

**1 Measurement of the Drell-Yan Absolute Cross-Section  
2 in  $pp$  and  $pd$  Collisions with a 120 GeV Proton Beam at  
3 Fermilab**

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**7 Abstract**

This analysis note reports on the determination of  $pp$  and  $pd$  Drell-Yan absolute cross sections from data collected using the Roadset 67 trigger. We seek preliminary approval of these results for presentation in upcoming conferences. This work extends previous analyses by incorporating both Liquid Hydrogen ( $LH_2$ ) and Liquid Deuterium ( $LD_2$ ) target data. Furthermore, significant updates to the efficiency corrections have been implemented. The reconstruction efficiency is now calculated using a global curve based on the  $D1$  occupancy variable, integrated over all kinematic bins, as demonstrated in DocDB 11427. Additionally, the hodoscope efficiency correction has been upgraded from a constant factor to a dimuon-level calculation using RoadIDs and paddle-specific efficiencies (DocDB 11467). In this work, we report the measurement of the double-differential Drell-Yan cross-sections,  $d^2\sigma/dx_F dM$ , and compare the results with theoretical predictions from Quantum Chromodynamics (QCD).

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78 

## 1 Introduction

79 The Drell-Yan process, where a quark from one hadron annihilates with an antiquark from  
80 another to produce a lepton-antilepton pair ( $q\bar{q} \rightarrow \ell^+\ell^-$ ), provides a clean and direct probe  
81 of the antiquark structure of nucleons. Over the past several decades, Drell-Yan experiments  
82 have been instrumental in mapping the parton distribution functions (PDFs) of the proton and  
83 other hadrons. However, most existing data are concentrated at small to moderate values of  
84 the parton momentum fraction,  $x < 0.3$ . The region of large  $x$  ( $x > 0.3$ ) remains relatively  
85 unexplored, yet it is crucial for understanding phenomena such as the flavor asymmetry of the  
86 proton's light antiquark sea ( $\bar{d}(x)/\bar{u}(x)$ ) and the fundamental mechanisms of non-perturbative  
87 QCD that govern hadron structure.

88 The SeaQuest experiment (E906) at Fermilab was designed specifically to explore this high- $x$   
89 frontier. By impinging a high-intensity 120 GeV proton beam from the Main Injector onto various  
90 fixed targets, including liquid hydrogen ( $LH_2$ ) and liquid deuterium ( $LD_2$ ), SeaQuest measures  
91 dimuon production in a kinematic region sensitive to antiquarks carrying a large fraction of the  
92 nucleon's momentum.

93 This analysis presents a measurement of the absolute double-differential Drell-Yan cross-  
94 section, binned in the dimuon invariant mass ( $M$ ) and Feynman- $x$  ( $x_F$ ), using data collected  
95 with the  $LH_2$  and  $LD_2$  targets. The p+p collisions are primarily sensitive to the  $\bar{u}$  distribution  
96 in the proton, while the p+d collisions provide information on the sum of  $\bar{u}$  and  $\bar{d}$ . These results  
97 provide stringent new constraints on modern PDF parameterizations in the valence-dominated  
98 region.

99 The cross-section is presented in its scaling form, which, in the leading-order Drell-Yan  
100 model, is independent of the center-of-mass energy,  $\sqrt{s}$ :

$$101 M^3 \frac{d^2\sigma}{dMdx_F} = f(\tau) \quad (1)$$

102 where  $\tau = M^2/s$ . The experimental determination of this quantity requires a precise under-  
103 standing of the integrated luminosity, detector acceptance, and reconstruction efficiencies, which  
104 are detailed in the subsequent sections of this document.

104 

## 2 Analysis Methodology

105 The extraction of the Drell-Yan cross-section from the raw data involves several distinct steps:  
106 selecting candidate dimuon events, subtracting backgrounds, calculating the integrated luminos-  
107 ity, and correcting for detector- and reconstruction-related inefficiencies.

108 

### 2.1 Data and Monte Carlo Samples

109 This analysis utilizes the “Roadset 67” dataset collected by the SeaQuest experiment. The  
110 primary data files for the liquid hydrogen ( $LH_2$ ) target and the corresponding empty “flask”  
111 target runs are saved in:

112 `/seaquest/users/apun/e906_projects/rs67_merged_files/`  
113 • **Data ( $LH_2$  Target):** `merged_RS67_3089LH2.root`  
114 • **Data ( $LD_2$  Target):** `merged_RS67_3089LD2.root`  
115 • **Background (Empty Flask):** `merged_RS67_3089Flask.root`

116 To properly correct for detector performance, we calculate the hodoscope and reconstruction  
117 efficiency corrections at the dimuon level. The above ROOT files were modified by adding the  
118 following variables to each event:

- `recoeff`: reconstruction efficiency correction
  - `recoeff_error`: propagated uncertainty of the reconstruction efficiency correction
  - `hodoeff`: hodoscope efficiency correction
  - `hodoeff_error`: propagated uncertainty of the hodoscope efficiency correction
- The updated datasets containing these variables are saved in the following locations:
- `/seaquest/users/ckuruppu/rootfiles/rs67/merged_RS67_3089_LH2_recoeff_hodoeff.root`
  - `/seaquest/users/ckuruppu/rootfiles/rs67/merged_RS67_3089_LD2_recoeff_hodoeff.root`
  - `/seaquest/users/ckuruppu/rootfiles/rs67/merged_RS67_3089_Flask_recoeff_hodoeff.root`
- The empty flask data are crucial for subtracting contributions from beam interactions with the target vessel walls and other upstream material.
- To correct for detector acceptance and reconstruction efficiencies, extensive Monte Carlo (MC) simulations were employed. The simulations model the Drell-Yan process and propagate the resulting muons through a Geant4-based model of the SeaQuest spectrometer. The primary MC files used are:
- **Acceptance Study:** Drell-Yan events were generated over a  $4\pi$  solid angle (“thrown”) and also processed through the full detector simulation and reconstruction chain (“accepted”). This study uses the `*_M027_S001_*` series of files saved in:
- ```

/seaquest/users/chleung/pT_ReWeight/

```
- `mc_drellyan_LH2_M027_S001_4pi_pTxFweight_v2.root`
  - `mc_drellyan_LH2_M027_S001_clean_occ_pTxFweight_v2.root`
  - `mc_drellyan_LH2_M027_S001_messy_occ_pTxFweight_v2.root`
  - `mc_drellyan_LD2_M027_S001_4pi_pTxFweight_v2.root`
  - `mc_drellyan_LD2_M027_S001_clean_occ_pTxFweight_v2.root`
  - `mc_drellyan_LD2_M027_S001_messy_occ_pTxFweight_v2.root`
- **Efficiency Study:** To model the effect of high detector occupancy on track reconstruction, simulated events were processed with (“messy”) and without (“clean”) the overlay of random background hits from experimental data. This study uses the `*_M027_S001_*` series of files also saved in the same location.
- All MC samples are weighted on an event-by-event basis to match the transverse momentum ( $p_T$ ) distribution observed in the data.
- ## 2.2 Event Selection
- A multi-tiered set of selection criteria is applied to isolate high-quality Drell-Yan dimuon events from the large background of other processes.
- **Data Quality:** Only data from “good spills,” as identified by standard run quality monitoring, are included in the analysis. A physics trigger condition (`MATRIX1 == 1`) is required, selecting events consistent with the passage of two muons through the spectrometer.

156 • **Track and Dimuon Quality:** A set of stringent cuts, developed by the collaboration and  
 157 referred to as “Chuck cuts,” are applied to ensure well-reconstructed positive and negative  
 158 muon tracks that form a high-quality common vertex. These cuts impose requirements on  
 159 track  $\chi^2$ , momentum, number of hits, and fiducial volume. The full details of these cuts  
 160 are provided in Appendix 8.

161 • **Kinematic Selection:** The analysis focuses on the high-mass continuum, away from the  
 162 charmonium resonances ( $J/\psi, \psi'$ ). A cut of  $M_{\mu\mu} > 4.2$  GeV is applied. The analysis is  
 163 restricted to the kinematic range  $0 < x_F < 0.8$ .

164 After applying the event selection criteria mentioned in the Appendix, the total and mix  
 165 yields for the LH<sub>2</sub>, LD<sub>2</sub>, and Empty Flask targets in each kinematic bin are extracted. The  
 166 distributions are shown in Figure 1.

### 167 2.3 Cross-Section Formalism

168 The double-differential cross-section in a given kinematic bin ( $\Delta M, \Delta x_F$ ) is calculated as (refer  
 169 DocDB 11445-V3):

$$\frac{d^2\sigma}{dMdx_F} = \frac{1}{\epsilon_{\text{acc}}\Delta M\Delta x_F} \left[ \frac{Y_{\text{total}}^{\text{LH2}} - Y_{\text{mixed}}^{\text{LH2}}}{\langle \epsilon_{\text{signal}}^{\text{LH2}} \rangle} - \frac{I_{\text{LH2}}}{I_{\text{flask}}} \left( \frac{Y_{\text{total}}^{\text{flask}} - Y_{\text{mixed}}^{\text{flask}}}{\langle \epsilon_{\text{signal}}^{\text{flask}} \rangle} \right) \right] \quad (2)$$

170 where:

- 171 •  $Y_{\text{total}}^{\text{LH2}}$  is the total LH2 target dimuon yield after the event selection criteria.
- 172 •  $Y_{\text{mixed}}^{\text{LH2}}$  is the estimated mixed background yield from mixed events for the LH2 target.
- 173 •  $Y_{\text{total}}^{\text{flask}}$  is the total flask target dimuon yield after the event selection criteria.
- 174 •  $Y_{\text{mixed}}^{\text{flask}}$  is the estimated mixed background yield from mixed events for the flask target.
- 175 •  $\langle \epsilon_{\text{signal}}^{\text{LH2}} \rangle$  is the average signal efficiency correction for the LH2 target dimuons.
- 176 •  $\langle \epsilon_{\text{signal}}^{\text{flask}} \rangle$  is the average signal efficiency correction for the flask target dimuons.
- 177 •  $\mathcal{L}$  is the integrated luminosity for the dataset.

178 The average signal efficiency correction can be calculated as:

$$\langle \epsilon_{\text{signal}} \rangle = \frac{1}{Y_{\text{total}} - Y_{\text{mixed}}} [\langle \epsilon_{\text{total}} \rangle - \langle \epsilon_{\text{mixed}} \rangle] \quad (3)$$

179 where:

- 180 •  $\langle \epsilon_{\text{total}} \rangle$  is the average total efficiency correction for the total yield.
- 181 •  $\langle \epsilon_{\text{mixed}} \rangle$  is the average mixed efficiency correction for the mixed background yield.

182 as explained in DocDB 11448-V2.

183 In each case, efficiency correction of the  $i^{\text{th}}$  dimuon is defined as:

$$\epsilon^i = \epsilon_{\text{recon}}^i \cdot \epsilon_{\text{hodo}}^i \quad (4)$$

184 where  $\epsilon_{\text{recon}}^i$  is the reconstruction efficiency for the  $i^{\text{th}}$  dimuon and  $\epsilon_{\text{hodo}}^i$  is the hodoscope ef-  
 185 ficiency for the  $i^{\text{th}}$  dimuon. The calculation of these efficiency corrections is detailed in the  
 186 following sections.

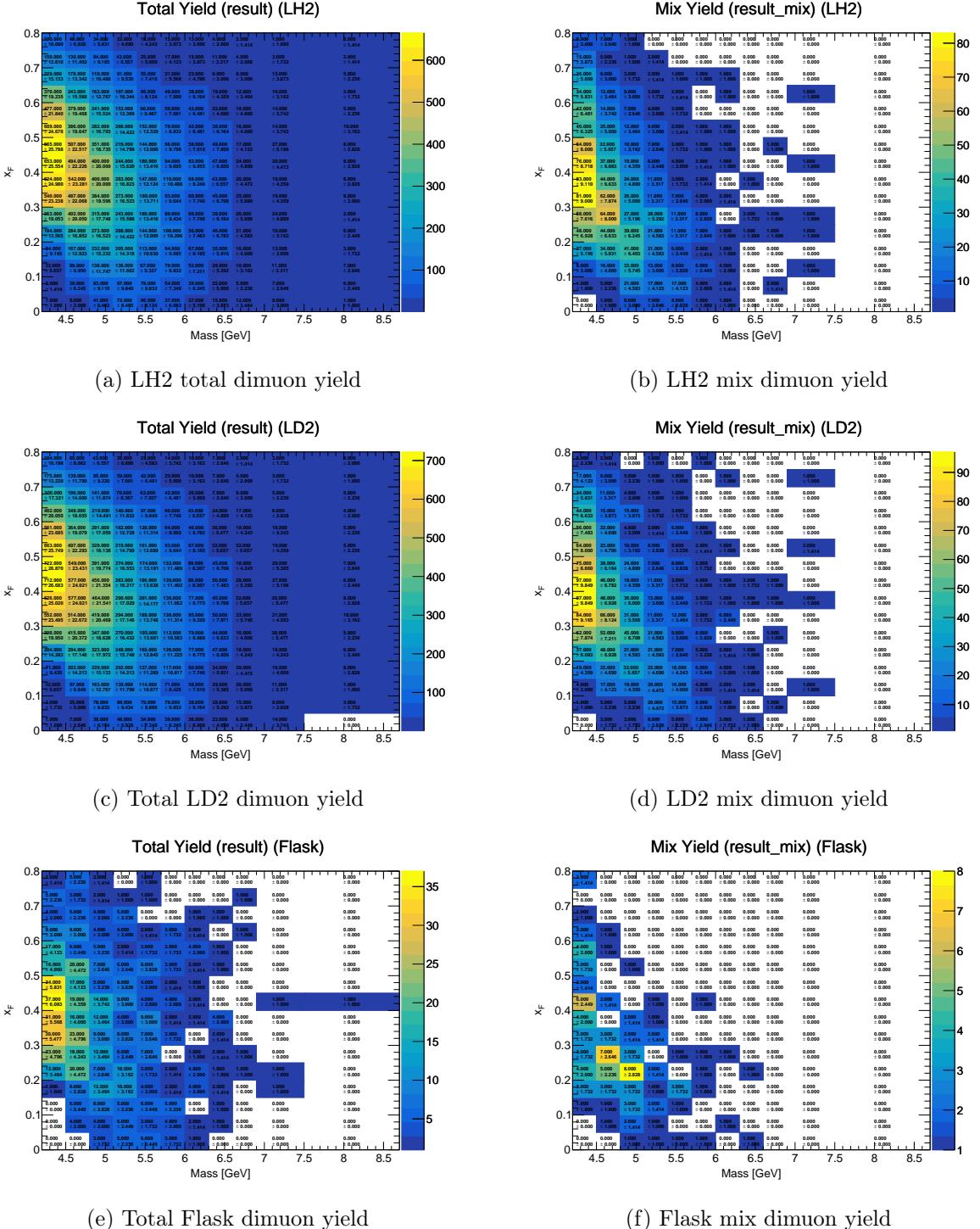


Figure 1: Dimuon distributions after applying event selection criteria.

187 The integrated luminosity,  $\mathcal{L}$ , is given by the product of the total number of protons incident  
 188 on the target and the number of target nuclei per unit area:

$$\mathcal{L} = N_{\text{incident}} \cdot \frac{N_A \rho L}{A} \cdot f_{\text{atten}} \quad (5)$$

189 Here,  $N_{\text{incident}}$  is the number of protons on target,  $N_A$  is Avogadro's number,  $\rho$  is the target  
 190 density,  $L$  is the target length,  $A$  is the molar mass, and  $f_{\text{atten}}$  is a correction factor for beam  
 191 attenuation within the thick target. For the  $L = 50.8$  cm long LH<sub>2</sub> target, with a density of

<sup>192</sup>  $\rho_H = 0.0708 \text{ g/cm}^3$ , the target thickness is  $3.5966 \text{ g/cm}^2$  with a beam attenuation factor of  
<sup>193</sup> 0.966. Also,  $\epsilon_{\text{acc}}$  is the geometric and kinematic acceptance of the spectrometer.

## <sup>194</sup> 3 Acceptance and Efficiency Corrections

### <sup>195</sup> 3.1 Detector Acceptance Correction

<sup>196</sup> The SeaQuest spectrometer has a finite geometric acceptance, which limits the fraction of pro-  
<sup>197</sup> duced dimuon events that can be detected. This acceptance depends strongly on the event  
<sup>198</sup> kinematics, primarily the dimuon invariant mass ( $M$ ) and Feynman- $x$  ( $x_F$ ). The acceptance  
<sup>199</sup> correction factor is determined using MC simulations.

<sup>200</sup> The acceptance,  $A(M, x_F)$ , is defined as the ratio of the number of simulated events that  
<sup>201</sup> are successfully reconstructed and pass all analysis cuts ( $N_{\text{reco}}$ ) to the total number of events  
<sup>202</sup> generated in a given kinematic bin ( $N_{\text{gen}}$ ):

$$\text{Acceptance (A)} = \frac{N_{\text{reco}}}{N_{\text{gen}}} \quad (6)$$

<sup>203</sup> This calculation is performed in bins of  $M$  and  $x_F$ . The kinematic binning used for this study  
<sup>204</sup> is defined by the following edges:

- <sup>205</sup> •  $x_F$  Edges:  $\{0, 0.05, 0.1, \dots, 0.8\}$  (16 bins)
- <sup>206</sup> • Mass Edges ( $\text{GeV}/c^2$ ):  $\{4.2, 4.5, 4.8, 5.1, 5.4, 5.7, 6, 6.3, 6.6, 6.9, 7.5, 8.7\}$  (11 bins)

<sup>207</sup> The following pages show the calculated acceptance as a function of mass for each of the  
<sup>208</sup> 16  $x_F$  bins. The plots show the acceptance for the  $\text{LH}_2$  and  $\text{LD}_2$  targets, their combined  
<sup>209</sup> average, and their ratio. The ratio is close to unity across the kinematic range, indicating that  
<sup>210</sup> target-dependent effects on the acceptance are small. In this case, we compare newly calculated  
<sup>211</sup> acceptance corrections to the existing acceptance calculations saved in Shivangi's file:

<sup>212</sup> `./shivangi/work/analysis/R008/diffCross/v42/5770/looseCut/final/acceptance_h.root`

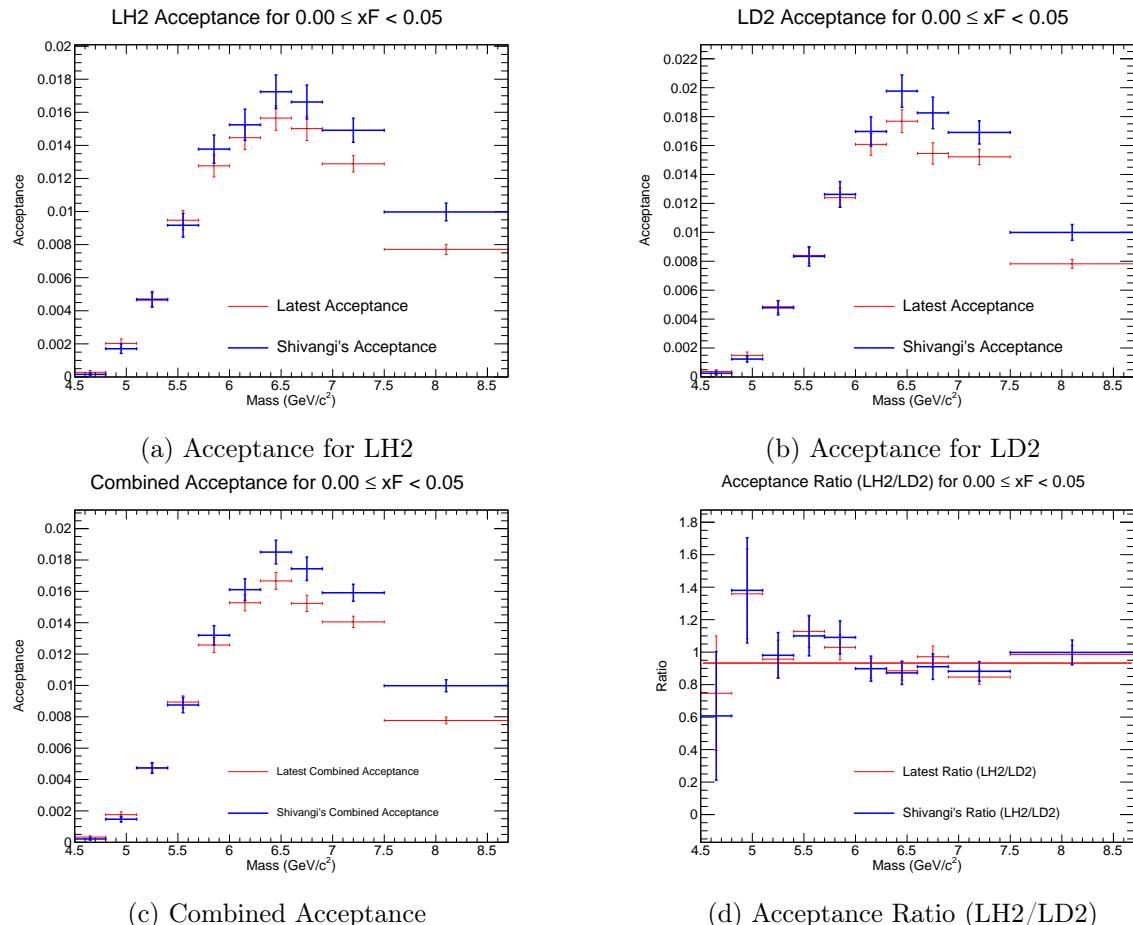


Figure 2: Acceptance plots for  $0.00 \leq x_F < 0.05$ .

