

A novel probabilistical electricity price forecasting using deep residual neural networks (Deep ResNet)

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Abstract

What we do? - This paper proposes a novel electricity price forecasting method based on a novel Deep Residual Neural Network (Deep ResNet) for probabilistic electricity price forecasting under price spike environment for GEFCom2014.

Why I do this? - The electricity price, in deregulation electricity market, has become more fluctuated and generally unanticipated price spike. The use of prediction interval or probabilistic forecasting has become much more common due to it help market participants to submit effective bid with low risks.

How I do this? - Both multilayer perceptrons neural network (MLP) and a new model is developed from novel Deep ResNet approach. MLP represents forecasting model without spike price prediction. On the other hand, Deep ResNet represents forecasting model with spike price prediction. Deep ResNet is consisting of two network layers. First neural network layer is spike prediction. Interval's value forecasting is another neural network layers. The input load and hourly values are fed into Deep ResNet and produce upper and lower bounds of forecasted electricity prices using quantile regression and mean-variance methods. The proposed forecasting model is test with GEFCom2014 dataset where there are 15 tasks for electricity price forecasting which high and spike price are include. The results are compared with benchmarks provided by GEFcom2014.

What is the result? - The performance of forecasting models is evaluated in accuracy and reliability metrics using Pinball Loss Function and Coverage

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Width-based Criterion (CWC), respectively. The significant outcome of this paper is forecasting method cooperated with price spike prediction improved the forecasting's performance in term of quality and quantity. Moreover, increasing confidence level could improve CWC values in order to ensure reliability's satisfaction.

Keywords: Electricity price forecasting, Residual neural network, GEFCOM2014

1. Introduction

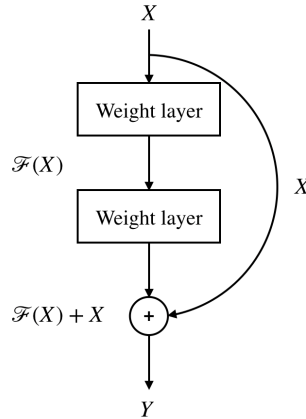
Since the transformation of the deregulation of modern power systems, electricity price forecasting has become more important process to energy market's participants at planning and operation levels. The electricity price in deregulation has become more and more fluctuated as well as the number of the price spikes occurrence has been increasing. The occurrence of price spikes can cause financial damage to both customers and producers. Price spike can be several times to thousand times of the normal price. Price spike appears due to increasing intermittent electricity production makes electricity prices more volatile, with spikes appearing either as very high prices (due to sudden lack of available generation) or as negative prices (due to excess of renewable generation). Several evidences shows that the price spike around 100\$/MWhr may simply resulted from normal congestion or unexpected overload, while price spike around \$500/MWhr led by lacking of reserve. This case the day ahead clearing price is the dominant feature what indicate insufficient reserve. The price spike above \$1,000/MWhr should be the consequence of the outage or breakdown of the generation or transmission system. Such outage or breakdown many comes from many factors, like weather, load profile, etc [1]. [2] provide fundamental reasons of price spike which are volatility of fuel price, load uncertainty, fluctuation in hydroelectricity production, generation outage, transmission congestion, behavior of market participation and market manipulation. [3] studied on technique and economical of on centralized voltage control with high PV penetration in

Portuguese network. The results show that improvement in both forecasting tools and communication systems have significant impact on dedicate resources
 25 and voltage control.

Over the past few decades, many powerful forecasting algorithms have been developed (for a recent comprehensive review, see [4]). The majority of emprical studies are on point forecasting (or call expected value of the spot price).

The conventional point predictions produce no information about the sam-
 30 pling erros and the predication accuracy. This lead to confidence intervals (CIs) and prediction intervals (PIs). CIs and PIs are two well-know toosl for quantifying and representing the uncertainty of predicitons. In literature, several methods have been proposed for construction of PIs and CIs assessment. Lower Upper Bounds Estimation (LUBE) method are formulated using mean and vari-
 35 ence estimation is proposed in [5]. Delta technique for PI construction is presented in [6]. Deep Residual Neural Network (Deep ResNet) is modified from deep Feed Forward Neural Networks (FFNNs) with extra connections (or called skip connections), passing input from one layer to a late layer as well as the next layer as shown in figure 1. Deep ResNet is widely used in computer vision
 40 and pattern reconigition. There are few used on deep residual neural network in forecasting applications.

