

Evolution on graphs and the transition to cancer

Chay Paterson

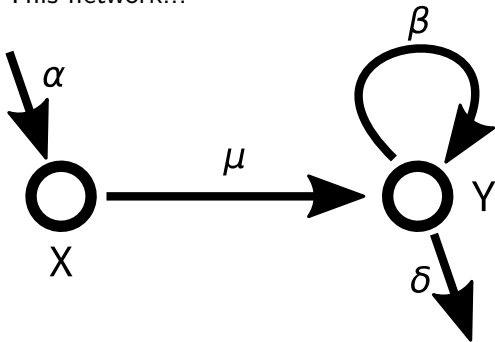
University of Manchester

18 January 2023

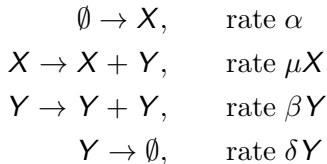
Warning

There will be very few equations in this talk!

This network...



corresponds to this stochastic process:...



and approximately this linear system...

$$\frac{d}{dt} \begin{pmatrix} E[X] \\ E[Y] \end{pmatrix} = \begin{bmatrix} 0 & 0 \\ \mu & \beta - \delta \end{bmatrix} \cdot \begin{pmatrix} E[X] \\ E[Y] \end{pmatrix} + \begin{pmatrix} \alpha \\ 0 \end{pmatrix}$$

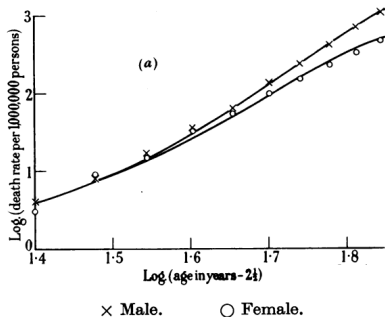
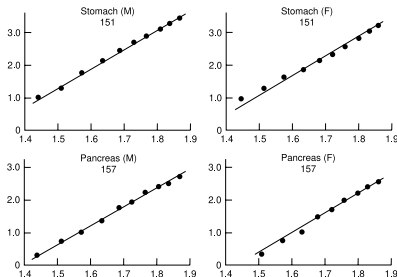
Most of our models are linear, high-dimensional and sparse¹

¹C. Paterson, I. Bozic, H. Clevers, PNAS 2020; 117(34): 20681-20688

Age and cancer

P. Armitage and R. Doll¹²

Risk of cancer increases with age:



¹P. Armitage and R. Doll, British Journal of Cancer 1954; 8: 1-12

²P. Armitage and R. Doll, British Journal of Cancer 1957; 11(2): 161-169

Age and cancer

P. Armitage and R. Doll¹²

Mutation and Retinoblastoma 823

Why? Accumulating
mutations¹²³:

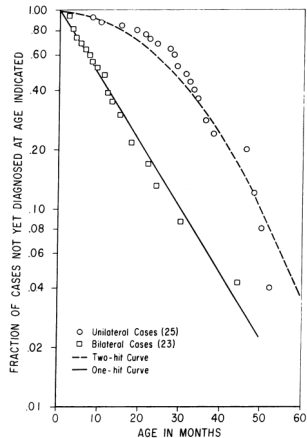
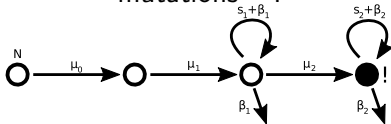


FIG. 1. Semilogarithmic plot of fraction of cases of retinoblastoma not yet diagnosed (S) vs. age in months (t). The one-hit curve was calculated from $\log S = -t/30$, the two-hit curve from $\log S = -4 \times 10^{-6} t^2$.

¹P. Armitage and R. Doll, British Journal of Cancer 1954; 8: 1-12

²P. Armitage and R. Doll, British Journal of Cancer 1957; 11(2): 161-169

³E. Michor, Y. Iwasa and M.A. Nowak, Nature Reviews Cancer 2004; 4:

Multi-stage clonal expansion models

2-3 rate limiting steps¹²³

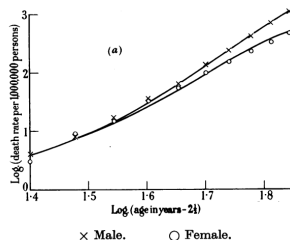
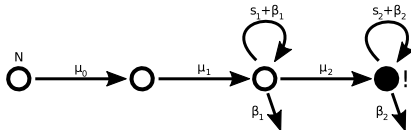
Problem: how to compute $P(\text{cancer}, t)$ for a given model?