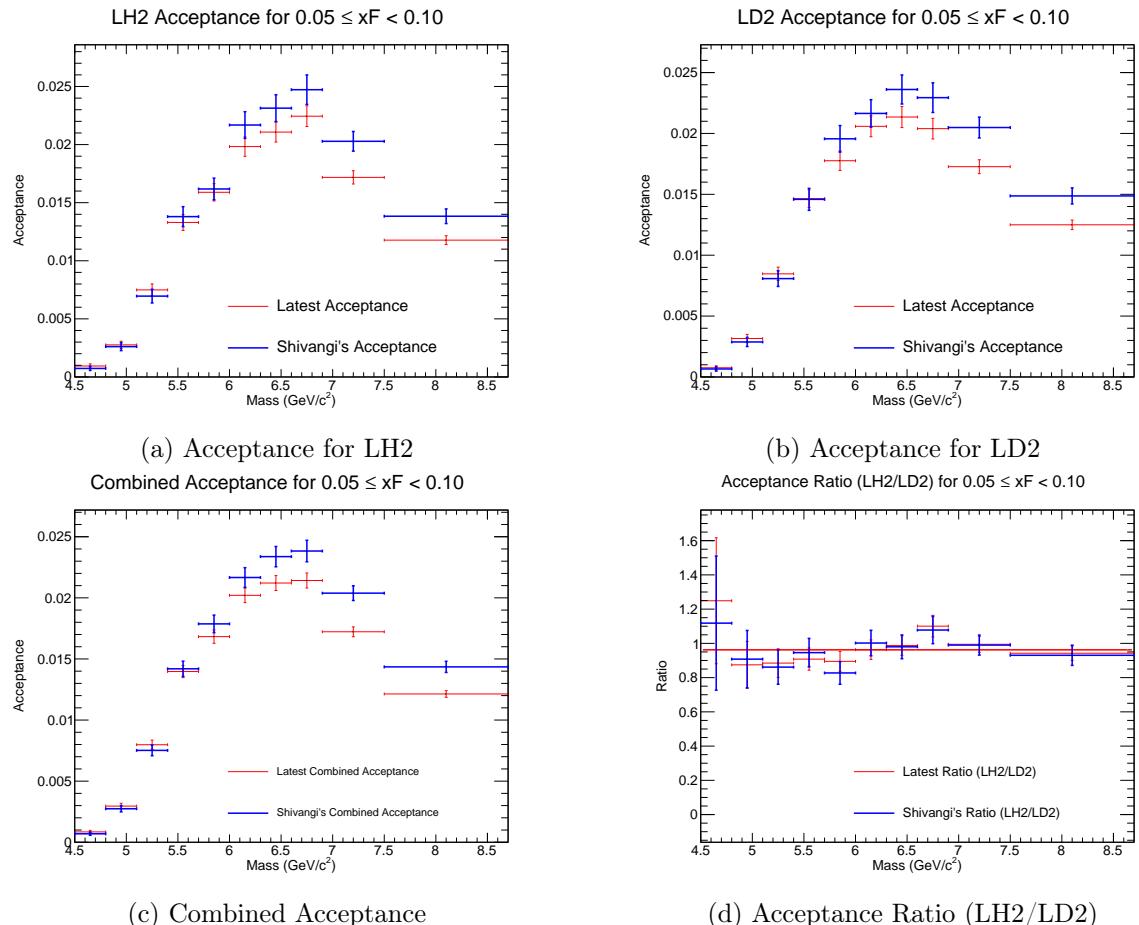


Figure 3: Acceptance plots for  $0.05 \leq x_F < 0.10$ .

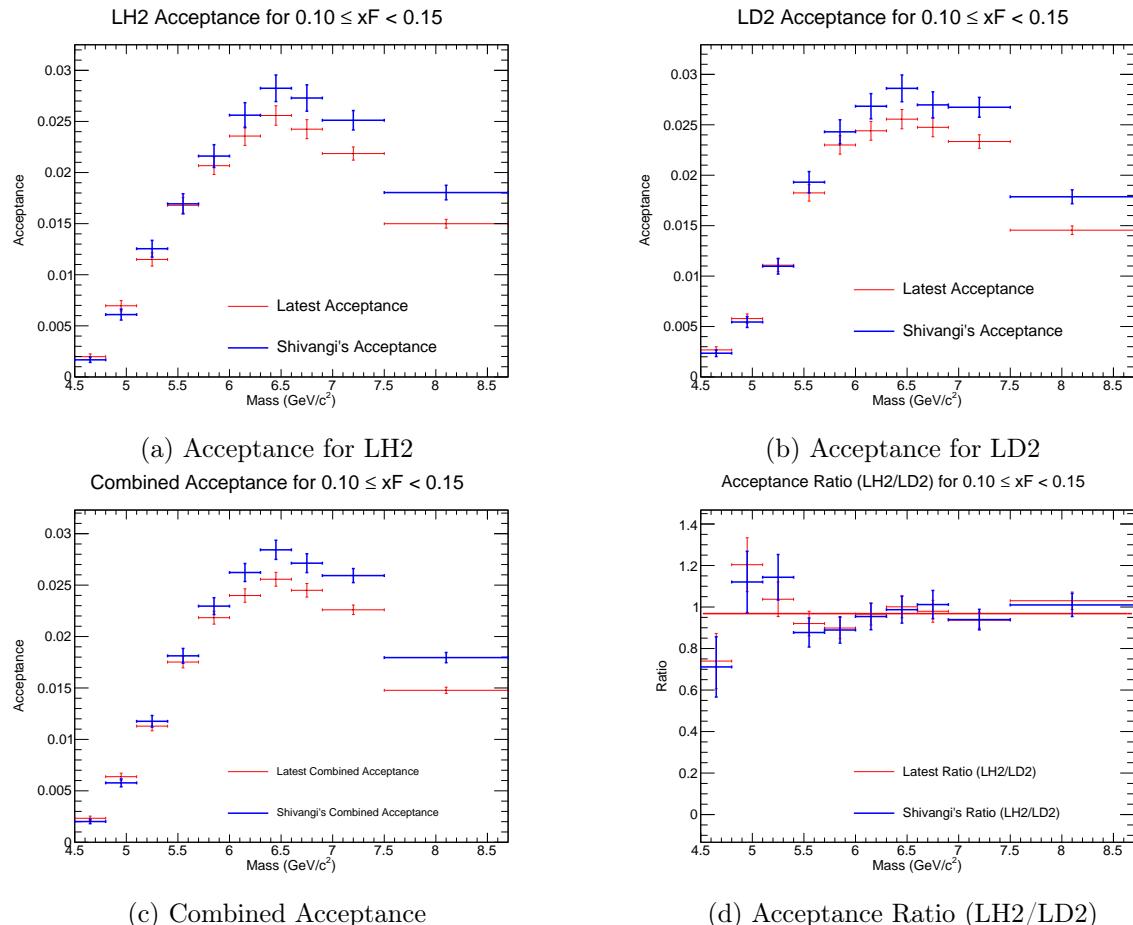


Figure 4: Acceptance plots for  $0.10 \leq x_F < 0.15$ .

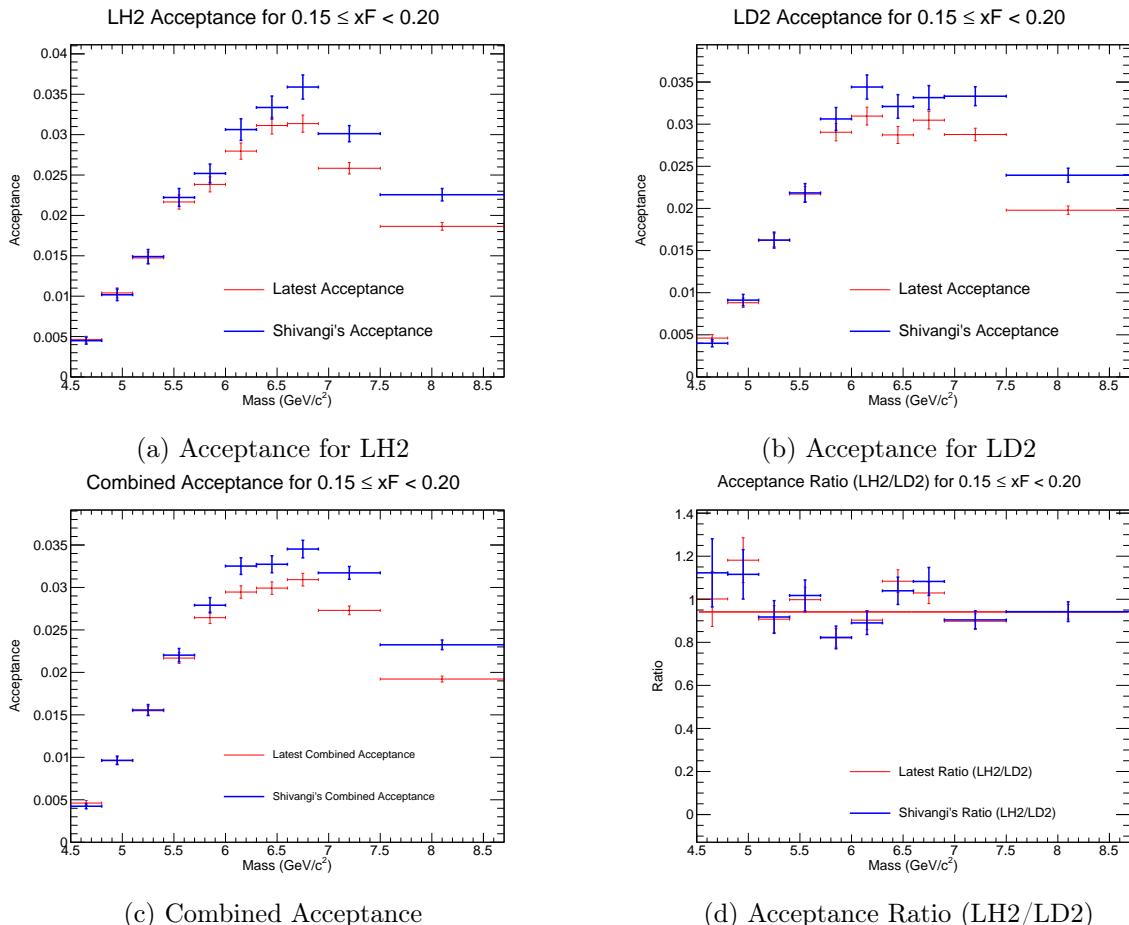


Figure 5: Acceptance plots for  $0.15 \leq x_F < 0.20$ .

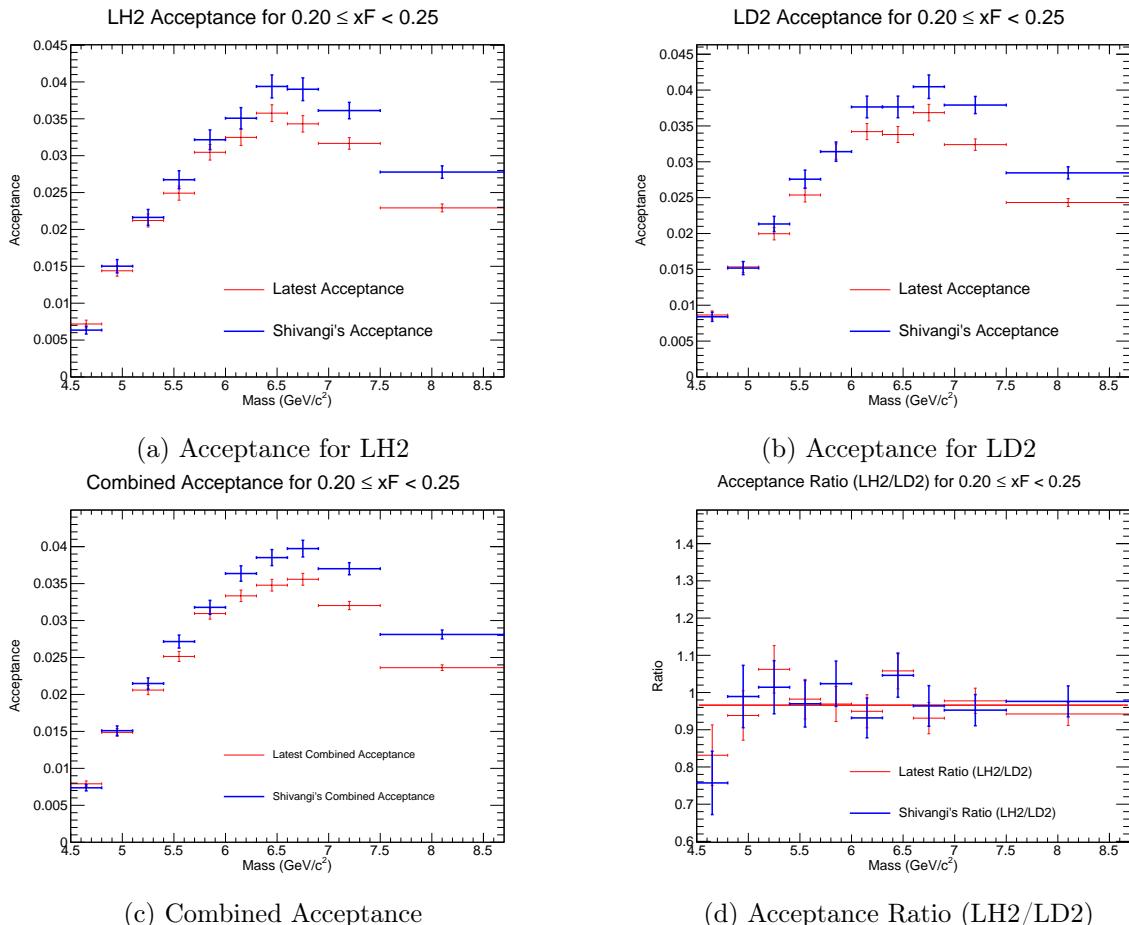


Figure 6: Acceptance plots for  $0.20 \leq x_F < 0.25$ .

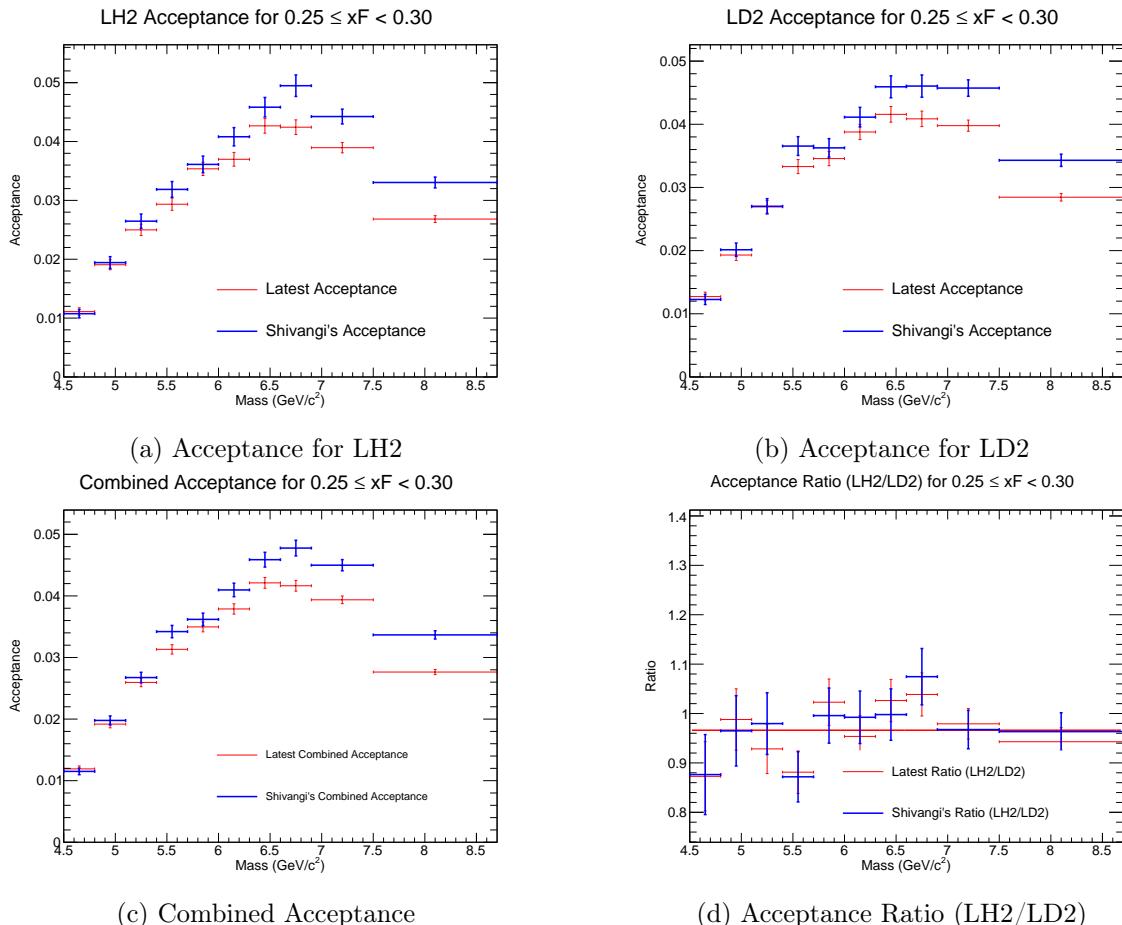


Figure 7: Acceptance plots for  $0.25 \leq x_F < 0.30$ .

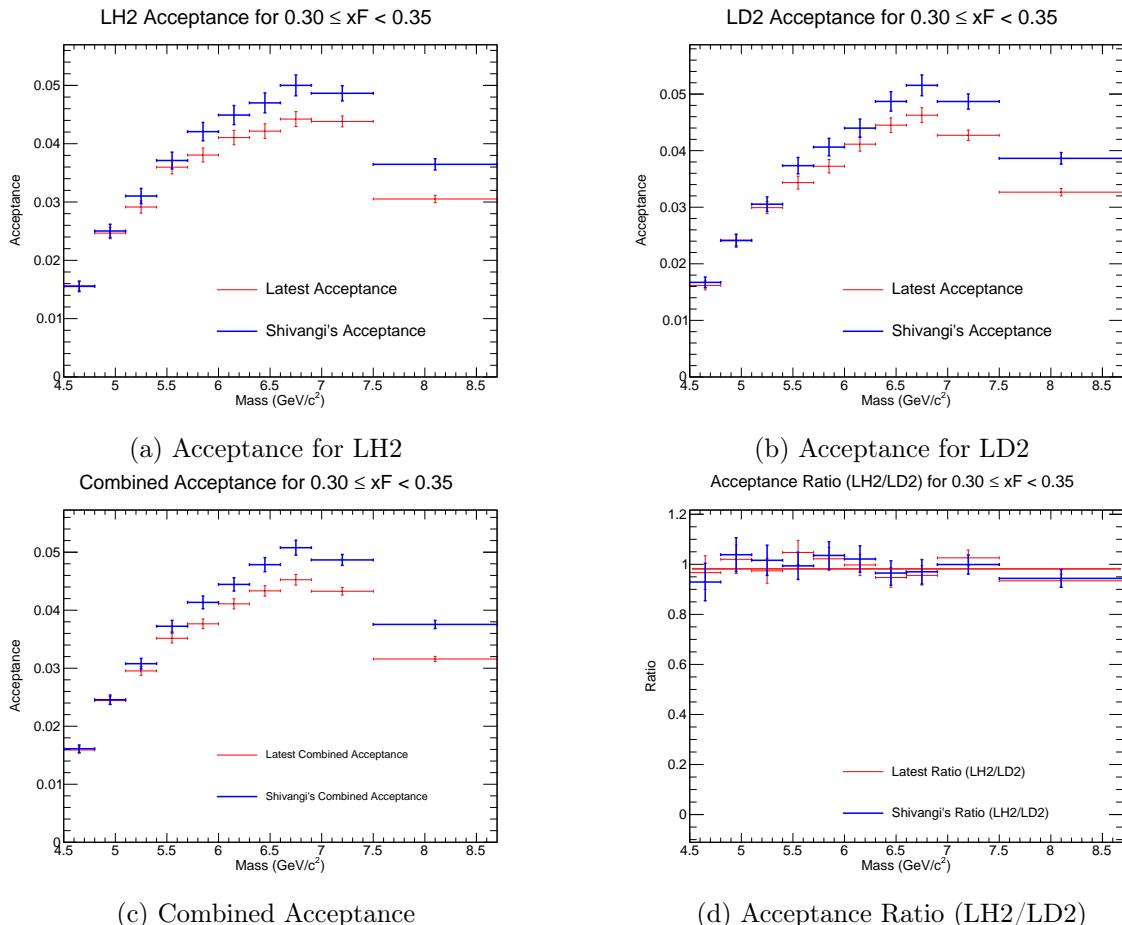


Figure 8: Acceptance plots for  $0.30 \leq x_F < 0.35$ .

