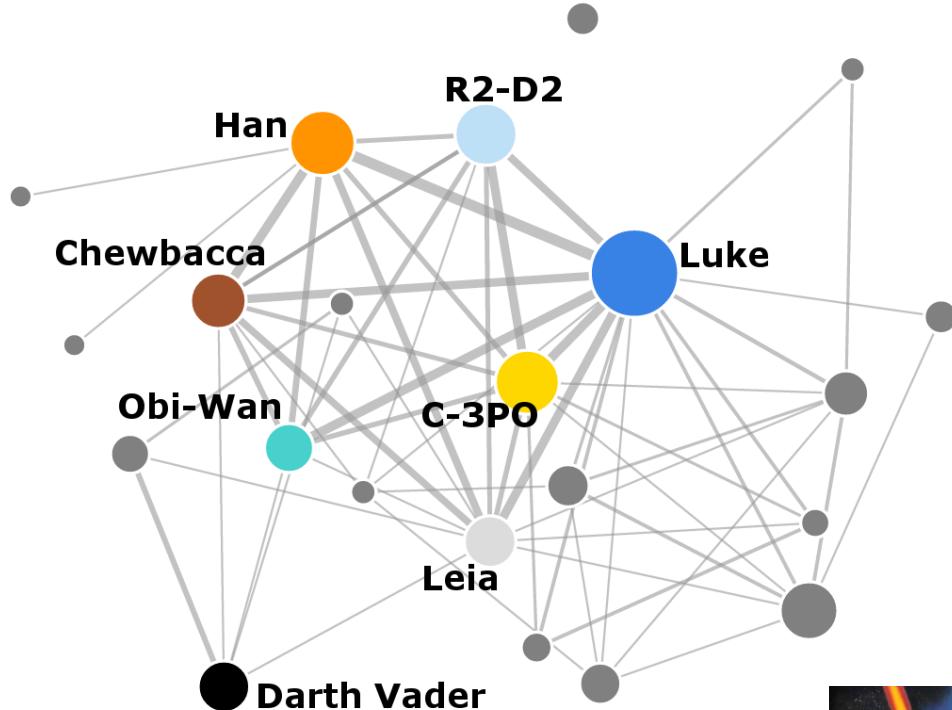


Ahn, Y. Y., Ahnert, S. E., Bagrow, J. P., & Barabási, A. L. (2011). Flavor network and the principles of food pairing. *Scientific reports*, 1, 196.

