



# 7/23 Meeting

Christina



## Three Global Methods

1. Monte Carlo (what we are currently using)
2. Differential Evolution
3. Basinhopping (a markov chain Monte Carlo method)



# Monte Carlo

Advantage: takes little time (although it becomes significant when the data set becomes huge)

Disadvantage: not robust to noise



# Differential Evolution

The algorithm randomly selects  $n$  points (population) from the 6D space (with user-defined range), then recombines the points and updates the points' new positions until there is only one point with the lowest  $\chi^2$  value left (or that the number of iteration exceeds the limit)

Advantage: very robust to noise; large rate of convergence when the population size is large

Disadvantage: Takes a significantly longer time (>30 seconds per event)



# Basinhopping

Given a starting point (initial condition), the algorithm calculates the local minimum of  $\chi^2$  value using a user-defined local method, then applies a random perturbation to the coordinates. The new position is accepted /rejected based on the Metropolis criteria. The point with the lowest  $\chi^2$  value is updated as the newest global minimum

Advantage: less time than Differential Evolution but gives comparable results

Disadvantage: not robust to noise

# Event 504

## Data with noise

Monte-Carlo: 90.04

Basinhopping with SLSQP as the local method: 83.8

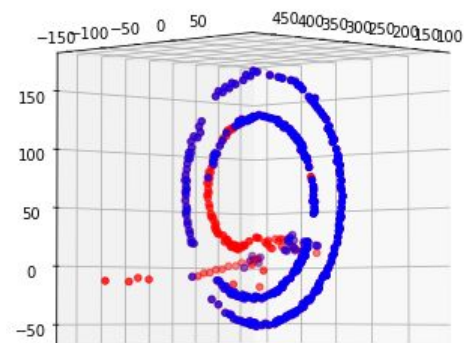
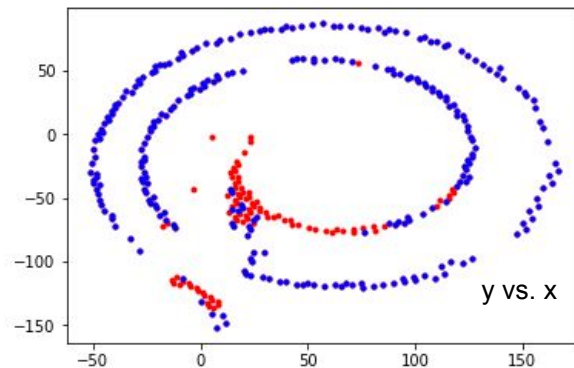
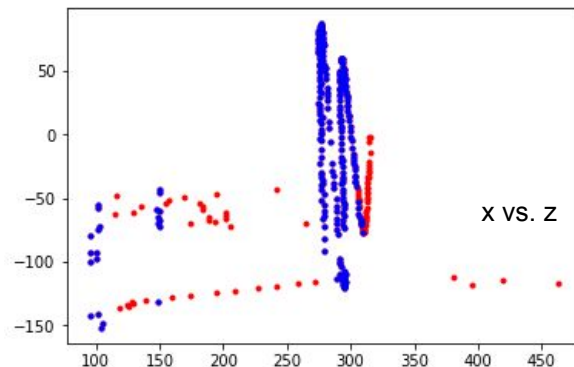
Differential Evolution: 68.06

## Data with reduced noise

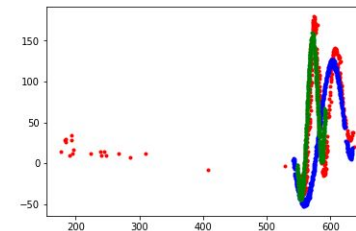
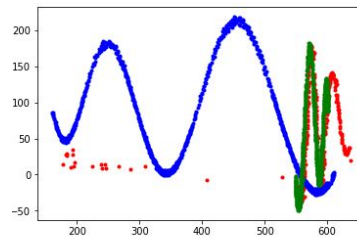
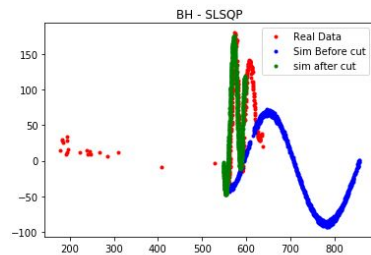
Monte-Carlo: 45.0

Basinhopping with SLSQP as the local method: 42.7

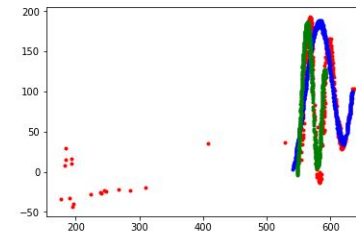
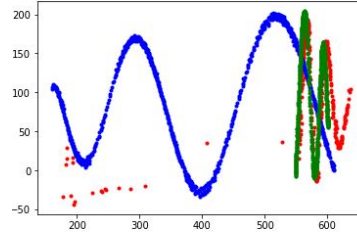
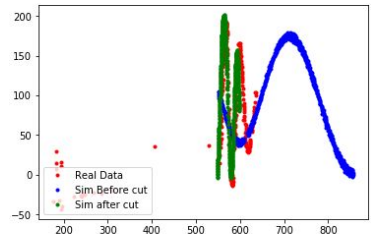
Differential Evolution: 57.61



