



# Report on the Second Edition of the CHC Competition

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April 7, Prague

# Constrained Horn Clauses



Formula in first order logic:

$$\varphi \wedge p_1(V) \wedge \dots \wedge p_k(V) \implies H$$

- where  $A$  is a constraint language  
(e.g., (non-)linear arithmetic, arrays, bit-vectors, etc.)
- $\varphi$  is a constraint in  $A$
- $p_1 \dots p_k$  are uninterpreted relation symbols
- each  $p_i(V)$  is an application of the predicate to variables
- $H$  is either some application  $p_i(V)$  or *false*

## System of CHCs

- Only one CHC with  $H = \textit{false}$
- Has a solution if there exists an interpretation for each  $p_i$   
making each CHC valid

# Example

## Program in C

```
int x, k, c = 0;  
int N = NONDET();  
assume (N ≥ 0);  
  
while (c ≠ N) {  
    c++;  
    if (k mod 2 == 0) x++;  
    k = x + c;  
}  
  
if (x ≠ N) ERROR();
```

## CHC-encoding



$$x = 0 \wedge k = 0 \wedge c = 0 \wedge N \geq 0 \implies \mathbf{Inv}(x, k, c, N)$$

$$\begin{aligned} & \mathbf{Inv}(x, k, c, N) \wedge c \neq N \wedge c' = c + 1 \wedge \\ & x' = \text{ite } (k \bmod 2 = 0, x + 1, x) \wedge \\ & k' = x' + c' \\ & \implies \mathbf{Inv}(x', k', c', N) \end{aligned}$$

$$\mathbf{Inv}(x, k, c, N) \wedge c = N \wedge x \neq N \implies \perp$$

# Validating Solutions of CHCs



## System of CHCs

$$x = 0 \wedge k = 0 \wedge c = 0 \wedge N \geq 0 \implies \boxed{\mathbf{Inv}(x, k, c, N)}$$

$$\boxed{\mathbf{Inv}(x, k, c, N)} \wedge c \neq N \wedge c' = c + 1 \wedge \\ x' = \text{ite}((k \bmod 2 = 0, x + 1, x) \wedge \\ k' = x' + c') \implies \boxed{\mathbf{Inv}(x', k', c', N)}$$

$$\boxed{\mathbf{Inv}(x, k, c, N)} \wedge c = N \wedge x \neq N \implies \perp$$

Inductive invariant

$$\mathbf{Inv}(x, k, c, N) = (k = x + c \wedge x = c)$$

# Validating Solutions of CHCs

**CHC**  
**COMP**

## System of CHCs

$$x = 0 \wedge k = 0 \wedge c = 0 \wedge N \geq 0 \implies (k = x + c \wedge x = c)$$

$$(k = x + c \wedge x = c) \wedge c \neq N \wedge c' = c + 1 \wedge x' = \text{ite}(k \bmod 2 = 0, x + 1, x) \wedge k' = x' + c' \implies (k' = x' + c' \wedge x' = c')$$

$$(k = x + c \wedge x = c) \wedge c = N \wedge x \neq N \implies \perp$$

Inductive invariant

$$\mathbf{Inv}(x, k, c, N) = (k = x + c \wedge x = c)$$

# CHC Solving Competition



- Second Edition: April 7 2019, HCVS@ETAPS
- The CHC competition (CHC-COMP) compares state-of-the-art tools for CHC solving with respect to performance and effectiveness on a set of publicly available benchmarks
- Web: <https://chc-comp.github.io/>
- Gitter: <https://gitter.im/chc-comp/Lobby>
- GitHub: <https://github.com/chc-comp>
- Format: <https://chc-comp.github.io/2018/format.html>

# CHC Format



- bench ::= (set-logic HORN)  
    fun\_decl+  
    (assert assert)\*  
    (assert query)  
    (check-sat)
- fun\_decl ::= (declare-fun symbol ( sort\* ) Bool)
- var\_decl ::= (symbol sort)
- head ::= (u\_predicate var\*)
- tail ::= (u\_predicate var\*) | SMT-LIB-formula | (and tail tail)
- assert ::= (forall ( var\_decl+ ) (=> tail head)) | head
- query ::= (forall ( var\_decl+ ) (=> tail false))

