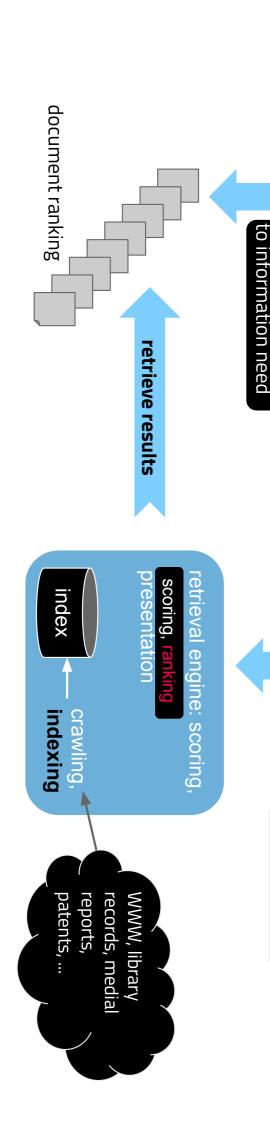
IN4325 Learning to Rank (L2R)

Claudia Hauff (WIS, TU Delft)

The big picture

I he essence of IR

download the latest beta version for macOS Sierra? **Information need**: Looks like I need Eclipse for this job. Where can I



Information need

to know more about Topic the user wants

Query

search engine into an input for the Translation of need

Relevance

information need answers to the A document is (partially) provides relevant if it

eclipse download osx underspecified

ncomplete,

user

retine++ a query

assess relevance

L2R

Conventional ranking models in IR

Language Modeling	BM25	Boolean model obta	Vector space model How	Query-dependent models
		number of models (continuously proposed in the literature) to obtain an even better model?	How can we combine a large	S Query-ind
Readahility	Spaminess	TrustRank	PageRank	ndependent models

Overview

Learning-to-rank

in the broad sense are all methods that use machine learning to solve the problem of ranking

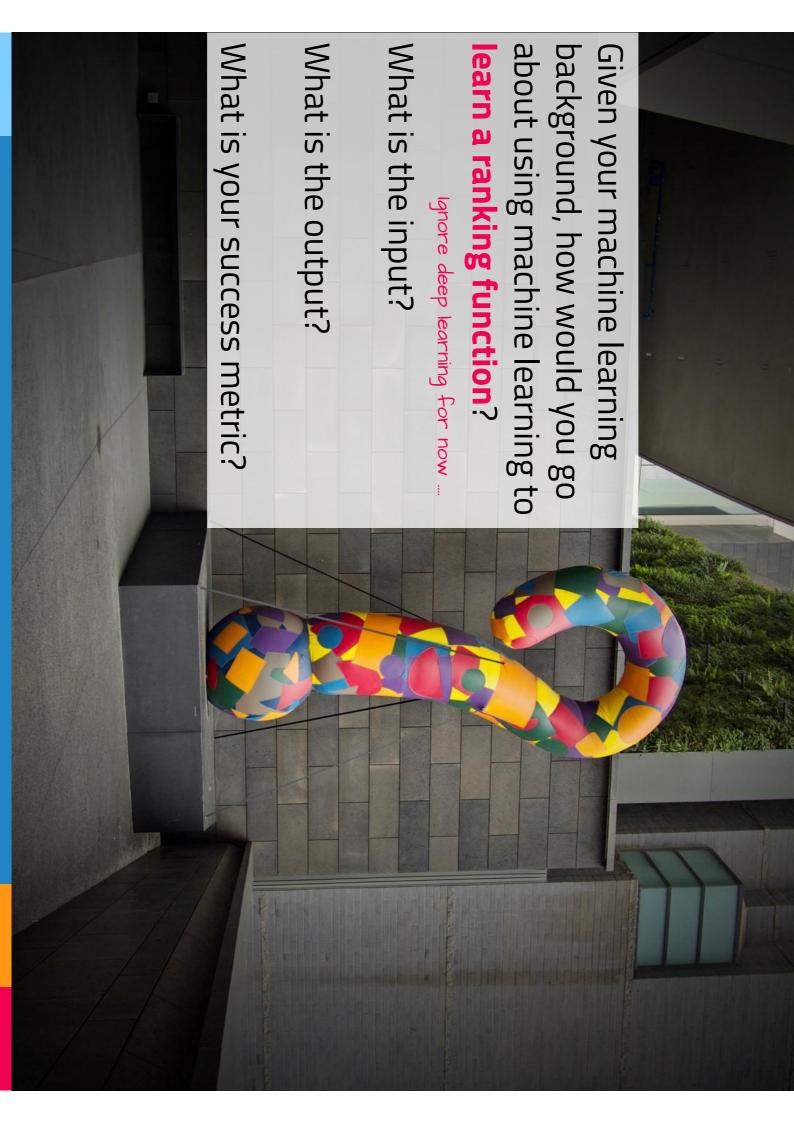
(e.g. relevance feedback, hyperparameter tuning of BM25 ...)

Learning-to-rank

in the narrow sense are all methods that learn the optimal way to combine **features** extracted from query-document pairs through **discriminative** training

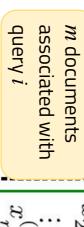
Learns the conditional probability distribution P(y|x).

Generative training learns P(x,y) instead.





_2R setup

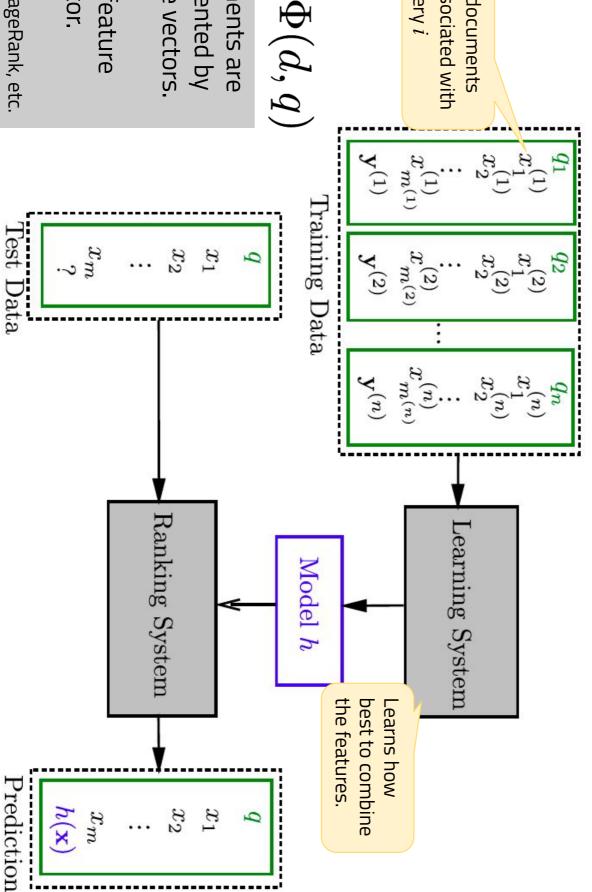


 $x = \Phi(d, q)$

represented by Documents are feature vectors.

