

Encoding

Represent radix-N numbers

	Binary	Octal	Hexadecimal	Decimal
Conversion Shortcuts	1 bit	3 bits	4 bits	Use a Calculator
Prefix	0b	0o	0x	0d
Examples	101001 1011	51 13	29 B	41 11

Signed Integer

Sign magnitude

Sign Magnitude

± Value

Range

$[-(2^{n-1}-1), (2^{n-1}-1)]$

	<i>Sign</i>	<i>Magnitude</i>	
40 = 0	101000	= 0101000	
-12 = 1	1100	= 11100	
-39 = 1	100111	= 1100111	

2's complement

- The leftmost bit tells us if the number is positive (0) or negative (1).
- To make a negative number, flip all the bits of the positive number and add 1.
- To make a positive number, subtract 1 first, flip all the bits of the negative number.

Fixed Point

- integer bits determin range
- Fractional bits determine accuracy
- cannot represent everything clearly, like 1/3

Decimal	100s	10s	1s	1/10s	1/100s	1/1000s
Binary	4s	2s	1s	1/2s	1/4s	1/8s

Floating Point

- Exponent usually in 2's complement
- Choose exponent to cover range

Sign Exponent

± 2^x

± 2^x

max error

Max error (floating point) = $(1/2) * (\text{Max number} - \text{Second max number})$

To do this we have to shift the numbers so they have the same exponent and then line them up and add them.

$$(2^3 * 0.1001_2) + (2^1 * 0.1010_2)$$

$$= (2^3 * 0.1001_2) + (2^3 * 0.00101_2)$$

$$= 2^3 * (0.1001_2 + 0.00101_2) = 2^3 * 0.10111$$

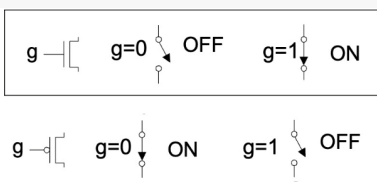
$$\approx 2^3 * 0.1100_2 \text{ (can only keep 4 mantissa bits so we round to nearest)}$$

We often have an incorrect answer when adding in floating point because two numbers may be very different sizes and so, when you change their exponents to be the same size, there are not enough mantissa bits to adequately represent the number.

Transistors, Boolean Algebra and Digital Logic

Transistors

MOS transistors are switches



Boolean Algebra and Digital Logic

Combinational Digital Logic
XOR (异或门)

A	B	A XOR B
0	0	0
0	1	1
1	0	1
1	1	0

A	B	A XNOR B
0	0	1
0	1	0
1	0	0
1	1	1

Gate	Symbol	Operator
AND		$A \cdot B$
OR		$A + B$
NOT		\bar{A}
NAND		$\overline{A \cdot B}$
NOR		$\overline{A + B}$
XOR		$A \oplus B$
XNOR		$\overline{A \oplus B}$

SOP/POS

- SOP (Sum of product) : $R = A \cdot B + C \cdot D + E \cdot F$
(Find lines which outputs are 1)
- POS (Product of Sum) : $R = (A + B) \cdot (C + D) \cdot (E + F)$
(Find lines which outputs are 0)

Sequential Digital Logic

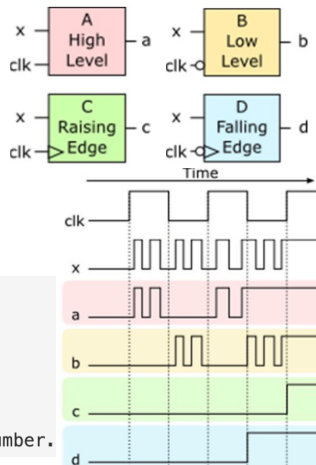
Clock, latches and flip-flops

Clock

- + Copy input when clock says so
- + Otherwise don't change value

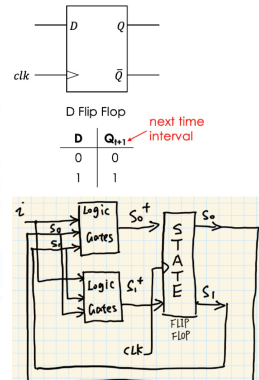
Latches

- + Level-sensitive: Changes or preserves state based on the level (high or low) of a control signal.
- + Transparent when enabled: When the enable signal is active the output immediately reflects changes in input.