# Tracks



Linear Integer Arithmetic, linear clauses (**LIA-Lin**)

at most one application of an uninterpreted relation symbol in each CHC tail

**Arrays + LIA-Lin**

formulas involve array variables

**NEW in 2019**

Linear Integer Arithmetic, nonlinear clauses (**LIA-Nonlin**)

tail of some CHC has more than one application of uninterpreted relation symbols

Linear Real Arithmetic, transition systems (**LRA-TS**)

one uninterpreted relation symbol, three CHCs

# Benchmarks



Linear Integer Arithmetic, linear clauses (**LIA-Lin**)

**325** instances contributed by Hoice, Ultimate, Eldarica, Sally, Kind2/Zustre, FreqHorn/FreqTerm, VMT

Arrays + LIA-Lin

**361** instances contributed by Spacer, Ultimate, FreqHorn

Linear Integer Arithmetic, nonlinear clauses (**LIA-Nonlin**)

**283** instances contributed by PCSat, Hoice, Ultimate, Eldarica

Linear Real Arithmetic, transition systems (**LRA-TS**)

**243** instances contributed by Sally, FreqHorn/FreqTerm, VMT

# Participants

PCSat

**NEW in 2019**

Yuki Satake,  
Tomoya Kashifuku, and  
Hiroshi Unno

Sally

Dejan Jovanovic,  
Martin Blichá

Eldarica

Hossein Hojjat and  
Philipp Rümmer

Rebus

unnamed solver  
not entered in  
the competition

Hoice

Adrien Champion

**Ultimate Tree Automizer**

Daniel Dietsch, Matthias Heizmann, Jochen  
Hoenicke, Mostafa M. Mohamed, Alexander Nutz,  
Andreas Podelski, and Daniel Tischner

**Ultimate Unihorn Automizer**

Daniel Dietsch, Matthias Heizmann, Jochen  
Hoenicke, Alexander Nutz, and Andreas Podelski

Spacer

Arie Gurfinkel, Anvesh Komuravelli, Nikolaj Bjorner,  
Krystof Hoder, Yakir Vizel, Bernhard Gleiss, and  
Matteo Marescotti

**Hors Concours**



# Competition Setup



- StarExec cluster environment
- Dedicated Queue of 20 nodes
- 2 jobs per node
- 64GB per job
- 600s timeout
- Benchmarks will be publicly available on StarExec
- Detailed results will be available by request

# The Friendliest Competition



## Fair selection of benchmarks

If a participant submitted a benchmark suit, organizers include a good (but randomly chosen) representation of it

## Help with frontend issues

Pre-processing of submitted benchmarks by CHC-COMP's tools to match the format more closely

