

# Estimate Power generation of invisible solar site using State estimation

1<sup>st</sup> Pornchai Chaweewat

EECC

AIT)

Pathumthani, Thailand

chaweewat.p@gmail.com

2<sup>nd</sup> Weerakorn Ongsakul

EECC

AIT)

Pathumthani, Thailand

email address

3<sup>rd</sup> Jai Govind Singh

EECC

AIT)

Pathumthani, Thailand

email address

4<sup>th</sup> Ali abur

EEC

NEU

Boston, MA, USA

email address

**Abstract**—The number of large scale and rooftop scale solar photovoltaic (PV) systems in electricity grid is growing at exponential rate. Invisible solar PV refers to small-scale and rooftop solar sites in distribution system that are not monitored by utilities. These invisible solar PV sites cause challenging to utilities and system operators. In this paper, a methodology is proposed to identify location and estimate installation capacity of solar PV sites. With measurement voltage at any buses and power flow in any lines, state estimation (SE) algorithm could find power consumption in any buses. The consumption are fed to find correlation with solar irradiation data. Thus, the correlation between these data could locate the site of invisible solar PV sites. Furthermore, the change point method and proposed algorithm could estimate installation capacity of invisible solar PV sites. The proposed methodology is test in distribution system i.e, four bus system and CIGRE Medium voltage distribution network with PV and Wind DER with randomly invisible solar PV sites location. The overall results of the study shows that the correlation between consumption and solar irradiation can perfectly identify invisible solar PV sites with  $F_1$  score above 0.96 and Matthews correlation coefficient (MCC) score above 0.90. The installation capacity estimation performs good with mean absolute error (MAPE) below 17%.

**Index Terms**—Solar photovoltaic, invisible solar PV site, Gaussian noise, state estimation, correlation, change point detection, Matthews correlation coefficient

## I. INTRODUCTION

Sixty years ago, the price of solar panels was astronomical. The price was over 1,000 US dollars per watt in today's money with 1 percent efficiency [1]. As the cost continues to drop, solar panel systems are becoming much more viable for the average household. Today's price is less than 2.8 US dollars per watt for solar panel system including solar module, inverter, wiring hardware, labor cost, and maintenance cost [2]. As result of exponentially accelerate increasing in number of globally solar PV integration, especially in residential sector.

Recently, the highest penetration of solar PV, recognized a large number of unauthorized solar PV installation [3]. Unauthorized solar PV installation creates safety risks and lack of visibility may result in incorrect planning, and operation, including over-voltage, back-feeding. Furthermore, in worst case scenario, it may damage system equipment such as transformers, voltage regulators, as well as customer applicants

[4], [5]. In previous studies, there are various reasons for unauthorized or incorrectly registered PV system. For example, owner decided not to apply for a permit to avoid fees [6]. The difference rules depending on size and type of PV installation can make the owners believe they do not need a permit [7].

Furthermore, many researchers have studied the impacts and risks of PV on distribution systems [8]- [11]. These impacts can cause physical and financial damage to utility and solar PV owners, especially invisible solar PV which utility could not monitor real-time. However, the detection and estimation of residential PV systems has not been the focus of the studies and related research. This issue is key motivation to this study.

The rest of the paper is structured as follows: Section II reviews related research on state estimation application for power system and previous detection and estimation techniques on invisible solar PV site. Section III formulates the mathematic model of measurement data as well as the structure of proposed methods as well as evaluation processes. Section IV shows the results of proposed method on test cases. Section V concludes the paper and discusses future research opportunities on invisible PV system detection and estimation.

## II. LITERATURE REVIEWS

### A. Applications of State estimation in power system

State estimation on distribution power system is reviewed in [12].

State estimation provides the optimum estimate of power system state based on received measurement units and the knowledge of network modeling. The measurement units may include as follows:

- power injection (real/reactive),
- power flow (real/reactive),
- bus voltage magnitude,
- phase angle,
- line current magnitude,
- current injection magnitude.

State Estimation provides various benefits for power system analysis as follows:

1) *Real time monitoring*: For power system in transmission and distribution levels [13]. The Advance Meter infrastructure (AMI) data are fed into SE to real-time monitor

distribution power system in [14]. It improved the accuracy comparing to pseudo measurement based on historical load.

2) *Load allocation*: In distribution power system, SE assigns active and reactive power values to bus downstream [15]. Class curves and individual average demand of clients improved accuracy of load allocation [16]. The data from AMR system, which are used as the pseudo-measurements, was used to estimate load on the distribution transformers. [13].