Different methods: Fast:

- ▶ Mean-field approximation¹
- ▶ Numerical quadrature²

Slow:

- ▶ Gillespie algorithm + sampling³
- ▶ tau leaping + sampling³



↓?

¹P. Armitage and R. Doll, British Journal of Cancer 1957; 11(2): 161-169

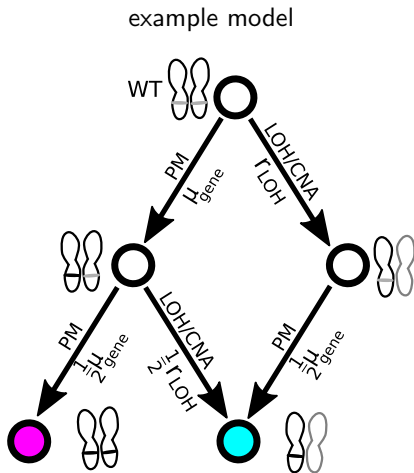
²S. Moolgavkar and G. Luebeck, JNCI 1992; 84(8): 610-618

³C. Paterson, I. Bozic, H. Clevers, PNAS 2020; 117(34): 20681-20688

(supp. material)

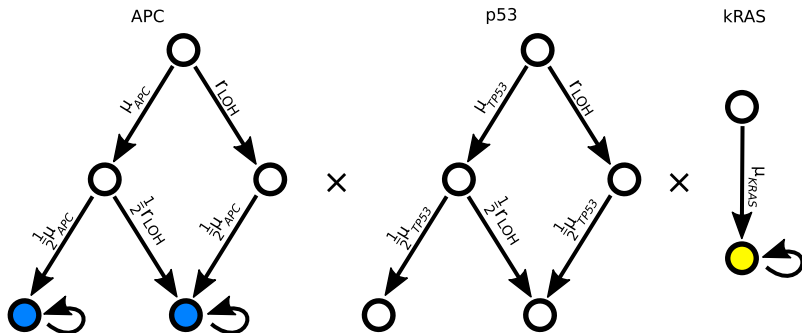
Network models

1. Study **specific genes** and mechanisms of interest (SNVs, LOH, CNA, etc.)
2. Fix parameters from sequences and experiments
3. Distinguish different orders of events



This gets us the incidence of *specific karyotypes*

Colorectal adenocarcinoma model



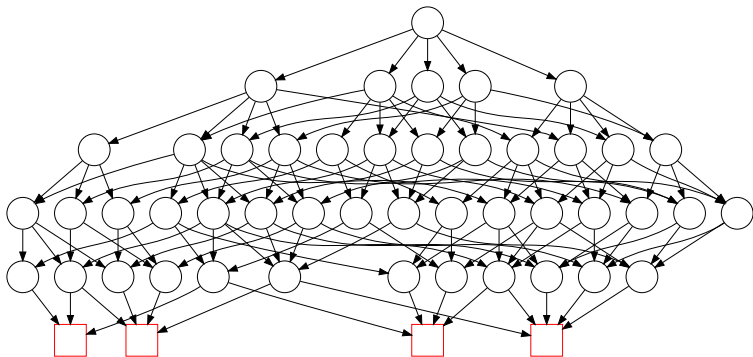
- ▶ *APC-p53-kRAS* combo accounts for about 15% of incidence
- ▶ 5-year survival about 60% (any stage)