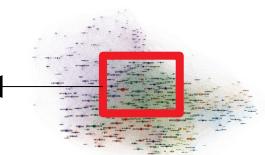
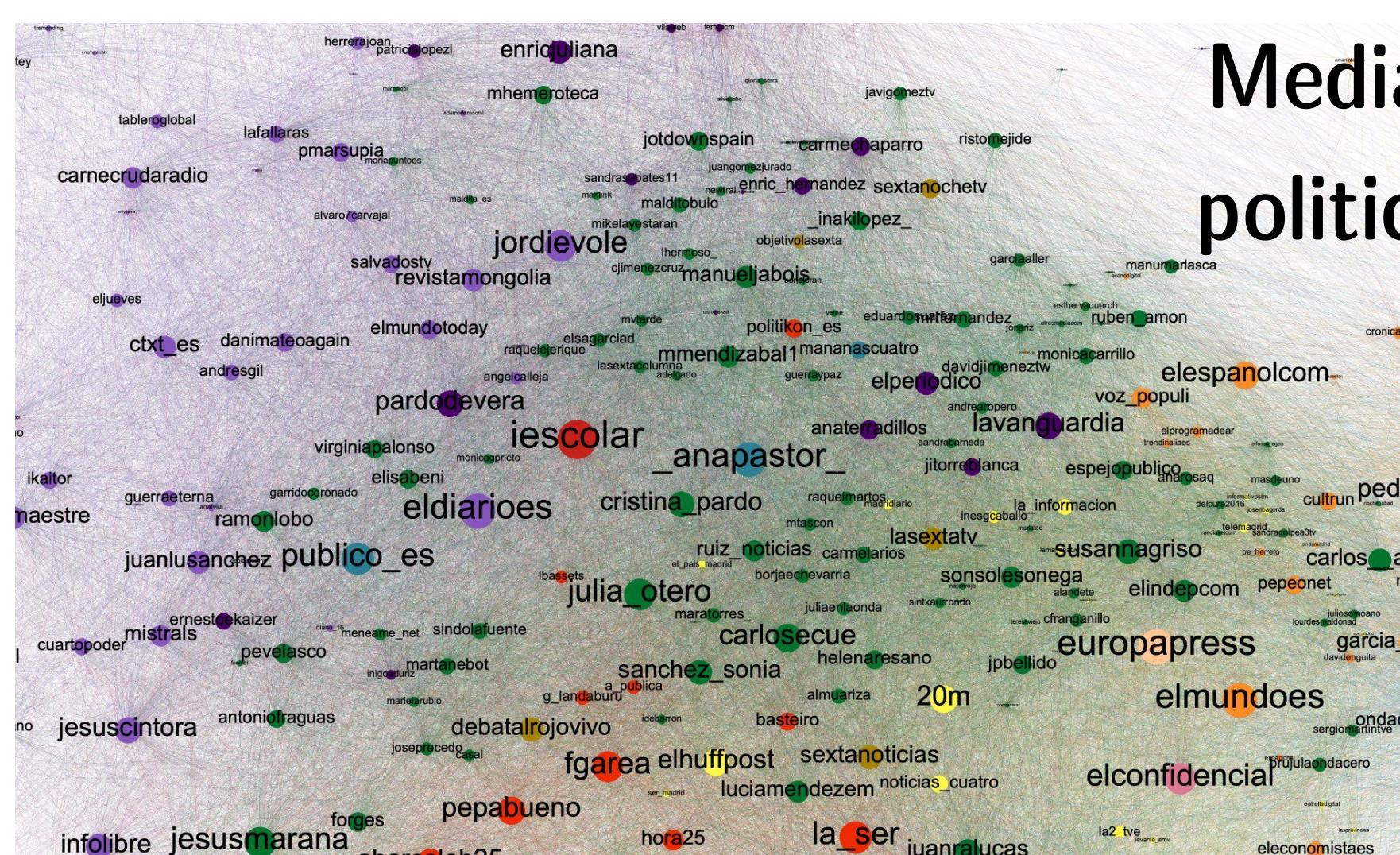
# Flavors (cont.)