Figure 1: Basis DRNN



Therefore, this paper seeks to apply Deep ResNet in electricity price forecasting. The performance of the Deep ResNet forecasting model is also compared with linear regression and MLP techniques. The remainder of the paper is organized as follows. First, the problem formulation is presented in brief in section 2. The, the main features of the ANN algorithm are presented . Next, the results after prediction in different cases of proposed method are discussed in section 4. Finally, conclusions are drawn in the last section of this paper.

2. Problem formulation

This section will describe construction of two proposed methods; MLP and Deep ResNet model. The MLP model will represent electricity price forecasting without spike price prediction (see related work in [7]) and the Deep ResNet model will represent electricity price forecasting with spike price prediction in the model. Both models will generate upper and lower bounds with respect to given confidence levels (5%, 10%, 15%, 20%, and 25%). The upper and lower bound will be generated using quantile regression and mean-variance estimation method.

2.1. Proposed Deep ResNet on interval forecasting

As mentioned earlier, this paper develops a novel Deep ResNet with spike price prediction.

Figure 2: Upper and lower bound and mean-variance estimation

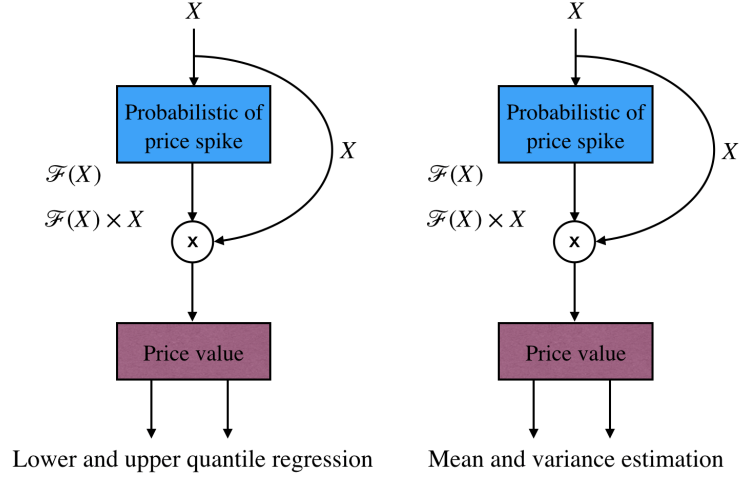
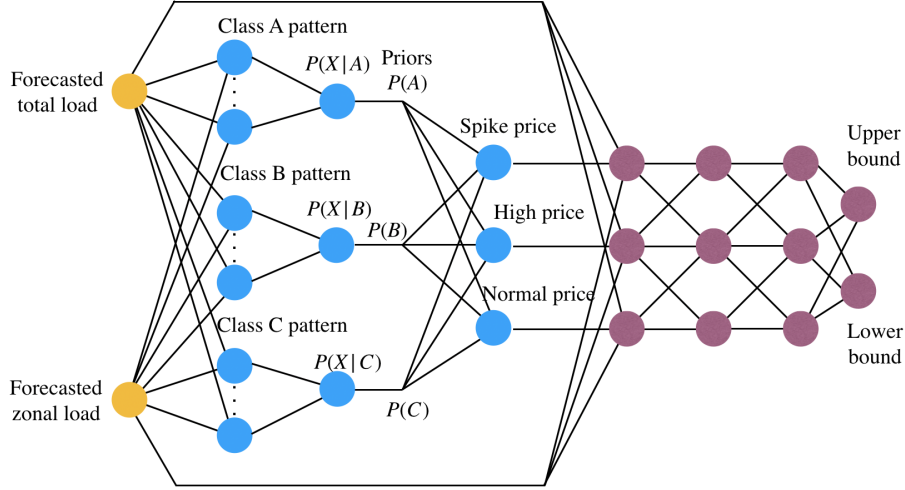


Figure 3: Proposed probabilistic Deep ResNet



2.2. Evaluation metrics

This section will describe evaluation metrics in accuracy and reliable point of view. In terms of accuracy metric, the forecasting results will be analyzed using

pinball function. The Coverage Width-baed Criterion (CWC) will take care of
65 reliability point of view.

2.2.1. Accuracy

The widely used measurement of forecasting's accuracy is mean absolute error (MAE) which is simply and generalized method. MAE work well of point of forecasting (single value). However, this problem is to formulate upper and lower bound of forecasting which is cooperated with confidence value. Hence, general MAE is not satisfied in this case. Pinball loss function are proposed in [8], also be benchmark of this paper, which returns the value that can be interpreted as accuracy of mean-variance and quantile regression forecasting models. The pinball loss function is formulated as below.

$$L_{\tau}(y, z) = \begin{cases} (y - z)\tau & \text{if } y \geq z \\ (z - y)(1 - \tau) & \text{if } z > y \end{cases} \quad (1)$$

where $L_{\tau}(y, z)$ is pinball loss function at τ confidence level, y is forecasted electricity price and z is actual electricty price. The final score of pinball loss function was computed as average L_{τ} across 24 hours for each task. The τ in
70 this paper is 0.05, 0.10, 0.15, 0.20 and 0.25 which are represent 5%, 10%, 15%, 20% and 25% confidence levels. The important results of pinball loss function is that the lower pinball loss, the more accurate forecasting model.