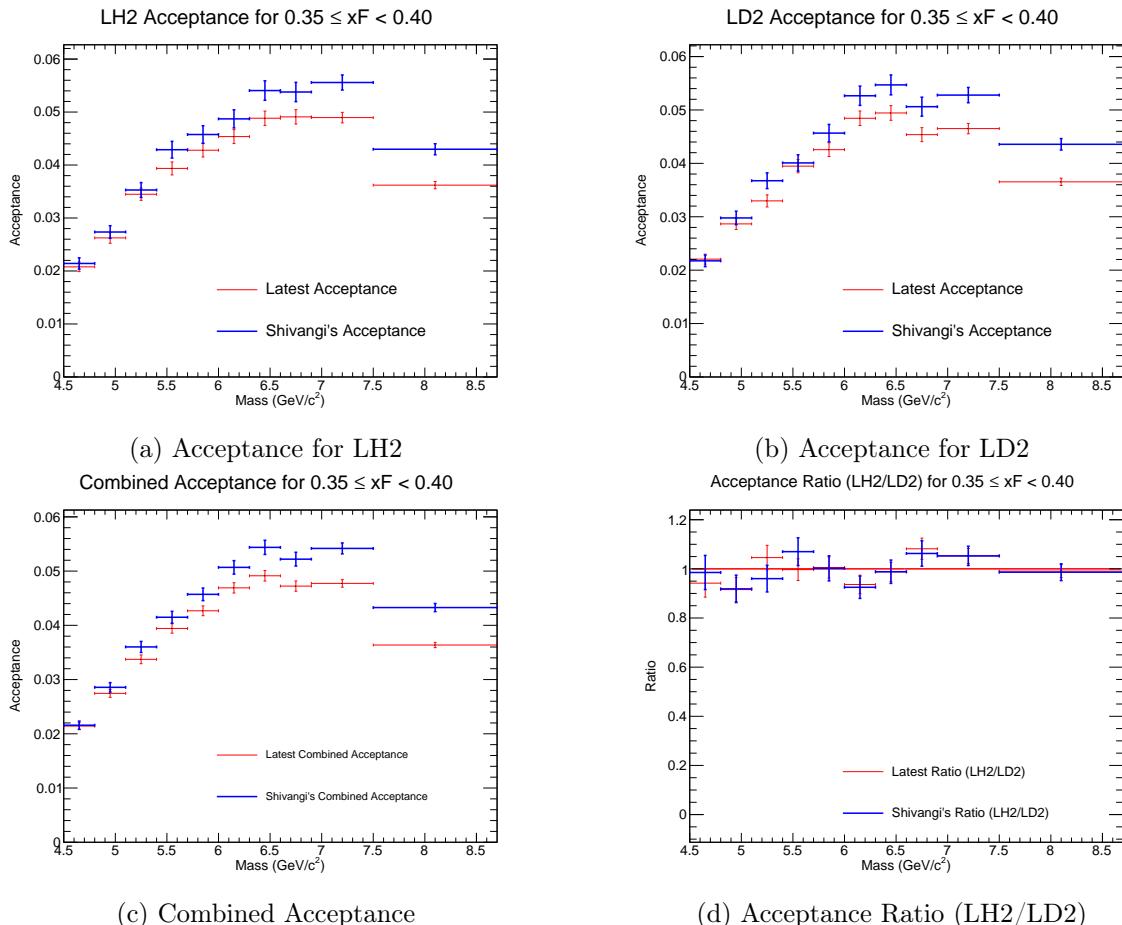


Figure 9: Acceptance plots for  $0.35 \leq x_F < 0.40$ .

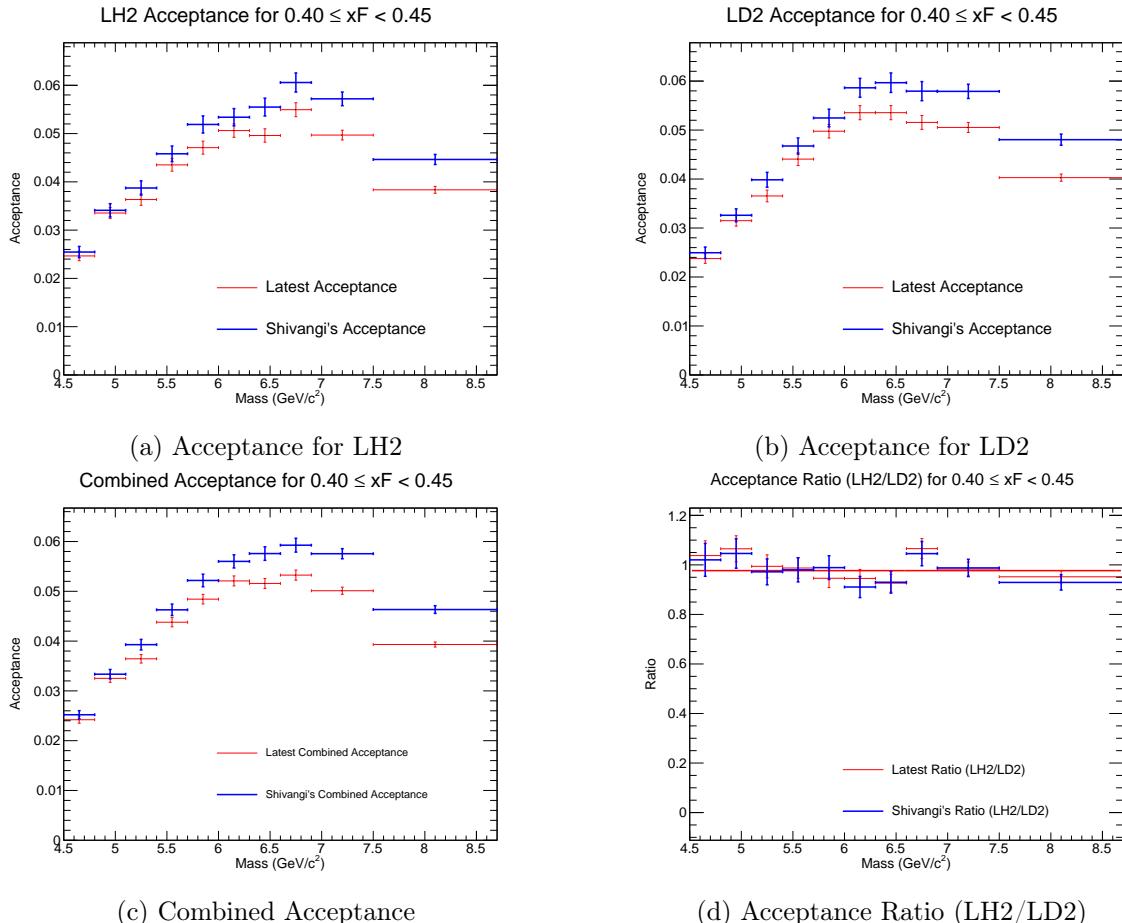


Figure 10: Acceptance plots for  $0.40 \leq x_F < 0.45$ .

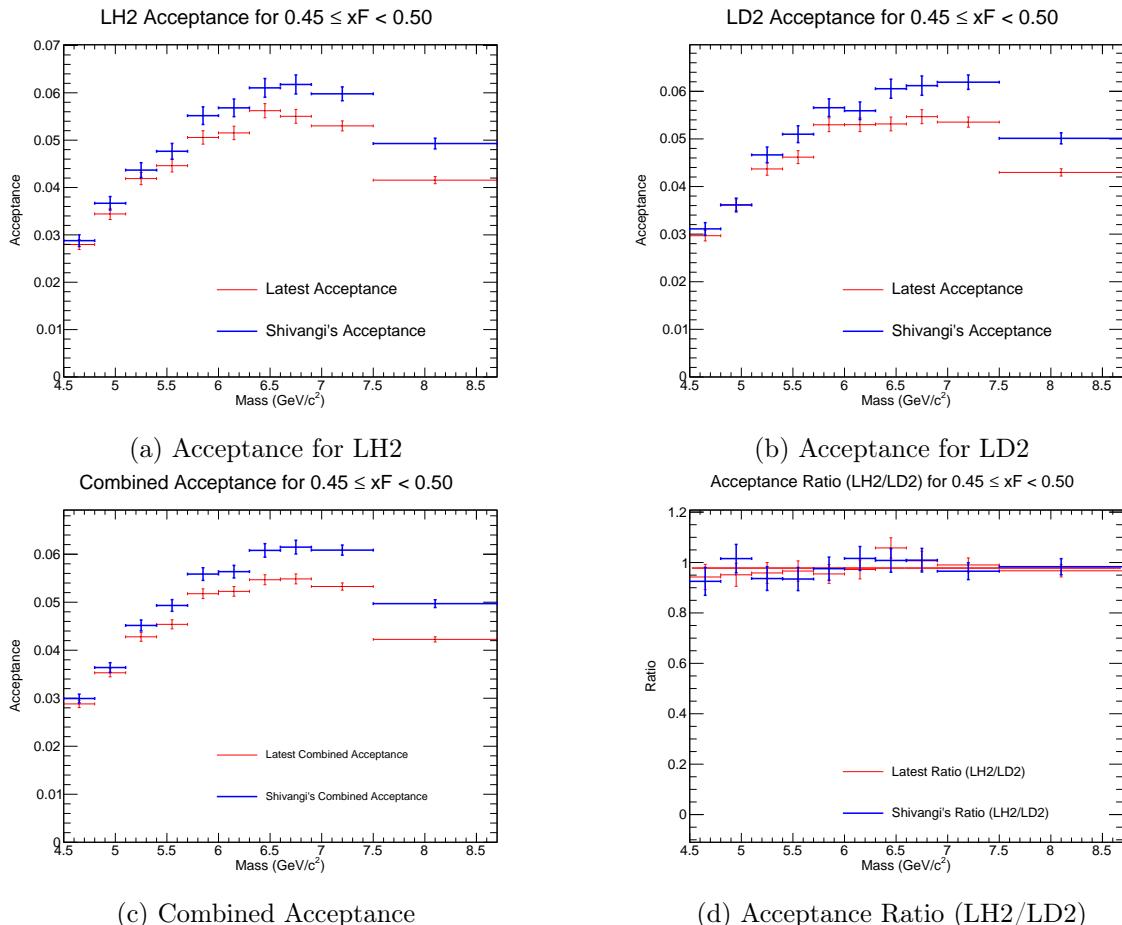


Figure 11: Acceptance plots for  $0.45 \leq x_F < 0.50$ .

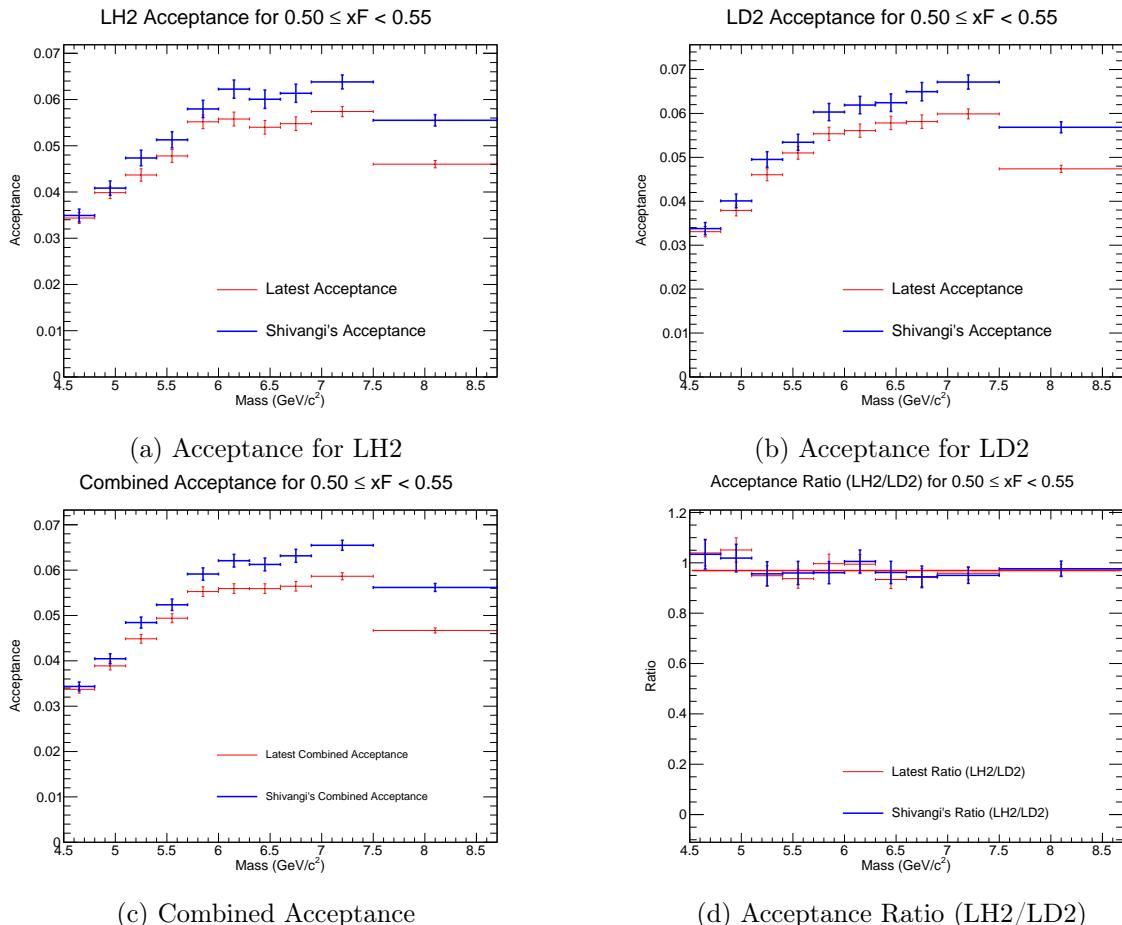


Figure 12: Acceptance plots for  $0.50 \leq x_F < 0.55$ .

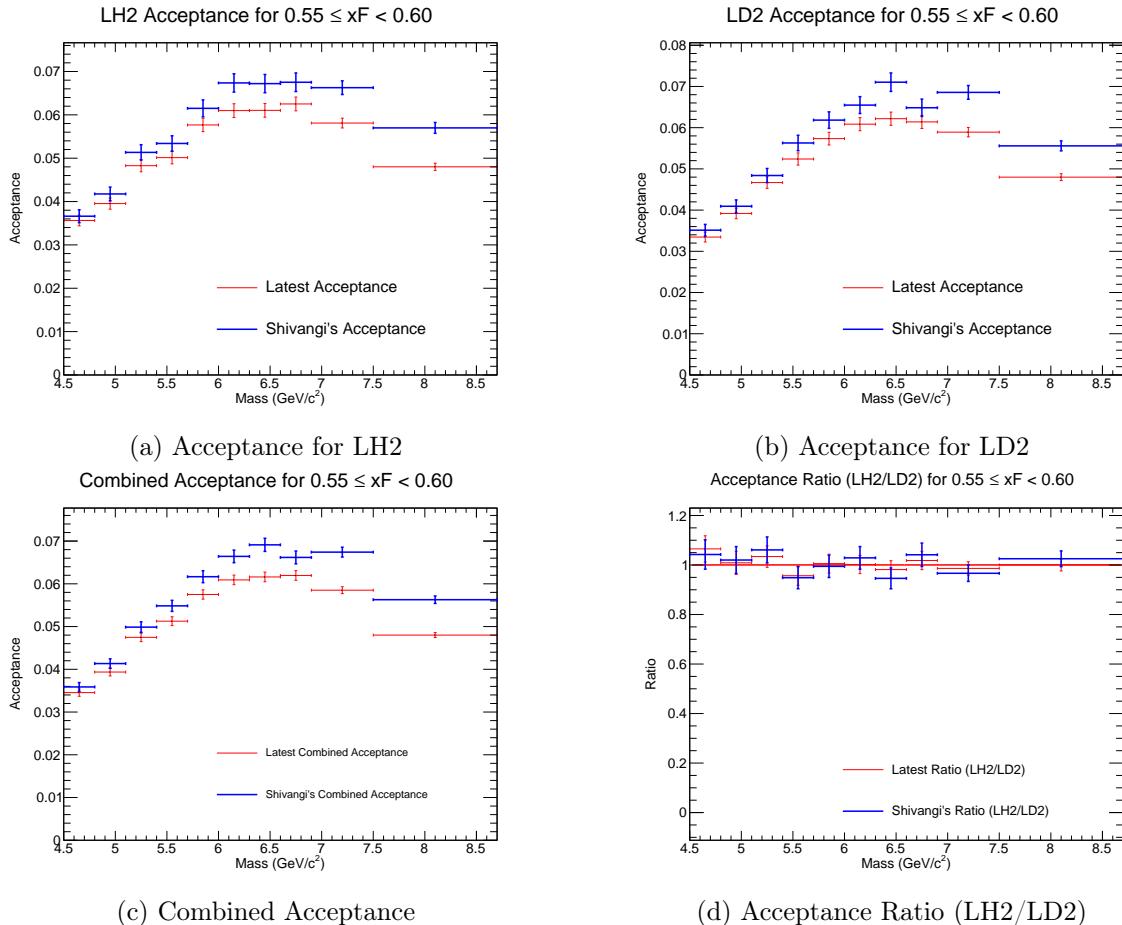


Figure 13: Acceptance plots for  $0.55 \leq x_F < 0.60$ .

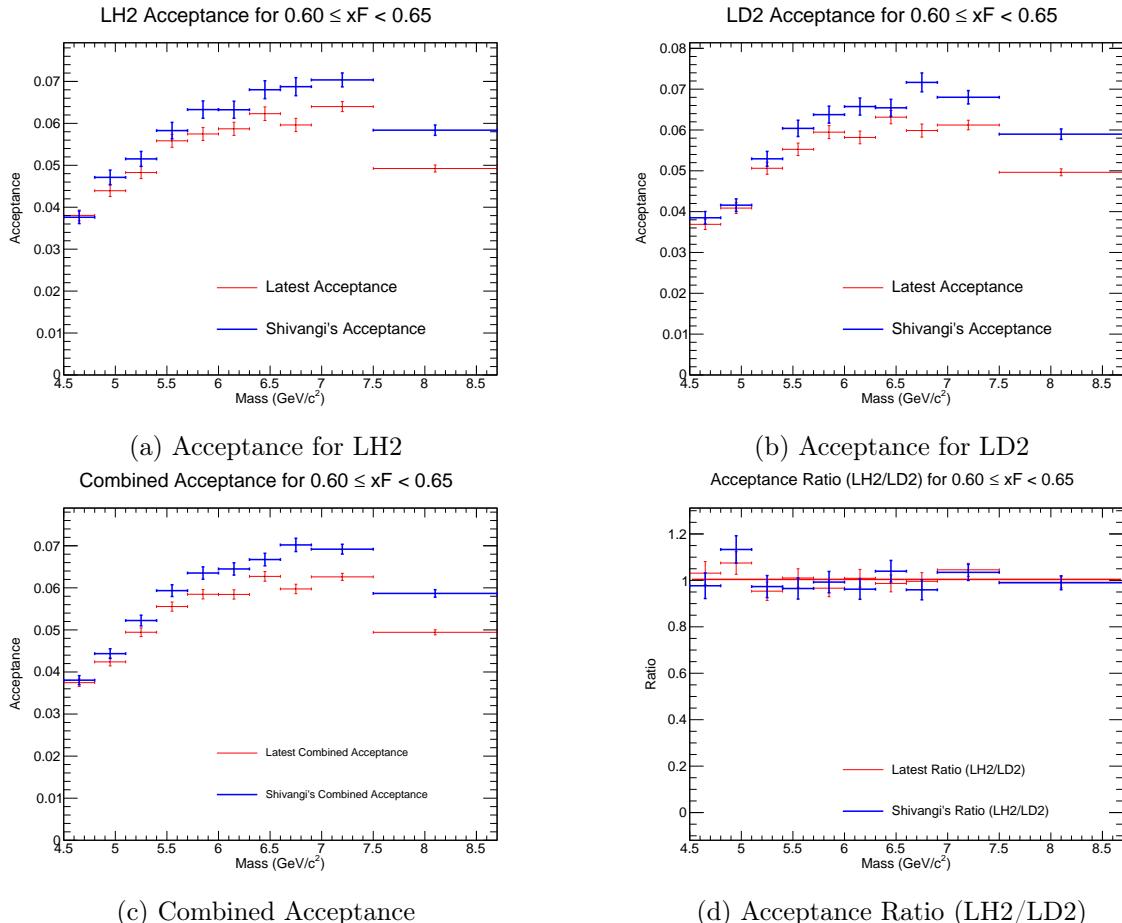


Figure 14: Acceptance plots for  $0.60 \leq x_F < 0.65$ .

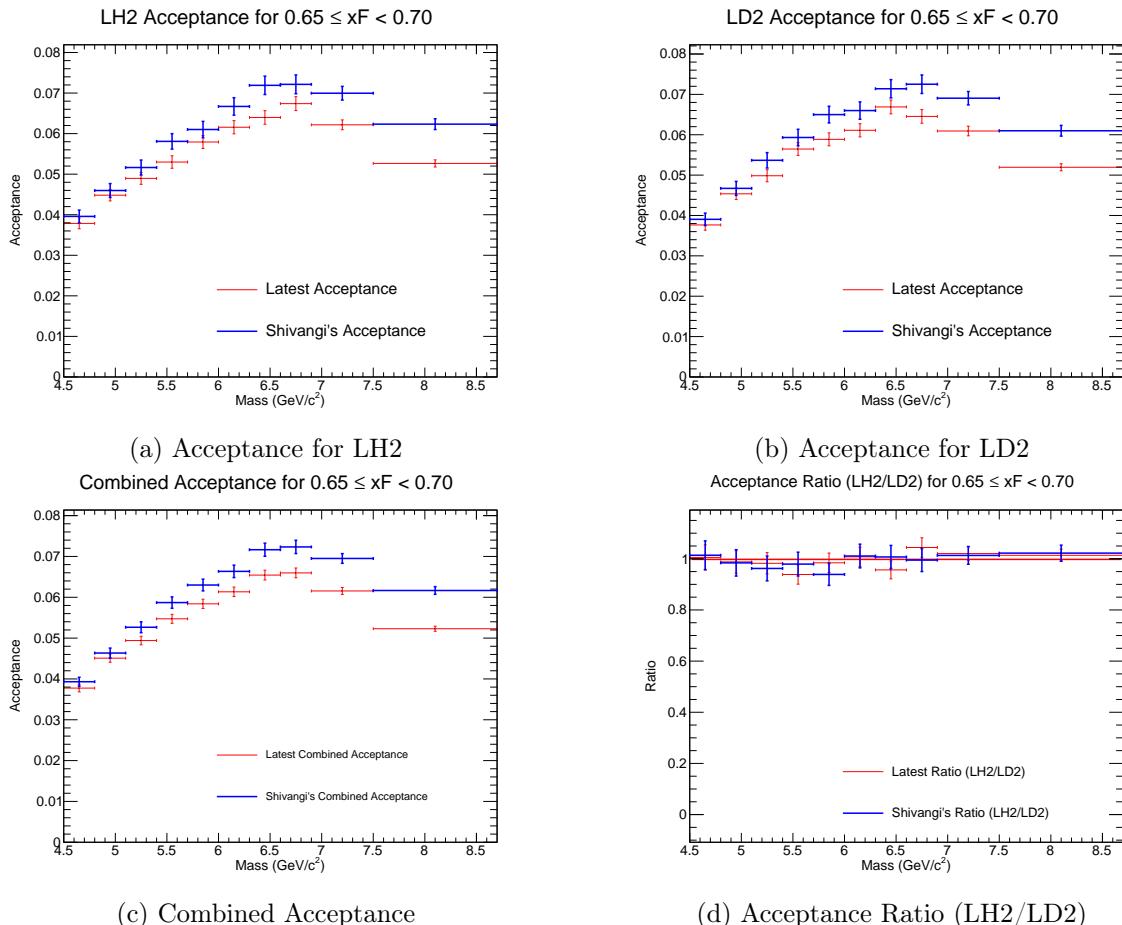


Figure 15: Acceptance plots for  $0.65 \leq x_F < 0.70$ .