## Introducing new tracks

As long as there is a solver that focuses on them

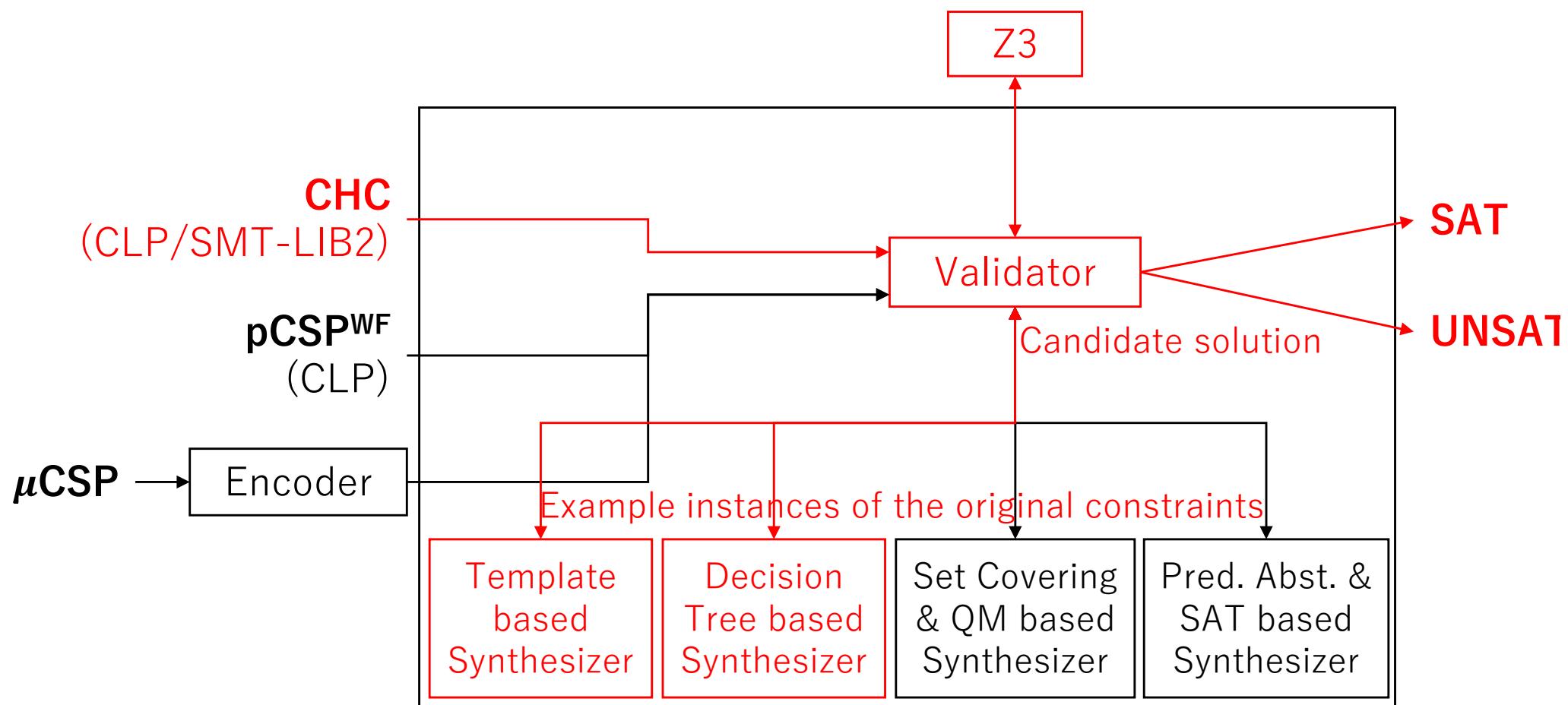
## Giving participants a second chance to submit solvers

After running trial runs on selections of benchmarks to avoid discrepancies

# PCSat: Predicate Constraint Satisfaction

- Developed since January 2019 by [Yuki Satake](#), [Tomoya Kashifuku](#), and [Hiroshi Unno](#) (University of Tsukuba, Japan) in the OCaml functional language
- Support **new classes of predicate constraint satisfaction problems beyond CHC**
  - **pCSP<sup>WF</sup>**: (possibly **non-Horn**) constrained clauses with **well-foundedness** constraints
  - **$\mu$ CSP**: (possibly **alternating**) least and **greatest** fixpoint constraints [[Nanjo+ LICS'18](#), [Unno HCVS'18](#)]
- Support LIA

# PCSat Architecture (red parts for CHC-COMP'19)



# Hoice [Champion et al., 2018]

## ICE-based Refinement Type Discovery for Higher-Order Functional Programs

Adrien Champion<sup>1</sup>, Tomoya Chiba<sup>1</sup>,  
Naoki Kobayashi<sup>1</sup>, Ryosuke Sato<sup>2</sup>