2.2.2. Reliability

In term of reliability measurement, the performance of forecasting model is measured to ensure that the ranges of forecasting can cover the observation values both quality and quantity. First, PI converage probility (PICP) refers to the ability of the constructed PIs to capture the actual target variables. PICP can be methematically stated as

$$PICP = \frac{1}{N} \sum_{i=1}^N C_i \quad (2)$$

where

$$C_i = \begin{cases} 1, & \text{if } t_i \in [L_i, U_i] \\ 0, & \text{if } t_i \notin [L_i, U_i] \end{cases} \quad (3)$$

where N is the number of samples in the test set, t_i represents the actual target, and L_i and U_i are lower and upper bounds of the i th PI, respectively. The range of PICP lies between 0% (when none of the targets are enclosed by PI) to 100% (when all targets are enclosed by PI). Ideally, PICP should be very close or larger than the nominal confidence level associated to the PIs. PICP has a direct relationship with the width of PIs. A satisfactorily large PICP can be easily achieved by widening PIs from either side. However, such PIs are too conservative and less useful in practice, as they do not show the variation of the targets. Therefore, a measure is required to check how wide the PIs are. Mean PI Width (MPIW) quantifies this aspect of PIs [9].

$$MPIW = \frac{1}{N} \sum_{i=1}^N (U_i - L_i) \quad (4)$$

Secondly, MPIW shows the average width of PIs. Normalizing MPIW by the range of the underlying target, R , allows us to compare PIs constructed for different datasets respectively (the new measure is called NMPIW),

$$NMPIW = \frac{MPIW}{R} \quad (5)$$

Both PICP and NMPIW, are representing quality and width of PIs, evaluate the quality of PIs from one aspect. A combined index is required for the comprehensive assessment of PIs from both coverage probability and width perspectives. The new measure should give a higher priority to PICP, as it is the key feature of PIs determining whether constructed PIs are theoretically correct or not. The Coverage Width-based Criterion (CWC) evaluates PIs from both coverage probability and width perspectives.

Where, η and μ are two hyperparameters controlling the location and amount of CWC jump. These measures can be easily determined based on the level of confidence associated with PIs. μ corresponds to the nominal confidence level

associated with PIs and can be set to $1-\alpha$. The design of CWC is based on two
95 principles:

- if PICP is less than the nominal confidence level, $(1-\alpha)\%$, CWC should be large regardless of the width of PIs (measures by NMIPW),
- if PICP is greater than or equal to its corresponding confidence level, then NMPIW should be the influential factor. $\gamma(\text{PICP})$, eliminates the
100 exponential term of CWC when PICP is greater or equal to the nominal confidence level.

2.3. Data description

All data in this paper is provided in Global Energy Forecasting Competition 2014 (see [10]). The aim of this competition is to forecast 15 tasks of electric-
105 ity prices in term of probabilistic distribution (in quantiles). Hourly data of locational marginal price (LMP), zonal load forecast and system load forecast are provided. The participants receive historical data and forecast for next day electricity price. In total, the price forecasting track involves about three years of locational marginal price, zonal and system load forecast. The summarized
110 solution data set of 15 tasks is shown in table 1.

Table 1: GEFcom2014 task solution

Task	Day	Holiday	Season	Normal price	High price	Spike price
1	Sun	Yes	Summer	24	-	-
2	Mon	No	Summer	24	-	-
3	Mon	No	Summer	22	2	-
4	Thu	No	Summer	24	-	-
5	Tue	No	Summer	22	2	-
6	Sat	Yes	Summer	24	-	-
7	Tue	No	Summer	16	8	-
8	Thu	No	Summer	12	8	4
9	Fri	No	Summer	13	6	5
10	Sat	Yes	Summer	18	6	-
11	Wed	No	Summer	24	-	-
12	Thu	No	Summer	24	-	-
13	Sat	Yes	Authumn	24	-	-
14	Sun	Yes	Authumn	24	-	-
15	Tue	No	Authumn	15	9	-

The participation teams in GEFCom2014 perform electricity price forecasting method i.e.; linear regression (IR)[7], multilayer perceptron (MLP)[7], multiple quantile regression[11], hybrid quantile estimation with pre-and-post processes[8]. These data are fed into the proposed MLP and Deep ResNet models during training section with the Levenberg-Marquardt algorithm to prevent overfitting problems.