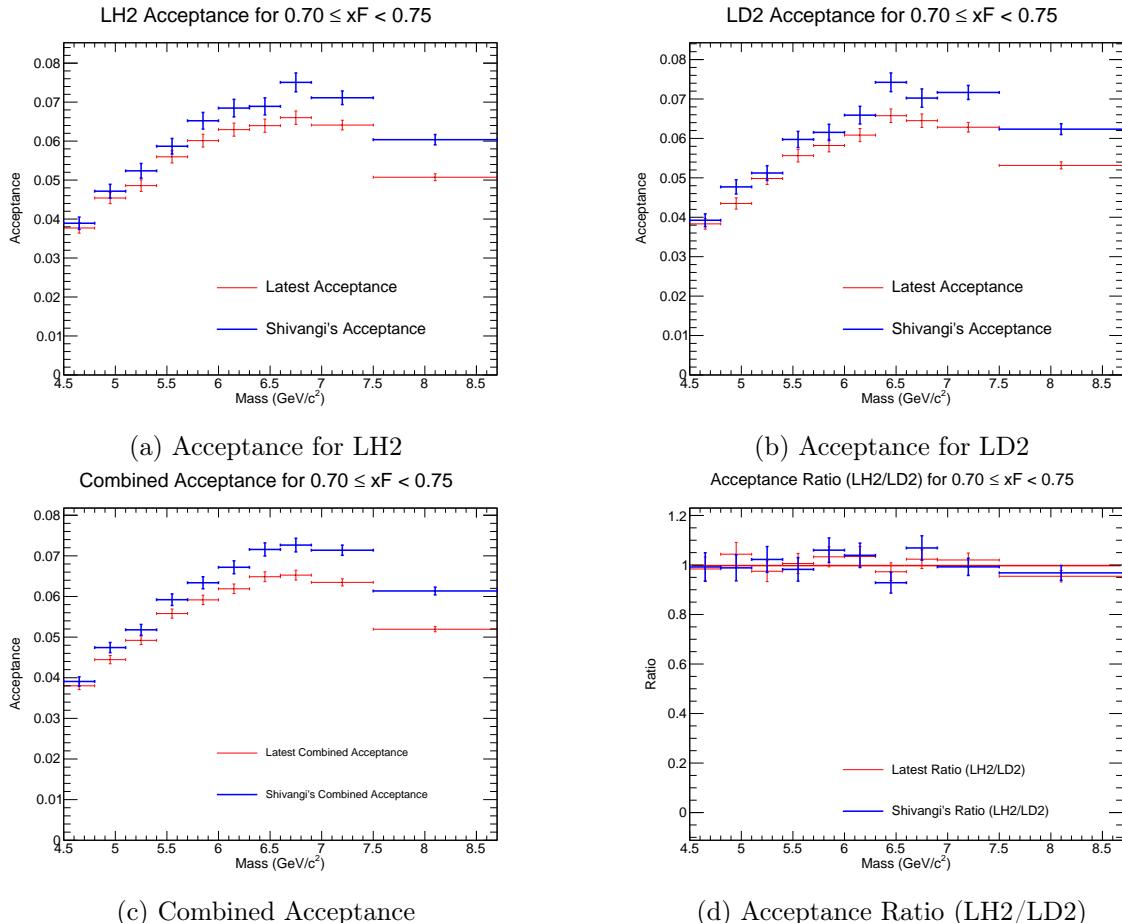


Figure 16: Acceptance plots for  $0.70 \leq x_F < 0.75$ .

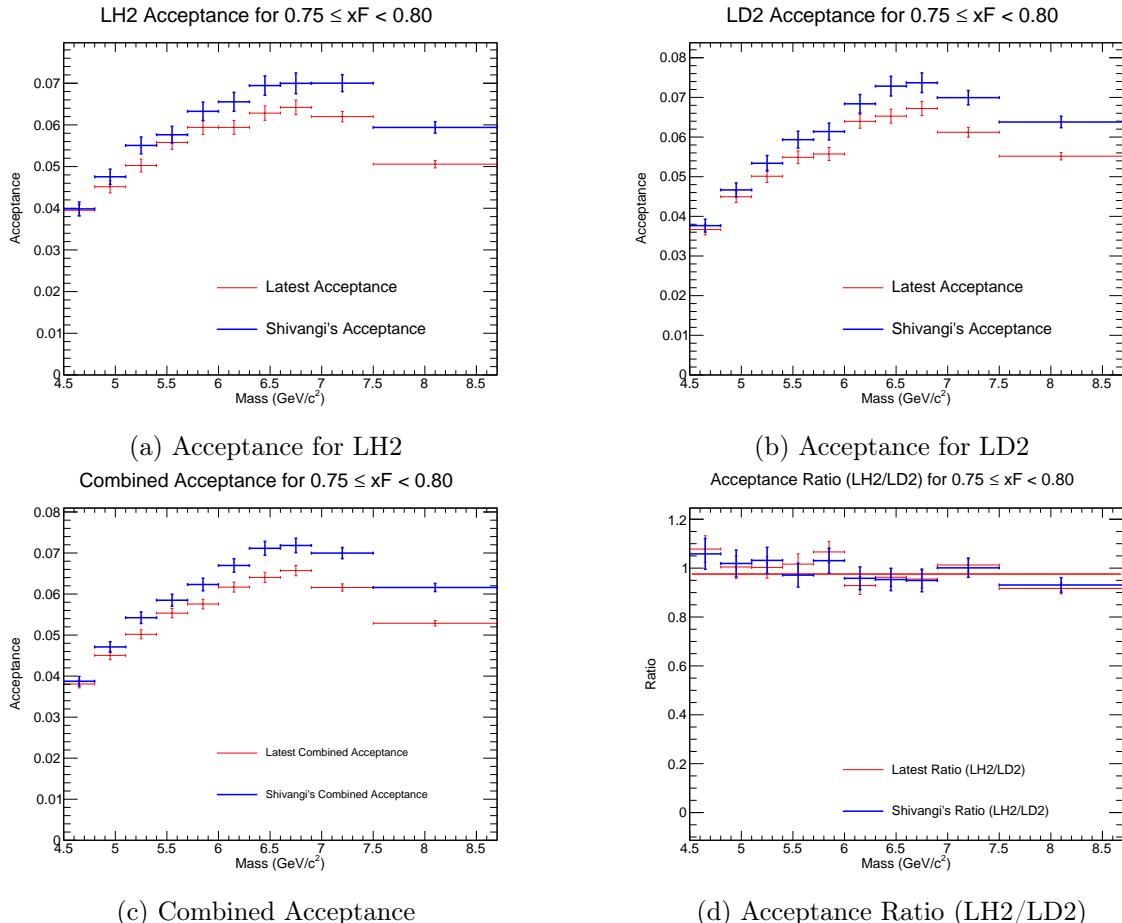


Figure 17: Acceptance plots for  $0.75 \leq x_F < 0.80$ .

## 213 4 Reconstruction Efficiency Correction

214 The track-finding algorithm (“kTracker”) has an efficiency that depends on the detector occu-  
 215 pancy; the number of hits in the detector during an event. This efficiency is studied using  
 216 “clean” MC simulations (signal only) and “messy” MC simulations (signal with background hits  
 217 overlaid). The reconstruction efficiency,  $\epsilon_{\text{recon}}$ , is defined as the ratio of events found in the  
 218 messy sample to those in the clean sample, as a function of an occupancy-related variable (e.g.,  
 219 D2, the number of hits in Drift Chamber Station 2).

$$\epsilon_{\text{recon}}(\text{D1}) = \frac{N_{\text{reco}}^{\text{messy}}(\text{D1})}{N_{\text{reco}}^{\text{clean}}(\text{D1})} \quad (7)$$

220 We have updated the reconstruction efficiency calculation compared to previous reconstruc-  
 221 tion efficiency calculation. Previously, reconstruction efficiency was calculated by creating curves  
 222 in each kinematic bin using the  $D2$  occupancy variable. However, it has been demonstrated that  
 223 there is little correlation between reconstruction efficiency and different kinematic bins (DocDB  
 224 11427). Therefore, we utilize a **global reconstruction efficiency curve**, defined with efficiency  
 225 on the y-axis and the  $D1$  occupancy variable on the x-axis, integrated over all kinematic bins.

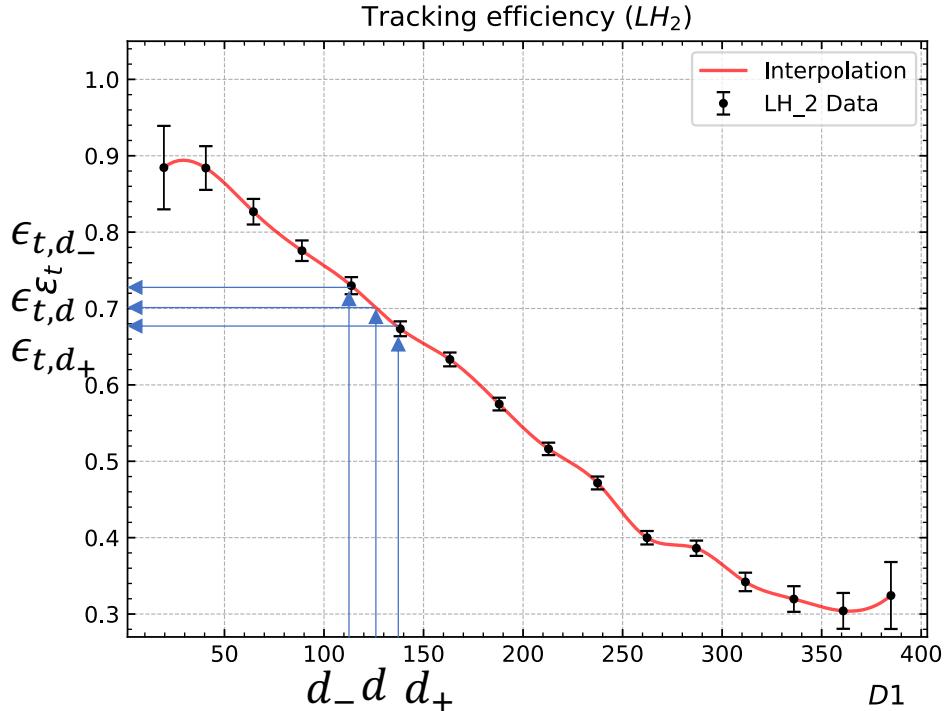


Figure 18: Global Reconstruction Efficiency curve as a function of the  $D1$  occupancy variable, integrated over all kinematic bins.

226 For each dimuon passing event selection, the reconstruction efficiency is calculated based on  
 227 its  $D1$  occupancy using following equation:

$$\epsilon_i = \epsilon(D1^-) + \left( \frac{\epsilon(D1^+) - \epsilon(D1^-)}{D1^+ - D1^-} \right) (D1^+ - D1_i) \quad (8)$$

228 where  $D1_i$  is the  $D1$  occupancy for the dimuon event, and  $D1^-$  and  $D1^+$  are the nearest lower  
 229 and upper bin edges on the global reconstruction efficiency curve. For **mixed events**, the  
 230 reconstruction efficiency is calculated using an average  $D1$  occupancy:

$$D1_{\text{mixed}} = \frac{D1_{\text{pos}} + D1_{\text{neg}}}{2} \quad (9)$$

231 An average reconstruction efficiency,  $\langle\epsilon_{\text{recon}}\rangle$ , with correctly propagated uncertainty, is then  
 232 calculated for each kinematic bin. The Global Reconstruction Efficiency curve and the 2-D  
 233 plots of the average efficiency for LH2 target dimuons and LH2 mixed events are presented  
 234 below.

## 235 4.1 Uncertainty Propagation

236 An important aspect of this procedure is the correct propagation of uncertainties. For each event  
 237 in the data with a measured D1 value, an efficiency  $\epsilon_i$  and its uncertainty  $\delta\epsilon_i$  are determined by  
 238 linear interpolation between points on the MC-derived efficiency curve. For a given event  $i$  the  
 239 efficiency will be interpolated:

$$\delta\epsilon_i = \frac{1}{D1^+ - D1^-} \sqrt{(D1^+ - D1_i)^2 \delta\epsilon(D1^+)^2 + (D1^- - D1_i)^2 \delta\epsilon(D1^-)^2} \quad (10)$$

240 where  $D1_i$  is the value of D1 for the event  $i$ ,  $D1^+$  is the nearest D1 value greater than  $D1_i$ ,  
 241  $D1^-$  is the nearest D1 value less than  $D1_i$ ,  $\epsilon(D1^\pm)$  is the value of the efficiency at  $D1^\pm$ , and  
 242  $\delta\epsilon(D1^\pm)$  is the uncertainty in  $\epsilon(D1^\pm)$ .

243 The average efficiency  $\langle\epsilon\rangle$  for a bin containing  $N$  data events is the mean of the individual  
 244 efficiencies:

$$\langle\epsilon\rangle = \frac{1}{N} \sum_{i=1}^N \epsilon_i \quad (11)$$

245 The uncertainty on this average,  $\delta\langle\epsilon\rangle$ , is based on the propagated error from the uncertainty  
 246 on the MC-derived efficiency curve itself.

$$\delta_{\text{prop}}\langle\epsilon\rangle = \frac{1}{N} \sqrt{\sum_{i=1}^N (\delta\epsilon_i)^2} \quad (12)$$

247 We calculate the average reconstruction efficiency and its propagated uncertainty for both  
 248 target dimuons and mixed dimuons in each kinematic bin. The average reconstruction efficiency  
 249 correction calculated for each kinematic bin with the propagated uncertainty for target dimuons  
 250 and mixed events are shown in 2-D plots below in Figure 19.

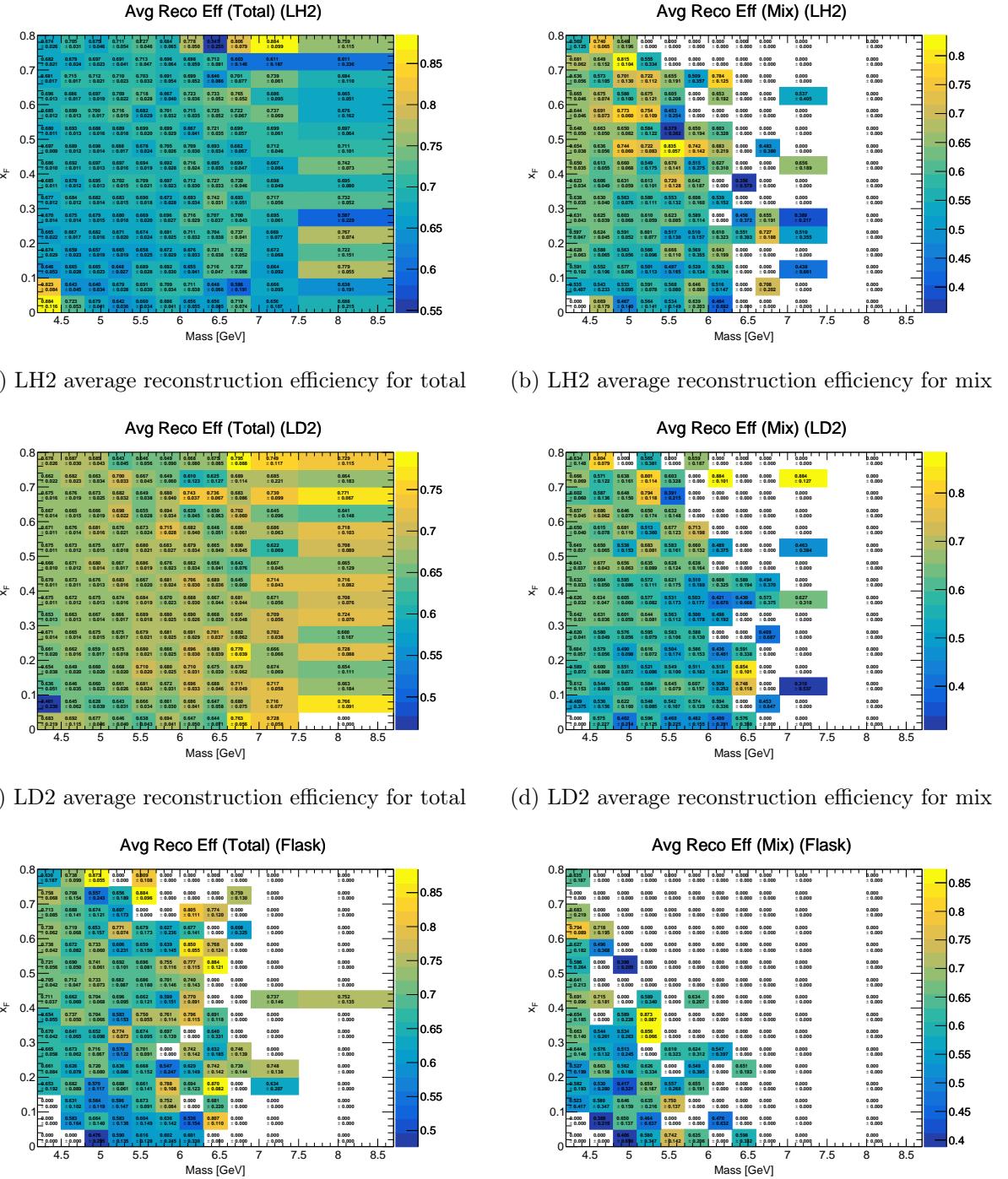


Figure 19: Average Reconstruction Efficiencies calculated each kinematic bin with the propagated uncertainties.

## 251 5 Hodoscope Efficiency Correction

252 Previously, a constant hodoscope efficiency correction of  $0.845 \pm 0.125$  was used (DocDB 11383-  
 253 v4). In this analysis, we calculate the hodoscope efficiency for both target dimuons and mixed  
 254 dimuons on an event-by-event basis. This is done by determining the roadID for the positive track  
 255 ('posRoad') and the negative track ('negRoad') and utilizing the hodoscope paddle efficiency  
 256 table created by Harsha (DocDB 11467-v4).

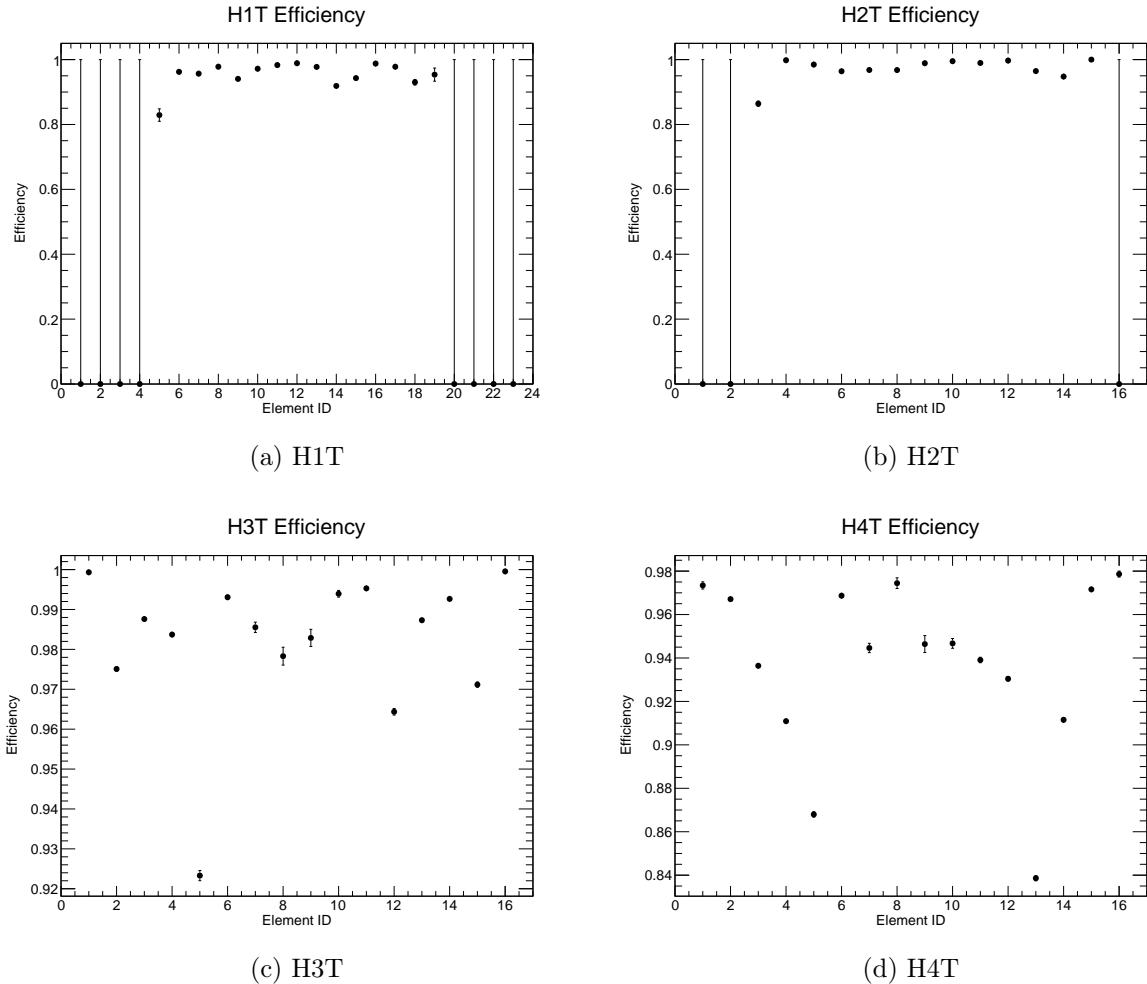


Figure 20: Hodoscope Paddle Efficiencies (Top Planes).