Flip-Flops

- + Edge-sensitive: Responds and changes state only at a specific edge (rising or falling) of the clock signal.
- + State preservation between clock edges: Maintains its state stable in the intervals between clock signal edges.



Finite State Machine

1. Write the truth table from the inputs and state bits, to future state bits.
2. Implement each of the outputs with a circuit.
3. Connect the outputs of the function to flip flops.
4. Connect the output of the latch to the inputs of the circuit.

Memory

Types of memory/Visualization

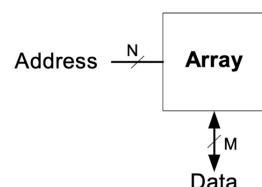
Register

A register is just a collection of **D-Flip-flops**

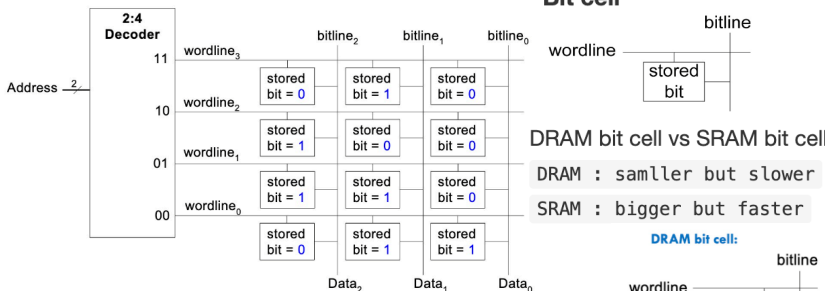
It allows you to represent 'words' (your encodings e.g. 4-bit unsigned binary)

RAM(ROM)

- KB 2^{10} Bytes
- MB 2^{20} Bytes
- GB 2^{30} Bytes
- See graph below
- N: Amount of the element
if Bits is given, actual number of address is 2^N
- M: bits of 'word'



Bit cell



DRAM bit cell vs SRAM bit cell

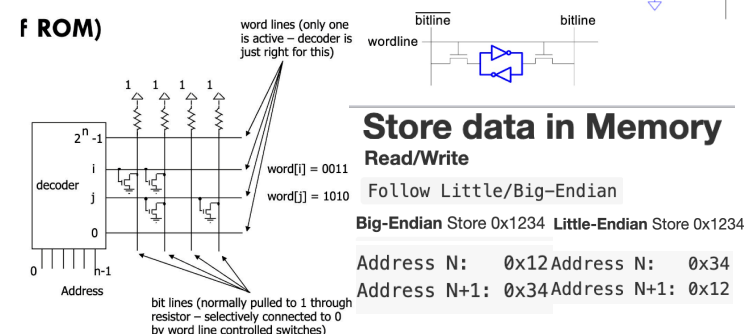
DRAM : smaller but slower

SRAM : bigger but faster

How does ROM work

Falsh (闪存) is a variant of ROM

f ROM)



Store data in Memory

Read/Write

Follow Little/Big-Endian

Big-Endian Store 0x1234 **Little-Endian** Store 0x1234

Address N: 0x12 Address N: 0x34

Address N+1: 0x34 Address N+1: 0x12

Array in Memory

Memory Allocation

- Each element in the array uses memory according to its data type.
For example, an int might use 4 bytes (depending on the platform) while a char typically uses 1 byte.
- The total memory used by the array is
the size of the data type multiplied by the number of elements.

