

Analysis of Algorithms.

Assignment 2.

Daniyal Asghar
53731

Problem 1: Linear Search.

```
int linearSearch(int arr[], int n, int target) {
    for (int i = 0; i < n; i++) {
        if (arr[i] == target) {
            return i;
        }
    }
    return -1;
}
```

Explanation:

- Single loop run from 0 to n-1
- Each iteration perform 1 comparison.
- worst case: all "n" elements checked
- Best case: found at index 1,

Calculation:

$$T(n) = n$$

$$O(n)$$

P. 2: Binary Search:

```
int binarySearch(int [], int left, int right, int target) {
    while (left <= right) {
        int mid = left + (right - left) / 2;
        if (arr[mid] == target) return mid;
        if (arr[mid] < target) left = mid + 1;
        else right = mid - 1;
    }
}
```

```
return -1;
}
```

~~Ex~~ Explanation:

- Each iteration, half the arr size
- Max step = $\log_2 n$
- Each step does constant comparison
- Best case: sorted at first mid.

Calculation:

interval after k step $= n/2^k$
 $n/2^k \leq 1 \quad \leftarrow k = \log_2 n$
 $T(n) = (\log_2 n)$
 $\rightarrow O(\log n)$

P.3: Bubble Sort:

```
void bubbleSort(int arr[], int n) {
    for (int i = 0; i < n-1; i++) {
        for (int j = 0; j < n-i-1; j++) {
            if (arr[j] > arr[j+1]) {
                std::swap(arr[j], arr[j+1]);
            }
        }
    }
}
```

Explanation

Two nested loops

after loop runs $n-1$ times

inner loop runs $(n-1) + (n-2) + \dots + 1$

Calculation:

inner loop $= 1 + 2 + \dots + (n-1)$

$(n-1)n/2 = (n^2 - n)/2$

$T(n) = n^2/2$

$O(n^2)$

4. Selection Sort:

Explanation:

outer loop runs $n-1$

inner loop compare elements to find min.

Total comparisons $\approx (n-1) + (n-2) + \dots + 1$

Swap $= n-1$ (negligible)

Calculation:

$$\text{Total Comparisons} = (n-1)n/2 = (n^2 - n)/2$$

$$T(n) = n^2/2$$

$$O(n^2)$$

5. Matrix Multiplication

Explanation:

Three nested loop (i, j, k)

$i \rightarrow n$ iteration

$j \rightarrow n$

$k \rightarrow n$

$$\text{Total} = n \times n \times n = O(n^3)$$

DATE: ___/___/___

DAY: ___/___/___

6 : Fibonacci (Recursive)

Explanation:

Each call generates 2 more call
Recursion tree double at each level
Growth is exponential,

Calculation:

$$T(n) = T(n-1) + T(n-2) + O(1)$$

$$\text{No. call} \approx 2^n$$

$$O(2^n)$$

7. Fibonacci (Iterative)

Explanation:

One loop run from 2 to n
Each iteration does constant work
Growth is linear.

Calculation:

loop executes (n-1) time

$$T(n) = n \times O(1) = n$$

$$O(n)$$

8. Factorial (Recursive)

Explanation:

Each call reduce n by 1

Total call = $n+1$ (including base)

Each call does constant work.

Calculation:

$$\text{Recursive: } T(n) = T(n-1) + 1$$

$$T(n) = n + 1$$

$$O(n)$$

9: Nested loop

Explanation:

outer loop run n time

inner loop also run n time.

$$\text{Total iteration} = n \times n$$

Calculation

$$n \times n = n^2$$

Each iteration = constant printing

$$T(n) = n^2$$

$$O(n^2)$$

DATE: ___/___/___

DAY: ___/___/___

10: Recursive Power Function:

~~find~~

Explanation:

Each call decreases n by 1

Total call = $n+1$ (including base)

Each call does constant

Multiplication

Linear growth.

Calculation:

$$T(n) = T(n-1) + 1$$

$$T(n) = n + 1$$

$$O(n)$$