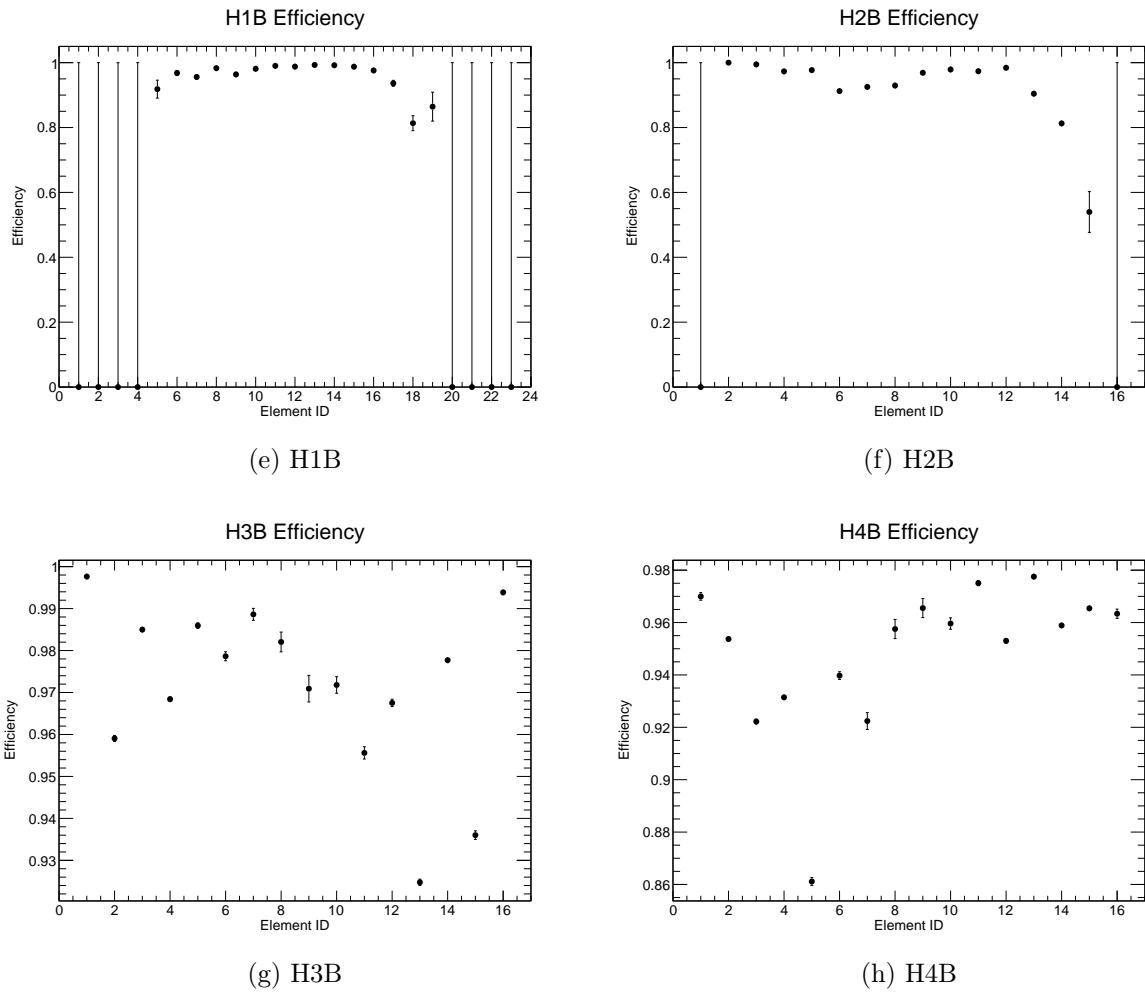


Figure 20: Hodoscope Paddle Efficiencies (Bottom Planes) – Continued.

257 We also calculated hit distributions for each hodoscope paddle and shown below in Figure  
258 21.

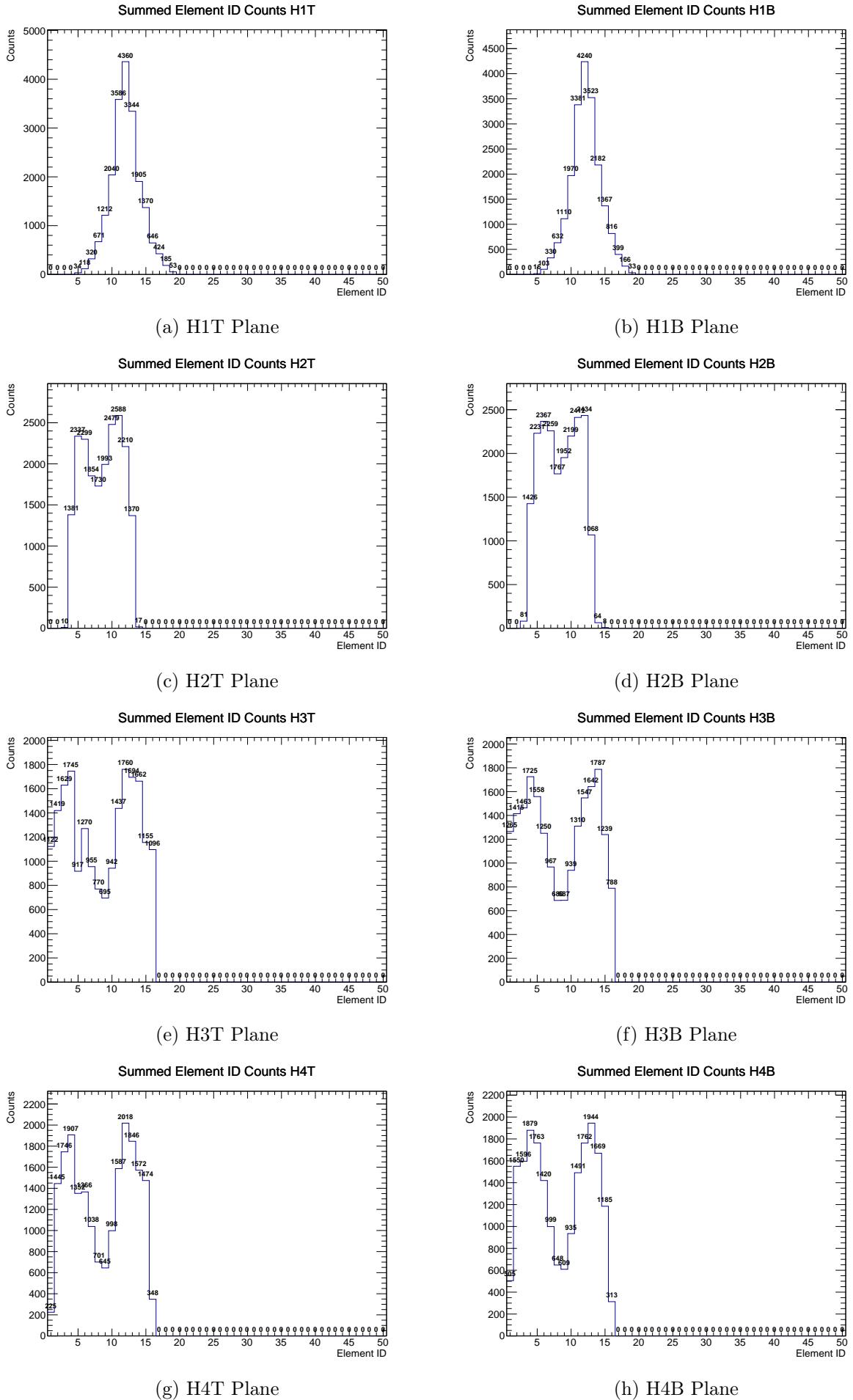


Figure 21: Hodoscope Paddle hit distributions arranged by Plane (Rows 1-4), Top vs Bottom.

259      The average hodoscope efficiency,  $\langle \epsilon_{\text{hodo}} \rangle$ , along with propagated uncertainty, is calculated  
 260      for each kinematic bin. 2-D plots are shown below in Figure 22.

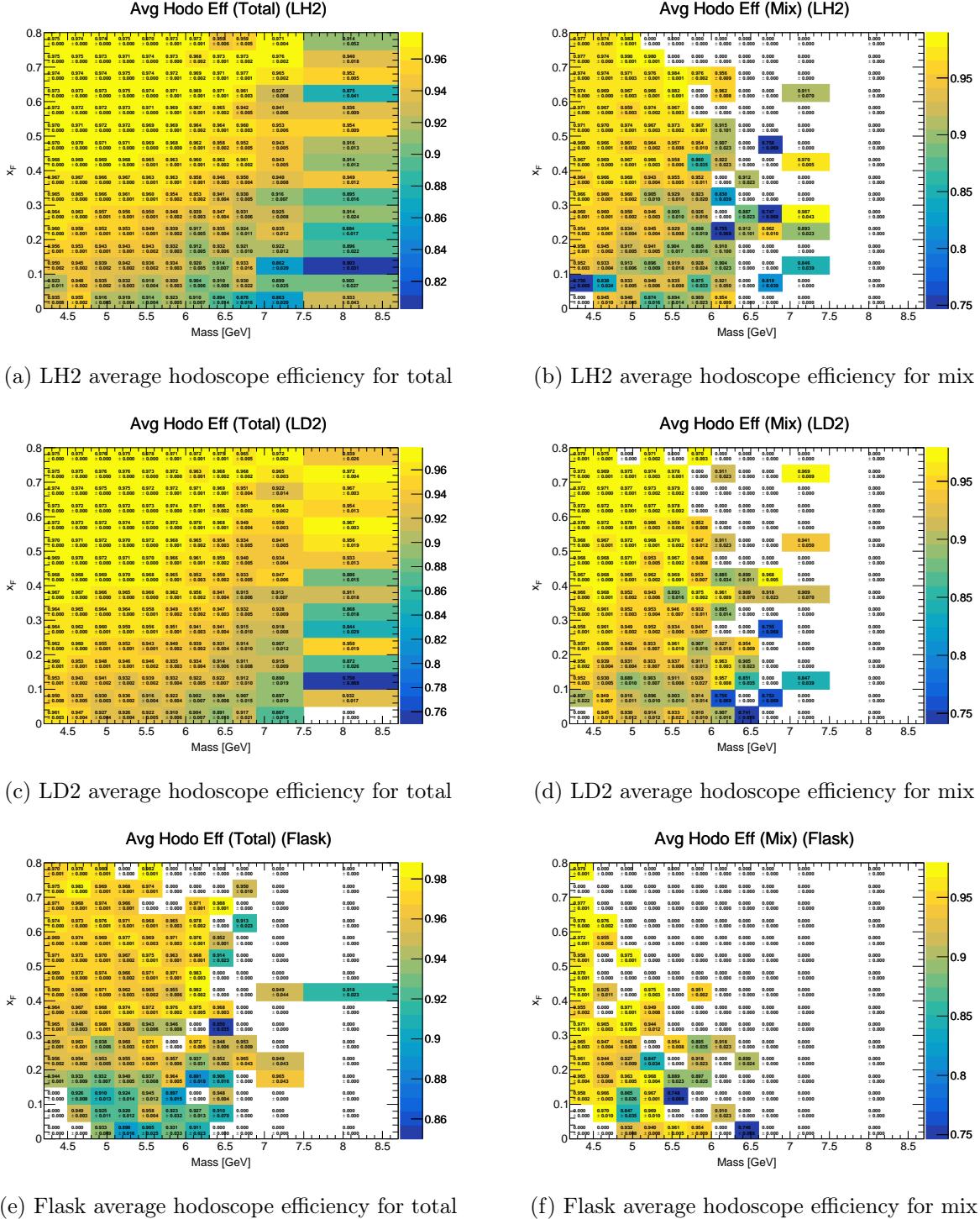


Figure 22: Average Hodoscope Efficiencies calculated each kinematic bin with the propagated uncertainty.

## 6 Total Efficiency Correction

The total efficiency correction  $\epsilon_{\text{total}}^i$  for the  $i^{\text{th}}$  is calculated on a dimuon-by-dimuon basis as the product of the reconstruction and hodoscope efficiencies as defined in the equation 4.

The average total efficiencies for the total and mixed event yields, along with their propagated uncertainties, are calculated for each kinematic bin and are shown below in Figure 23.

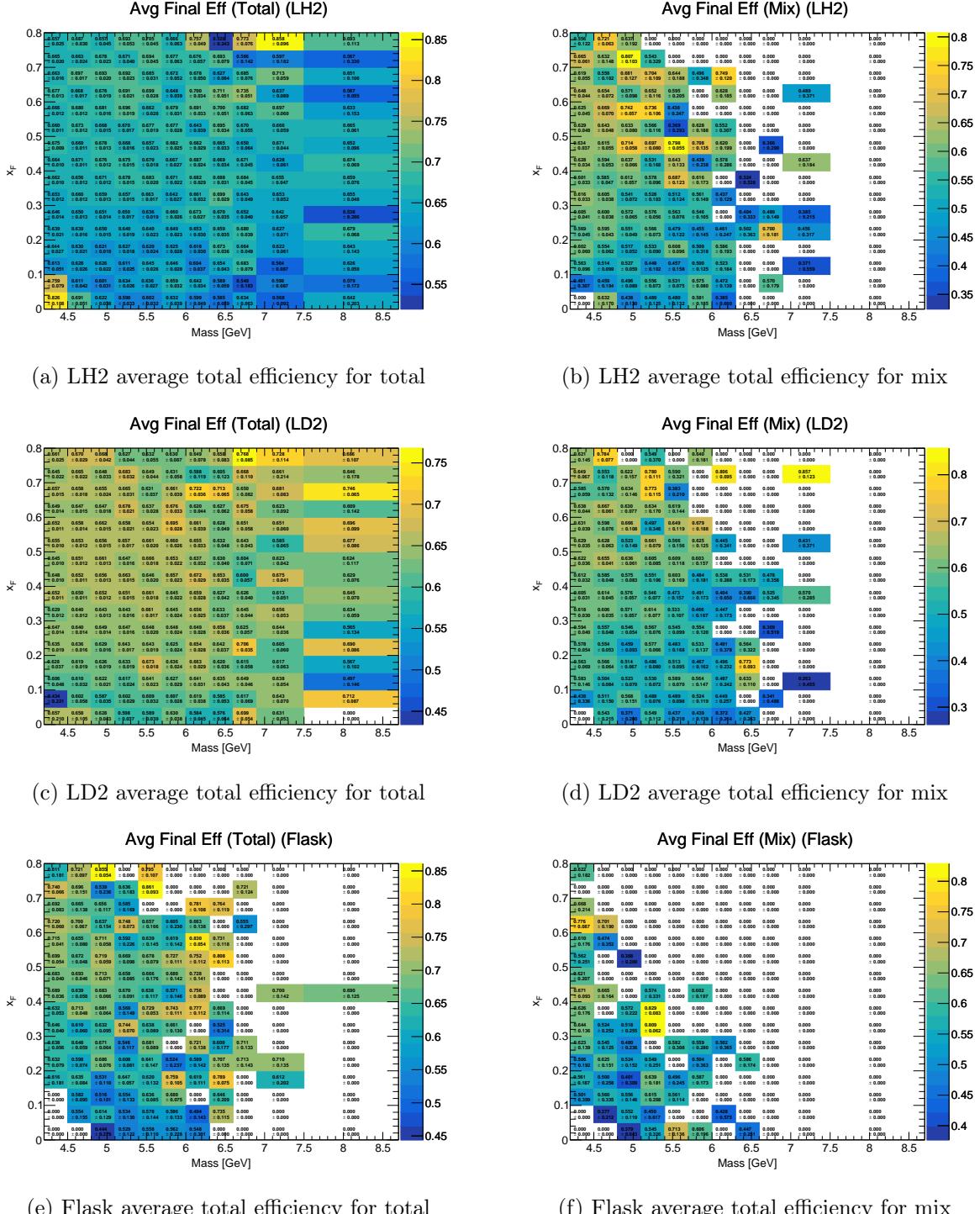


Figure 23: Average total Efficiencies calculated each kinematic bin with the propagated uncertainties.

266 **7 Determination of Corrected Yields**

267 With the average total efficiencies determined, we extract the corrected yields by calculating the  
268 average signal efficiency correction using the following equation:

$$\langle \epsilon_{\text{sig}} \rangle = \frac{1}{Y_{\text{total}} - Y_{\text{mix}}} [\epsilon_{\text{total}} Y_{\text{total}} - \epsilon_{\text{mix}} Y_{\text{mix}}] \quad (13)$$

269 We then apply this correction factor to determine the final background-subtracted yield for the  
270 signal:

$$Y_{\text{corrected}} = \frac{Y_{\text{total}} - Y_{\text{mix}}}{\langle \epsilon_{\text{sig}} \rangle} \quad (14)$$

271 The resulting average signal efficiency corrections and the corrected signal yields for each target  
272 configuration are presented in Figure 24.

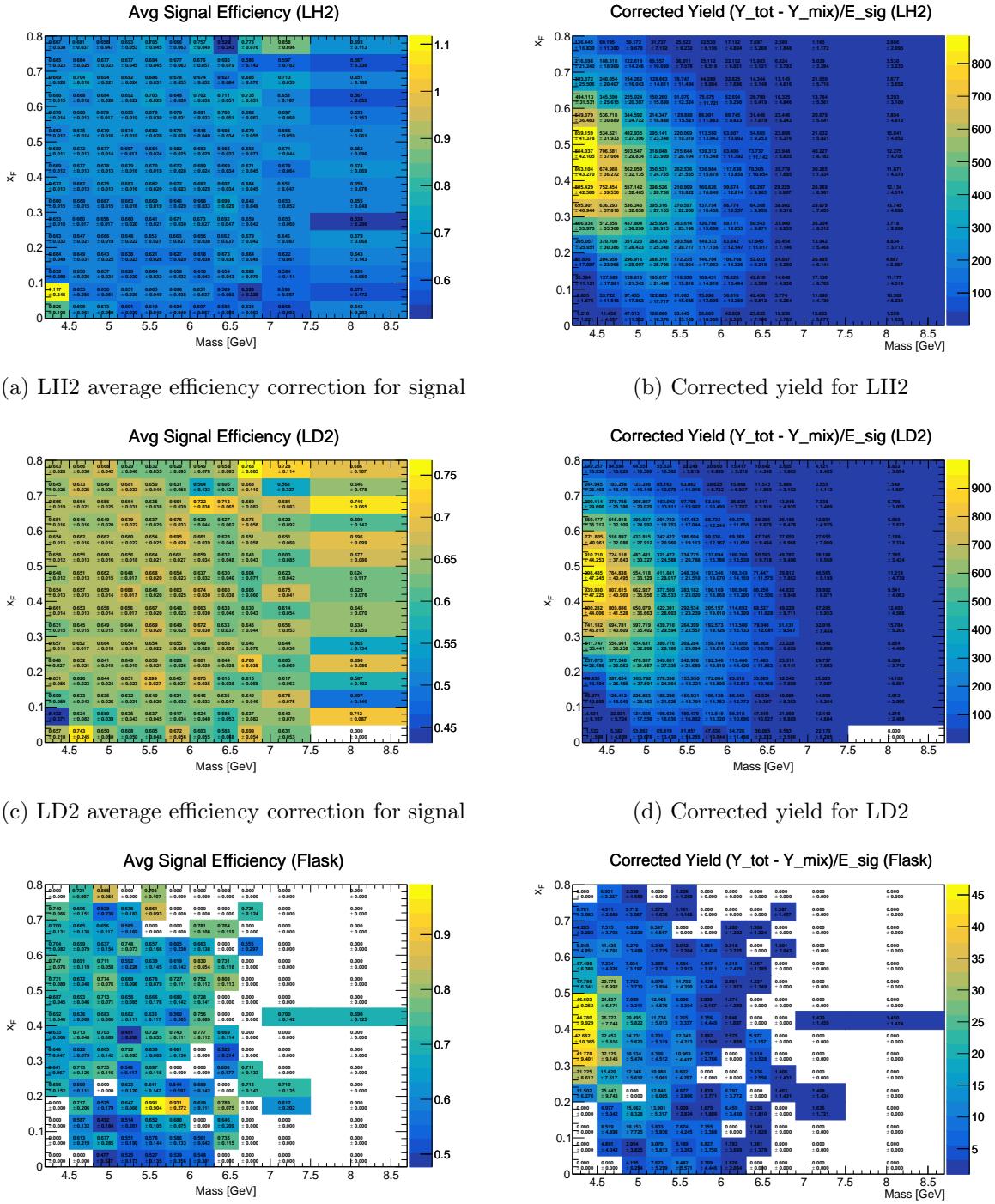


Figure 24: Average efficiency correction for signal and final corrected yields.