Accessing Elements

base_address + (element_size * index)

Data Types

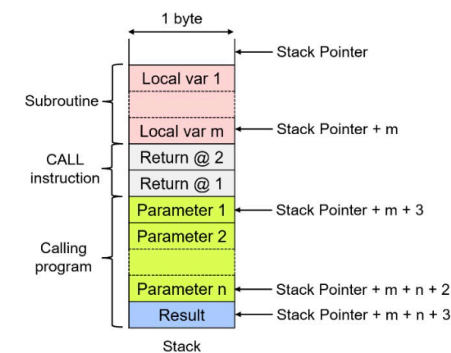
Boolean	1 bit
Character	2 bytes
Integer	4 bytes
Long	8 bytes
Float	4 bytes
Double	8 bytes

Load

```
LDI Rd,K
; Load Immediate
; R16-31, 8 bits number .end
LD Rd,X/Y+/-X
; Load Indirect from Data Space
to Register using Index X/Y/Z
LDD Rd,Y/Y+3/Y-1 ;
only support Y and Z
LDS(32-bit) Rd,k ; Load Direct from Data Space
; 0 <= k <= 65535
; PC = PC + 2
; 32 bits opcode
```

Store

```
ST X/-X/X+,Rr
; Store Indirect From Register
to Data Space (X/Y/Z)
STD Y/Z + q
; Store Indirect From Register
to Data Space with Displacement (only Y/Z)
; q is an integer in [0,63], 6 bits
STS k,Rr ; this is a 32-bit version
; Store Direct to Data Space
; 0 <= k <= 65535
; PC = PC + 2
; 32 bits opcode
!!! there is a 16 bits version
```



```
boolean A, B, C, D, E, F, G;
int count = 0;

void setup() {
  pinMode(2, INPUT);
  pinMode(6, OUTPUT); // G
  .....
  pinMode(12, OUTPUT); // A
  attachInterrupt(0, x, FALLING); //pin2
  Serial.begin(9600);
}
```

```
void loop() {
  Serial.println(digitalRead(2));
  switch (count) {
    case 0: A=1; B=1; C=1; D=1; E=1; F=1; G=0; break;
    .....
  }

  digitalWrite(6, G);
  .....
  digitalWrite(12, A);
  delay(500);
}

void x() {
  count = (count + 1) % 10;
}
```

Avr

```
.section .data
;define variables

.section .text
;doing calculations
.global asm_function

asm_function:
;here is your main function
ret
```

IF/ELSE

```
[Before-if/else code here]
cp r1, r2 ;
br.. else ;

if:
[IF code here] ; You didn't
jmp end_if

else:
[ELSE code here] ; You did
end_if:
[code here] ;
```

Branches

```
CP Rd,Rr
; Rd >= Rr -> Flag C = 0
; Rd < Rr -> Flag C = 1
; Rd = Rr -> Flag Z = 0

CALL k
; SP = SP + 2
; The return address is
loaded from the STACK

BREQ k
; branch if Flag Z = 1
(Rd = Rr / Rd = k)

BRNE
; branch if Flag Z != 1
(Rd != Rr / Rd != k)

BRSH k
; branch if Flag C = 0
(Rd >= Rr / Rd >= k)

BRLO k
; branch if Flag C = 1
(Rd < Rr / Rd < k)
```

```
BREQ k
; branch if Flag Z = 1
(Rd = Rr / Rd = k)

BRNE
; branch if Flag Z != 1
(Rd != Rr / Rd != k)

BRSH k
; branch if Flag C = 0
(Rd >= Rr / Rd >= k)

BRLO k
; branch if Flag C = 1
(Rd < Rr / Rd < k)
```

```
void forwardMedium() {
  Serial.println("Moving forward at medium speed");
  leftServo.writeMicroseconds(1600);
  rightServo.writeMicroseconds(1400);
  delay(1000);
  stopMotion();
}

void turnLeftSlow() {
  Serial.println("Turning left at slow speed");
  leftServo.writeMicroseconds(1450);
  rightServo.writeMicroseconds(1450);
  delay(1000);
  stopMotion();
}
```

```
#include <Servo.h>

pinMode(leftPhotoResistor, INPUT);
pinMode(rightPhotoResistor, INPUT);
Servo leftServo;
Servo rightServo;

const int leftPhotoResistor = A0;
const int rightPhotoResistor = A1;
```

While Loop

```
loop_comparison: ;

start_loop_body:
[loop body code here] ;
JMP loop_comparison

end_loop:
[code here] ;

For loop
```

```
init_loop_iterator:
[initialise_loop_iterator]

loop_comparison :
CP R1, R2 ;
BRLO end_loop;

start_loop_body:
[loop body code here] ;
[modify_loop_iterator] ;
JMP loop_comparison ;

end_loop:
[code here] ;

JMP k
; 0 <= k < 4M
; PC = k
```

Computer Architecture

CISC vs RISC

RISC

- can do everything that CISC can do.
- instruction faster(in a basic way,RISC runs faster, but CISC can use pipelining to be faster)
- shorter instructions
- simpler compiler

CISC

- takes longer to decode
- has direct access to operands in memory.(RISC not)
- almost always has less lines of code.