# Star Wars



# Media and politicians?

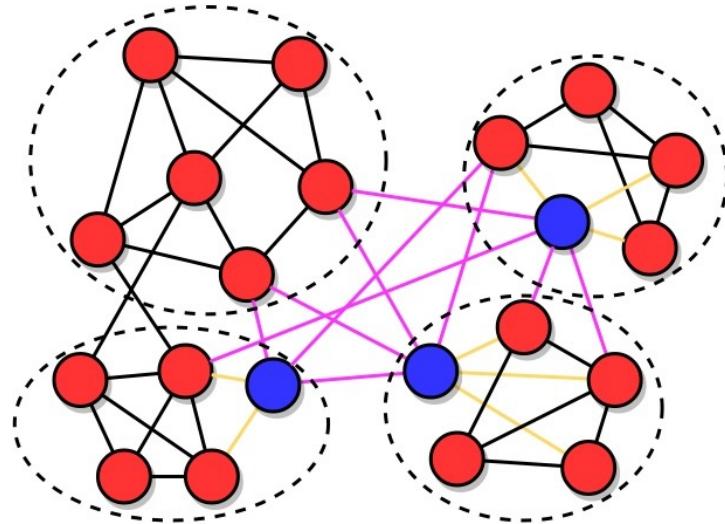


<https://twitter.com/jbo/status/1120444347772821504/photo/1>

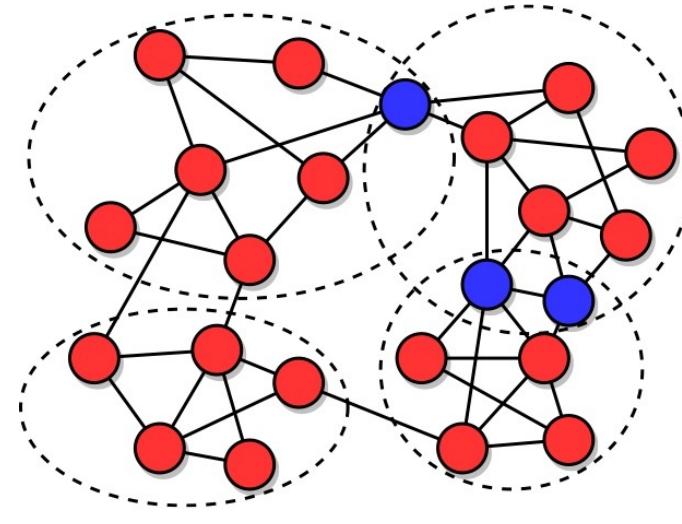
# Partitions vs Overlapping communities

## Hierarchical communities

# Partition vs Overlapping communities



Partition, or *hard* clusters

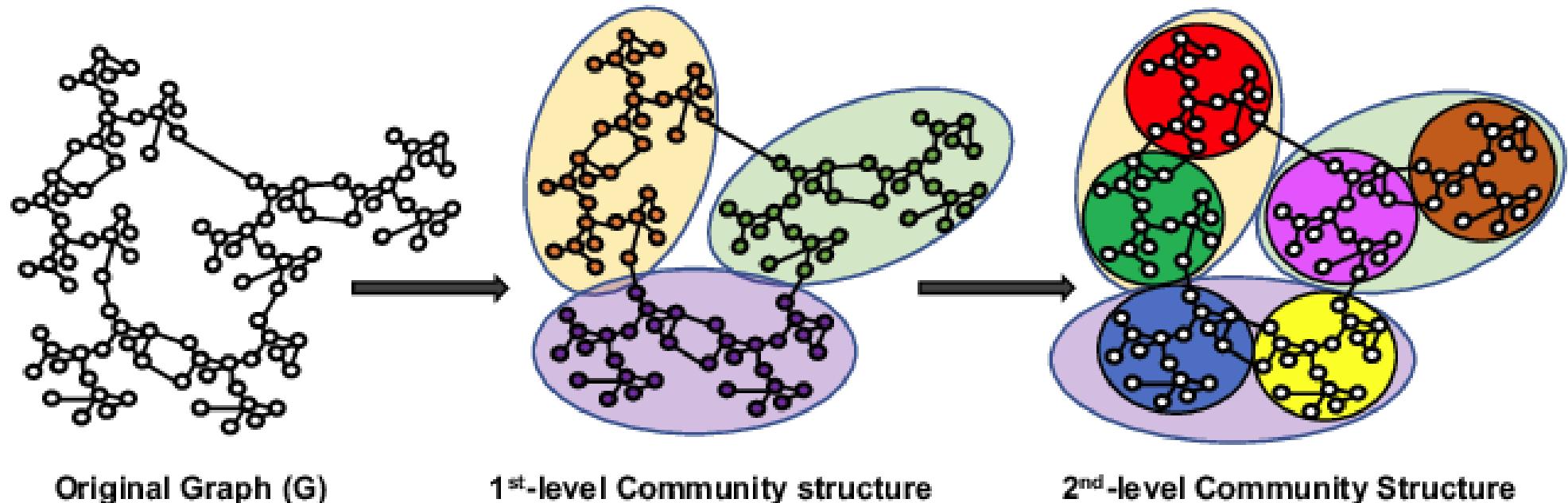


Overlapping communities, or *soft* clusters

What's special about blue nodes?

Blue nodes are in more than one community

# Hierarchical communities



Original Graph ( $G$ )

1<sup>st</sup>-level Community structure

2<sup>nd</sup>-level Community Structure

# Summary

# Things to remember

- Many networks have community structure
- Sometimes it's:
  - One dense sub-graph
  - Two communities (polarization)
  - Multiple communities
- Partitions vs overlapping communities
- Hierarchical communities