¹ Fearon et al. TODO

¹ M. S. Lawrence et al., Nature 2014; 505: 495–501

² Office for National Statistics, England 2019

Colorectal adenocarcinoma model

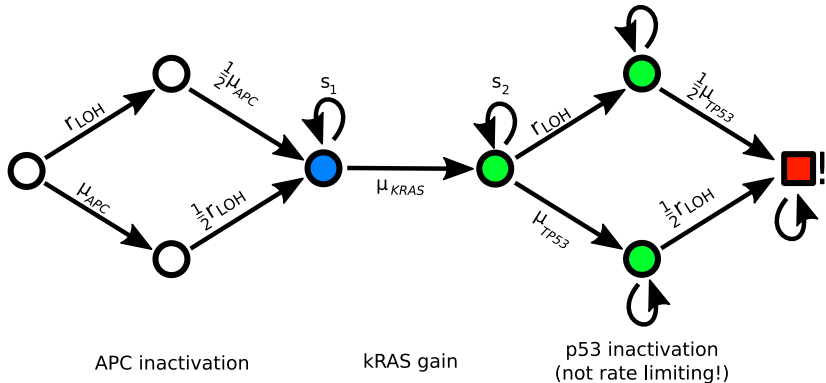


each end node is a different copy number profile

e.g. $(-17p, -5q)$, etc

¹C. Paterson, I. Bozic, H. Clevers, PNAS 2020; 117(34): 20681-20688
(supp. material)

Colorectal adenocarcinoma model



$$P(t) \sim te^{s_2 t}$$

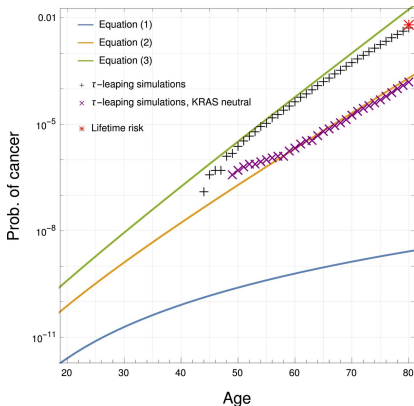
- ▶ The 4 most likely paths account for 50% of the risk
- ▶ Consistent with classic model²

¹C. Paterson, I. Bozic, H. Clevers, PNAS 2020; 117(34): 20681-20688

²Kinzler and Vogelstein 1990

Colorectal adenocarcinoma model

Successful *ab initio* model



- ▶ Can constrain *APC/KRAS* epistasis ($s_2 < 0.31/\text{yr}$)
- ▶ Timing of *p53* inactivation: must be *late*
- ▶ *Compatible with 3-hit* models, similar curve: *p53 not rate limiting*

but:

- ▶ Mean-field breaks down at old ages / large probabilities
- ▶ Stochastic simulations are *extremely slow*

¹C. Paterson, I. Bozic, H. Clevers, PNAS 2020; 117(34): 20681-20688

²(relative to the others)

Why study vestibular schwannoma?

Sometimes rare events make more interesting science possible

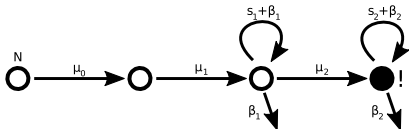
1. genomic subtypes better characterised: *NF2/Merlin* altered in 85 – 100% of cases^{1,2}, *TP53* in $\approx 0\%$
2. usually benign = **easier to study timing!** (of drivers, malignant transformation...)
3. only 3 hits, weak selection (almost neutral)
4. probabilities low: approximations v. accurate **because it's rare**

¹ML Carlson et al., *Otology & Neurotology*: 2018;39(9):860 – 871

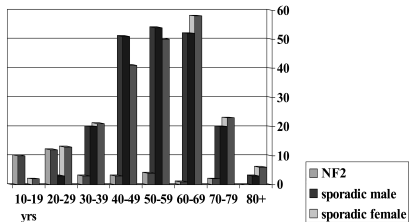
²AL Håvik et al., *Journal of Neurosurgery JNS*. 2017;128(3):911 – 922.

Vestibular schwannoma

3-event model



- ▶ Fitness suspiciously low, $s \approx 0.005/\text{yr}$ ¹
- ▶ Suggests nearly-neutral 3-hit model³



Gareth Evans 2005²

¹R. Woods *et al.* Genetic Epidemiology (2003)24: 265–272

²DGR. Evans *et al.* Otology & Neurotology (2005)26:93–97

³C Paterson, I Bozic, MJ Smith, X Hoad, DGR Evans, <https://doi.org/10.1038/s41416-022-01955-8>