<sup>1</sup> The University of Tokyo

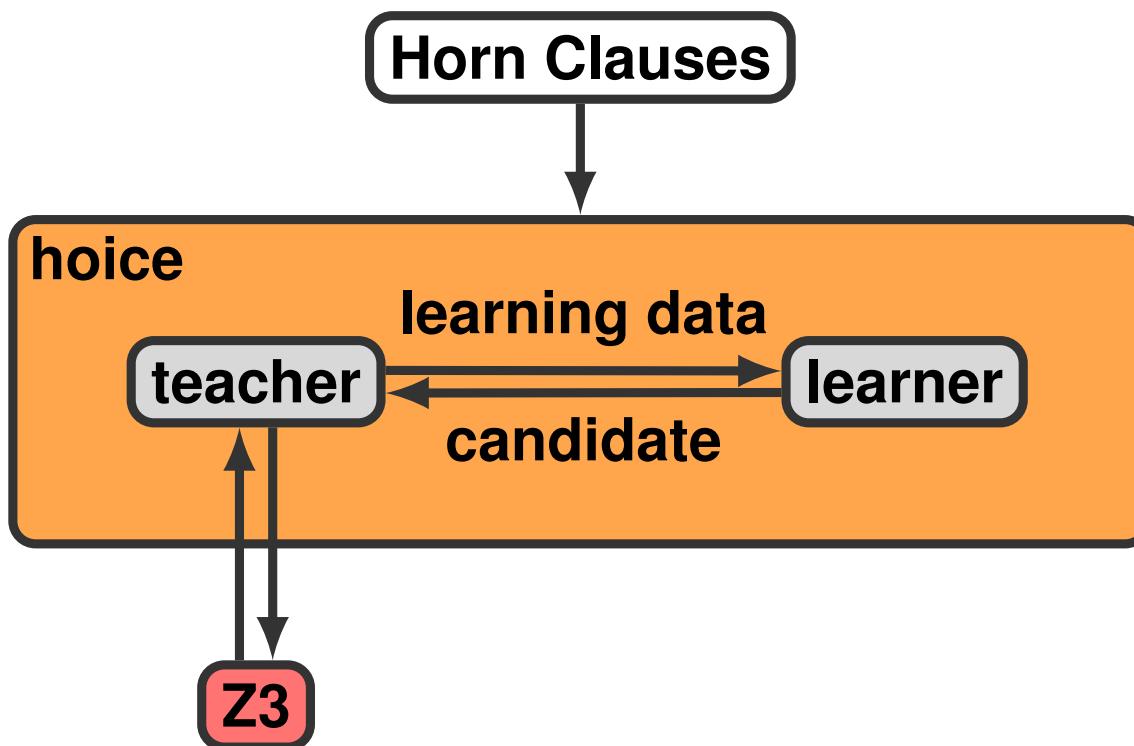
<sup>2</sup> Kyushu University

<https://github.com/hopv/hoice>

- machine-learning-based Horn clause solver:  
generalized ICE framework [Garg et al., 2014]
- context: higher-order program verification
- supports Int, Real, Array, datatypes

## Hoice [Champion et al., 2018]

- learner produces candidates for the predicates
- teacher checks each clause is respected
- ⇒ each check is a quantifier-free (**non-Horn**) formula
- using Z3 [[de Moura and Bjørner, 2008](#)] (separate process)