Why different instructions? Size/Power/Performance/Mistakes

RISC stands for

"Reduced Instruction Set Computer".

This architecture is characterized by:

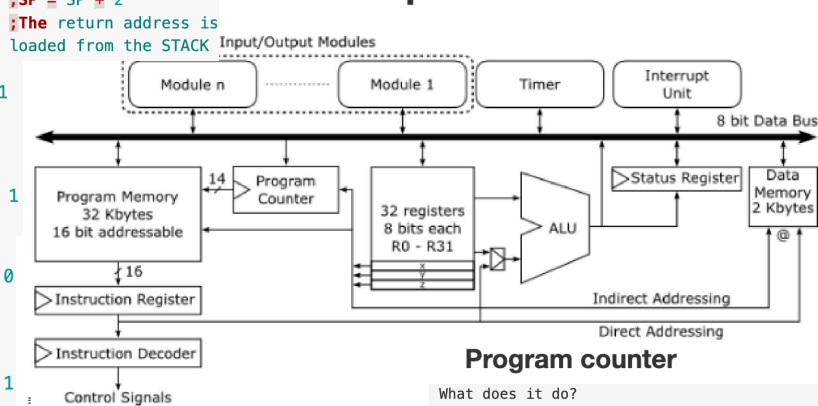
- Instructions have at most 2 operands.
- There are 32 general-purpose registers that arithmetic operations (ADD, SUB, MUL) can operate over.
- The first register in an instruction is both the destination and one of the sources (e.g., 'ADD R15, R16').
- There is an instruction ('LOAD') to load a value from a memory location with a symbol name (e.g., 'LOAD R2, x' to load variable 'x' from memory to 'R2').
- There is an instruction ('STORE') to store a value from a register to a memory location.

CISC stands for "Complex Instruction Set Computer".

This architecture is characterized by:

- Instructions have three operands.
- There are 32 general-purpose registers.
- The first operand is the destination, and the second and third are source operands (e.g., 'ADD R2, R15, R16').
- There is an instruction ('LOAD') to load a value from a memory location with a symbol name (e.g., 'LOAD R2, x' to load variable 'x' from memory to 'R2').
- There is an instruction ('STORE') to store a value from a register to a memory location.
- Arithmetic operations (ADD, SUB, MUL) can have any of its source operands in memory.

AVR Microprocessor



Program memory

What does it do? Store instructions
What operations does it perform? Read /write
What are its properties?
- Each cell is ? bit
- Read/write is always ? bits
- Different to data memory

Register File

What is it?
- Tiny, local memory
* Temporary storage
What digital circuit is this?
- 32 8-bit Registers (r0 to r31)
What are X,Y,Z?
- Design decision
- Enable 26,27 (x), 28,29 (y), 30,31 (z) to be 16-bit manipulations

Data memory

What does it do?
- Stores integers Arrays...
2KB. How many address bits?
- Needs 11
- Actually has 12
* Pretend larger memory
* Gives 256 additional fake address
* Allows some faster operations.

Instruction decoder

Program counter

What does it do?
- Stores address of next instruction
- Increments when move to next instruction
What type of digital circuit is it?
- Register
- Adder(conditional)
- Multiplexer

ALU

What does it do?
- Calculations
- Add/Sub/Conjunction/Negation
How many bits can it add?
- Tie to the registers

Instruction register

What does it do?
- Remembers current instruction
What does it do?
- Stores flags of special conditions
- Zero/overflow
What does it listen to?
- ALU

Status Register

Where is this information used?
- Subsequent instruction
What does it do?
- Open instruction, decide what to do
- Controls rest of circuit
* Operation: Adding/subtracting
* Operands
* Where to write result