extractor. Φ is a feature

can be a feature. BM25, PageRank, etc.



Document judgment strategies

with respect to a query (topic)

- Specifying whether a document is relevant (binary) or specifying a degree of relevance (Fair > Bad)
- Specifying whether a document is more preterence) relevant than another one (relative
- Specifying the partial or total order of documents (a set of permutations)

UQV100: many queries per topic

about buying one, and wonder how much they cost. model called a Raspberry Pi. You start thinking being the way of the future, including one recent You have heard quite a lot about cheap computing മ മ

amazon raspberry pi

best deal raspberry pi computer

buy Raspberry Pi

buying a raspberry pi price

cheap Raspberry Pi

cost of raspberry pi computing model

how much a Raspberry Pi?

how much Raspberry Pi

Pi cost

price comparions for 'Raspberry Pi' computer

100 topics of the 2013/14 TREC Web track

10,835 queries were collected from 263 crowd workers

Relevance judgments on a depth pool of 10 (based on Indri-BM25)

UQV100: many queries per topic

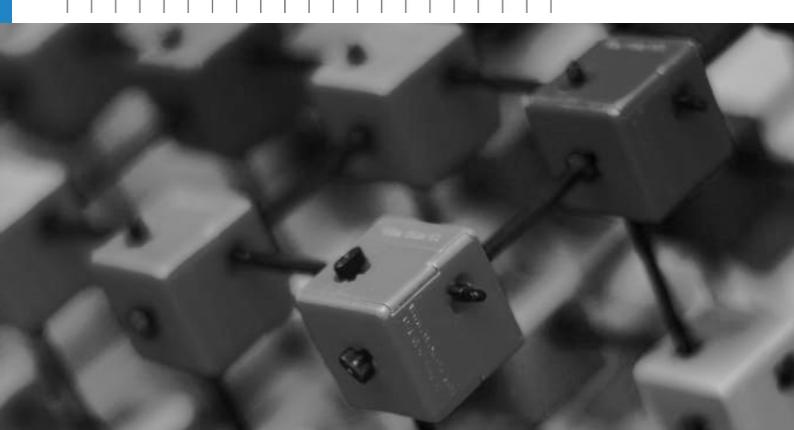
BM25 of URL

LETOR features

LEarning TO Rank for Information Retrieval

BM25 of title	BM25 of anchor	BM25 of body	DL of whole document	DL of URL	DL of title	DL of anchor	DL(Document length) of body	TF*IDF of whole document	TF*IDF of URL	TF*IDF of title	TF*IDF of anchor	TF*IDF of body	IDF of whole document	IDF of URL	IDF of title	IDF of anchor	IDF(Inverse document frequency) of body	TF of whole document	TF of URL	TF of title	TF of anchor	TF(Term frequency) of body	
---------------	----------------	--------------	----------------------	-----------	-------------	--------------	-----------------------------	--------------------------	---------------	-----------------	------------------	----------------	-----------------------	------------	--------------	---------------	---	----------------------	-----------	-------------	--------------	----------------------------	--

																body	body				
Number of child page	Length of URL	Number of slash in URL	Outlink number	Inlink number	PageRank	LMIR.JM of whole document	LMIR.JM of URL	LMIR.JM of title	LMIR.JM of anchor	LMIR.JM of body	LMIR.DIR of whole document	LMIR.DIR of URL	LMIR.DIR of title	LMIR.DIR of anchor	LMIR.DIR of body	LMIR.ABS of whole document	LMIR.ABS of URL	LMIR.ABS of title	LMIR.ABS of anchor	LMIR.ABS of body	BM25 of whole document



Approaches

Pointwise approach

Each document for itself.

<u>Input space</u>: feature vector of each doc.

Output space:

relevance degree of each document

Hypothesis space: functions that take a doc. feature vector as input and output a relevance degree

Regression or classification loss.

Pairwise approach

Each doc. pair for itself.

<u>Input space</u>: feature vectors of a pair of docs

Output space: pairwise preferences

Hypothesis space: functions that take a document pair as input and outputs their relative order

Loss function considers the relative order between the two docs.

Listwise approach

ground truth)

Hypothesis space

Output space (learning target)

Input space (feature vectors)

Loss function (prediction vs.

Designed for ranking

Input space:

$$\mathbf{x} = \{x_j\}_{j=1}^m$$

Output space: (1) relevance degrees of all documents, (2) ranked list of documents

Hypothesis space:

functions that take x as input and produce (1) or (2)

Loss function considers (1) or (2)

Approaches

Pointwise approach

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Output space:

relevance degree of each document

Hypothesis space:

functions the Different loss functions but doc. feature one and the same evaluation

relevance degree

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Loss function (prediction vs. ground truth)

Hypothesis space

Output space (learning target)

Input space (feature vectors)

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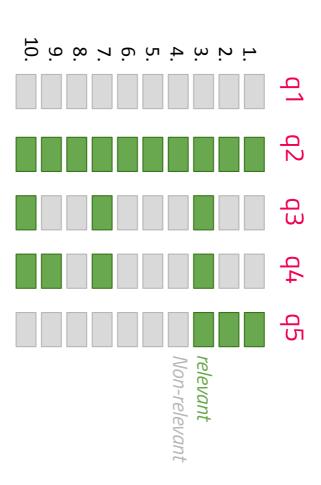
functions that take x as input and produce (1) or

Loss function considers (1) or (2)

Document ranking is easy.