273 **8 Appendix: Event Selection Criteria (Chuck Cuts)**

274 The event selection criteria, commonly referred to as “Chuck Cuts,” are designed to select high-  
 275 quality dimuon events originating from the target while rejecting backgrounds from the beam  
 276 dump, upstream interactions, and cosmic rays. The cuts are applied at three levels: single track  
 277 quality, dimuon vertex/kinematics, and detector occupancy.

278 In the following tables, the beam vertical offset is denoted as  $y_{\text{beam}} = 1.6 \text{ cm}$ .

279 **8.1 Single Track Cuts**

280 These cuts are applied individually to both the positive and negative muon tracks to ensure they  
 281 are well-reconstructed and pass through the spectrometer magnet apertures correctly.

Table 1: Single track selection criteria.

| Variable                                              | Condition                                                                                                                     |
|-------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------|
| <b>Track Fit Quality</b>                              |                                                                                                                               |
| Target $\chi^2$                                       | $\chi^2_{\text{target}} < 15$                                                                                                 |
| Reduced $\chi^2$                                      | $\chi^2/(N_{\text{hits}} - 5) < 12$                                                                                           |
| Vertex Assumption                                     | $\chi^2_{\text{target}} < 1.5 \times \chi^2_{\text{dump}}$ AND $\chi^2_{\text{target}} < 1.5 \times \chi^2_{\text{upstream}}$ |
| <b>Hits &amp; Geometry</b>                            |                                                                                                                               |
| Number of Hits                                        | $N_{\text{hits}} > 13$                                                                                                        |
| Station 1 Z-Momentum                                  | $9 < p_{z,\text{st1}} < 75 \text{ GeV}/c$                                                                                     |
| Single Track Vertex $z$                               | $-320 < z_v < -5 \text{ cm}$                                                                                                  |
| <b>Aperture &amp; Trajectory</b>                      |                                                                                                                               |
| Radial pos. at target ( $z \approx -130 \text{ cm}$ ) | $x^2 + (y - y_{\text{beam}})^2 < 320 \text{ cm}^2$                                                                            |
| Radial pos. at dump ( $z \approx 50 \text{ cm}$ )     | $16 < x^2 + (y - y_{\text{beam}})^2 < 1100 \text{ cm}^2$                                                                      |
| Vertical Focusing                                     | $y_{\text{st1}}/y_{\text{st3}} < 1$                                                                                           |
| Vertical Projection                                   | $y_{\text{st1}} \cdot y_{\text{st3}} > 0$                                                                                     |
| Min Vertical Momentum                                 | $ p_{y,\text{st1}}  > 0.02 \text{ GeV}/c$                                                                                     |
| <b>Momentum Conservation</b>                          |                                                                                                                               |
| KMag Momentum Kick                                    | $  p_{x,\text{st1}} - p_{x,\text{st3}}  - 0.416  < 0.008 \text{ GeV}/c$                                                       |
| Vertical Bend (Null)                                  | $ p_{y,\text{st1}} - p_{y,\text{st3}}  < 0.008 \text{ GeV}/c$                                                                 |
| Longitudinal (Null)                                   | $ p_{z,\text{st1}} - p_{z,\text{st3}}  < 0.08 \text{ GeV}/c$                                                                  |

282 **8.2 Dimuon Cuts**

283 After forming a dimuon pair, the following cuts ensure the vertex is valid and the kinematics  
 284 fall within the trustworthy region of the spectrometer acceptance.

285 **8.3 Occupancy and Topology Cuts**

286 These cuts remove events with high detector activity (which complicates reconstruction) and en-  
 287 sure the two muons pass through opposite sides of the spectrometer (the standard “top/bottom”  
 288 trigger topology).

Table 2: Dimuon kinematic and vertex selection criteria.

| Variable                    | Condition                                                                    |
|-----------------------------|------------------------------------------------------------------------------|
| <b>Vertex Position</b>      |                                                                              |
| Transverse Offset ( $x$ )   | $ dx  < 0.25 \text{ cm}$                                                     |
| Vertical Offset ( $y$ )     | $ dy - y_{\text{beam}}  < 0.22 \text{ cm}$                                   |
| Radial Vertex               | $dx^2 + (dy - y_{\text{beam}})^2 < 0.06 \text{ cm}^2$                        |
| Longitudinal Vertex ( $z$ ) | $-280 < dz < -5 \text{ cm}$                                                  |
| Vertex Fit Quality          | $\chi^2_{\text{dimuon}} < 18$                                                |
| Vertex Consistency          | $ \chi^2_{\text{trk1}} + \chi^2_{\text{trk2}} - \chi^2_{\text{dimuon}}  < 2$ |
| <b>Kinematics</b>           |                                                                              |
| Invariant Mass              | $4.2 < M_{\mu\mu} < 8.8 \text{ GeV}/c^2$                                     |
| Feynman- $x$                | $-0.1 < x_F < 0.95$                                                          |
| Transverse Scaling $x_T$    | $0.05 < x_T \leq 0.58$                                                       |
| Costh (Collins-Soper)       | $ \cos \theta  < 0.5$                                                        |
| Longitudinal Momentum       | $38 < p_z < 116 \text{ GeV}/c$                                               |
| Transverse Momentum limits  | $ dp_x  < 1.8 \text{ GeV}/c,  dp_y  < 2.0 \text{ GeV}/c$                     |
| Total $p_T$                 | $dp_x^2 + dp_y^2 < 5.0 \text{ (GeV}/c)^2$                                    |
| Track Separation            | $\text{sep} < 270 \text{ cm}$                                                |

Table 3: Occupancy and topological cuts.

| Variable                 | Condition                                                                       |
|--------------------------|---------------------------------------------------------------------------------|
| <b>Chamber Occupancy</b> |                                                                                 |
| Drift Chamber 1 Hits     | $D1 < 400$                                                                      |
| Drift Chamber 2 Hits     | $D2 < 400$                                                                      |
| Drift Chamber 3 Hits     | $D3 < 400$                                                                      |
| Total Chamber Hits       | $D1 + D2 + D3 < 1000$                                                           |
| <b>Topology</b>          |                                                                                 |
| Opposite Quadrants       | $y_{\text{st3}}^{\text{trk1}} \cdot y_{\text{st3}}^{\text{trk2}} < 0$           |
| Total Hits on Tracks     | $N_{\text{hits}}^{\text{trk1}} + N_{\text{hits}}^{\text{trk2}} > 29$            |
| Station 1 Hits Sum       | $N_{\text{hits, st1}}^{\text{trk1}} + N_{\text{hits, st1}}^{\text{trk2}} > 8$   |
| Station 1 X-Sum          | $ x_{\text{st1}}^{\text{trk1}} + x_{\text{st1}}^{\text{trk2}}  < 42 \text{ cm}$ |

<sup>289</sup> **9 Appendix: Efficiency Plots**

<sup>290</sup> This appendix contains the efficiency studies used in this analysis. Figures 19, 22, and 21 show  
<sup>291</sup> the relevant efficiency and distribution maps.

<sup>292</sup> **10 Appendix: Table of Systematic Errors**

Table 4: Detailed Systematic Error calculation for Bins in  $x_F$  and Mass

| $x_F$ Bin     | Mass Bin (GeV) | Trigger Eff. | Acceptance | k-Tracker Eff. | Total Syst. |
|---------------|----------------|--------------|------------|----------------|-------------|
| [0.00 - 0.05) | [4.50 - 4.80)  | 0.779025     | 1.873238   | 0.946767       | 2.238809    |
| [0.00 - 0.05) | [4.80 - 5.10)  | 0.058272     | 0.052304   | 0.009351       | 0.078860    |
| [0.00 - 0.05) | [5.10 - 5.40)  | 0.081048     | 0.047749   | 0.018181       | 0.095809    |
| [0.00 - 0.05) | [5.40 - 5.70)  | 0.033849     | 0.013951   | 0.004059       | 0.036835    |
| [0.00 - 0.05) | [5.70 - 6.00)  | 0.025896     | 0.009169   | 0.005236       | 0.027966    |
| [0.00 - 0.05) | [6.00 - 6.30)  | 0.019771     | 0.006552   | 0.003990       | 0.021207    |
| [0.00 - 0.05) | [6.30 - 6.60)  | 0.019741     | 0.006295   | 0.007003       | 0.021872    |
| [0.00 - 0.05) | [6.60 - 6.90)  | 0.012449     | 0.004049   | 0.002978       | 0.013425    |
| [0.00 - 0.05) | [6.90 - 7.50)  | 0.007375     | 0.001898   | 0.002170       | 0.007919    |
| [0.00 - 0.05) | [7.50 - 8.70)  | 0.000946     | 0.000252   | 0.000628       | 0.001163    |
| [0.05 - 0.10) | [4.50 - 4.80)  | 0.284881     | 0.378813   | 0.155516       | 0.498841    |
| [0.05 - 0.10) | [4.80 - 5.10)  | 0.166470     | 0.128867   | 0.041569       | 0.214586    |
| [0.05 - 0.10) | [5.10 - 5.40)  | 0.055664     | 0.025882   | 0.005169       | 0.061605    |
| [0.05 - 0.10) | [5.40 - 5.70)  | 0.032285     | 0.011302   | 0.003966       | 0.034436    |
| [0.05 - 0.10) | [5.70 - 6.00)  | 0.019937     | 0.006339   | 0.002229       | 0.021039    |
| [0.05 - 0.10) | [6.00 - 6.30)  | 0.018107     | 0.005156   | 0.001957       | 0.018928    |
| [0.05 - 0.10) | [6.30 - 6.60)  | 0.015415     | 0.004246   | 0.003557       | 0.016380    |
| [0.05 - 0.10) | [6.60 - 6.90)  | 0.002562     | 0.000686   | 0.001166       | 0.002897    |
| [0.05 - 0.10) | [6.90 - 7.50)  | 0.004064     | 0.000910   | 0.001134       | 0.004316    |
| [0.05 - 0.10) | [7.50 - 8.70)  | 0.003523     | 0.000764   | 0.001074       | 0.003762    |
| [0.10 - 0.15) | [4.50 - 4.80)  | 0.198459     | 0.182806   | 0.040656       | 0.272868    |
| [0.10 - 0.15) | [4.80 - 5.10)  | 0.083380     | 0.040798   | 0.013031       | 0.093736    |
| [0.10 - 0.15) | [5.10 - 5.40)  | 0.081948     | 0.031238   | 0.010558       | 0.088333    |
| [0.10 - 0.15) | [5.40 - 5.70)  | 0.030329     | 0.009540   | 0.002815       | 0.031918    |
| [0.10 - 0.15) | [5.70 - 6.00)  | 0.024458     | 0.006894   | 0.002083       | 0.025497    |
| [0.10 - 0.15) | [6.00 - 6.30)  | 0.023572     | 0.006173   | 0.002268       | 0.024472    |
| [0.10 - 0.15) | [6.30 - 6.60)  | 0.011184     | 0.002813   | 0.001083       | 0.011583    |
| [0.10 - 0.15) | [6.60 - 6.90)  | 0.006021     | 0.001560   | 0.001047       | 0.006307    |
| [0.10 - 0.15) | [6.90 - 7.50)  | 0.004337     | 0.000867   | 0.000718       | 0.004481    |
| [0.10 - 0.15) | [7.50 - 8.70)  | 0.002871     | 0.000555   | 0.000388       | 0.002950    |
| [0.15 - 0.20) | [4.50 - 4.80)  | 0.124062     | 0.075232   | 0.015770       | 0.145945    |
| [0.15 - 0.20) | [4.80 - 5.10)  | 0.115363     | 0.046469   | 0.012767       | 0.125024    |
| [0.15 - 0.20) | [5.10 - 5.40)  | 0.072817     | 0.024387   | 0.004930       | 0.076950    |
| [0.15 - 0.20) | [5.40 - 5.70)  | 0.041137     | 0.011396   | 0.003480       | 0.042828    |
| [0.15 - 0.20) | [5.70 - 6.00)  | 0.035444     | 0.009302   | 0.002872       | 0.036756    |
| [0.15 - 0.20) | [6.00 - 6.30)  | 0.020001     | 0.004856   | 0.001682       | 0.020651    |
| [0.15 - 0.20) | [6.30 - 6.60)  | 0.010531     | 0.002410   | 0.000921       | 0.010843    |
| [0.15 - 0.20) | [6.60 - 6.90)  | 0.008260     | 0.001887   | 0.001449       | 0.008596    |
| [0.15 - 0.20) | [6.90 - 7.50)  | 0.002937     | 0.000541   | 0.000443       | 0.003019    |
| [0.15 - 0.20) | [7.50 - 8.70)  | 0.000973     | 0.000170   | 0.000400       | 0.001065    |
| [0.20 - 0.25) | [4.20 - 4.50)  | 0.166120     | 0.120909   | 0.026450       | 0.207158    |
| [0.20 - 0.25) | [4.50 - 4.80)  | 0.145103     | 0.071032   | 0.012123       | 0.162010    |
| [0.20 - 0.25) | [4.80 - 5.10)  | 0.102147     | 0.034999   | 0.005624       | 0.108123    |
| [0.20 - 0.25) | [5.10 - 5.40)  | 0.053289     | 0.015003   | 0.002962       | 0.055440    |
| [0.20 - 0.25) | [5.40 - 5.70)  | 0.041865     | 0.010845   | 0.002727       | 0.043332    |

Cont'd on next page

Table 4: (Continued)

| $x_F$ Bin     | Mass Bin (GeV) | Trigger Eff. | Acceptance | k-Tracker Eff. | Total Syst. |
|---------------|----------------|--------------|------------|----------------|-------------|
| [0.20 - 0.25) | [5.70 - 6.00)  | 0.027889     | 0.006527   | 0.001469       | 0.028680    |
| [0.20 - 0.25) | [6.00 - 6.30)  | 0.013039     | 0.002957   | 0.001025       | 0.013410    |
| [0.20 - 0.25) | [6.30 - 6.60)  | 0.016485     | 0.003541   | 0.001461       | 0.016924    |
| [0.20 - 0.25) | [6.60 - 6.90)  | 0.006353     | 0.001394   | 0.000605       | 0.006533    |
| [0.20 - 0.25) | [6.90 - 7.50)  | 0.001365     | 0.000229   | 0.000204       | 0.001398    |
| [0.20 - 0.25) | [7.50 - 8.70)  | 0.001336     | 0.000211   | 0.000136       | 0.001359    |
| [0.25 - 0.30) | [4.20 - 4.50)  | 0.141343     | 0.072939   | 0.010257       | 0.159384    |
| [0.25 - 0.30) | [4.50 - 4.80)  | 0.130167     | 0.051529   | 0.006463       | 0.140145    |
| [0.25 - 0.30) | [4.80 - 5.10)  | 0.079605     | 0.023998   | 0.003471       | 0.083216    |
| [0.25 - 0.30) | [5.10 - 5.40)  | 0.054612     | 0.014272   | 0.002683       | 0.056510    |
| [0.25 - 0.30) | [5.40 - 5.70)  | 0.038571     | 0.009218   | 0.001867       | 0.039701    |
| [0.25 - 0.30) | [5.70 - 6.00)  | 0.023376     | 0.005079   | 0.001591       | 0.023974    |
| [0.25 - 0.30) | [6.00 - 6.30)  | 0.017654     | 0.003770   | 0.001225       | 0.018093    |
| [0.25 - 0.30) | [6.30 - 6.60)  | 0.007693     | 0.001519   | 0.000560       | 0.007862    |
| [0.25 - 0.30) | [6.60 - 6.90)  | 0.007726     | 0.001536   | 0.001007       | 0.007941    |
| [0.25 - 0.30) | [6.90 - 7.50)  | 0.005124     | 0.000778   | 0.000489       | 0.005206    |
| [0.25 - 0.30) | [7.50 - 8.70)  | 0.000519     | 0.000076   | 0.000209       | 0.000565    |
| [0.30 - 0.35) | [4.20 - 4.50)  | 0.143223     | 0.062852   | 0.006469       | 0.156541    |
| [0.30 - 0.35) | [4.50 - 4.80)  | 0.100283     | 0.033699   | 0.003193       | 0.105842    |
| [0.30 - 0.35) | [4.80 - 5.10)  | 0.078522     | 0.020901   | 0.002863       | 0.081307    |
| [0.30 - 0.35) | [5.10 - 5.40)  | 0.052272     | 0.012726   | 0.001692       | 0.053826    |
| [0.30 - 0.35) | [5.40 - 5.70)  | 0.035353     | 0.007742   | 0.001569       | 0.036225    |
| [0.30 - 0.35) | [5.70 - 6.00)  | 0.019840     | 0.004222   | 0.001174       | 0.020318    |
| [0.30 - 0.35) | [6.00 - 6.30)  | 0.016108     | 0.003287   | 0.001254       | 0.016488    |
| [0.30 - 0.35) | [6.30 - 6.60)  | 0.010060     | 0.002023   | 0.000634       | 0.010281    |
| [0.30 - 0.35) | [6.60 - 6.90)  | 0.008018     | 0.001569   | 0.000793       | 0.008208    |
| [0.30 - 0.35) | [6.90 - 7.50)  | 0.003694     | 0.000533   | 0.000421       | 0.003756    |
| [0.30 - 0.35) | [7.50 - 8.70)  | 0.001747     | 0.000242   | 0.000186       | 0.001773    |
| [0.35 - 0.40) | [4.20 - 4.50)  | 0.106457     | 0.037922   | 0.003043       | 0.113051    |
| [0.35 - 0.40) | [4.50 - 4.80)  | 0.100531     | 0.029480   | 0.003146       | 0.104811    |
| [0.35 - 0.40) | [4.80 - 5.10)  | 0.072502     | 0.018895   | 0.002326       | 0.074960    |
| [0.35 - 0.40) | [5.10 - 5.40)  | 0.048131     | 0.010864   | 0.001538       | 0.049365    |
| [0.35 - 0.40) | [5.40 - 5.70)  | 0.020800     | 0.004392   | 0.000837       | 0.021275    |
| [0.35 - 0.40) | [5.70 - 6.00)  | 0.020491     | 0.004143   | 0.000980       | 0.020928    |
| [0.35 - 0.40) | [6.00 - 6.30)  | 0.013363     | 0.002624   | 0.000720       | 0.013637    |
| [0.35 - 0.40) | [6.30 - 6.60)  | 0.006047     | 0.001135   | 0.000396       | 0.006165    |
| [0.35 - 0.40) | [6.60 - 6.90)  | 0.005933     | 0.001107   | 0.000667       | 0.006072    |
| [0.35 - 0.40) | [6.90 - 7.50)  | 0.003348     | 0.000459   | 0.000269       | 0.003390    |
| [0.35 - 0.40) | [7.50 - 8.70)  | 0.001436     | 0.000183   | 0.000247       | 0.001469    |
| [0.40 - 0.45) | [4.20 - 4.50)  | 0.099323     | 0.033040   | 0.002941       | 0.104716    |
| [0.40 - 0.45) | [4.50 - 4.80)  | 0.075954     | 0.020641   | 0.002128       | 0.078738    |
| [0.40 - 0.45) | [4.80 - 5.10)  | 0.055286     | 0.012835   | 0.001577       | 0.056778    |
| [0.40 - 0.45) | [5.10 - 5.40)  | 0.038052     | 0.008469   | 0.001399       | 0.039008    |
| [0.40 - 0.45) | [5.40 - 5.70)  | 0.028172     | 0.005715   | 0.000987       | 0.028763    |
| [0.40 - 0.45) | [5.70 - 6.00)  | 0.015105     | 0.002920   | 0.000688       | 0.015400    |
| [0.40 - 0.45) | [6.00 - 6.30)  | 0.014939     | 0.002774   | 0.000734       | 0.015213    |
| [0.40 - 0.45) | [6.30 - 6.60)  | 0.012131     | 0.002291   | 0.000940       | 0.012381    |
| [0.40 - 0.45) | [6.60 - 6.90)  | 0.005773     | 0.001030   | 0.000398       | 0.005877    |