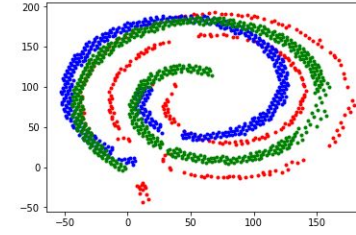
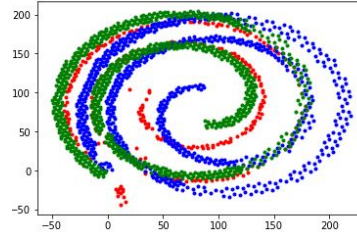
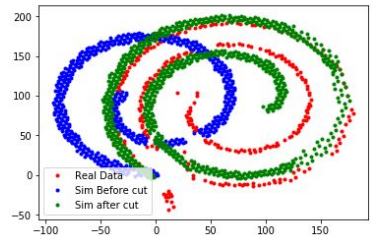
blue: after cleaning  
red: before cleaning



x vs. z



y vs. z



y vs. x

Basinhopping

Monte Carlo

Diff Evolution

Red: real data (with noise)

Blue: fittings of data with noise

Green: fitting of data without noise

# Event 765

## Data with noise

Monte-Carlo: 100.05

Basinhopping with SLSQP as the local method: 95.8

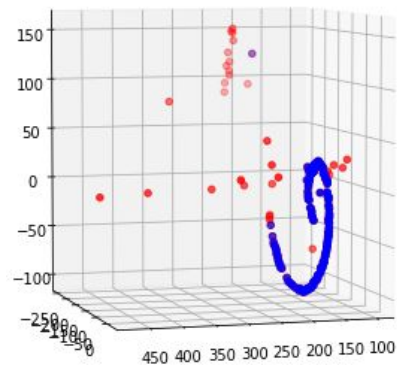
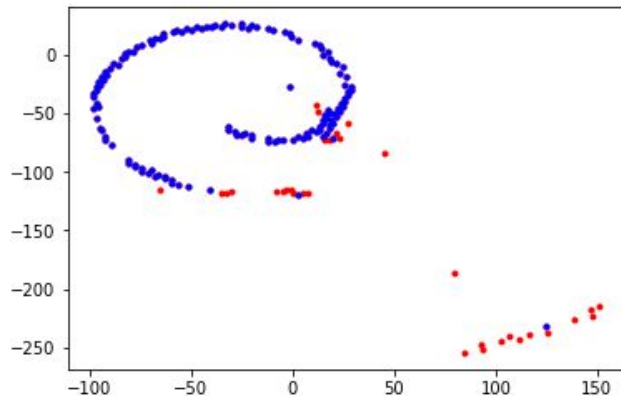
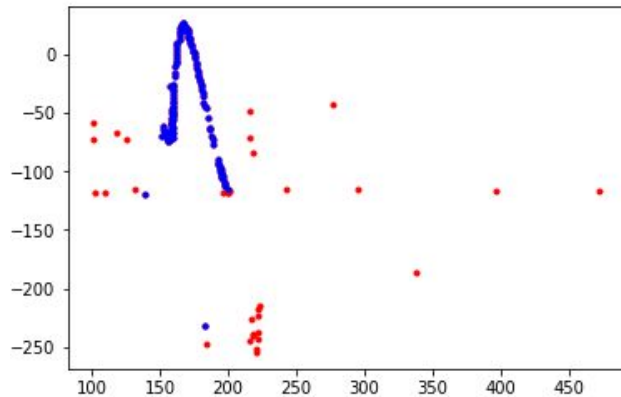
Differential Evolution: 35.45

## Data with reduced noise

Monte-Carlo: 33.53

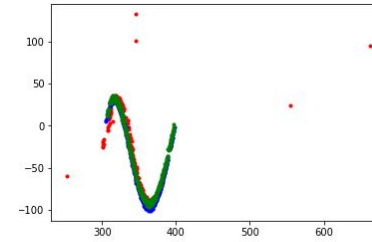
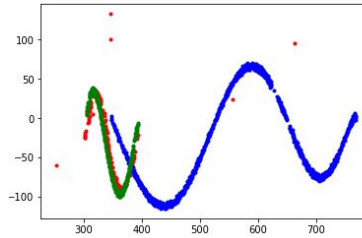
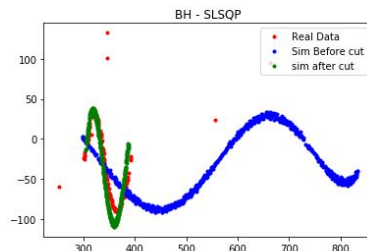
Basinhopping with SLSQP as the local method: 37.9