3) *Bad data analysis*: In several real application, it happens that some flow measurement has no sign or the sign is wrong. A re-weighting technique was used to reduced the weights association to these measurements [15]. It also could helps to treat of power flow with erroneous sign. Futhurmore, SE was implemented in cyber attack events [17] on power system states. A detection false data injection method is proposed in [18].

4) *Topology indentification*: the status of branches and switches are indentified in [15].

#### B. previous solar PV detection techniques

The previous studies has been done on detection of location and estimation of power generation of invisible solar PV sites. Reference [19] proposed a change-point detection algorithm for a time series for residential solar PV detection. These method required smart meter data and historical load profile. The uncertainty of solar PV site and the data generated by a small set of selected representative sites were taken into account to estimates the power gngeneration of known solar PV site in [20]. The new hybrid k-means and PCA techniques provided good accuracy of estimating invisible solar PV sites. The big data characterization of smart grids and two-layer dynamuc optimal synchrophasor measurement devices selection algorithm for fault detection, identification, and causal impact analysis was proposed in [21]. The utility data based on random matrix theroy (RMT) are used in detection and estimation of invisible solar PV in real case in China in [22].

#### C. Contributions

Many researchers have studied the detection and estimation location of invisible solar PV installation [19]- [22]. These study depended on smart meter data, data set of solar PV generation, as well as historical demand of customer in each load. This paper proposed method which identify location using state estimation, correlation measured and estimating the installation capacity using change point method of invisible solar PV site. All solar PV's site is assumed to operate at unity power factor. The solar PV is located randomly at any bus excepted slack bus. The measurement units are located at optimum locations. The measured data such as solar irradiation, power flow measurements in lines and voltage measurements at busses are generated with gaussian noise. The proposed method consists of four steps:

- collect solar irradiation, measurement data
- allocate power demand in each buses, nodes.
- indentify invisible solar PV site
- estimate solar PV site's installation capacity

### III. PROBLEM FORMULATION

This section will presents the overall methodology of the study which will be devided into four parts. The conceptual of methodology is illustrated in Fig. 1.

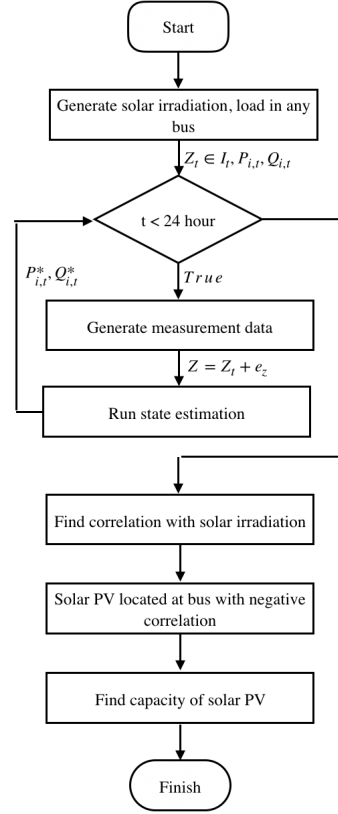


Fig. 1. conceptual methodology

#### A. Measurement devices, measured data and accuracy

In this study, there are three type of measurements; bus, line, and transformers measurement. Voltage magnitude in per unit is measurement at bus. Active and reactive power flow, and magnitude curreng are measured at line and trasformers. Bus measurement has 1% error and line measurement has 3% error.

To generate measurement data for testing prupposes, measurement error was added to tha actual measurements as shown in Equation (1).

$$Z = Z_a \pm e_z \quad (1)$$

where  $Z_a$  is actual data and  $e_z$  is error added base on accuracy of the measurement.

These error are assumed to be modeled independent Gaussian random variable [23], where where the error value is expected value from gaussian distribution. noise is gaussian distribution,as shown in Equation (2).

$$g(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}((x-\mu)/\sigma)^2} \quad (2)$$

### B. Load allocation based state estimation

SE is based on the weighted least square (WLS) approach [24]. The method solves the following WLS problem to obtain an estimate of the system operating point defined by the system state  $x$ :

$$\min_x J(x) = \sum_{i=1}^m w_i (z_i - h_i(x))^2 = [z - h(x)]^T W [z - h(x)] \quad (3)$$

where  $w_i$  and  $h_i(x)$  represent the weight and the measurements function associated with measurement  $z_i$ , respectively. For the solution of this problem the conventional iterative method is adapted by solving following normal equations at each iteration, to compute the update  $x^{k+1} = x^k + \Delta x^k$ .

$$[G(x^k)] \Delta x^k = H^T(x^k) W [z - h(x^k)] \quad (4)$$

Where

$$G(x) = H^T(x) W H(x) \quad (5)$$

is the gain matrix and  $H$  is the jacobian of the measurement function  $h(x)$ .