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Table 4: (Continued)

| $x_F$ Bin     | Mass Bin (GeV) | Trigger Eff. | Acceptance | k-Tracker Eff. | Total Syst. |
|---------------|----------------|--------------|------------|----------------|-------------|
| [0.40 - 0.45) | [6.90 - 7.50)  | 0.002557     | 0.000353   | 0.000241       | 0.002593    |
| [0.40 - 0.45) | [7.50 - 8.70)  | 0.000491     | 0.000061   | 0.000040       | 0.000496    |
| [0.45 - 0.50) | [4.20 - 4.50)  | 0.078635     | 0.023049   | 0.002059       | 0.081969    |
| [0.45 - 0.50) | [4.50 - 4.80)  | 0.067541     | 0.017403   | 0.001706       | 0.069768    |
| [0.45 - 0.50) | [4.80 - 5.10)  | 0.053760     | 0.012443   | 0.001688       | 0.055207    |
| [0.45 - 0.50) | [5.10 - 5.40)  | 0.028610     | 0.005965   | 0.001078       | 0.029245    |
| [0.45 - 0.50) | [5.40 - 5.70)  | 0.020809     | 0.004172   | 0.000821       | 0.021239    |
| [0.45 - 0.50) | [5.70 - 6.00)  | 0.015482     | 0.002928   | 0.000738       | 0.015774    |
| [0.45 - 0.50) | [6.00 - 6.30)  | 0.010741     | 0.001999   | 0.000674       | 0.010946    |
| [0.45 - 0.50) | [6.30 - 6.60)  | 0.011477     | 0.002063   | 0.000873       | 0.011694    |
| [0.45 - 0.50) | [6.60 - 6.90)  | 0.004200     | 0.000754   | 0.000554       | 0.004303    |
| [0.45 - 0.50) | [6.90 - 7.50)  | 0.004274     | 0.000573   | 0.000231       | 0.004319    |
| [0.45 - 0.50) | [7.50 - 8.70)  | 0.000999     | 0.000121   | 0.000098       | 0.001011    |
| [0.50 - 0.55) | [4.20 - 4.50)  | 0.091374     | 0.025832   | 0.003131       | 0.095007    |
| [0.50 - 0.55) | [4.50 - 4.80)  | 0.038797     | 0.009116   | 0.001196       | 0.039872    |
| [0.50 - 0.55) | [4.80 - 5.10)  | 0.035794     | 0.007792   | 0.001215       | 0.036652    |
| [0.50 - 0.55) | [5.10 - 5.40)  | 0.025971     | 0.005366   | 0.000845       | 0.026533    |
| [0.50 - 0.55) | [5.40 - 5.70)  | 0.017990     | 0.003538   | 0.000653       | 0.018346    |
| [0.50 - 0.55) | [5.70 - 6.00)  | 0.010504     | 0.001914   | 0.000561       | 0.010691    |
| [0.50 - 0.55) | [6.00 - 6.30)  | 0.006640     | 0.001204   | 0.000587       | 0.006773    |
| [0.50 - 0.55) | [6.30 - 6.60)  | 0.007154     | 0.001324   | 0.000432       | 0.007288    |
| [0.50 - 0.55) | [6.60 - 6.90)  | 0.004000     | 0.000731   | 0.000474       | 0.004094    |
| [0.50 - 0.55) | [6.90 - 7.50)  | 0.001946     | 0.000254   | 0.000172       | 0.001970    |
| [0.50 - 0.55) | [7.50 - 8.70)  | 0.001279     | 0.000149   | 0.000130       | 0.001294    |
| [0.55 - 0.60) | [4.20 - 4.50)  | 0.049012     | 0.013093   | 0.001356       | 0.050748    |
| [0.55 - 0.60) | [4.50 - 4.80)  | 0.045199     | 0.010565   | 0.001338       | 0.046436    |
| [0.55 - 0.60) | [4.80 - 5.10)  | 0.031162     | 0.006899   | 0.001131       | 0.031937    |
| [0.55 - 0.60) | [5.10 - 5.40)  | 0.019065     | 0.003784   | 0.000735       | 0.019451    |
| [0.55 - 0.60) | [5.40 - 5.70)  | 0.011066     | 0.002143   | 0.000544       | 0.011285    |
| [0.55 - 0.60) | [5.70 - 6.00)  | 0.007673     | 0.001386   | 0.000453       | 0.007810    |
| [0.55 - 0.60) | [6.00 - 6.30)  | 0.003981     | 0.000698   | 0.000228       | 0.004048    |
| [0.55 - 0.60) | [6.30 - 6.60)  | 0.003434     | 0.000599   | 0.000281       | 0.003497    |
| [0.55 - 0.60) | [6.60 - 6.90)  | 0.003400     | 0.000586   | 0.000348       | 0.003468    |
| [0.55 - 0.60) | [6.90 - 7.50)  | 0.002152     | 0.000282   | 0.000214       | 0.002181    |
| [0.55 - 0.60) | [7.50 - 8.70)  | 0.000563     | 0.000065   | 0.000074       | 0.000571    |
| [0.60 - 0.65) | [4.20 - 4.50)  | 0.040173     | 0.010809   | 0.001161       | 0.041617    |
| [0.60 - 0.65) | [4.50 - 4.80)  | 0.024563     | 0.005615   | 0.000889       | 0.025212    |
| [0.60 - 0.65) | [4.80 - 5.10)  | 0.017374     | 0.003688   | 0.000696       | 0.017775    |
| [0.60 - 0.65) | [5.10 - 5.40)  | 0.011024     | 0.002225   | 0.000393       | 0.011254    |
| [0.60 - 0.65) | [5.40 - 5.70)  | 0.007261     | 0.001362   | 0.000352       | 0.007396    |
| [0.60 - 0.65) | [5.70 - 6.00)  | 0.006245     | 0.001139   | 0.000455       | 0.006364    |
| [0.60 - 0.65) | [6.00 - 6.30)  | 0.004809     | 0.000872   | 0.000317       | 0.004898    |
| [0.60 - 0.65) | [6.30 - 6.60)  | 0.003639     | 0.000641   | 0.000299       | 0.003707    |
| [0.60 - 0.65) | [6.60 - 6.90)  | 0.001526     | 0.000273   | 0.000098       | 0.001554    |
| [0.60 - 0.65) | [6.90 - 7.50)  | 0.001164     | 0.000147   | 0.000132       | 0.001181    |
| [0.60 - 0.65) | [7.50 - 8.70)  | 0.000334     | 0.000038   | 0.000062       | 0.000342    |
| [0.65 - 0.70) | [4.20 - 4.50)  | 0.024537     | 0.006446   | 0.000859       | 0.025384    |
| [0.65 - 0.70) | [4.50 - 4.80)  | 0.018367     | 0.004297   | 0.000734       | 0.018877    |

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Table 4: (Continued)

| $x_F$ Bin     | Mass Bin (GeV) | Trigger Eff. | Acceptance | k-Tracker Eff. | Total Syst. |
|---------------|----------------|--------------|------------|----------------|-------------|
| [0.65 - 0.70) | [4.80 - 5.10)  | 0.010196     | 0.002166   | 0.000407       | 0.010432    |
| [0.65 - 0.70) | [5.10 - 5.40)  | 0.008613     | 0.001753   | 0.000384       | 0.008798    |
| [0.65 - 0.70) | [5.40 - 5.70)  | 0.008247     | 0.001614   | 0.000508       | 0.008419    |
| [0.65 - 0.70) | [5.70 - 6.00)  | 0.004495     | 0.000836   | 0.000349       | 0.004586    |
| [0.65 - 0.70) | [6.00 - 6.30)  | 0.002948     | 0.000528   | 0.000258       | 0.003006    |
| [0.65 - 0.70) | [6.30 - 6.60)  | 0.000881     | 0.000156   | 0.000132       | 0.000905    |
| [0.65 - 0.70) | [6.60 - 6.90)  | 0.001730     | 0.000297   | 0.000210       | 0.001768    |
| [0.65 - 0.70) | [6.90 - 7.50)  | 0.002013     | 0.000264   | 0.000280       | 0.002049    |
| [0.65 - 0.70) | [7.50 - 8.70)  | 0.004838     | 0.000546   | 0.017062       | 0.017743    |
| [0.70 - 0.75) | [4.20 - 4.50)  | 0.018003     | 0.004826   | 0.000928       | 0.018662    |
| [0.70 - 0.75) | [4.50 - 4.80)  | 0.014316     | 0.003395   | 0.000682       | 0.014729    |
| [0.70 - 0.75) | [4.80 - 5.10)  | 0.009071     | 0.001949   | 0.000519       | 0.009293    |
| [0.70 - 0.75) | [5.10 - 5.40)  | 0.005102     | 0.001052   | 0.000465       | 0.005230    |
| [0.70 - 0.75) | [5.40 - 5.70)  | 0.002947     | 0.000565   | 0.000295       | 0.003015    |
| [0.70 - 0.75) | [5.70 - 6.00)  | 0.002329     | 0.000432   | 0.000339       | 0.002393    |
| [0.70 - 0.75) | [6.00 - 6.30)  | 0.002535     | 0.000456   | 0.000594       | 0.002644    |
| [0.70 - 0.75) | [6.30 - 6.60)  | 0.001917     | 0.000343   | 0.000707       | 0.002072    |
| [0.75 - 0.80) | [4.20 - 4.50)  | 0.012861     | 0.003466   | 0.001181       | 0.013372    |
| [0.75 - 0.80) | [4.50 - 4.80)  | 0.002016     | 0.000478   | 0.000132       | 0.002076    |
| [0.75 - 0.80) | [4.80 - 5.10)  | 0.019900     | 0.004388   | 0.022716       | 0.030517    |

<sup>293</sup> **11 Appendix: Table of Cross-Section Values**

Table 5: Detailed cross-section calculation for Bins in  $x_F$  and Mass

| $x_F$ Bin    | Mass Bin (GeV) | Bin Center (GeV) | Bin Average (GeV) | Cross-Section (nb-GeV $^2$ ) | stat. error (nb-GeV $^2$ ) | syst. error (nb-GeV $^2$ ) |
|--------------|----------------|------------------|-------------------|------------------------------|----------------------------|----------------------------|
| [0.00, 0.05) | [4.5, 4.8)     | 4.650            | 4.740             | $5.266 \times 10^0$          | $3.059 \times 10^0$        | $2.239 \times 10^0$        |
| [0.00, 0.05) | [4.8, 5.1)     | 4.950            | 5.006             | $3.939 \times 10^{-1}$       | $2.024 \times 10^{-1}$     | $7.886 \times 10^{-2}$     |
| [0.00, 0.05) | [5.1, 5.4)     | 5.250            | 5.250             | $5.479 \times 10^{-1}$       | $1.864 \times 10^{-1}$     | $9.581 \times 10^{-2}$     |
| [0.00, 0.05) | [5.4, 5.7)     | 5.550            | 5.512             | $2.288 \times 10^{-1}$       | $9.988 \times 10^{-2}$     | $3.684 \times 10^{-2}$     |
| [0.00, 0.05) | [5.7, 6.0)     | 5.850            | 5.828             | $1.751 \times 10^{-1}$       | $7.393 \times 10^{-2}$     | $2.797 \times 10^{-2}$     |
| [0.00, 0.05) | [6.0, 6.3)     | 6.150            | 6.178             | $1.336 \times 10^{-1}$       | $4.716 \times 10^{-2}$     | $2.121 \times 10^{-2}$     |
| [0.00, 0.05) | [6.3, 6.6)     | 6.450            | 6.432             | $1.334 \times 10^{-1}$       | $4.608 \times 10^{-2}$     | $2.187 \times 10^{-2}$     |
| [0.00, 0.05) | [6.6, 6.9)     | 6.750            | 6.749             | $8.415 \times 10^{-2}$       | $2.777 \times 10^{-2}$     | $1.343 \times 10^{-2}$     |
| [0.00, 0.05) | [6.9, 7.5)     | 7.200            | 7.171             | $4.985 \times 10^{-2}$       | $1.846 \times 10^{-2}$     | $7.919 \times 10^{-3}$     |
| [0.00, 0.05) | [7.5, 8.7)     | 8.100            | 7.914             | $6.397 \times 10^{-3}$       | $6.502 \times 10^{-3}$     | $1.163 \times 10^{-3}$     |
| [0.05, 0.10) | [4.5, 4.8)     | 4.650            | 4.627             | $1.926 \times 10^0$          | $1.237 \times 10^0$        | $4.988 \times 10^{-1}$     |
| [0.05, 0.10) | [4.8, 5.1)     | 4.950            | 4.944             | $1.125 \times 10^0$          | $3.799 \times 10^{-1}$     | $2.146 \times 10^{-1}$     |
| [0.05, 0.10) | [5.1, 5.4)     | 5.250            | 5.251             | $3.763 \times 10^{-1}$       | $1.199 \times 10^{-1}$     | $6.160 \times 10^{-2}$     |
| [0.05, 0.10) | [5.4, 5.7)     | 5.550            | 5.526             | $2.182 \times 10^{-1}$       | $6.716 \times 10^{-2}$     | $3.444 \times 10^{-2}$     |
| [0.05, 0.10) | [5.7, 6.0)     | 5.850            | 5.865             | $1.348 \times 10^{-1}$       | $5.227 \times 10^{-2}$     | $2.104 \times 10^{-2}$     |
| [0.05, 0.10) | [6.0, 6.3)     | 6.150            | 6.086             | $1.224 \times 10^{-1}$       | $4.329 \times 10^{-2}$     | $1.893 \times 10^{-2}$     |
| [0.05, 0.10) | [6.3, 6.6)     | 6.450            | 6.408             | $1.042 \times 10^{-1}$       | $3.840 \times 10^{-2}$     | $1.638 \times 10^{-2}$     |
| [0.05, 0.10) | [6.6, 6.9)     | 6.750            | 6.725             | $1.732 \times 10^{-2}$       | $1.601 \times 10^{-2}$     | $2.897 \times 10^{-3}$     |
| [0.05, 0.10) | [6.9, 7.5)     | 7.200            | 7.125             | $2.747 \times 10^{-2}$       | $1.126 \times 10^{-2}$     | $4.316 \times 10^{-3}$     |
| [0.05, 0.10) | [7.5, 8.7)     | 8.100            | 7.731             | $2.382 \times 10^{-2}$       | $1.045 \times 10^{-2}$     | $3.762 \times 10^{-3}$     |
| [0.10, 0.15) | [4.5, 4.8)     | 4.650            | 4.685             | $1.342 \times 10^0$          | $4.340 \times 10^{-1}$     | $2.729 \times 10^{-1}$     |
| [0.10, 0.15) | [4.8, 5.1)     | 4.950            | 4.956             | $5.636 \times 10^{-1}$       | $1.621 \times 10^{-1}$     | $9.374 \times 10^{-2}$     |
| [0.10, 0.15) | [5.1, 5.4)     | 5.250            | 5.231             | $5.540 \times 10^{-1}$       | $1.229 \times 10^{-1}$     | $8.833 \times 10^{-2}$     |
| [0.10, 0.15) | [5.4, 5.7)     | 5.550            | 5.500             | $2.050 \times 10^{-1}$       | $6.525 \times 10^{-2}$     | $3.192 \times 10^{-2}$     |
| [0.10, 0.15) | [5.7, 6.0)     | 5.850            | 5.816             | $1.653 \times 10^{-1}$       | $5.186 \times 10^{-2}$     | $2.550 \times 10^{-2}$     |
| [0.10, 0.15) | [6.0, 6.3)     | 6.150            | 6.139             | $1.593 \times 10^{-1}$       | $3.486 \times 10^{-2}$     | $2.447 \times 10^{-2}$     |
| [0.10, 0.15) | [6.3, 6.6)     | 6.450            | 6.440             | $7.560 \times 10^{-2}$       | $2.478 \times 10^{-2}$     | $1.158 \times 10^{-2}$     |
| [0.10, 0.15) | [6.6, 6.9)     | 6.750            | 6.746             | $4.070 \times 10^{-2}$       | $1.434 \times 10^{-2}$     | $6.307 \times 10^{-3}$     |
| [0.10, 0.15) | [6.9, 7.5)     | 7.200            | 7.114             | $2.932 \times 10^{-2}$       | $1.115 \times 10^{-2}$     | $4.481 \times 10^{-3}$     |
| [0.10, 0.15) | [7.5, 8.7)     | 8.100            | 7.838             | $1.941 \times 10^{-2}$       | $7.930 \times 10^{-3}$     | $2.950 \times 10^{-3}$     |
| [0.15, 0.20) | [4.5, 4.8)     | 4.650            | 4.656             | $8.386 \times 10^{-1}$       | $2.133 \times 10^{-1}$     | $1.459 \times 10^{-1}$     |
| [0.15, 0.20) | [4.8, 5.1)     | 4.950            | 4.920             | $7.798 \times 10^{-1}$       | $1.766 \times 10^{-1}$     | $1.250 \times 10^{-1}$     |
| [0.15, 0.20) | [5.1, 5.4)     | 5.250            | 5.251             | $4.922 \times 10^{-1}$       | $1.046 \times 10^{-1}$     | $7.695 \times 10^{-2}$     |
| [0.15, 0.20) | [5.4, 5.7)     | 5.550            | 5.520             | $2.781 \times 10^{-1}$       | $6.083 \times 10^{-2}$     | $4.283 \times 10^{-2}$     |
| [0.15, 0.20) | [5.7, 6.0)     | 5.850            | 5.833             | $2.396 \times 10^{-1}$       | $5.007 \times 10^{-2}$     | $3.676 \times 10^{-2}$     |
| [0.15, 0.20) | [6.0, 6.3)     | 6.150            | 6.138             | $1.352 \times 10^{-1}$       | $3.967 \times 10^{-2}$     | $2.065 \times 10^{-2}$     |
| [0.15, 0.20) | [6.3, 6.6)     | 6.450            | 6.467             | $7.119 \times 10^{-2}$       | $2.568 \times 10^{-2}$     | $1.084 \times 10^{-2}$     |
| [0.15, 0.20) | [6.6, 6.9)     | 6.750            | 6.748             | $5.584 \times 10^{-2}$       | $1.640 \times 10^{-2}$     | $8.596 \times 10^{-3}$     |
| [0.15, 0.20) | [6.9, 7.5)     | 7.200            | 6.919             | $1.985 \times 10^{-2}$       | $1.594 \times 10^{-2}$     | $3.019 \times 10^{-3}$     |
| [0.15, 0.20) | [7.5, 8.7)     | 8.100            | 7.632             | $6.576 \times 10^{-3}$       | $3.945 \times 10^{-3}$     | $1.065 \times 10^{-3}$     |
| [0.20, 0.25) | [4.2, 4.5)     | 4.350            | 4.347             | $1.123 \times 10^0$          | $3.376 \times 10^{-1}$     | $2.072 \times 10^{-1}$     |
| [0.20, 0.25) | [4.5, 4.8)     | 4.650            | 4.653             | $9.809 \times 10^{-1}$       | $2.274 \times 10^{-1}$     | $1.620 \times 10^{-1}$     |
| [0.20, 0.25) | [4.8, 5.1)     | 4.950            | 4.953             | $6.905 \times 10^{-1}$       | $1.291 \times 10^{-1}$     | $1.081 \times 10^{-1}$     |
| [0.20, 0.25) | [5.1, 5.4)     | 5.250            | 5.237             | $3.602 \times 10^{-1}$       | $7.549 \times 10^{-2}$     | $5.544 \times 10^{-2}$     |

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Table 5: (Continued)