Differential Evolution: 34.27

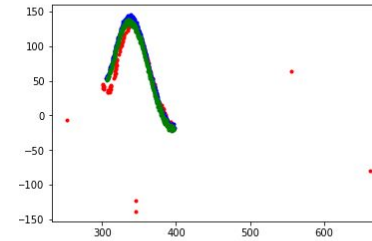
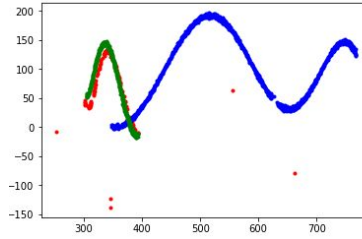
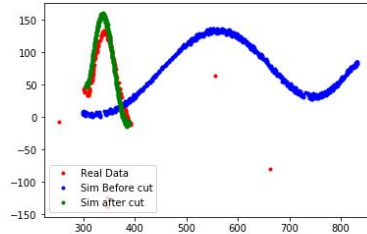


blue: after cleaning  
red: before cleaning

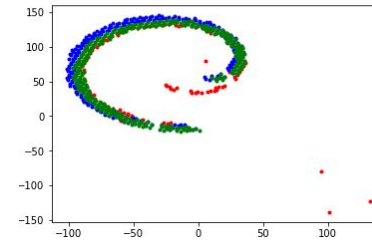
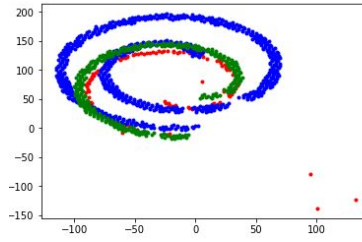
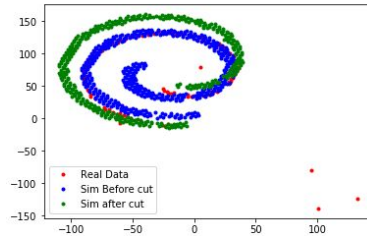




X vs. Z



y vs. Z



y vs. X

Basinhopping

Monte Carlo

Diff Evolution

Red: real data (with noise)  
 Blue: fittings of data with noise  
 Green: fitting of data without noise



## Monte Carlo

average time with noise: 0.9150381401965493 seconds  
average time without noise: 0.7961778515263608 seconds  
average chi2 value (with noise): 58.50360822485877  
average chi2 value (without noise): 35.912268307746764

## Differential Evolution

average time: 33.156591317483354 seconds  
average chi2 value (with noise): 42.02732836605447  
average chi2 value (without noise): 42.00646858265847

## Basinhopping niter = 10

average time for Nelder-Mead: 7.100889333656856 seconds  
chi2 value (with noise) for Nelder-Mead: 56.602099562368004  
chi2 value (without noise) for Nelder-Mead: 36.739391372534904  
average time for Powell: 15.809054085186549 seconds  
chi2 value (with noise) for Powell: 72.39768213081769  
chi2 value (without noise) for Powell: 48.439384824847956  
average time for CG: 5.473999002150127 seconds  
chi2 value (with noise) for CG: 85.06981919655972  
chi2 value (without noise) for CG: 68.7291566328876  
average time for BFGS: 6.69640759059361 seconds  
chi2 value (with noise) for BFGS: 71.78550302526396  
chi2 value (without noise) for BFGS: 57.42162601972965  
average time for L-BFGS-B: 5.841121426650456 seconds  
chi2 value (with noise) for L-BFGS-B: 81.43751391791639  
chi2 value (without noise) for L-BFGS-B: 66.45097907673568  
average time for TNC: 6.563905213560377 seconds  
chi2 value (with noise) for TNC: 74.96609741576006  
chi2 value (without noise) for TNC: 58.198438073015446  
average time for COBYLA: 1.666680829865592 seconds  
chi2 value (with noise) for COBYLA: 78.49874464606329  
chi2 value (without noise) for COBYLA: 66.19309393961564  
average time for SLSQP: 2.873416449342455 seconds  
chi2 value (with noise) for SLSQP: 62.756947144902846  
chi2 value (without noise) for SLSQP: 37.88723205549305

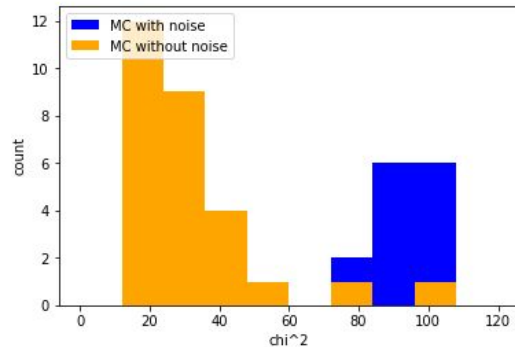
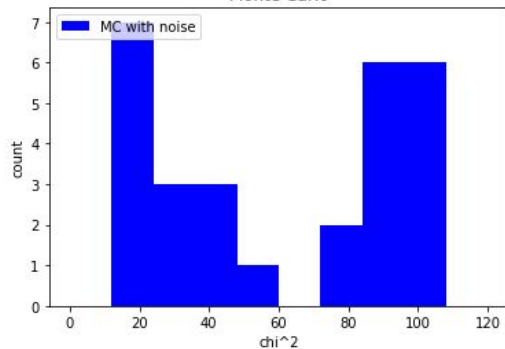
## Basinhopping niter = 25