# The ELDARICA Horn Solver

Hossein Hojjat<sup>1</sup>    Philipp Rümmer<sup>2</sup>

<sup>1</sup>Rochester Institute of Technology

<sup>2</sup>Uppsala University

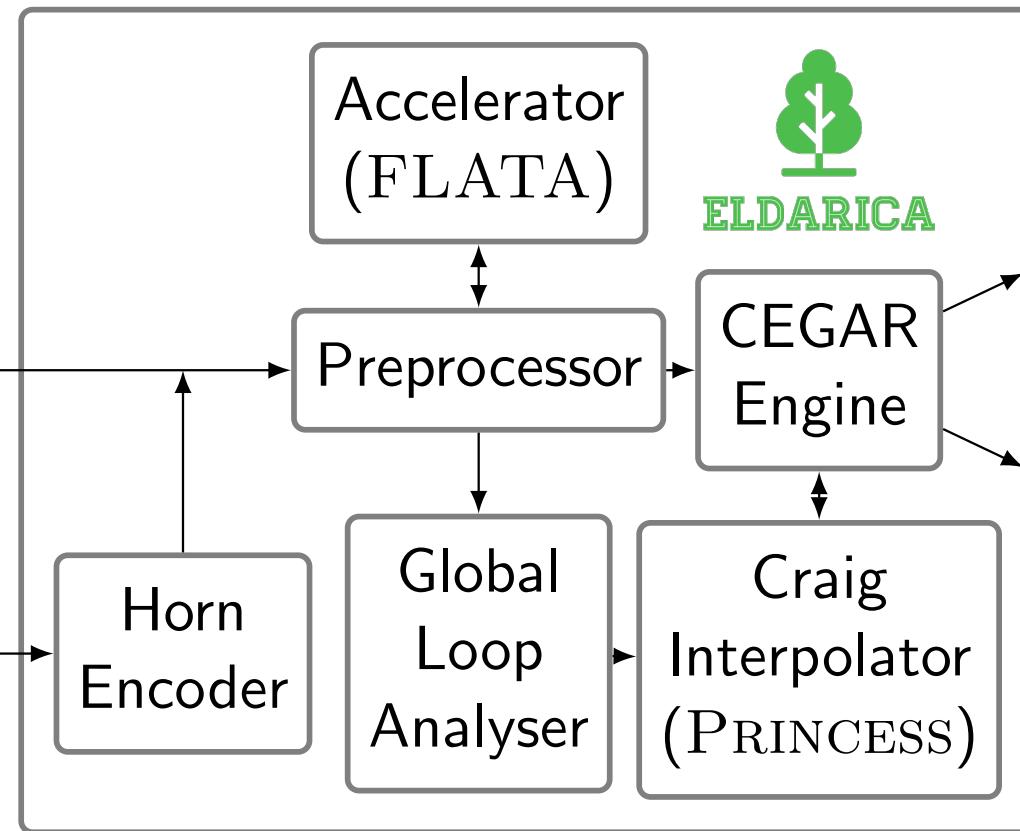
# ELDARICA Overview

- Horn solver developed since 2011
- Open-source, implemented in Scala, running in JVM
- **Input formats:**  
SMT-LIB, Prolog, C, timed automata
- **Theories:**  
LIA, NIA, arrays, algebraic data-types, bit-vectors
- Scala/Java API
- Support for linear + non-linear clauses
- <https://github.com/uuverifiers/eldarica>

# ELDARICA Architecture

**Horn clauses**  
Prolog, SMT-LIB

**Programs**  
NTS , C,  
Timed Automata





## Approach

- ▶ Similar to **trace abstraction** for programs
  - ▶ Represent set of **all sequences of statements** that can reach an error location as **nested word automaton**.
  - ▶ Program is correct iff each word of this language is **infeasible**.
- ▶ Trace abstraction for Horn clauses
  - ▶ Represent set of **all derivation trees** of a set of CHCs as **tree automaton**.
  - ▶ Set of CHCs is sat iff each tree of this language is a **derivation of false**.

## Tools

- ▶ ULTIMATE AUTOMATA LIBRARY
- ▶ SMTINTERPOL

## Contributors

Daniel Dietsch, Matthias Heizmann, Jochen Hoenicke, Mostafa M. Mohamed, Alexander Nutz, Andreas Podelski, Daniel Tischner



## Approach

1. Encode set of CHCs  $\Phi$  as (possibly recursive) program  $P_\Phi$  s.t.  
 $P_\Phi$  is safe iff  $\Phi$  is sat
2. Apply off-the-shelf program verifier

## Tools

- ▶ Program verifier: ULTIMATE AUTOMIZER
- ▶ Predicate providers: Newton-style interpolation (Unsat. core + projection), SMTINTERPOL
- ▶ SMT Solvers: CVC4, MATHSAT 5, SMTINTERPOL, Z3
- ▶ ULTIMATE AUTOMATA LIBRARY

## Contributors

Daniel Dietsch, Matthias Heizmann, Jochen Hoenicke, Alexander Nutz,  
Andreas Podelski

# Sally

- Model checker for infinite state systems described as transition systems
- <http://sri-csl.github.io/sally/>
- *Property-directed k-induction*, Jovanović, Dutertre, FMCAD 2016
- Support of different reasoning engines
  - Bounded model checking (BMC)
  - k-induction (KIND)
  - Property-directed k-induction (PDKIND)
- Supported SMT solvers: Yices2, MathSAT5, OpenSMT2 (unofficially)
- Developed by Dejan Jovanović
- Support for CHC format (limited) and OpenSMT2 contributed by Martin Blichá