How to rank a whole set of documents? Another step is needed.

Mean Average Precision



One system, five queries

Given a set of queries, the average effectiveness is the mean over AvP.

MAP remains one of the most commonly employed retrieval evaluation measure to this day.

$$MAP = \frac{1}{|Q|} \sum_{q \in Q}^{s} \frac{\sum_{k=1}^{s} P@k \times rel(k)}{R}$$

AvP

0.0 1.0 0.09 0.13 0.3

(assume R=10)

MAP = 0.364

Normalized Discounted Cumulative Gain (NDCG)

internet", "dinosaurs", "solar panels" Standard Web search queries are short (2-3 terms), e.g. "cheap

Graded relevance scales needed (e.g. 0-3); NDCG measures the "gain" of documents

Normalization so that a perfect ranking at k for query j is 1

assessors gave

Relevance score

D at query J

 $NDCG(Q,k) = \frac{1}{|Q|} \sum_{j=1}^{|Q|} Z_{kj} \sum_{m=1}^{k} \frac{2^{R(j,m)} - 1}{\log_2(1+m)}$

Assumptions:

- Highly relevant documents are more valuable than marginally relevant documents
- valuable it is for the user The greater the ranked position of a relevant document, the less
- Few users go further than the first 10 blue links
- Probability of reaching the document is lower
- Users have limited time
- aiready Users may have seen the information in the document

Key questions

- How do the proposed algorithms differ? What are their strengths and weaknesses?
- that we should focus on? What are the theoretical issues for ranking
- Which of the proposed learning to rank algorithms perform best empirically?

L2R categorization

	SVM	Boosting	Neural net	Others
Pointwise		McRank		PRank
Pairwise	RankSVM	RankBoost, LambdaMART, GBRank	RankNet, LambdaRank, FRank	
Listwise	SVM MAP	AdaRank	ListNet	SoftRank, SmoothRank

and LARF are Pareto optimal learning to rank methods" Tax et al. (2015): "ListNet, SmoothRank, FenchelRank, FSMRank, LRUF

Pointwise approach

Direct application of standard supervised ML.

Pointwise categories

Regression based algorithms

Real-valued relevance scores

Classification based algorithms

Non-ordered categories

Ordinal regression based algorithms

Variables with a natural categorical ordering





Polynomial regression function

quantitatively is encoded Qualitative judgment

Given q and associated $\mathbf{x} = \{x_j\}_{j=1}^m$,

let the ground truth label be: doc judged non-relevant binary: $\vec{y_j}=(0,1)$ or $\vec{y_j}=(1,0)$

ordered categories: $\vec{y_j} = (0, 0, ..., 1, ...0)$

doc judged belonging to a category (e.g. 'Fair' or 'Good')

Predictor of kth element in the ground truth vec.

Scoring function: $\vec{f} = (f_1, f_2, ..., f_k)$ with

Tth feature in feature vector j

$$f_k(x_j) = w_{k,0} + w_{k,1} \times x_{j,1} + \dots + w_{k,T} \times x_{j,T} + \dots + w_{k,T+1} \times x_{j,1}^2 + \dots + w_{k,T+1} \times x_{j,1}^2 + w_{k,T+2} \times x_{j,1} \times x_{j,2} + \dots$$

Combination coefficient

Loss function: $L(f; x_j, \vec{y_j}) = ||\vec{y_j} - f(x_j)||^2$

Pairwise approach

Pairwise

Many algorithms have been proposed, e.g.

- RankNet
- RankBoost
- Ranking SVM
- LambdaRank

:

Focus: relative ordering of pairs of documents

Ranking problem reduced to a classification problem (goal: minimize #misclassified pairs)

Training data:

$$\{(x_1, x_2, +1), (x_1, x_3, -1), ..., (x_i, x_j, +1), ...\}$$

RankNet

Log Loss when true label = 1

Given q and two documents x_u and x_v ,

modeled prob: $P_{u,v}(f) = \frac{1}{1 + \exp(f(x_u) - f(x_v))}$ $\exp(f(x_u) - f(x_v))$

the two documents' scores Based on the diff. between

Shallow neural network gradient descent as learns scoring function f;

optimization alg

 $L(f; x_u, x_v, y_{u,v}) = -P_{u,v} \log P_{u,v}(f)$

Cross-entropy loss

 $-(1-\bar{P}_{u,v})\log(1-P_{u,v}(f))$

Target probability:

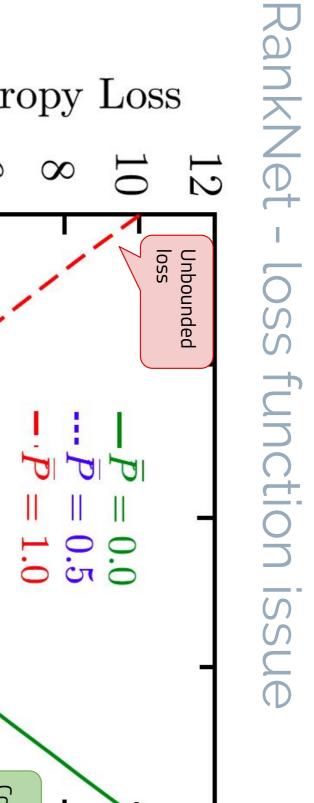
$$P_{u,v} = 1, if y_{u,v} = 1;$$

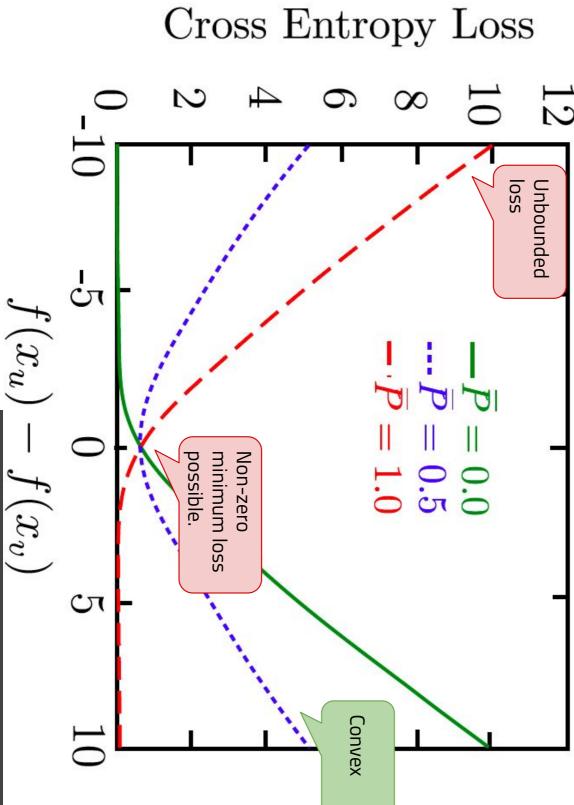
 $P_{u,v}=0$ otherwise

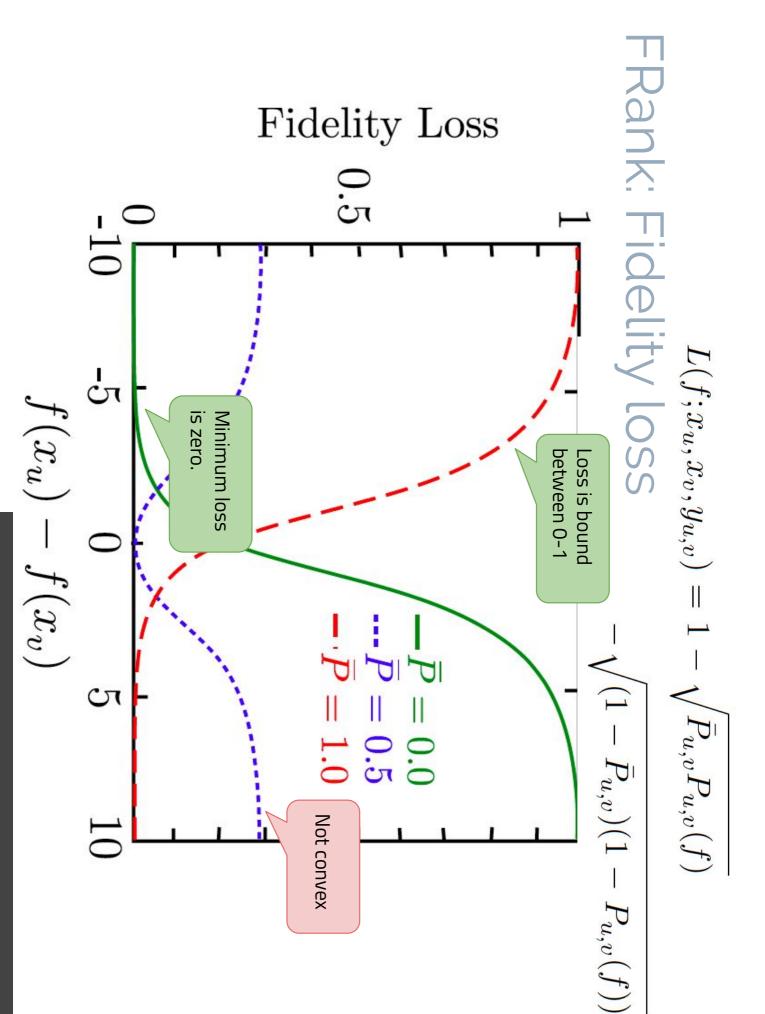
2 Why is

convexity

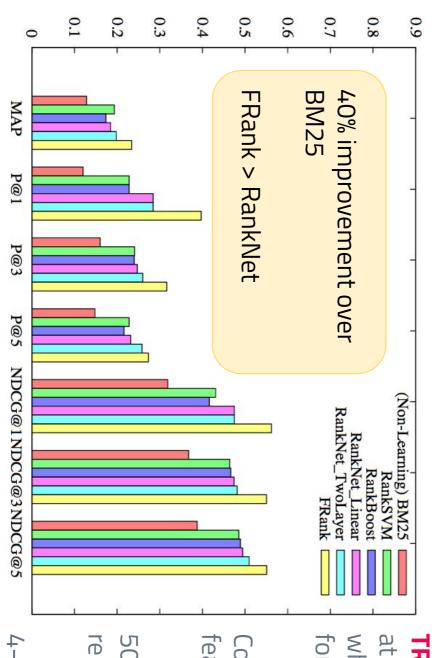
important?







Experimentally: RankNet vs. FRank



TREC topic distillation aims

at finding key resources which are high-quality pages for certain topics.

Corpus: 1M . gov pages, 14 features per document

50 topics (between 1 and 86 relevant docs per topic)

4-fold cross validation



) Is training of the pairwise approach slower/faster than the pointwise one?

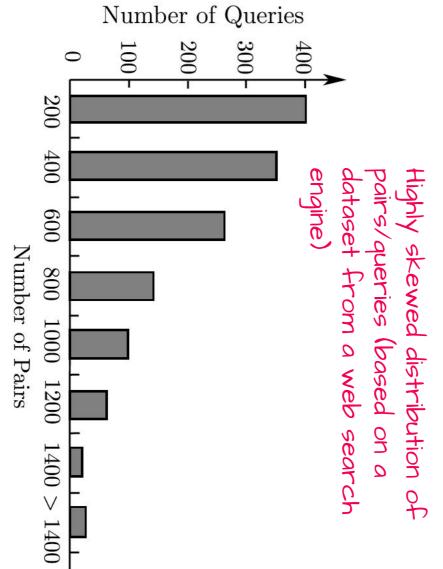
Document pair issue

Document pairs only make it into the training set if their relevance degrees differ

Worst case: number of pairs quadratic in the document number

Queries differ widely in the number of pairs they generate

Loss will be dominated by queries with many pairs (requires query-level normalization)



Beyond RankNet ...

>> LambdaRank

- Insight: neural net training of the cost function requires only the gradients
- Heuristic rules on how the rankings are swapped cost changes if document

>> LambdaMART

Gradient boosted decision trees



Listwise approach

- Optimize a continuous & differentiable approximation of an IR metric
- 2) Optimize a continuous & differentiable bound of an IR metric
- W Choose optimization approach that can handle complex objectives.