average time for Nelder-Mead: 20.268136343785695 seconds  
chi2 value (with noise) for Nelder-Mead: 49.02851080971168  
chi2 value (without noise) for Nelder-Mead: 30.06558285392754  
average time for Powell: 36.70845403841564 seconds  
chi2 value (with noise) for Powell: 59.04416700450565  
chi2 value (without noise) for Powell: 47.49919979627662  
average time for BFGS: 16.16957257475172 seconds  
chi2 value (with noise) for BFGS: 68.93500843710063  
chi2 value (without noise) for BFGS: 46.31901726906612  
average time for SLSQP: 6.993133834430149 seconds  
chi2 value (with noise) for SLSQP: 63.31442266173478  
chi2 value (without noise) for SLSQP: 33.89991591501348

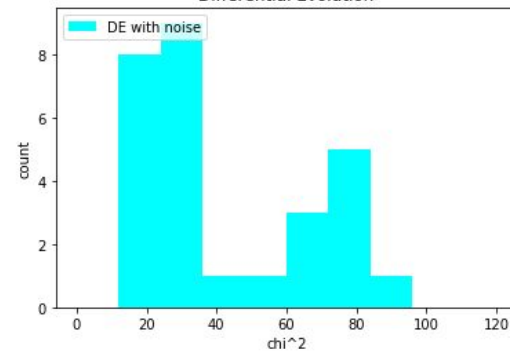
# Histograms



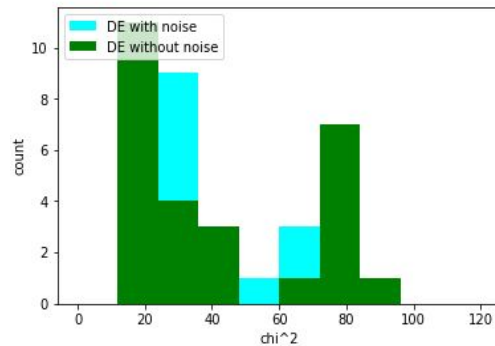
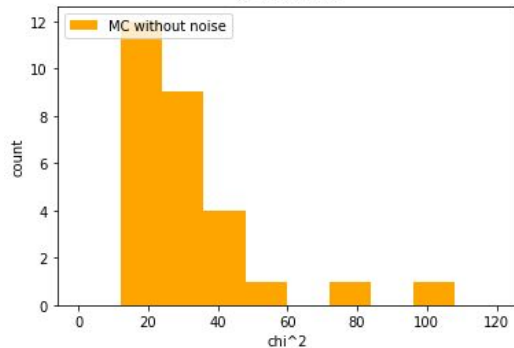
Monte Carlo



