

Deviation Impact on MSO_g (for small α)

Let,

The total number of contours be k (IC_1, IC_k)

Cost of all contours except IC_{k-1} is deviated by $(1 + \alpha)$

Cost Incurred due to Bouquet Sequence

$$BS_{cost} = CC_{k-1} + (1 + \alpha) * (CC_k + \sum_{i=1}^{k-2} CC_i)$$

Best possible cost

$$OPT_{cost} = \lim_{h \rightarrow 0} (CC_{k-1} + h) = CC_{k-1}$$

$$\begin{aligned} MSO_g &= \frac{BS_{cost}}{OPT_{cost}} = \frac{(1 + \alpha) * \sum_{i=1}^k CC_i - \alpha * CC_{k-1}}{CC_{k-1}} \\ &= (1 + \alpha) * \frac{r_{pb}^2}{r_{pb}-1} - \alpha \\ &\leq \frac{r_{pb}^2}{r_{pb}-1} * (1 + \alpha) = \frac{r_{pb}^2}{r_{pb}-1} * \eta \end{aligned}$$

Using $r_{pb} = 2$, we will get MSO_g

$$4 * (1 + \alpha) = 4 * \eta$$

Cost Deviation (η) should always respect

$$1 \leq (1 + \alpha) = \eta \ll r_{pb}$$