3. Results

What is comparison? benchmark is provided from GEFCom2014, task4-[7], [8], [5]

The proposed Deep ResNet generates upper and lower bound values using quantile regression and mean-variance method. In accuracy point of view, the results are summarized in 2.

Table 2: The results of probabilistic electricity price forecasting compared to benchmarks

Method	Task 4	Task 5	Task 6	Task 7	Task 8	Task 9	Task 10	Task 11	Task 12	Task 13	Task 14	Task 15
Benchmark 1 ^a	4.03	7.97	5.70	22.32	38.34	44.23	18.22	31.57	42.95	2.86	3.20	22.38
Benchmark 2 ^b	1.00	1.82	1.19	2.82	7.56	4.21	2.60	1.05	1.24	4.06	1.08	3.07
MLP-MV	4.19	4.33	4.18	10.48	31.57	33.35	6.28	4.28	4.25	4.06	4.05	13.02
MLP-QR	2.57	4.03	2.55	12.96	34.76	36.24	8.83	2.51	2.49	2.47	2.62	16.81
Deep ResNet-MV	2.45	3.36	2.39	5.79	8.79	6.95	5.80	2.41	2.41	2.34	2.43	11.02
Deep ResNet-QR	2.11	3.47	1.93	6.14	9.41	7.63	6.38	1.88	1.91	2.01	2.22	11.70

Notes: The numbers are calculated according to the pinball function

^a provided by GEFcom2014

^b provided in [8].

The figure 4 illustrates the reliability perspective of MLP and Deep ResNet models. The CWC values are average values of task 1 to 15.

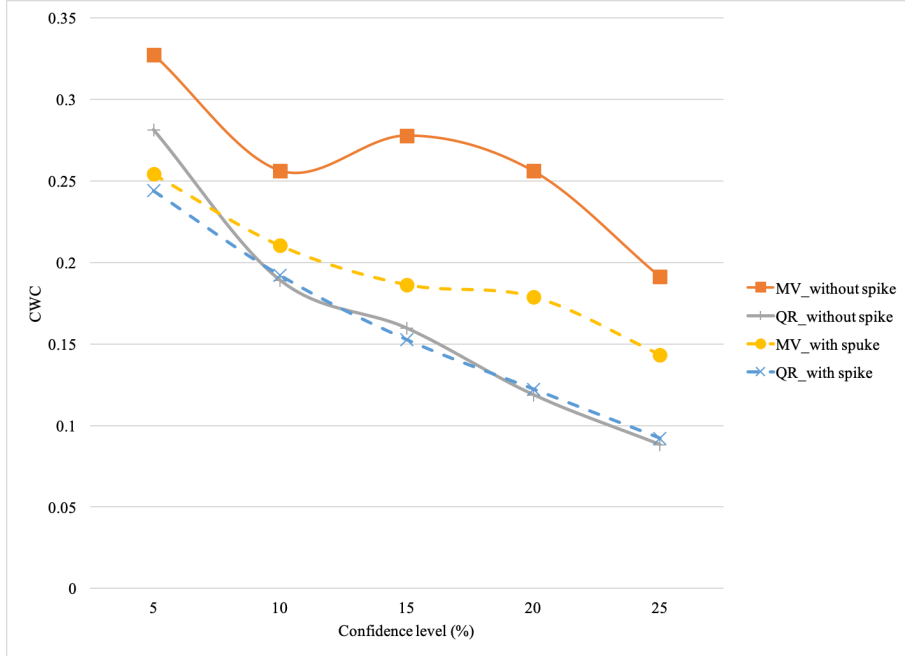


Figure 4: CWC result

125 The results of the proposed MLP and Deep ResNet models using quantile
 regression are illustrated on Task 9. In Figure 5, the filled area represent interval
 prediction of MLP-QR and Deep ResNet-QR with 5% confidence level. In this
 task 9, Deep ResNet-QR can handle high price and spike price in observation
 values where MLP could not handle it. Consequently, the proposed Deep ResNet
 130 could improve reliability of forecasting model.