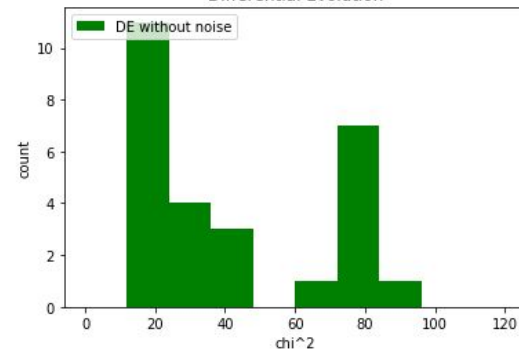
Differential Evolution

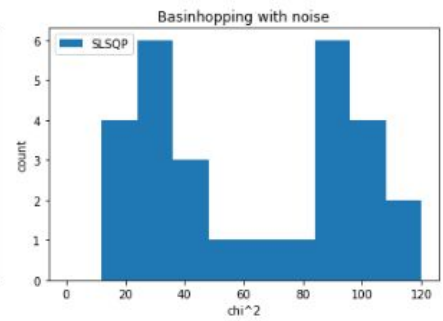
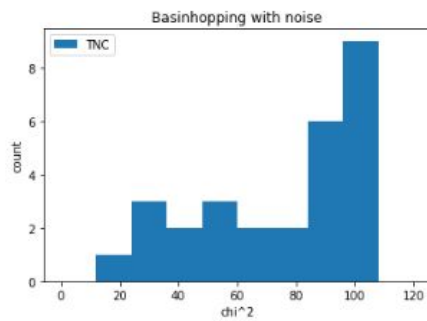
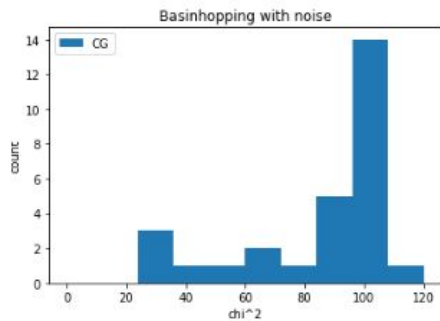
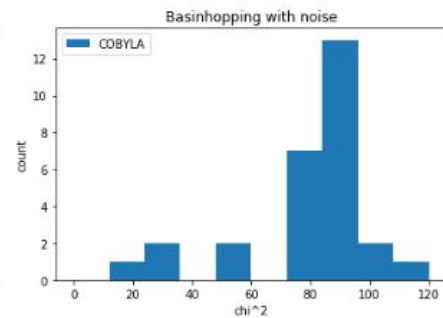
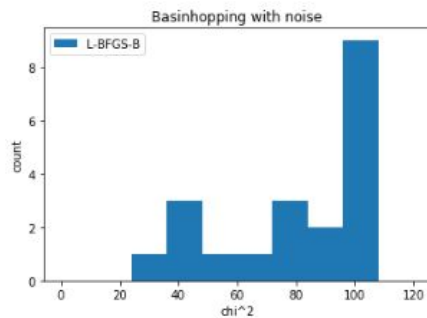
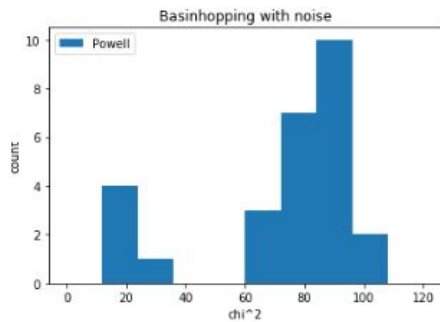
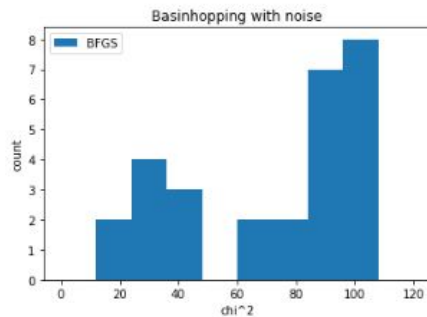
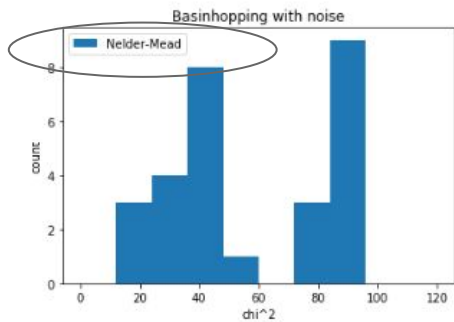


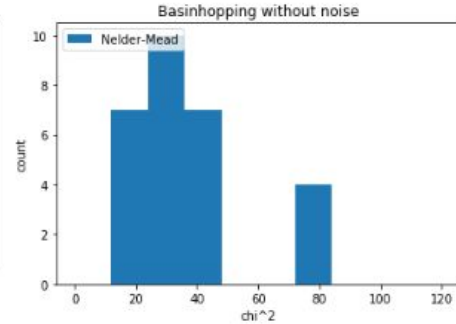
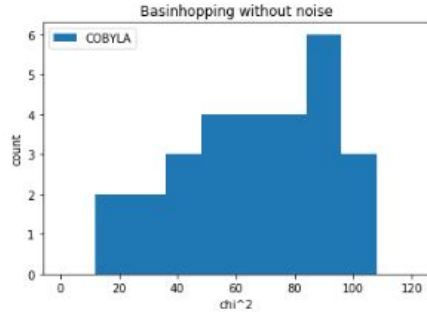
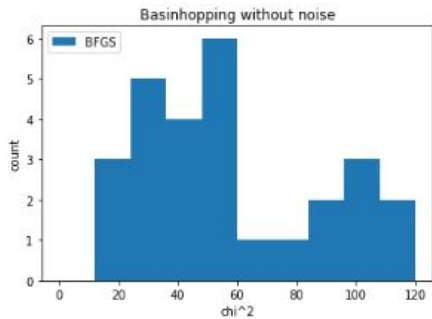
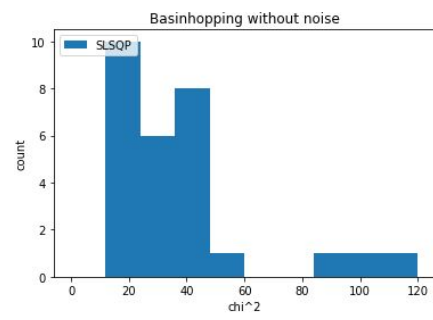
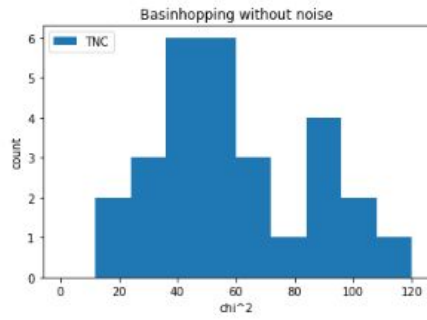
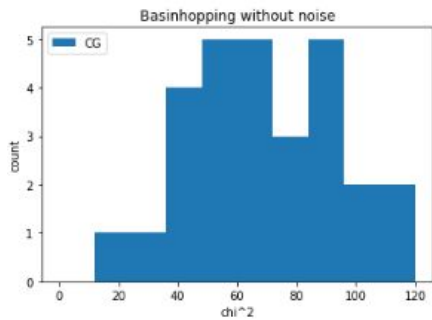
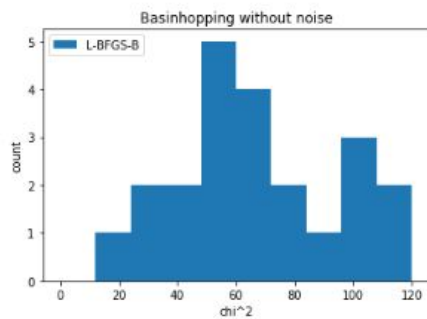
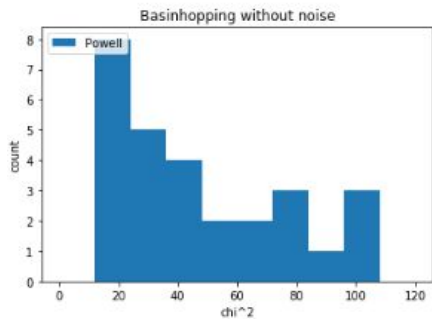
Monte Carlo

