

# SGN-45006 Fundamentals of Robot Vision

## Exercise Round 6

April 8, 2019

For these exercises you will need Python or Matlab which should be available on the university computers. Return your answers as a pdf along with your modified code to Moodle. Exercise points will be granted after a teaching assistant has checked your answers. Returns done before the solution session will result in maximum of 3 points, whereas returns after the session will result in maximum of 1 point.

**Task 1.** Camera calibration. (Programming exercise) (2 points)

In this exercise you will need to implement the direct linear transform (DLT) method for camera calibration. The algorithm is described in the lecture slides. It is also presented in the book by Hartley & Zisserman (Section 7.1 in the second edition).

The calibration object is a bookshelf whose dimensions are known. That is, width of a shelf is 758 mm, depth is 295 mm, and height between shelves is 360 mm.

Proceed as follows:

Run the script `cam_calibration`. The corners of the bookshelf are already manually localized from the given two images and visualized by the script. See the comments in the source code. Implement the missing function `camcalibDLT`, which should use the DLT algorithm described below.

$$\begin{pmatrix} 0^\top & \mathbf{X}_1^\top & -y_1\mathbf{X}_1^\top \\ \mathbf{X}_1^\top & 0^\top & -x_1\mathbf{X}_1^\top \\ \vdots & \vdots & \vdots \\ 0^\top & \mathbf{X}_n^\top & -y_n\mathbf{X}_n^\top \\ \mathbf{X}_n^\top & 0^\top & -x_n\mathbf{X}_n^\top \end{pmatrix} \begin{pmatrix} \mathbf{P}_1 \\ \mathbf{P}_2 \\ \mathbf{P}_3 \end{pmatrix} = 0$$

Here  $\mathbf{X}_n$  is the known 3D coordinate, and  $x_n$  and  $y_n$  are the known image projection coordinates. Let's denote the above equation as  $\mathbf{A}\mathbf{p} = 0$ . The task is to find  $\mathbf{p}$  minimizing  $\|\mathbf{A}\mathbf{p}\|^2$  (homogeneous least squares). The solution is given by the eigenvector of  $\mathbf{A}^\top\mathbf{A}$  with the smallest eigenvalue.

After implementing the algorithm, both cameras should be calibrated correctly. Check the results visually.

**Include both output images in your pdf, also return your version of the code**

Tasks continue on the next page...

**Task 2.** Triangulation. (Programming exercise) (1 point)

In this exercise you will need to implement the linear triangulation method also described in the lecture slides. (The method is also presented in the book by Hartley & Zisserman.) You must again find a least-squares solution to a system of linear equations. In a similar manner as in exercise problem 1, it can be computed by solving the eigenvectors and eigenvalues of a real symmetric matrix.

As illustrated by the script, the points that will be triangulated are the corner points of the picture on the cover of the course book. As a result of the triangulation we will get the coordinates of these corner points in the world coordinate frame. By computing the distances between the points, we can measure the width and height of the picture in millimeters.

Proceed as follows:

Run the script `triangulation_task`. The corners of the picture on the book cover are already manually localized from the given two images and visualized by the script. See the comments in the source code. Your task is to implement the missing function `trianglin`.

Cross-product as a matrix multiplication can be written as

$$\mathbf{a} \times \mathbf{b} = \begin{pmatrix} 0 & -a_z & a_y \\ a_z & 0 & -a_x \\ -a_y & a_x & 0 \end{pmatrix} \begin{pmatrix} b_x \\ b_y \\ b_z \end{pmatrix} = [\mathbf{a}_\times] \mathbf{b}$$

The goal is to find the least squares solution to the two independent equations  $[\mathbf{x}_{1\times}] \mathbf{P}_1 \mathbf{X} = 0$  and  $[\mathbf{x}_{2\times}] \mathbf{P}_2 \mathbf{X} = 0$  in terms of  $\mathbf{X}$ . Start by calculating  $[\mathbf{x}_{1\times}] \mathbf{P}_1$  and  $[\mathbf{x}_{2\times}] \mathbf{P}_2$  and stack these vertically to acquire  $\mathbf{A}$ . This can then be used to calculate the least squares solution for the corresponding world coordinate  $\mathbf{X}$  similarly as in task 1.

Triangulate the three given point correspondences and calculate the estimated width and height of the picture by computing the distances between triangulated world points.

**Write the estimated width and height in your pdf, also return your version of the code.**