

$$y = \beta_1^0 x + \varepsilon$$

SUB MODEL

$$y = \beta_0 + \beta_1 x + \varepsilon$$

FULL MODEL

$$\varepsilon \sim N(0, \sigma^2)$$

$$SSD_0 = \sum (\hat{\beta}_1^0 x_i - (x_i + \alpha))^2 \quad SSD = \sum (\hat{\beta}_1 x_i + \hat{\beta}_0 - (x_i + \alpha))^2$$

$$x_1, \dots, x_n$$

$$SSD_0 \approx SSD$$

$$y_i = x_i + \alpha + \varepsilon_i$$

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$$\text{cov}(\hat{\beta}_1, \hat{\beta}_1^0)$$

in general

$$\text{cov}(\hat{\beta}_1 - \hat{\beta}_1^0, \hat{\beta}_1) = 0 \quad \text{or} \quad \text{cov}(\hat{\beta}_1 - \hat{\beta}_1^0, \hat{\beta}_1^0) = 0$$

$\hat{\beta}_1^0$ is unbiased for β_1 .

$$y_t = \beta_0 + \beta_1 x_t + \varepsilon_t$$

(x_t) (y_t) time series

$$\Delta y_t = \beta_1 \Delta x_t + \Delta \varepsilon_t$$

$$\text{cov}(\Delta \varepsilon_t, \Delta \varepsilon_{t-1}) \neq 0$$

↑ variable y in change form