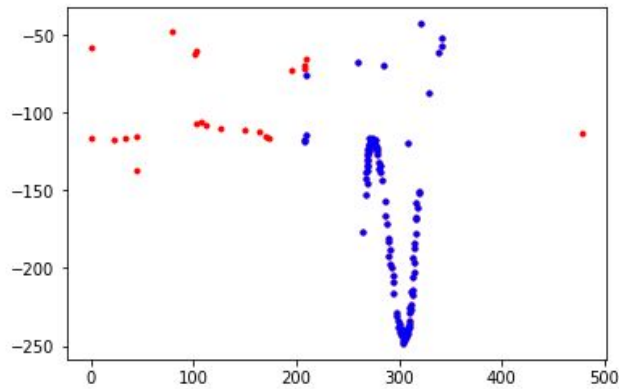


Differential Evolution



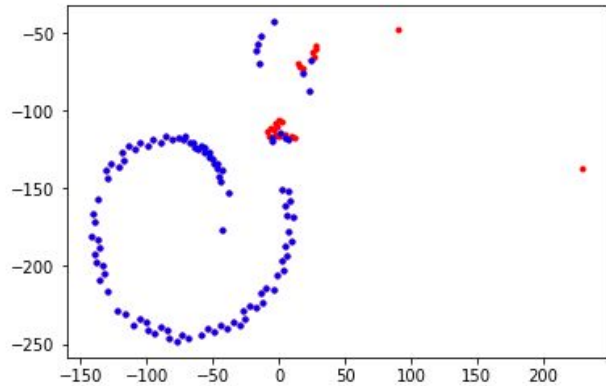






Cleaning's effect on processing time (Monte Carlo)

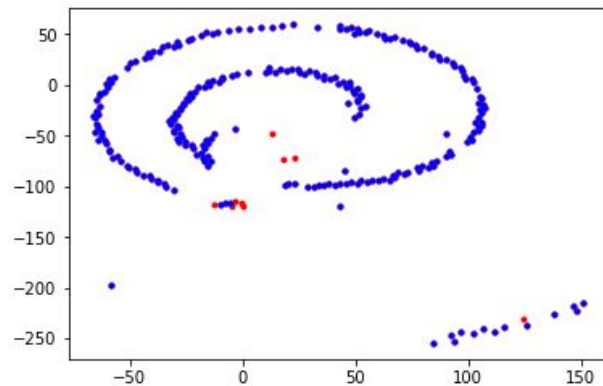
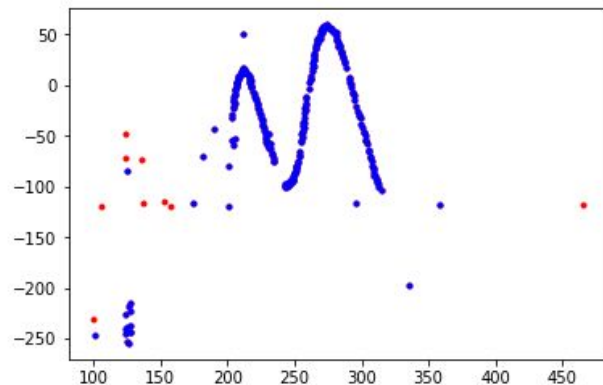
blue: after cleaning  
red: before cleaning