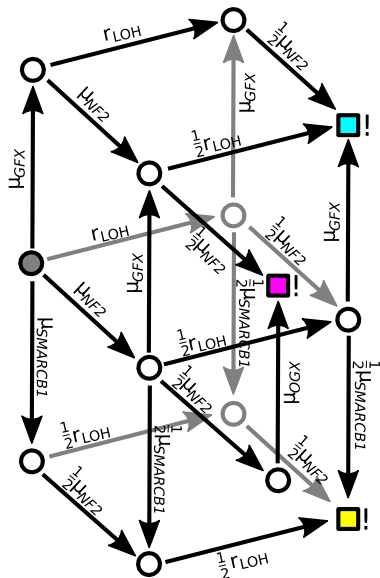
Vestibular schwannoma incidence

Our model for sporadic VS

- ▶ Include *NF2*, *SMARCB1* and (simplified) linkage
- ▶ Add hypothetical oncogene *GFX*

Risk of each subtype looks like

$$P(\text{cyan}) \propto \frac{t^3}{3!}$$



Vestibular schwannoma incidence

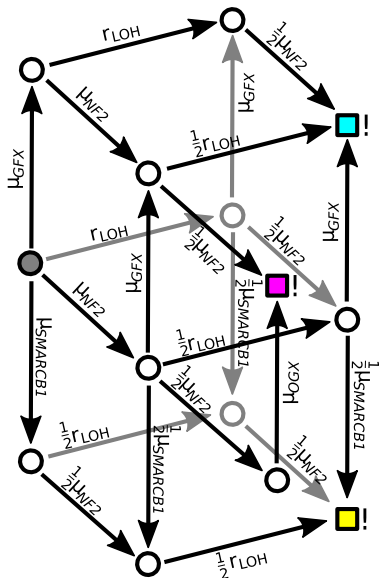
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Risk of each subtype looks like

$$P(\text{cyan}) \propto \frac{t^3}{3!}$$

$$P(\text{cyan}) \approx N_{WT} \mu_{GFX} r_{LOH} \frac{1}{2} \mu_{NF2} \frac{t^3}{3!} \times 6$$



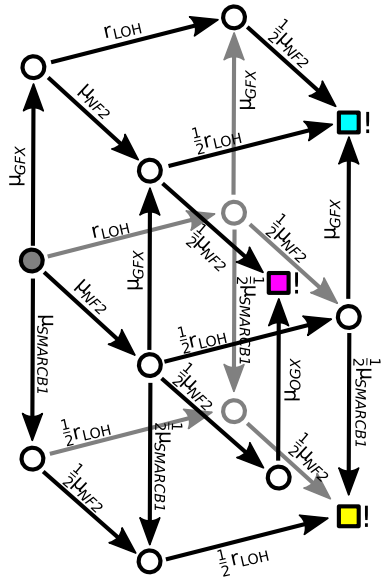
Our model for sporadic VS

- ▶ Don't use *ab initio* point estimates for u , r_{LOH} , n_{GFX} this time...

► Instead use

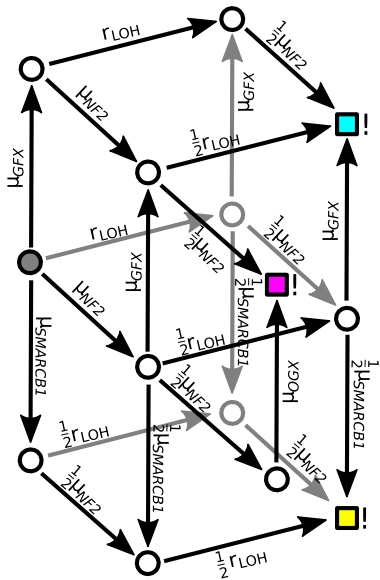
$$P(t) = \text{cyan} + \text{yellow} + \text{magenta},$$
$$f_{LOH} = \frac{\text{cyan} + \text{yellow}}{\text{cyan} + \text{yellow} + \text{magenta}}, \text{ and}$$
$$f_{SMARCB1} = \frac{\text{yellow}}{\text{cyan} + \text{yellow} + \text{magenta}} \text{ to fix}$$

the parameters!