Direct optimization



degrees of all docs associated with q. Output space contains relevance Loss function optimizes an IR metric.

non-continuous & non-differentiable Not easy as MAP, NDCG, ... are

Most optimization techniques are differentiable functions designed for continuous and

Examples: SoftRank, AdaRank

Permutation-based

associated with q. permutation of the documents The output space contains the

given by the hypothesis and the ground truth permutation. difference between the permutation The loss function measures the

Examples: <u>ListNet</u>, ListMLE

ListNet

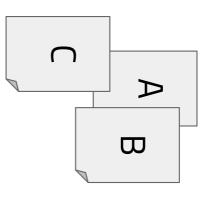
Required: a loss function that considers the document list

function hypothesized and one on the reference ranking. Use a metric that compares the two probability distributions as loss Idea: define two probability distributions, one on the

define a prob. for each possible permutation π of the documents: and document relevance scores $\mathbf{s} = \{s_j\}_{j=1}^m$, where $s_j = f(x_j)$, Given scoring function f

permutation $P(\pi|\mathbf{s}) = \prod_{j=1}^{\infty} \frac{\varphi(s_{\pi^{-1}(j)})}{\sum_{u=j}^{m} \varphi(s_{\pi^{-1}(u)})}$ doc. ranked at jth position in the permutation station j=1conditional probability

ListNet permutation example



A-B-C? Given 3 documents for query q, what is the probability of the ranking permutation

$$P_{\pi} = P_1 \times P_2 \times P_3$$

$$P_1 = \frac{\varphi(s_A)}{\varphi(s_A) + \varphi(s_B) + \varphi(s_C)}$$

A's score to B's and C's scores. Determined by comparing ranked at the top. Probability of doc A being

$$P_2 = \frac{\varphi(s_B)}{\varphi(s_B) + \varphi(s_B)}$$

 $\varphi(s_B) + \varphi(s_C)$ been ranked already. at position 2, given that A has Probability of B being ranked

$$P_3=1\,\,$$
 Only C is left.

ListNet

on the scores given by the scoring function ListNet defines the permutation probability distribution based

on the ground truth labels The reference permutation probability distribution is based

define the listwise ranking loss: KL divergence between both distributions to

$$L(f; \mathbf{x}, \pi_y) = D(P(\pi | \varphi(f(w, \mathbf{x}))) || P_y(\pi))$$
Shallow neural network

Practical issue:

learns scoring function f; gradient descent as optimization alg

Practical issue: training over all possible permutations of a list is impractical (*m!* permutations of size *m*)

Benchmarks & practice

Microsoft	Yahoo!	Yandex	LETOR 4.0	LETOR 3.0 – Ohsumed	LETOR 3.0 - Gov	
31,531 3,771	36,251	20,267	2,476	106	575	Queries
3,771 k	883 k	$213 \mathrm{k}$	85 k	16 k	$568\mathrm{k}$	Doc.
O T	೮	೮	သ	3	2	Rel.
136	700	245	46	45	64	Feat.
2010	2010	2009	2009	2008	2008	Year

measure, and four (and the other net) were trained using NDCG. Extended training sets tree style MART algorithm, which itself may be viewed as a gradient descent algorithm. instantiated using neural nets, LambdaMART implements the same ideas using the boostednets, and 2 of which were logistic regression models. While LambdaRank was originally LambdaMART (Burges, 2010) boosted tree models, 2 of which were LambdaRank neural were also generated by randomly deleting feature vectors for each query. Four of the LambdaMART rankers (and one of the nets) were trained using the ERR Burges et al. (2011) used a linear combination of 12 ranking models, 8 of which were

Implicit feedback

behaviour information Incorporating user



Evaluating the accuracy of implicit feedback (clicks)



Implicit feedback

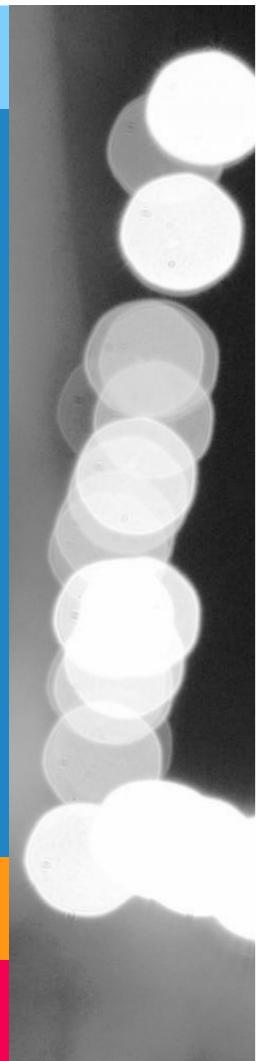
Incorporating user behaviour information

Explicit vs. implicit

Learning to rank, BM25, LM ...

- Need training data to effectively learn the models' (hyper)parameters
- Often explicit relevance judgments are used

(can become outdated quickly for dynamic collections) Explicit grels are extremely expensive to accumulate





Topics (ad hoc task)



Pooled documents (k=100)



Systems



Assessor hours

experiments!

TREC-8 numbers (ran in 1999)

At \$20 an hour, that amounts to \$14,460.

And thus, We are still using the TREC-8 corpus to this day for

Potential source: clickthrough data

RQ: How effective is **implicit feedback** in practice (i.e. in a large-scale operational environment)?