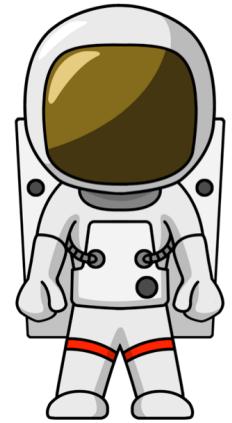
# CHC-COMP configurations

- Support for CHC limited to transition systems in LRA
- PDKIND engine using Yices2 as the main reasoning engine and
  - MathSAT5 as the interpolation back-end
  - OpenSMT2 as the interpolation back-end with different interpolation algorithms
- MathSAT5 with default settings (Farkas interpolation)
- OpenSMT2 with four LRA interpolation algorithms
  1. Farkas interpolation
  2. dual Farkas interpolation
  3. decomposed interpolation
  4. dual decomposed interpolation
  - *LRA Interpolants from No Man's Land*, Alt, Hyvärinen, Sharygina, HVC 2017
  - *Decomposing Farkas Interpolants*, Blich, Hyvärinen, Kofroň, Sharygina, TACAS 2019

# Spacer: Solving SMT-constrained CHC

Spacer: a solver for SMT-constrained Horn Clauses

- now the default (and only) CHC solver in Z3
  - <https://github.com/Z3Prover/z3>
  - dev branch at <https://github.com/agurfinkel/z3>



Supported SMT-Theories

- Linear Real and Integer Arithmetic
- Quantifier-free theory of arrays
- *Universally quantified theory of arrays + arithmetic*
- Best-effort support for many other SMT-theories
  - data-structures, bit-vectors, non-linear arithmetic

Support for Non-Linear CHC

- for procedure summaries in inter-procedural verification conditions
- for compositional reasoning: abstraction, assume-guarantee, thread modular, etc.