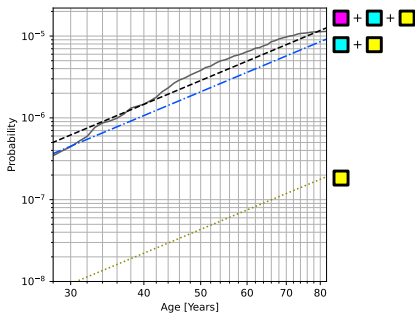


Vestibular schwannoma incidence

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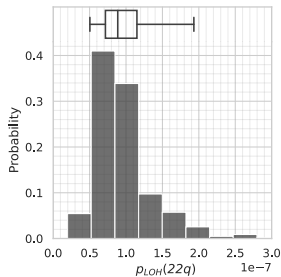
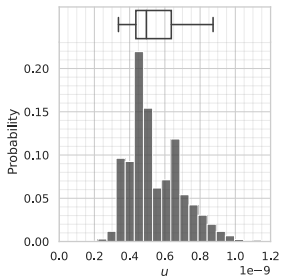
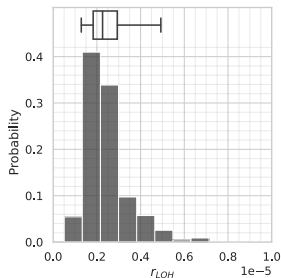
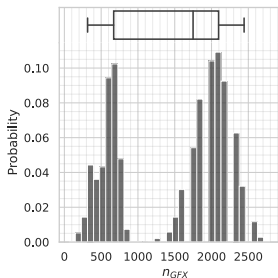


Cumulative incidence of vestibular schwannoma



Vestibular schwannoma incidence

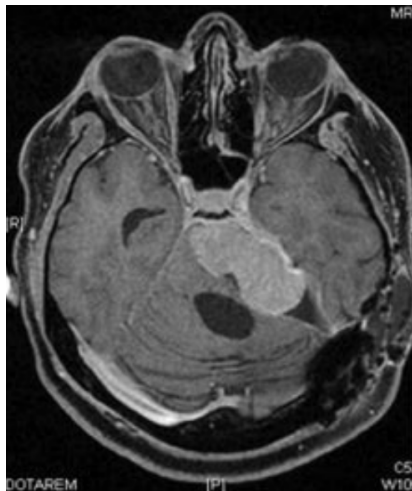
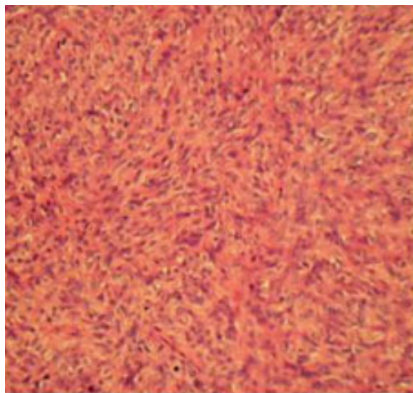
New parameter estimates



Malignant transformation in vestibular schwannoma

Very rare, very bad

- ▶ Risk $\approx 0.1\%$ of VS cases
- ▶ 5-year survival $\approx 12 - 20\%$

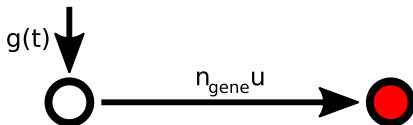


¹AK Demetriades et al. Skull Base (2010)20:381–387.

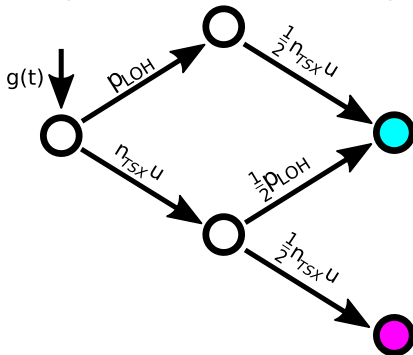
Malignant schwannoma: two models

Timing and identity of drivers

Oncogene activation:



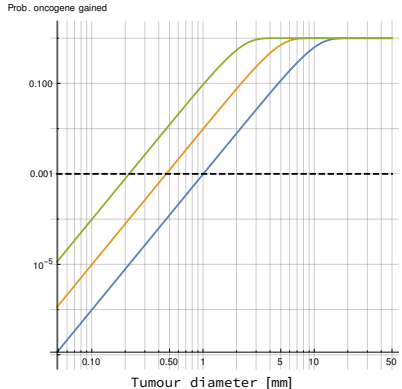
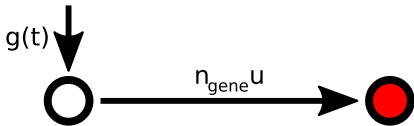
TSX inactivation:



Malignant VS is *extremely* rare!