- Web search engines use thousands of features and are heavily tuned
- Tuning is a continuous process

ranking produced by the search system? RQ: How can implicit feedback be combined with the existing

traces aggregate information from multiple, unreliable search session Insight: Instead of treating a user as a reliable "expert",

evidence Clickthrough data as independent

- Retrieve an initial ranking (low cost)
- Assign an expected relevance/user satisfaction score
- based on previous interactions

Merge the **rank orders** of the original and implicit

Order results by the merge score

feedback (IF) based ranking

original rank of doc d

Empirically found to work well

$$S_M(d,I_d,O_d,w_I) = \left\{ egin{array}{l} rac{\overline{O_d+1}}{\overline{O_d+1}}, & if \ no \ IF \ exists \ w_Irac{1}{I_d+1} + rac{1}{\overline{O_d+1}}, & otherwise \ \end{array}
ight.$$

implicit rank of doc d

influence of implicit feedback

extremely high, clicked If the influence of IF is above unclicked results results are simply ranked

Clickthrough data in L2R

- Derive a set of features from implicit feedback
- At runtime, the search engine needs to fetch the implicit feedback features associated with each (query, URL) pair

L2R needs to be robust to missing values: long tail issue

Here: RankNet

- Neural net based tuning algorithm that optimizes feature weights to best match explicitly provided **pairwise** user preterences
- Has both train- and run-time efficiency
- Aggregate (query, URL) pair features across all instances in the session logs



How does a search engine get this

Features

Different types of user action features

Directly observed vs. derived features (derivations)

Browsing behaviour after the result has been clicked

Snippet based features are included as users often determine relevance based on snippet information

https://dl.acm.org/citation.cfm?id=1148177

Clickthrough features	
Position	Position of the URL in Current ranking
ClickFrequency	Number of clicks for this query, URL pair
ClickProbability	Probability of a click for this query and URL
ClickDeviation	Deviation from expected click probability
IsNextClicked	1 if clicked on next position, 0 otherwise
IsPreviousClicked	1 if clicked on previous position, 0 otherwise
IsClickAbove	1 if there is a click above, 0 otherwise
IsClickBelow	1 if there is click below, 0 otherwise
Browsing features	
TimeOnPage	Page dwell time
CumulativeTimeOnPage	Cumulative time for all subsequent pages after search
TimeOnDomain	Cumulative dwell time for this domain
TimeOnShortUrl	Cumulative time on URL prefix, no parameters
IsFollowedLink	1 if followed link to result, 0 otherwise
IsExactUrlMatch	0 if aggressive normalization used, 1 otherwise
IsRedirected	1 if initial URL same as final URL, 0 otherwise
IsPathFromSearch	1 if only followed links after query, 0 otherwise
ClicksFromSearch	Number of hops to reach page from query
AverageDwellTime	Average time on page for this query
DwellTimeDeviation	Deviation from average dwell time on page
CumulativeDeviation	Deviation from average cumulative dwell time
DomainDeviation	Deviation from average dwell time on domain
Query-text features	
TitleOverlap	Words shared between query and title
SummaryOverlap	Words shared between query and snippet
QueryURLOverlap	Words shared between query and URL
QueryDomainOverlap	Words shared between query and URL domain
QueryLength	Number of tokens in query
QueryNextOverlap	

Evaluation

Random sample of queries from a Microsoft query log with associated results and traces of user actions

8 weeks of user interactions with 1.2M unique queries (sufficient interactions for 50% of queries) and 12M interactions

On average, 30 results judged per query by human assessors on a **six point scale** (83K results judged)



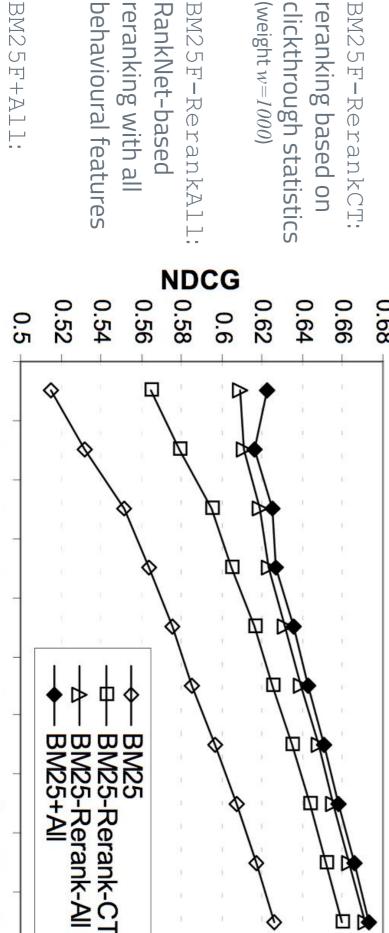
	MAP
BM25F (content + link-based info)	0.184
RankNet	0.215
ReRanking	
BM25F + Click-through statistics only	0.215
BM25F + Implicit feedback	0.222
Integrated as features	
RankNet + Implicit feedback	0.248

Results

BM25F: content-based (fields) and query-independent

BM25F-RerankCT link-based information (PageRank, URL depth, etc.); does not reranking based on make use of implicit/explicit feedback 0.68 0.66

reranking with all RankNet-based BM25F-RerankAll: clickthrough statistics (weight w=1000)



BM25F+All:

on BM25F features+IF RankNet-based ranking

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Results ctd.

on explicit judgments RankNet (RN): hundreds of features of a Web search engine; based

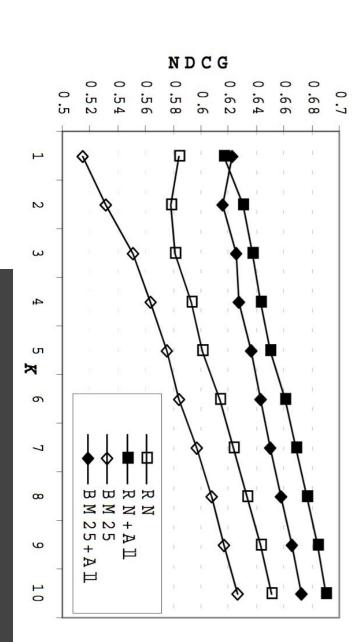
RankNet+All: including IF features

BM25F: content-based (fields) and query-independent link-based information (PageRank, URL depth, etc.)

 ${ t BM25F+All:}$ train RankNet over the feature set of BM25F and IF

BM25F 0.1	MAP
	0.184
BM25F-Rerank-CT 0.2	0.215
BM25F-RerankImplicit 0.2	0.218
BM25F+Implicit 0.2	0.222
RN 0.2	0.215
RN+All 0.2	0.248

IF can replace hundreds of features



Implicit feedback

Evaluating the accuracy of implicit feedback (clicks)



Generating training data from clicks

automatically from clickthrough data? RQ: can training examples (qrels) be generated

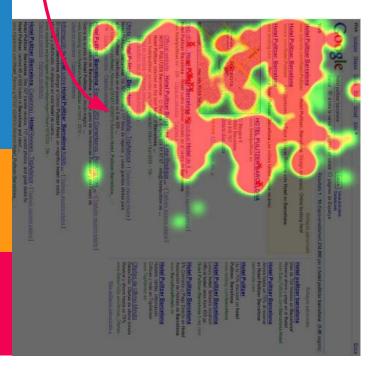
up-to-date burdening the user (no relevance feedback), Advantages: cost effective, large quantities, without

Disadvantages: more difficult to interpret & noisy

Controlled study!