We can see that the cleaned data takes a lot less time

Monte Carlo event 12 with noise: 0.6670424938201904 seconds  
position chi2: 12.25689314692066 energy chi2: 10.461460892477122 vertex chi<sup>2</sup>: 2.2916093421940524 total chi2: 25.00996338  
1591835  
Monte Carlo event 12 without noise: 0.37213635444641113 seconds  
position chi2: 6.920917079017351 energy chi2: 17.256624086433263 vertex chi<sup>2</sup>: 2.6925715154967915 total chi2: 26.87011268  
0947404





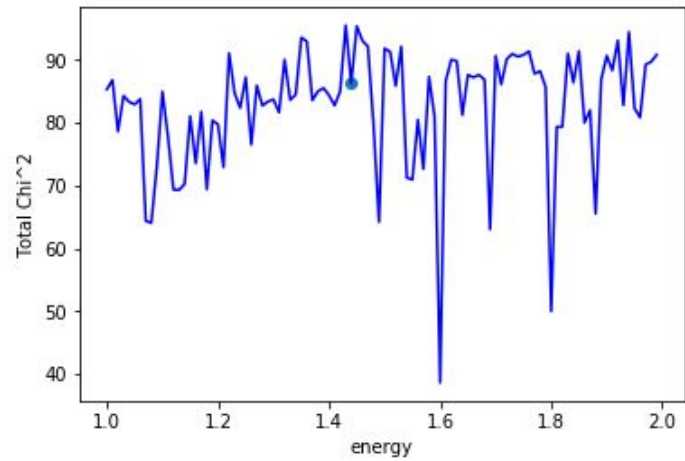
Monte Carlo event 9 with noise: 0.9181435108184814 seconds

position  $\chi^2$ : 16.211907888359203 energy  $\chi^2$ : 3.762711409690692 vertex  $\chi^2$ : 5.841481496590662 total  $\chi^2$ : 25.816100794640555

Monte Carlo event 9 without noise: 0.5298173427581787 seconds

position  $\chi^2$ : 15.814149343876108 energy  $\chi^2$ : 3.474156675673004 vertex  $\chi^2$ : 6.084244782769689 total  $\chi^2$ : 25.3725508023188

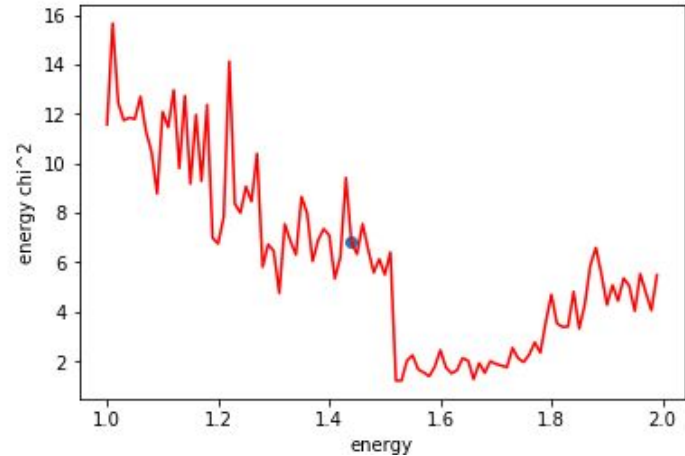




The energy  $\chi^2$  only counts towards a small part of the total  $\chi^2$  value.

The blue points here shows the energy value that minimizes the total value of the objective function.

`Text(0,0.5,'energy  $\chi^2$ ')`





# Scipy Reference Guide

Local methods: `scipy.optimize.minimize`

<https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.minimize.html#scipy.optimize.minimize>

Global methods:

**Basinhopping**: <https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.basinhopping.html#scipy.optimize.basinhopping>