Malignant schwannoma: first model

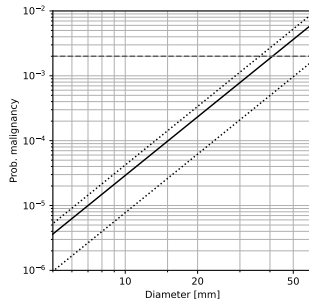
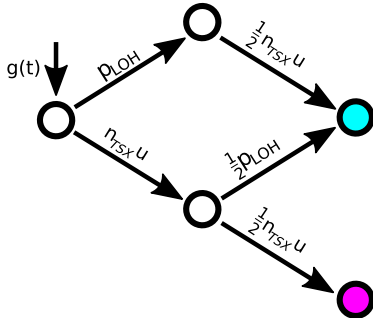
Oncogene activation



- ▶ Oncogene activation \implies high risk
- ▶ But it's a rare outcome
- ▶ So it's probably not caused by oncogene activation

Malignant schwannoma: second model

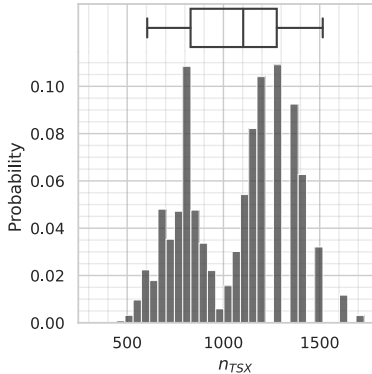
Tumour suppressor TSX inactivation



- ▶ TSX inactivation \Rightarrow low risk
- ▶ Can also estimate n_{TSX} that's consistent with incidence

Who is *TSX*?

Parameter estimates for n_{TSX}

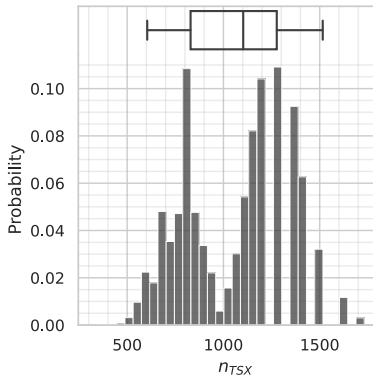


Probably multiple distinct tumour suppressors

Disclaimer: assumes neutrality & haplosufficiency

Who is *TSX*?

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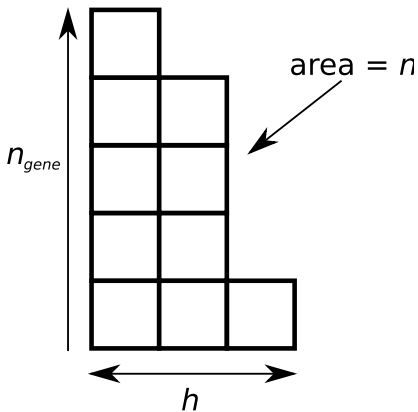


Probably multiple distinct tumour suppressors

i.e. not (just) *TP53*: $n_{TP53} = 73$

Who is *TSX*?

Parameter estimates for n_{TSX}



How many genes are there in this set? Assuming $n_{TSX} = 1000$, estimate

$$h \approx \frac{\sqrt{6} \ln 2}{\pi} \sqrt{n_{TSX}} \approx 17$$

genes account for $\approx 80\%$ of the total.

Watch this space!

Main outputs

1. Better estimates of event rates in Schwann cells
2. Can constrain timing of “*TSX*” (resp. for malignancy)
3. Can constrain size of *GFX* and *TSX*

Main outputs

but...

1. Uncertainties still large
2. Identity of *TSX* unknown
3. Constraints weak: *GFX* and *TSX* probably multiple genes

Need to identify n_{GFX} and n_{TSX}

To do list

How to do this:

- ▶ Sequence all tumours in NF2 database in Manchester

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Just won funding for the above!

Acknowledgements



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In order of appearance...

- ▶ Ivana Božić
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- ▶ Gareth Evans
- ▶ Xanthe Hoad
- ▶ Miriam Smith
- ▶ David Wedge