SERP **User study** investigating users' interaction with the

- feedback) and explicit relevance judgments Relationship between click behaviour (=implicit
- Eye-tracking experiment provides insights into users' subconscious behaviour



Generating training data from clicks

Important to know what results a user actually views

Implicit relevance judgments need to be considered in this context (a result not viewed cannot be considered non-relevant)

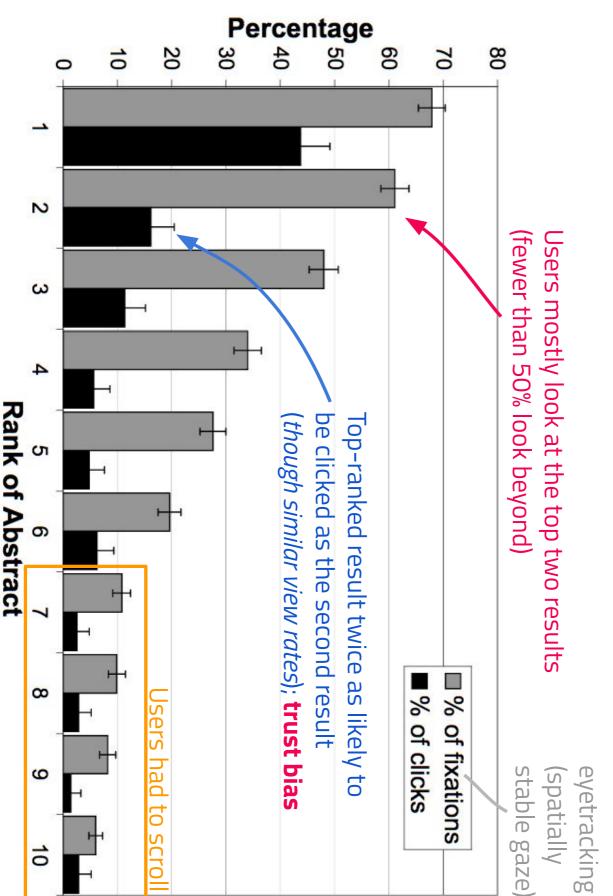
result (i.e. a click = a positive relevance judgment) Early work assumed that each click represents an endorsement of the

User study with 3 experimental conditions (10 topics)

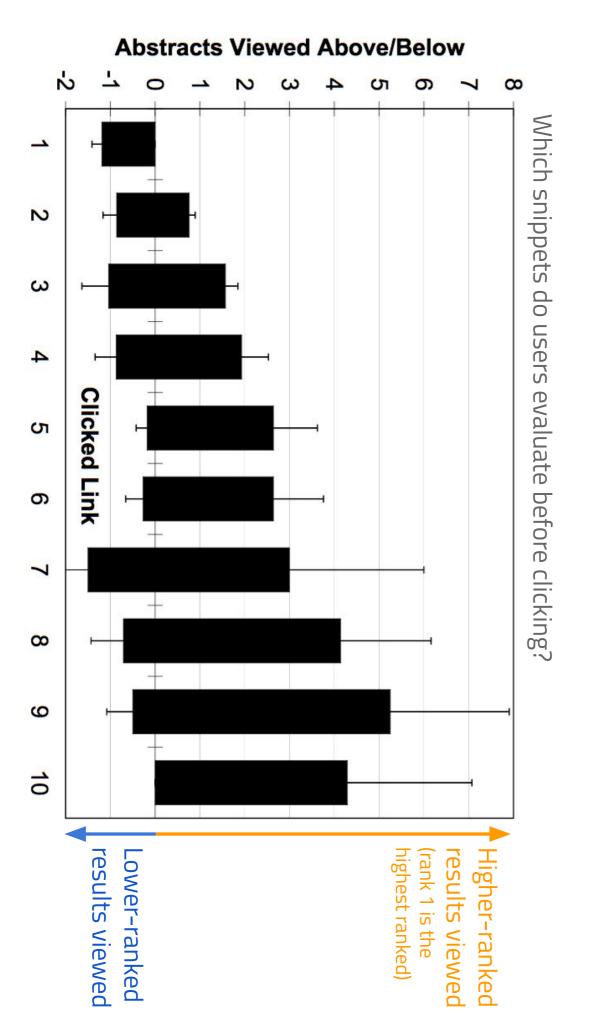
- Normal (original SERP)
- **Swapped** (top two results swapped on the SERP)
- **Reversed** (top-10 results on the SERP in reverse order)

Explicit relevance judgments collected as control

Result ranks vs. clicks & views



Scanning the SERF

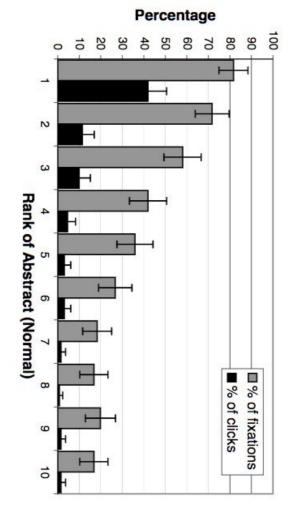


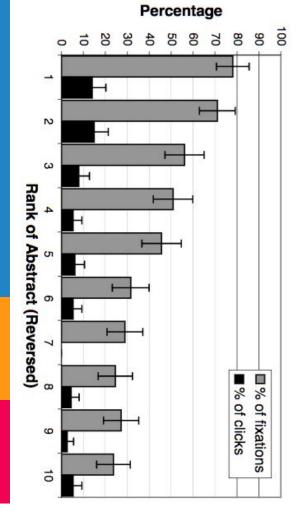
Relevance vs. user decisions

So far: clicks considered independent of relevance

Reverse condition (degraded ranking)

- Users view lower ranks more frequently
- Users are less likely to click on result 1 (av. click rank 4 vs. 2.7 in normal)
- Quality-of-context bias: clicks are less relevant on average compared to the normal condition (clicks dependent on overall quality of the system)