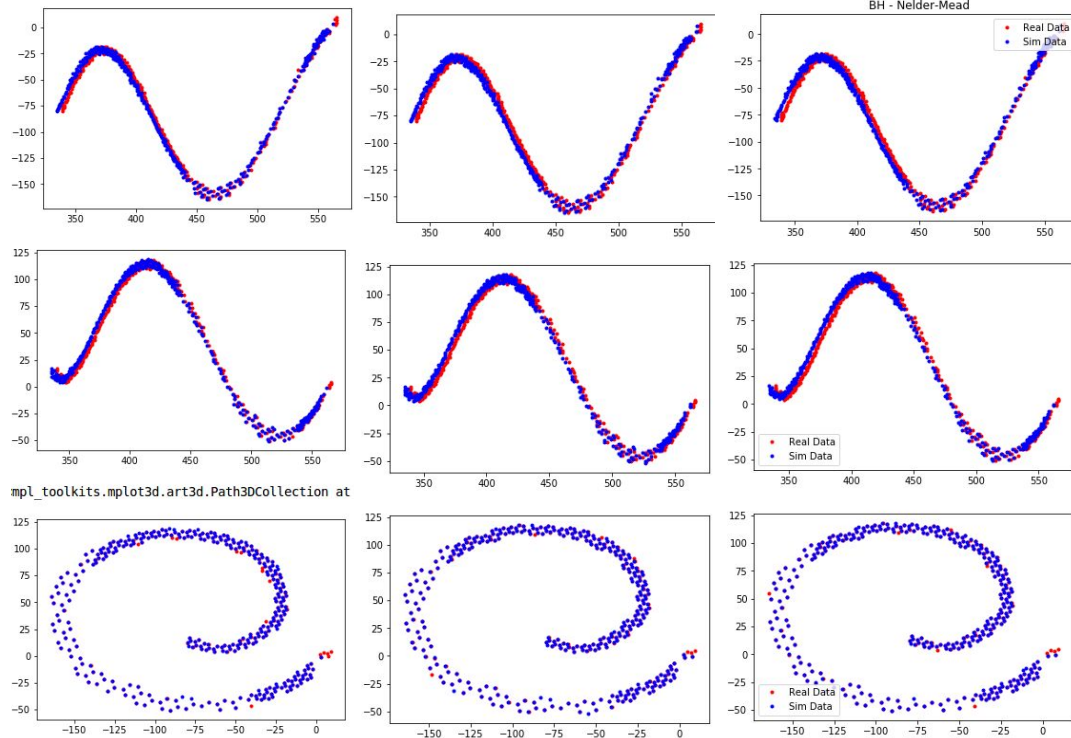
**Differential**

**Evolution**: [https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.differential\\_evolution.html#scipy.optimize.differential\\_evolution](https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.differential_evolution.html#scipy.optimize.differential_evolution)

[https://en.wikipedia.org/wiki/Differential\\_evolution](https://en.wikipedia.org/wiki/Differential_evolution)

# Simulated Data - proton-like event

Monte-Carlo: 1.59  
Differential Evolution: 1.26  
Basinhopping: 1.78 with Nelder-Mead  
(SLSQP did not work for simulated data)



Monte Carlo

Differential Evolution

Basinhopping

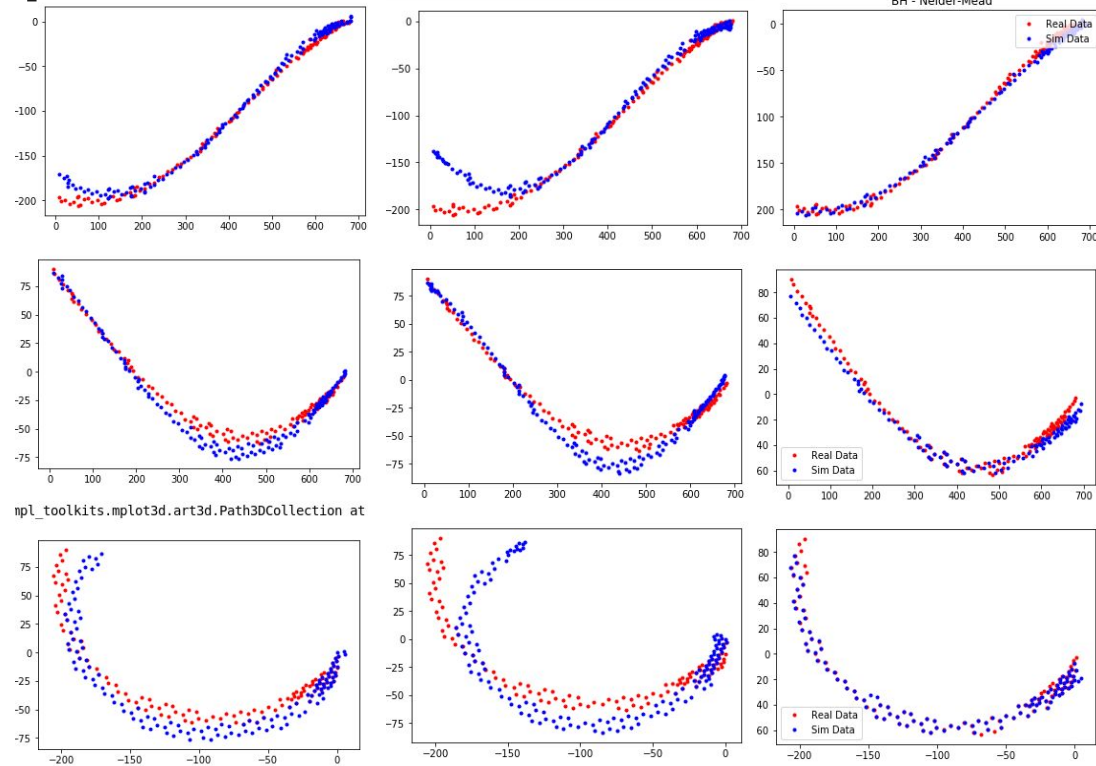
# Simulated Data - less proton-like



Monte-Carlo: 30.899

Differential Evolution: 40.335

Basinhopping: 14.07 with Nelder-Mead  
18.27 with SLSQP



Monte Carlo

Differential Evolution

Basinhopping