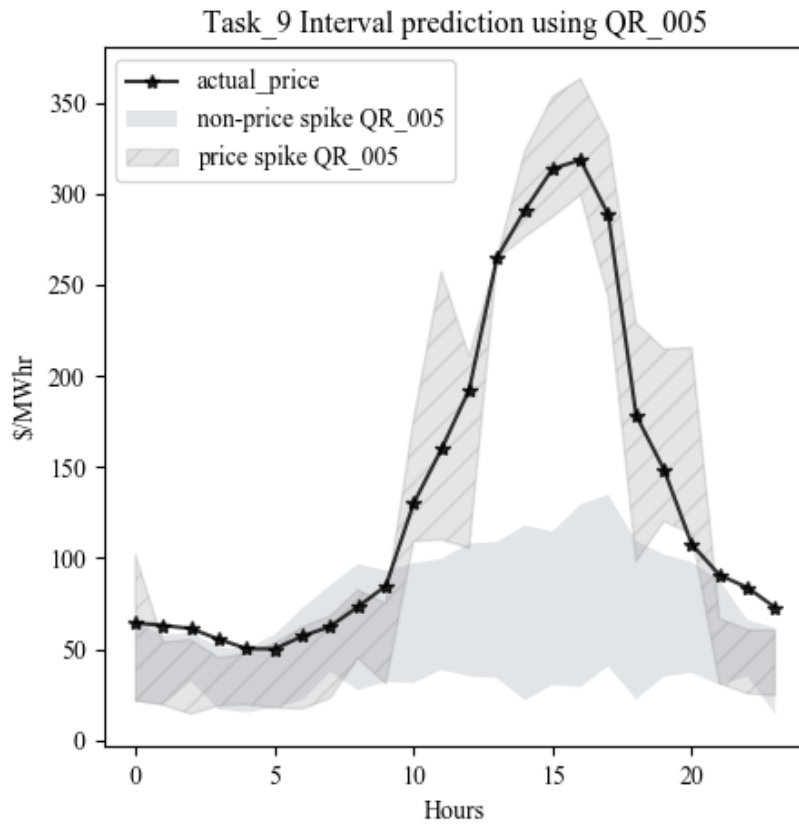


Figure 5: Task 9 between spike and non spike model

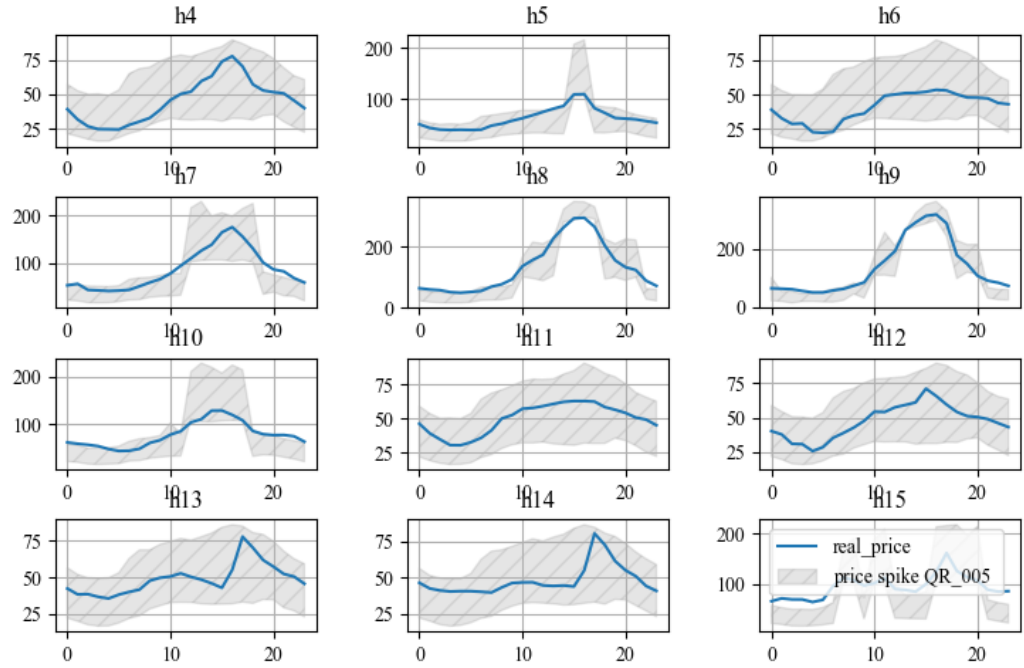


Figure 6: All task with Deep ResNet-QR with 5% confidence level

4. Conclusions

This paper proposes a novel application of Deep Residual Neural Network (Deep ResNet) based approach to probabilistic electricity price forecasting in term of quantile regression and mean-variance estimation. The two significant

135 observation results were: (i)

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