# Spacer Contributors

Arie Gurfinkel

Anvesh Komuravelli

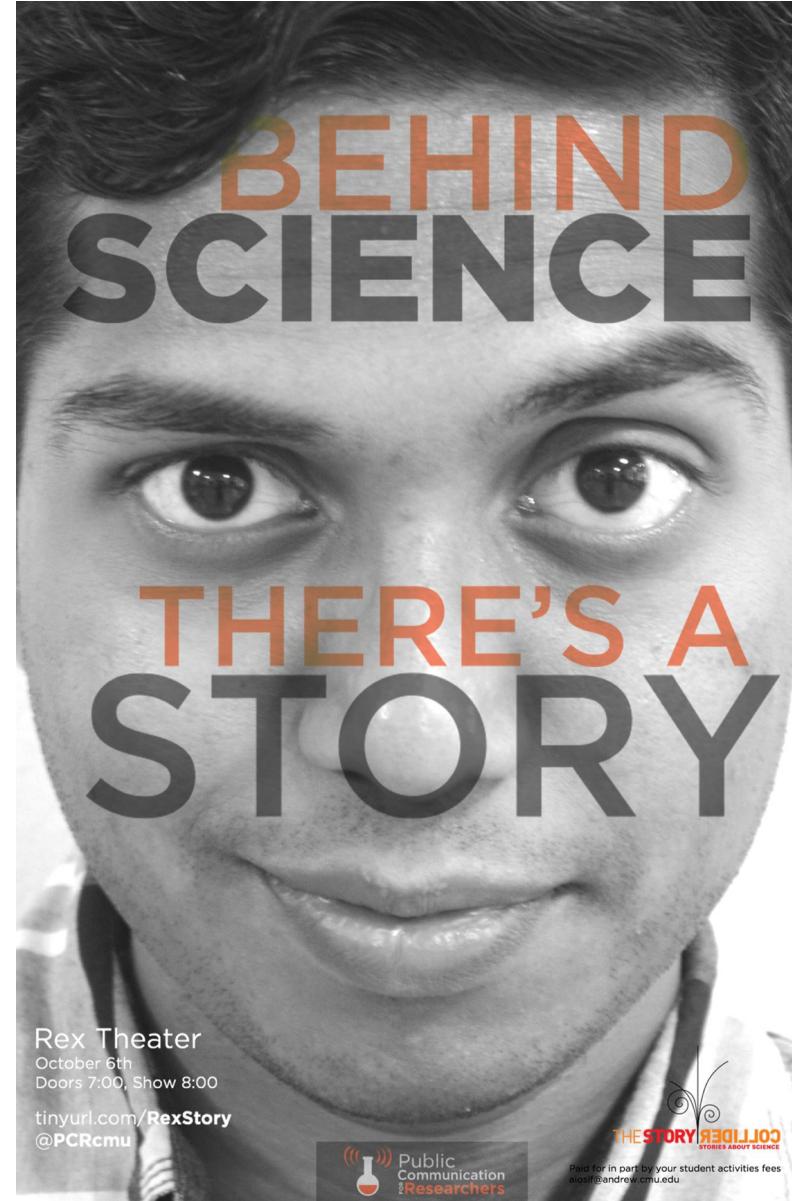
Nikolaj Bjorner

(Krystof Hoder)

Yakir Vizel

Bernhard Gleiss

Matteo Marescotti



# Scoring Schema



- Three possible outputs
  - Sat / Unsat / Unknown
- We count #Sat + #Unsat
  - Solvers with equal total score are ordered w.r.t. running time
- Disqualification for wrong results
- No witness generation (yet)

# Results: LIA-Lin



Solver	Score	#SAT	#UNSAT	Avg time
Spacer	279	194	85	28.90
Rebus	267	188	79	41.85
Eldarica	209	129	80	24.55
Ultimate Unihorn Automizer	133	63	70	23.05
Hoice	129	65	64	7.09
Ultimate Tree Automizer	107	42	65	29.15
PCSat	45	33	12	23.74

\* 325 instances total

# Results: LIA-Nonlin



Solver	Score	#SAT	#UNSAT	Avg time
Spacer	<b>270</b>	153	117	5.04
Eldarica	<b>234</b>	131	103	15.93
Ultimate Unihorn Automizer	<b>177</b>	96	81	36.94
Hoice	<b>176</b>	110	66	9.85
PCSat	<b>123</b>	81	42	24.69
Ultimate Tree Automizer	<b>73</b>	29	44	4.85

\* **283** instances total

# Results: LIA+Array



Solver	Score	#SAT	#UNSAT	Avg time
Spacer	159	76	83	9.60
Ultimate Unihorn Automizer	90	44	46	28.47
Ultimate Tree Automizer	71	39	32	44.14
Hoice	35	24	11	0.06
Eldarica	20	20	0	100.14

\* 361 instances total

# Results: LRA-TS



Solver	Score	#SAT	#UNSAT	Avg time
Sally-y2o2-decomposed-itp	<b>194</b>	150	44	43.71
Sally-y2o2-Farkas-itp	<b>194</b>	150	44	44.34
Rebus	<b>190</b>	137	53	53.24
Sally-y2o2-dual-Farkas-itp	<b>188</b>	144	44	53.46
Sally-y2m5	<b>179</b>	135	44	40.07
Spacer	<b>173</b>	126	47	46.19
Sally-y2o2-dual-decomposed-itp	<b>157</b>	118	39	67.67
Ultimate Tree Automizer	<b>93</b>	73	20	55.15
Ultimate Unihorn Automizer	<b>67</b>	50	17	22.21

\* **243** instances total

Congrats to



**Eldarica**

LIA-Lin and LIA-Nonlin categories

**Ultimate Unihorn Automizer**

LIA+Array category

**Sally**

LRA-TS category

**Spacer**

(unofficially) all LIA categories



Big thanks to



# Discussion



- Any fairness / transparency concerns?
- Frontend / format issues?
- New benchmarks / new tracks?
- Solution validation?
- CHC-COMP 2020 dates / organizers?

# Thank you!