### C. Solar PV site's location identification

This part will describe location identification of invisible solar PV's site. The correlation-based feature selection (CFS) is key tool here. The basis of the CFS that was introduced in [25]. The CFS will be performed as a statistical measure of relationship between solar irradiation and load allocation from previous part. The measure is best used in these two variables that demonstrate a linear relationship between each other. The correlation coefficient that indicates the strength of the relationship between these two variables can be found using following formula:

$$r_{IP} = \frac{\sum (I_i - \bar{I})(P_i - \bar{P})}{\sqrt{\sum (I_i - \bar{I})^2 \sum (P_i - \bar{P})^2}} \quad (6)$$

where  $r_{IP}$  is the correlation coefficient of the linear relationship between the solar irradiation ( $I$ ) and load consumption ( $P$ ),  $I_i$  is the values of the solar irradiation variable in a sample,  $\bar{I}$  is the mean of  $I$ ,  $P_i$  is the values of the load consumption variable in a sample,  $\bar{P}$  is the mean of  $P$ .

The negative correlation shows that the variables tend to move in opposite directions (i.e., when one variable increases, the other variable decreases). The probability of solar PV site located at bus  $i$  is expressed in Equation (7)

$$\text{prob}_i = \begin{cases} 0 & \text{if } r_i \geq 0 \\ 1 & \text{if } r_i < 0 \end{cases} \quad (7)$$

### D. Estimate solar PV site's installation capacity

Once, we can identify location of invisible solar PV located. Then, we try to estimate size of invisible solar PV units. We deploy change-point detection of change-point analysis. The change-point detection algorithm is a powerful tool used

to detect abrupt changes in time series data. We add solar irradiation and load allocation where invisible solar PV located. Then, we can find changing point of the dataset.

$$\Delta D_{i,t} = p_e \Delta I_{i,t} \quad (8)$$

where  $p_e$  is the size of the unauthorized PV system at bus  $i$ , and time  $t$ .

Then, we remove noise and find mean, range or other to estimate solar capacity.

### E. Evaluation

This section will describe evaluation methods will be used in this paper. There are two parts to evaluate the proposed invisible solar PV size. First, the identification of the invisible solar PV location is evaluated by confusion matrix,  $\text{text}F_1$  score, and Matthews correlation coefficient (MCC). Second, the estimation of installation of invisible solar PV size is evaluated by mean absolute error (MAE), and mean absolute percentage error (MAPE).

The results of location of invisible solar PV detection will be represented in confusion matrix as exemplified in Table I

TABLE I  
CONFUSION MATRIX

		True condition	
		Condition positive	Condition negative
Prediction condition	Prediction condition positive	True positive (TP)	False positive (FP)
	Prediction condition negative	False negative (FN)	True negative (TN)

where TP, TN, FP, and FN are defined as number of hit, correct rejection, false alarm and miss, respectively.

1)  $F_1$  score: The  $F_1$  score is a measure of a test's accuracy. The  $F_1$  score is the harmonic average of the precision and recall, where an  $F_1$  score reaches its best value at 1 (perfect precision) and worst at 0. The  $F_1$  is formulated in Equation (9).

$$F_1 = \frac{2 \times \text{TP}}{2 \times \text{TP} + \text{FP} + \text{FN}} \quad (9)$$

2) *Matthews correlation coefficient*: The Matthews correlation coefficient (MCC) is first introduced by biochemist Brian W. Matthews in 1975 [26]. The MCC is essence an correlation coefficient between the observed and predicted binary classification; it returns a value between -1 and +1. A coefficient of +1 represents a perfect prediction, 0 no better than random prediction and -1 indicates total disagreement between prediction and observation. An Equation (10) shows the formula of MCC for 2 classes. The derivations are expressed in [27].

$$\text{MCC} = \frac{\text{TP} \times \text{TN} - \text{FP} \times \text{FN}}{\sqrt{(\text{TP} + \text{FP})(\text{TP} + \text{FN})(\text{TN} + \text{FP})(\text{TN} + \text{FN})}} \quad (10)$$

3) *Mean absolute error and Mean absolute percentage error*: The MAE defines as the difference between the actual and estimated invisible solar PV capacity which is computed by Equation (11). The MAPE expresses the scaled difference between the actual and estimated invisible solar PV capacity as a percentage of the actual invisible solar PV capacity. MAPE is scale independent and it can be used to compare estimation performance across different data sets. MAPE can be calculated by Equation (12).

$$MAE = \frac{1}{N} \sum_{i=1}^N |p_a - p_e| \quad (11)$$

$$MAPE = \frac{100}{N} \sum_{i=1}^N \left| \frac{p_a - p_e}{p_a} \right| \quad (12)$$

where  $p_a$  and  $p_e$  are the actual and estimated solar PV installation capacity.  $N$  is the number of sample.