| $x_F$ Bin    | Mass Bin (GeV) | Bin Center (GeV) | Bin Average (GeV) | Cross-Section (nb-GeV $^2$ ) | stat. error (nb-GeV $^2$ ) | syst. error (nb-GeV $^2$ ) |
|--------------|----------------|------------------|-------------------|------------------------------|----------------------------|----------------------------|
| [0.20, 0.25) | [5.4, 5.7)     | 5.550            | 5.539             | $2.830 \times 10^{-1}$       | $5.529 \times 10^{-2}$     | $4.333 \times 10^{-2}$     |
| [0.20, 0.25) | [5.7, 6.0)     | 5.850            | 5.835             | $1.885 \times 10^{-1}$       | $3.880 \times 10^{-2}$     | $2.868 \times 10^{-2}$     |
| [0.20, 0.25) | [6.0, 6.3)     | 6.150            | 6.157             | $8.814 \times 10^{-2}$       | $3.025 \times 10^{-2}$     | $1.341 \times 10^{-2}$     |
| [0.20, 0.25) | [6.3, 6.6)     | 6.450            | 6.463             | $1.114 \times 10^{-1}$       | $2.832 \times 10^{-2}$     | $1.692 \times 10^{-2}$     |
| [0.20, 0.25) | [6.6, 6.9)     | 6.750            | 6.761             | $4.295 \times 10^{-2}$       | $1.858 \times 10^{-2}$     | $6.533 \times 10^{-3}$     |
| [0.20, 0.25) | [6.9, 7.5)     | 7.200            | 7.136             | $9.224 \times 10^{-3}$       | $1.130 \times 10^{-2}$     | $1.398 \times 10^{-3}$     |
| [0.20, 0.25) | [7.5, 8.7)     | 8.100            | 7.634             | $9.030 \times 10^{-3}$       | $3.932 \times 10^{-3}$     | $1.359 \times 10^{-3}$     |
| [0.25, 0.30) | [4.2, 4.5)     | 4.350            | 4.390             | $9.555 \times 10^{-1}$       | $2.055 \times 10^{-1}$     | $1.594 \times 10^{-1}$     |
| [0.25, 0.30) | [4.5, 4.8)     | 4.650            | 4.653             | $8.799 \times 10^{-1}$       | $1.686 \times 10^{-1}$     | $1.401 \times 10^{-1}$     |
| [0.25, 0.30) | [4.8, 5.1)     | 4.950            | 4.947             | $5.381 \times 10^{-1}$       | $9.957 \times 10^{-2}$     | $8.322 \times 10^{-2}$     |
| [0.25, 0.30) | [5.1, 5.4)     | 5.250            | 5.243             | $3.692 \times 10^{-1}$       | $6.835 \times 10^{-2}$     | $5.651 \times 10^{-2}$     |
| [0.25, 0.30) | [5.4, 5.7)     | 5.550            | 5.555             | $2.607 \times 10^{-1}$       | $5.198 \times 10^{-2}$     | $3.970 \times 10^{-2}$     |
| [0.25, 0.30) | [5.7, 6.0)     | 5.850            | 5.840             | $1.580 \times 10^{-1}$       | $3.113 \times 10^{-2}$     | $2.397 \times 10^{-2}$     |
| [0.25, 0.30) | [6.0, 6.3)     | 6.150            | 6.144             | $1.193 \times 10^{-1}$       | $2.663 \times 10^{-2}$     | $1.809 \times 10^{-2}$     |
| [0.25, 0.30) | [6.3, 6.6)     | 6.450            | 6.466             | $5.200 \times 10^{-2}$       | $1.901 \times 10^{-2}$     | $7.862 \times 10^{-3}$     |
| [0.25, 0.30) | [6.6, 6.9)     | 6.750            | 6.755             | $5.223 \times 10^{-2}$       | $1.888 \times 10^{-2}$     | $7.941 \times 10^{-3}$     |
| [0.25, 0.30) | [6.9, 7.5)     | 7.200            | 7.107             | $3.464 \times 10^{-2}$       | $9.170 \times 10^{-3}$     | $5.206 \times 10^{-3}$     |
| [0.25, 0.30) | [7.5, 8.7)     | 8.100            | 7.598             | $3.508 \times 10^{-3}$       | $2.544 \times 10^{-3}$     | $5.647 \times 10^{-4}$     |
| [0.30, 0.35) | [4.2, 4.5)     | 4.350            | 4.355             | $9.682 \times 10^{-1}$       | $1.855 \times 10^{-1}$     | $1.565 \times 10^{-1}$     |
| [0.30, 0.35) | [4.5, 4.8)     | 4.650            | 4.665             | $6.779 \times 10^{-1}$       | $1.236 \times 10^{-1}$     | $1.058 \times 10^{-1}$     |
| [0.30, 0.35) | [4.8, 5.1)     | 4.950            | 4.947             | $5.308 \times 10^{-1}$       | $9.068 \times 10^{-2}$     | $8.131 \times 10^{-2}$     |
| [0.30, 0.35) | [5.1, 5.4)     | 5.250            | 5.249             | $3.533 \times 10^{-1}$       | $6.288 \times 10^{-2}$     | $5.383 \times 10^{-2}$     |
| [0.30, 0.35) | [5.4, 5.7)     | 5.550            | 5.542             | $2.390 \times 10^{-1}$       | $4.623 \times 10^{-2}$     | $3.623 \times 10^{-2}$     |
| [0.30, 0.35) | [5.7, 6.0)     | 5.850            | 5.844             | $1.341 \times 10^{-1}$       | $2.975 \times 10^{-2}$     | $2.032 \times 10^{-2}$     |
| [0.30, 0.35) | [6.0, 6.3)     | 6.150            | 6.133             | $1.089 \times 10^{-1}$       | $2.213 \times 10^{-2}$     | $1.649 \times 10^{-2}$     |
| [0.30, 0.35) | [6.3, 6.6)     | 6.450            | 6.384             | $6.800 \times 10^{-2}$       | $2.056 \times 10^{-2}$     | $1.028 \times 10^{-2}$     |
| [0.30, 0.35) | [6.6, 6.9)     | 6.750            | 6.741             | $5.420 \times 10^{-2}$       | $1.360 \times 10^{-2}$     | $8.208 \times 10^{-3}$     |
| [0.30, 0.35) | [6.9, 7.5)     | 7.200            | 7.045             | $2.497 \times 10^{-2}$       | $6.858 \times 10^{-3}$     | $3.756 \times 10^{-3}$     |
| [0.30, 0.35) | [7.5, 8.7)     | 8.100            | 7.919             | $1.181 \times 10^{-2}$       | $4.331 \times 10^{-3}$     | $1.773 \times 10^{-3}$     |
| [0.35, 0.40) | [4.2, 4.5)     | 4.350            | 4.337             | $7.196 \times 10^{-1}$       | $1.297 \times 10^{-1}$     | $1.131 \times 10^{-1}$     |
| [0.35, 0.40) | [4.5, 4.8)     | 4.650            | 4.640             | $6.796 \times 10^{-1}$       | $1.152 \times 10^{-1}$     | $1.048 \times 10^{-1}$     |
| [0.35, 0.40) | [4.8, 5.1)     | 4.950            | 4.943             | $4.901 \times 10^{-1}$       | $8.446 \times 10^{-2}$     | $7.496 \times 10^{-2}$     |
| [0.35, 0.40) | [5.1, 5.4)     | 5.250            | 5.238             | $3.254 \times 10^{-1}$       | $5.543 \times 10^{-2}$     | $4.937 \times 10^{-2}$     |
| [0.35, 0.40) | [5.4, 5.7)     | 5.550            | 5.515             | $1.406 \times 10^{-1}$       | $3.281 \times 10^{-2}$     | $2.127 \times 10^{-2}$     |
| [0.35, 0.40) | [5.7, 6.0)     | 5.850            | 5.832             | $1.385 \times 10^{-1}$       | $2.843 \times 10^{-2}$     | $2.093 \times 10^{-2}$     |
| [0.35, 0.40) | [6.0, 6.3)     | 6.150            | 6.125             | $9.033 \times 10^{-2}$       | $2.093 \times 10^{-2}$     | $1.364 \times 10^{-2}$     |
| [0.35, 0.40) | [6.3, 6.6)     | 6.450            | 6.446             | $4.087 \times 10^{-2}$       | $1.947 \times 10^{-2}$     | $6.165 \times 10^{-3}$     |
| [0.35, 0.40) | [6.6, 6.9)     | 6.750            | 6.727             | $4.011 \times 10^{-2}$       | $1.084 \times 10^{-2}$     | $6.072 \times 10^{-3}$     |
| [0.35, 0.40) | [6.9, 7.5)     | 7.200            | 7.175             | $2.263 \times 10^{-2}$       | $6.209 \times 10^{-3}$     | $3.390 \times 10^{-3}$     |
| [0.35, 0.40) | [7.5, 8.7)     | 8.100            | 7.764             | $9.710 \times 10^{-3}$       | $3.761 \times 10^{-3}$     | $1.469 \times 10^{-3}$     |
| [0.40, 0.45) | [4.2, 4.5)     | 4.350            | 4.351             | $6.714 \times 10^{-1}$       | $1.212 \times 10^{-1}$     | $1.047 \times 10^{-1}$     |
| [0.40, 0.45) | [4.5, 4.8)     | 4.650            | 4.642             | $5.134 \times 10^{-1}$       | $8.883 \times 10^{-2}$     | $7.874 \times 10^{-2}$     |
| [0.40, 0.45) | [4.8, 5.1)     | 4.950            | 4.934             | $3.737 \times 10^{-1}$       | $6.449 \times 10^{-2}$     | $5.678 \times 10^{-2}$     |
| [0.40, 0.45) | [5.1, 5.4)     | 5.250            | 5.231             | $2.572 \times 10^{-1}$       | $4.759 \times 10^{-2}$     | $3.901 \times 10^{-2}$     |
| [0.40, 0.45) | [5.4, 5.7)     | 5.550            | 5.514             | $1.904 \times 10^{-1}$       | $3.491 \times 10^{-2}$     | $2.876 \times 10^{-2}$     |
| [0.40, 0.45) | [5.7, 6.0)     | 5.850            | 5.854             | $1.021 \times 10^{-1}$       | $2.355 \times 10^{-2}$     | $1.540 \times 10^{-2}$     |
| [0.40, 0.45) | [6.0, 6.3)     | 6.150            | 6.176             | $1.010 \times 10^{-1}$       | $2.152 \times 10^{-2}$     | $1.521 \times 10^{-2}$     |

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Table 5: (Continued)

| $x_F$ Bin    | Mass Bin (GeV) | Bin Center (GeV) | Bin Average (GeV) | Cross-Section (nb-GeV $^2$ ) | stat. error (nb-GeV $^2$ ) | syst. error (nb-GeV $^2$ ) |
|--------------|----------------|------------------|-------------------|------------------------------|----------------------------|----------------------------|
| [0.40, 0.45) | [6.3, 6.6)     | 6.450            | 6.422             | $8.200 \times 10^{-2}$       | $1.722 \times 10^{-2}$     | $1.238 \times 10^{-2}$     |
| [0.40, 0.45) | [6.6, 6.9)     | 6.750            | 6.751             | $3.902 \times 10^{-2}$       | $9.905 \times 10^{-3}$     | $5.877 \times 10^{-3}$     |
| [0.40, 0.45) | [6.9, 7.5)     | 7.200            | 7.100             | $1.729 \times 10^{-2}$       | $8.435 \times 10^{-3}$     | $2.593 \times 10^{-3}$     |
| [0.40, 0.45) | [7.5, 8.7)     | 8.100            | 7.821             | $3.316 \times 10^{-3}$       | $4.877 \times 10^{-3}$     | $4.960 \times 10^{-4}$     |
| [0.45, 0.50) | [4.2, 4.5)     | 4.350            | 4.344             | $5.316 \times 10^{-1}$       | $9.382 \times 10^{-2}$     | $8.197 \times 10^{-2}$     |
| [0.45, 0.50) | [4.5, 4.8)     | 4.650            | 4.642             | $4.566 \times 10^{-1}$       | $7.742 \times 10^{-2}$     | $6.977 \times 10^{-2}$     |
| [0.45, 0.50) | [4.8, 5.1)     | 4.950            | 4.940             | $3.634 \times 10^{-1}$       | $6.084 \times 10^{-2}$     | $5.521 \times 10^{-2}$     |
| [0.45, 0.50) | [5.1, 5.4)     | 5.250            | 5.238             | $1.934 \times 10^{-1}$       | $3.633 \times 10^{-2}$     | $2.925 \times 10^{-2}$     |
| [0.45, 0.50) | [5.4, 5.7)     | 5.550            | 5.523             | $1.407 \times 10^{-1}$       | $2.747 \times 10^{-2}$     | $2.124 \times 10^{-2}$     |
| [0.45, 0.50) | [5.7, 6.0)     | 5.850            | 5.841             | $1.047 \times 10^{-1}$       | $2.125 \times 10^{-2}$     | $1.577 \times 10^{-2}$     |
| [0.45, 0.50) | [6.0, 6.3)     | 6.150            | 6.135             | $7.260 \times 10^{-2}$       | $1.647 \times 10^{-2}$     | $1.095 \times 10^{-2}$     |
| [0.45, 0.50) | [6.3, 6.6)     | 6.450            | 6.437             | $7.758 \times 10^{-2}$       | $1.612 \times 10^{-2}$     | $1.169 \times 10^{-2}$     |
| [0.45, 0.50) | [6.6, 6.9)     | 6.750            | 6.741             | $2.839 \times 10^{-2}$       | $8.681 \times 10^{-3}$     | $4.303 \times 10^{-3}$     |
| [0.45, 0.50) | [6.9, 7.5)     | 7.200            | 7.198             | $2.889 \times 10^{-2}$       | $7.053 \times 10^{-3}$     | $4.319 \times 10^{-3}$     |
| [0.45, 0.50) | [7.5, 8.7)     | 8.100            | 7.828             | $6.752 \times 10^{-3}$       | $2.599 \times 10^{-3}$     | $1.011 \times 10^{-3}$     |
| [0.50, 0.55) | [4.2, 4.5)     | 4.350            | 4.353             | $6.177 \times 10^{-1}$       | $1.029 \times 10^{-1}$     | $9.501 \times 10^{-2}$     |
| [0.50, 0.55) | [4.5, 4.8)     | 4.650            | 4.620             | $2.623 \times 10^{-1}$       | $4.829 \times 10^{-2}$     | $3.987 \times 10^{-2}$     |
| [0.50, 0.55) | [4.8, 5.1)     | 4.950            | 4.949             | $2.420 \times 10^{-1}$       | $4.259 \times 10^{-2}$     | $3.665 \times 10^{-2}$     |
| [0.50, 0.55) | [5.1, 5.4)     | 5.250            | 5.246             | $1.756 \times 10^{-1}$       | $3.222 \times 10^{-2}$     | $2.653 \times 10^{-2}$     |
| [0.50, 0.55) | [5.4, 5.7)     | 5.550            | 5.534             | $1.216 \times 10^{-1}$       | $2.718 \times 10^{-2}$     | $1.835 \times 10^{-2}$     |
| [0.50, 0.55) | [5.7, 6.0)     | 5.850            | 5.843             | $7.100 \times 10^{-2}$       | $1.676 \times 10^{-2}$     | $1.069 \times 10^{-2}$     |
| [0.50, 0.55) | [6.0, 6.3)     | 6.150            | 6.121             | $4.488 \times 10^{-2}$       | $1.451 \times 10^{-2}$     | $6.773 \times 10^{-3}$     |
| [0.50, 0.55) | [6.3, 6.6)     | 6.450            | 6.417             | $4.836 \times 10^{-2}$       | $1.310 \times 10^{-2}$     | $7.288 \times 10^{-3}$     |
| [0.50, 0.55) | [6.6, 6.9)     | 6.750            | 6.690             | $2.704 \times 10^{-2}$       | $7.906 \times 10^{-3}$     | $4.094 \times 10^{-3}$     |
| [0.50, 0.55) | [6.9, 7.5)     | 7.200            | 7.135             | $1.315 \times 10^{-2}$       | $4.040 \times 10^{-3}$     | $1.970 \times 10^{-3}$     |
| [0.50, 0.55) | [7.5, 8.7)     | 8.100            | 7.861             | $8.646 \times 10^{-3}$       | $3.042 \times 10^{-3}$     | $1.294 \times 10^{-3}$     |
| [0.55, 0.60) | [4.2, 4.5)     | 4.350            | 4.348             | $3.313 \times 10^{-1}$       | $5.895 \times 10^{-2}$     | $5.075 \times 10^{-2}$     |
| [0.55, 0.60) | [4.5, 4.8)     | 4.650            | 4.634             | $3.055 \times 10^{-1}$       | $5.112 \times 10^{-2}$     | $4.644 \times 10^{-2}$     |
| [0.55, 0.60) | [4.8, 5.1)     | 4.950            | 4.951             | $2.106 \times 10^{-1}$       | $3.677 \times 10^{-2}$     | $3.194 \times 10^{-2}$     |
| [0.55, 0.60) | [5.1, 5.4)     | 5.250            | 5.247             | $1.289 \times 10^{-1}$       | $2.334 \times 10^{-2}$     | $1.945 \times 10^{-2}$     |
| [0.55, 0.60) | [5.4, 5.7)     | 5.550            | 5.524             | $7.481 \times 10^{-2}$       | $1.696 \times 10^{-2}$     | $1.129 \times 10^{-2}$     |
| [0.55, 0.60) | [5.7, 6.0)     | 5.850            | 5.830             | $5.187 \times 10^{-2}$       | $1.452 \times 10^{-2}$     | $7.810 \times 10^{-3}$     |
| [0.55, 0.60) | [6.0, 6.3)     | 6.150            | 6.118             | $2.691 \times 10^{-2}$       | $1.286 \times 10^{-2}$     | $4.048 \times 10^{-3}$     |
| [0.55, 0.60) | [6.3, 6.6)     | 6.450            | 6.420             | $2.321 \times 10^{-2}$       | $9.228 \times 10^{-3}$     | $3.497 \times 10^{-3}$     |
| [0.55, 0.60) | [6.6, 6.9)     | 6.750            | 6.697             | $2.299 \times 10^{-2}$       | $6.715 \times 10^{-3}$     | $3.468 \times 10^{-3}$     |
| [0.55, 0.60) | [6.9, 7.5)     | 7.200            | 7.185             | $1.455 \times 10^{-2}$       | $4.465 \times 10^{-3}$     | $2.181 \times 10^{-3}$     |
| [0.55, 0.60) | [7.5, 8.7)     | 8.100            | 7.799             | $3.803 \times 10^{-3}$       | $1.816 \times 10^{-3}$     | $5.711 \times 10^{-4}$     |
| [0.60, 0.65) | [4.2, 4.5)     | 4.350            | 4.357             | $2.716 \times 10^{-1}$       | $4.774 \times 10^{-2}$     | $4.162 \times 10^{-2}$     |
| [0.60, 0.65) | [4.5, 4.8)     | 4.650            | 4.666             | $1.660 \times 10^{-1}$       | $3.053 \times 10^{-2}$     | $2.521 \times 10^{-2}$     |
| [0.60, 0.65) | [4.8, 5.1)     | 4.950            | 4.945             | $1.174 \times 10^{-1}$       | $2.239 \times 10^{-2}$     | $1.777 \times 10^{-2}$     |
| [0.60, 0.65) | [5.1, 5.4)     | 5.250            | 5.240             | $7.452 \times 10^{-2}$       | $1.633 \times 10^{-2}$     | $1.125 \times 10^{-2}$     |
| [0.60, 0.65) | [5.4, 5.7)     | 5.550            | 5.547             | $4.908 \times 10^{-2}$       | $1.178 \times 10^{-2}$     | $7.396 \times 10^{-3}$     |
| [0.60, 0.65) | [5.7, 6.0)     | 5.850            | 5.815             | $4.222 \times 10^{-2}$       | $1.379 \times 10^{-2}$     | $6.364 \times 10^{-3}$     |
| [0.60, 0.65) | [6.0, 6.3)     | 6.150            | 6.146             | $3.251 \times 10^{-2}$       | $1.119 \times 10^{-2}$     | $4.898 \times 10^{-3}$     |
| [0.60, 0.65) | [6.3, 6.6)     | 6.450            | 6.406             | $2.460 \times 10^{-2}$       | $6.754 \times 10^{-3}$     | $3.707 \times 10^{-3}$     |
| [0.60, 0.65) | [6.6, 6.9)     | 6.750            | 6.708             | $1.032 \times 10^{-2}$       | $8.032 \times 10^{-3}$     | $1.554 \times 10^{-3}$     |
| [0.60, 0.65) | [6.9, 7.5)     | 7.200            | 7.225             | $7.869 \times 10^{-3}$       | $3.112 \times 10^{-3}$     | $1.181 \times 10^{-3}$     |

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Table 5: (Continued)

| $x_F$ Bin    | Mass Bin (GeV) | Bin Center (GeV) | Bin Average (GeV) | Cross-Section (nb-GeV $^2$ ) | stat. error (nb-GeV $^2$ ) | syst. error (nb-GeV $^2$ ) |
|--------------|----------------|------------------|-------------------|------------------------------|----------------------------|----------------------------|
| [0.60, 0.65) | [7.5, 8.7)     | 8.100            | 8.039             | $2.259 \times 10^{-3}$       | $1.368 \times 10^{-3}$     | $3.421 \times 10^{-4}$     |
| [0.65, 0.70) | [4.2, 4.5)     | 4.350            | 4.324             | $1.659 \times 10^{-1}$       | $3.011 \times 10^{-2}$     | $2.538 \times 10^{-2}$     |
| [0.65, 0.70) | [4.5, 4.8)     | 4.650            | 4.650             | $1.242 \times 10^{-1}$       | $2.342 \times 10^{-2}$     | $1.888 \times 10^{-2}$     |
| [0.65, 0.70) | [4.8, 5.1)     | 4.950            | 4.923             | $6.892 \times 10^{-2}$       | $1.510 \times 10^{-2}$     | $1.043 \times 10^{-2}$     |
| [0.65, 0.70) | [5.1, 5.4)     | 5.250            | 5.219             | $5.822 \times 10^{-2}$       | $1.511 \times 10^{-2}$     | $8.798 \times 10^{-3}$     |
| [0.65, 0.70) | [5.4, 5.7)     | 5.550            | 5.535             | $5.575 \times 10^{-2}$       | $1.145 \times 10^{-2}$     | $8.419 \times 10^{-3}$     |
| [0.65, 0.70) | [5.7, 6.0)     | 5.850            | 5.840             | $3.039 \times 10^{-2}$       | $7.325 \times 10^{-3}$     | $4.586 \times 10^{-3}$     |
| [0.65, 0.70) | [6.0, 6.3)     | 6.150            | 6.125             | $1.993 \times 10^{-2}$       | $8.279 \times 10^{-3}$     | $3.006 \times 10^{-3}$     |
| [0.65, 0.70) | [6.3, 6.6)     | 6.450            | 6.440             | $5.959 \times 10^{-3}$       | $6.988 \times 10^{-3}$     | $9.048 \times 10^{-4}$     |
| [0.65, 0.70) | [6.6, 6.9)     | 6.750            | 6.734             | $1.170 \times 10^{-2}$       | $4.284 \times 10^{-3}$     | $1.768 \times 10^{-3}$     |
| [0.65, 0.70) | [6.9, 7.5)     | 7.200            | 7.164             | $1.361 \times 10^{-2}$       | $4.073 \times 10^{-3}$     | $2.049 \times 10^{-3}$     |
| [0.65, 0.70) | [7.5, 8.7)     | 8.100            | 7.654             | $3.270 \times 10^{-2}$       | $2.300 \times 10^{-2}$     | $1.774 \times 10^{-2}$     |
| [0.70, 0.75) | [4.2, 4.5)     | 4.350            | 4.334             | $1.217 \times 10^{-1}$       | $2.425 \times 10^{-2}$     | $1.866 \times 10^{-2}$     |
| [0.70, 0.75) | [4.5, 4.8)     | 4.650            | 4.635             | $9.677 \times 10^{-2}$       | $1.880 \times 10^{-2}$     | $1.473 \times 10^{-2}$     |
| [0.70, 0.75) | [4.8, 5.1)     | 4.950            | 4.944             | $6.132 \times 10^{-2}$       | $1.289 \times 10^{-2}$     | $9.293 \times 10^{-3}$     |
| [0.70, 0.75) | [5.1, 5.4)     | 5.250            | 5.257             | $3.449 \times 10^{-2}$       | $9.039 \times 10^{-3}$     | $5.230 \times 10^{-3}$     |
| [0.70, 0.75) | [5.4, 5.7)     | 5.550            | 5.585             | $1.992 \times 10^{-2}$       | $6.850 \times 10^{-3}$     | $3.015 \times 10^{-3}$     |
| [0.70, 0.75) | [5.7, 6.0)     | 5.850            | 5.829             | $1.574 \times 10^{-2}$       | $4.508 \times 10^{-3}$     | $2.393 \times 10^{-3}$     |
| [0.70, 0.75) | [6.0, 6.3)     | 6.150            | 6.128             | $1.714 \times 10^{-2}$       | $5.156 \times 10^{-3}$     | $2.644 \times 10^{-3}$     |
| [0.70, 0.75) | [6.3, 6.6)     | 6.450            | 6.475             | $1.296 \times 10^{-2}$       | $4.424 \times 10^{-3}$     | $2.072 \times 10^{-3}$     |
| [0.75, 0.80) | [4.2, 4.5)     | 4.350            | 4.347             | $8.694 \times 10^{-2}$       | $1.875 \times 10^{-2}$     | $1.337 \times 10^{-2}$     |
| [0.75, 0.80) | [4.5, 4.8)     | 4.650            | 4.615             | $1.363 \times 10^{-2}$       | $8.592 \times 10^{-3}$     | $2.076 \times 10^{-3}$     |
| [0.75, 0.80) | [4.8, 5.1)     | 4.950            | 4.935             | $1.345 \times 10^{-1}$       | $7.332 \times 10^{-2}$     | $3.052 \times 10^{-2}$     |

<sup>294</sup> **12 Appendix: Transverse Momentum Distributions**

295 References

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