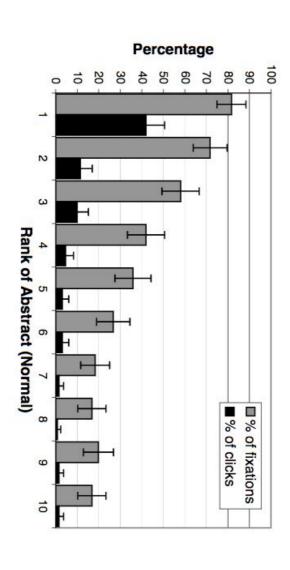


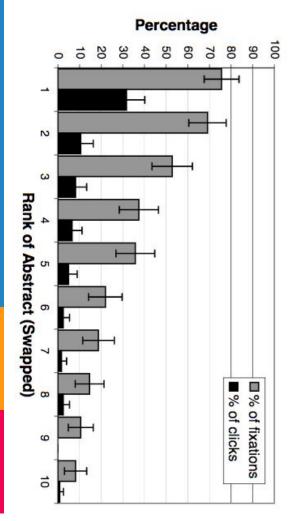


Relevance vs. user decisions

Swapped condition

- Trust bias (Google must be right)
- Users are influenced by result order
- Decision to click influenced by result position





Inus ...

Interpreting clicks as <u>absolute</u> relevance judgments is likely to fail.

the system quality into account Accurate interpretations need to take a user's trust and

We exploit the fact that some results were not clicked. Clicks can be seen as preference statements.

$$l_1^* \ l_2 \ l_3^* \ l_4 \ l_5^* \ l_6 \ l_7; \ ^*=click$$

$$rel(l3)>rel(l2) \ rel(l5)>rel(l4), rel(l5)>rel(l2)$$

Extracting preference feedback

$$l_1^* l_2 l_3^* l_4 l_5^* l_6 l_7; *=click$$
 $rel(l3)>rel(l2) rel(l5)>rel(l4), rel(l5)>rel(l2)$

ahead of l2 and l5 ahead of l2 and l4**Partial rankings**: a relevance based ranking should return *13*

Strategy: Click > Skip-Above

 $rel(l_7) > rel(l_4)$

 $rel(l_7) > rel(l_3)$

 $rel(l_{7}) > rel(l_{1})$

 $rel(l_7) > rel(l_6)$

 $rel(l_5) > rel(l_3)$

 $rel(l_5) > rel(l_4)$

 $rel(l_5) > rel(l_1)$

 $rel(l_2) > rel(l_1)$

 $C = \{2,5,7\}$

Takes trust bias and quality-of-context into account

 $rel(l_i) > rel(l_j)$ for all pairs $1 \le j < i$, with $i \in C$ and $j \notin C$ of the clicked results, extract a preference example For a ranking $(l_1, l_2, ...)$ and a set C containing the ranks

Extracting preference feedback

$$l_1^* l_2 l_3^* l_4 l_5^* l_6 l_7; *=click$$
 $rel(l3)>rel(l2)$ $rel(l5)>rel(l4), rel(l5)>rel(l2)$

Partial rankings: a relevance based ranking should return *l3*

Strategy: Last Click > Skip-Above

Intuition: later clicks are more informative than earlier ones

clicked results, let $i \in C$ be the rank of the last click. Extract a For a ranking $(l_1, l_2,...)$ and a set C containing the ranks of the

preference example $rel(l_i) > rel(l_j)$ for all pairs $1 \le j < i$, and $j \notin C$.

Accuracy of extracted feedback



Click > Skip Above yields 81% correct preferences

Last Click > Skip Above yields 83% correct preferences

Random baseline: 50% accuracy

(upper bound) Inter-annotator agreement (human assessors): 90% accuracy

Query chains

reformulation after zero-click SERP $\sim \operatorname{oed} \implies l_1 \ l_2 \ l_3 \ l_4 \ l_5 \ l_6 \ l_7$

 \rightarrow oxford english dictionary $\Rightarrow l_{1} l_{2} l_{3} l_{3} l_{4} l_{5} l_{6} l_{7}$

May be relevant to "oed"

same query (within-query preferences) Generated preferences: comparison between the results from the

Too restrictive:

- Strategies only produce preferences between the top few results shown to the use
- Typically users run query chains (reformulations)

results from **different queries** within a chain of query reformulations (same information need) Goal: generate accurate relative preference judgments between

Query chains

Strategy: Click > Skip Earlier QC

for all pairs $i \in C$ and $j < \max(C)$, with $j \notin C$. on results, extract a preference example $rel(l_i) > rel(l_i)$ chain and sets C and C containing the ranks of the clicked (not necessarily immediately) within the same query For a ranking $(l_1, l_2,....)$ followed by ranking $(l_1, l_2,....)$

Accuracy depends on the presentation order: 85% (normal) vs. 55% (reversed)

$$q_1 : l_{11} \ l_{12} \ l_{13} \ l_{14} \ l_{15} \ l_{16} \ l_{17}$$

$$q_2 : l_{21}^* \ l_{22} \ l_{23}^* \ l_{24} \ l_{25}^* \ l_{26} \ l_{27}$$

$$q_3 : l_{31} \ l_{32}^* \ l_{33} \ l_{34} \ l_{35} \ l_{36} \ l_{37}$$

$$q_4 : l_{41}^* \ l_{42} \ l_{43} \ l_{44} \ l_{45} \ l_{46} \ l_{47}$$

$$rel(l_{32}) > rel(_{22})$$

 $rel(l_{32}) > rel(l_{24})$
 $rel(l_{41}) > rel(l_{22})$
 $rel(l_{41}) > rel(l_{24})$
 $rel(l_{41}) > rel(l_{24})$
 $rel(l_{41}) > rel(l_{31})$

Summary L2R

With sufficiently many features, L2R outperforms BM25 and similar non-ML baselines

It is not sufficient to deploy standard classifiers; need to be adapted towards ranking (pairwise, listwise)

Listwise vs. pairwise: the former makes most theoretical sense, the latter is empirically more robust and efficient

L2R is often neural-network based (shallow, not deep)

Best results are achieved in ensembles