#### IV. TEST CASES AND RESULTS

Two power system are tested. There two test cases are based on four bus system and CIGRE Task Force C6.04.02 paper [28].

##### A. four bus system

The one line diagram of the four bus system is shown in Fig. 2.

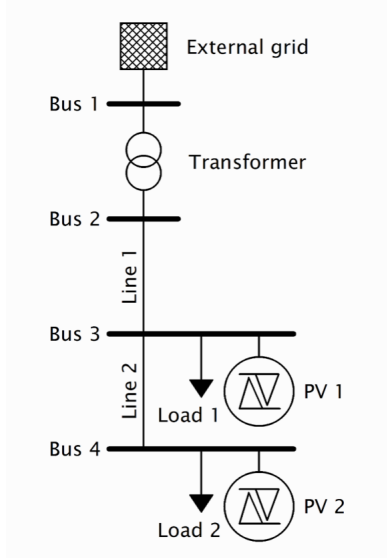


Fig. 2. four bus system

Table II shows the results. From the table, II it can be seen that the proposed method can predict perfectly location of invisible solar PV.

TABLE II  
RESULTS OF INVISIBLE SOLAR PV IDENTIFICATION ON 4 BUS SYSTEM

		Actual PV located	
		Yes	No
Prediction	Yes	126	0
PV located	No	9	60

The results is tested by  $F_1$  score and MCC using Equation 9, 10. The  $F_1$  score is 0.965. The MCC is 0.901 The false negative (FN) occurs when invisible solar PV's capacity is 1-2 kW where maximum demand is around 30 kW.

TABLE III  
RESULTS OF INVISIBLE SOLAR PV ESTIMATION ON 4 BUS SYSTEM

Size of invisible solar PV (kW)	MAE(kW)	MAPE (%)
1-10	0.77	13.9
11-20	2.4	16.9
21-30	3.75	14.2
31-40	4.42	12
41-50	3.85	8.4

The overall MAPE is 13.587 % and MAE is 2.919 kW.

##### B. CIGRE system

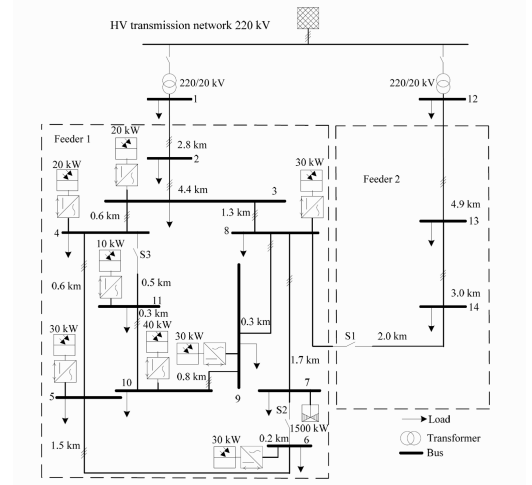


Fig. 3. CIGRE network

Table IV shows the results. From the table, II it can be seen that the proposed method can predict perfectly location of invisible solar PV.

TABLE IV  
RESULTS OF INVISIBLE SOLAR PV IDENTIFICATION ON CIGRE SYSTEM

		Actual PV located	
		Yes	No
Prediction	Yes	154	8
PV located	No	3	159

The results is tested by  $F_1$  score and MCC using Equation 9, 10. The  $F_1$  score is 0.965. The MCC is 0.9325. The false negative (FN) occurs when invisible solar PV's capacity is 10-20 kW.

TABLE V  
RESULTS OF INVISIBLE SOLAR PV ESTIMATION ON CIGRE SYSTEM

Size of invisible solar PV (kW)	MAE (kW)	MAPE (%)
1-100	9.01	17.60
101-200	24.3	15.97
201-300	50.00	19.85
301-400	52.55	13.98
401-500	54.92	12.28

The overall MAPE is 16.27 % and MAE is 37.58 kW.

## V. CONCLUSION

Here is Conclusion.

## ACKNOWLEDGMENT

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